Dominik Szombathy Theoretical modeling of the collective tunneling of a Wigner necklace October 25, 2022

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