

Streaming Bayes GFlowNets

Tiago da Silva, Daniel Augusto, Diego Mesquita

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Approximate Bayesian Inference

Let $\mathcal{X} = \{x_1, \dots, x_N\}$ be a finite, compositional space.

Also, let \mathcal{D} be the data space, $f(\cdot \mid x) : \mathcal{D} \rightarrow \mathbb{R}$ be a likelihood function, and $\pi : \mathcal{X} \rightarrow \mathbb{R}$ be a prior on \mathcal{X} .



Approximate Bayesian inference

Our objective is to approximate the a sequence of posterior distributions,

$$\pi(x \mid D_1, \dots, D_i) \propto f(D_1, \dots, D_i \mid x)\pi(x) \text{ for } i \geq 1.$$

This is known as the **streaming Bayes problem**.

That is, Bayesian inference over unbounded data.

Approximate Bayesian inference

For conciseness, we will let

$$R_i(x) = f(D_1, \dots, D_i \mid x)\pi(x)$$

be the unnormalized posterior distribution.

Important.

We assume that D_i and D_j are independent.

BUT each D_i may have its own likelihood function.

Approximate Bayesian inference

We approximate

$$(R_i)_{i \geq 1}$$

with a tractable family $(p^{\theta_i})_{i \geq 1}$ parametrized by θ .

Obviously we are only interested in the latest θ_i for each i .

No need to store unboundedly many models!

Approximate Bayesian inference

Traditional techniques (e.g., MFVI) rely on R_i 's gradient.

However, $\nabla_x R_i(x)$ does not exist in discrete spaces.

GFlowNets (Bengio, 2021) address this problem.

They can also be used for Streaming Bayes, as I will show.

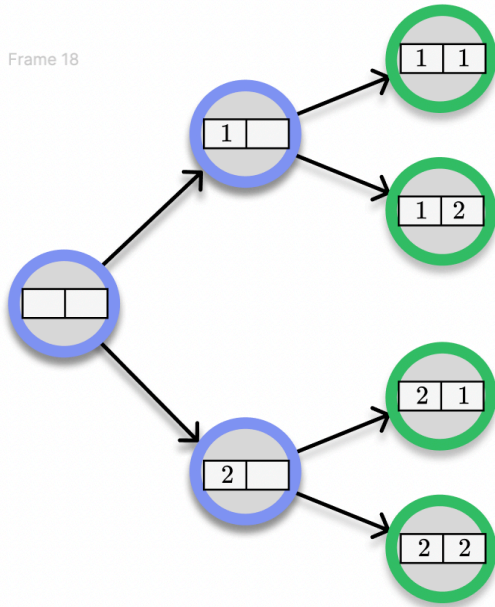
Generative Flow Networks (GFlowNets)

Compositional objects (e.g., Street Fighter combos) are uniquely characterized by:

1. A **state space**, \mathcal{S} , with both incomplete and complete objects. \mathcal{S} also contains the **simplest of states** s_o .
2. A **terminal state space**, \mathcal{X} , which is our original parameter space. Clearly, $\mathcal{X} \subseteq \mathcal{S}$.
3. A **state graph** dictating how to navigate between states.

Generative Flow Networks (GFlowNets)

Frame 18



State graph (SG).

A GFlowNet learns a policy $p_F(\cdot \mid s)$.

$p_F(\cdot \mid s)$ is a distribution over s 's children on the SG.

$p_F(\cdot \mid s)$ is a neural network

$$h_\theta : \mathcal{S} \rightarrow \Delta_{A-1}$$

with parameter θ . Δ_{A-1} is a simplex, and A is the SG's maximum outdegree.

GFlowNets

Our objective is to find a θ_i such that

$$\sum_{\tau \rightsquigarrow x} \underbrace{\prod_{1 \leq t \leq |\tau|} p_F^{\theta_i}(\tau_{t+1} \mid \tau_t)}_{p_F(\tau \mid s_o)} \propto R_i(x)$$

($\tau \rightsquigarrow x$ is a state-sequence from s_o to $x \in \mathcal{X}$).

For this, we introduce a backward policy $p_B(\cdot \mid s)$.

$p_B(\cdot \mid s)$ is an uniform distribution over s 's parents.

We solve this problem by minimizing

$$\theta_i^*, Z_i^* = \min_{\theta_i, Z_i} \mathbb{E}_{\tau} \left[\left(\log \frac{R_i(\tau_{-1}) p_B(\tau \mid \tau_{-1})}{Z_i \cdot p_F^{\theta_i}(\tau \mid \tau_o)} \right)^2 \right]$$

τ_{-1} is the last element of the trajectory τ (which is on \mathcal{X}).

$\tau_o = s_o$ is the first.

Z_i is an auxiliary parameter.

We can demonstrate that the unconstrained global optima solves our sampling problem (Bengio, 2021).

Streaming Bayes GFlowNets

Our prior approach results in a policy $p_F^{\theta_i}$.

This policy generates approximate samples from $R_{i(x)}$.

Research question.

How to update $p_F^{\theta_i}$ when novel data D_{i+1} are observed?

Or: how to sample from R_{i+1} given a model for R_i ?

(Recall that $R_i(x) = f(D_1, \dots, D_i \mid x)\pi(x)$).

Streaming Bayes GFlowNets

We use the i th model as a prior for the $(i + 1)$ model.

To understand this, notice that

$$\begin{aligned} R_{i+1}(x) &= f(D_1, \dots, D_{i+1} \mid x) \pi(x) \\ &= \underbrace{f(D_1, \dots, D_i \mid x) \pi(x)}_{R_i(x)} f(D_{i+1} \mid x) \\ &= R_i(x) f(D_{i+1} \mid x). \end{aligned}$$

Streaming Bayes GFlowNets

$$R_{i+1}(x) = R_i(x)f(D_{i+1} \mid x).$$

Let τ_x be any trajectory from s_o to x . Since

$$R_i(x) = \frac{Z_i^\star \cdot p_F^{\theta_i^\star}(\tau_x \mid s_o)}{p_B(\tau_x \mid x)},$$

then

$$R_{i+1}(x) = \frac{Z_i^\star \cdot p_F^{\theta_i^\star}(\tau_x \mid s_o)}{p_B(\tau_x \mid x)} \cdot f(D_{i+1} \mid x)$$

Streaming Bayes GFlowNets

Our learning objective then becomes

$$\begin{aligned} \theta_{i+1}^*, Z_{i+1}^* &= \min_{\theta_{i+1}, Z_{i+1}} \mathbb{E}_{\tau} \left[\left(\log \frac{R_{i+1}(\tau_{-1}) p_B(\tau \mid \tau_{-1})}{Z_{i+1} \cdot p_F^{\theta_{i+1}}(\tau \mid \tau_o)} \right)^2 \right] \\ &= \min_{\theta_{i+1}, Z_{i+1}} \mathbb{E}_{\tau} \left[\left(\log \frac{p_B(\tau \mid \tau_{-1})}{Z_{i+1} \cdot p_F^{\theta_{i+1}}(\tau \mid \tau_o)} + \log \frac{Z_i^* \cdot p_F^{\theta_i^*}(\tau \mid \tau_o)}{p_B(\tau \mid \tau_{-1})} \cdot f(D_{i+1} \mid \tau_{-1}) \right)^2 \right] \end{aligned}$$

This is the streaming Bayes objective (L_{SB}).

Streaming Bayes GFlowNets (catch-up)

1. A sequence of independent data sets, $(D_i)_{i \geq 1}$.
2. A likelihood function, $f(\cdot \mid x)$, indexed by $x \in \mathcal{X}$.

Algorithm:

1. We first learn a policy $p_F^{\theta_1^*}$ that approximates $\pi(\cdot \mid D_1)$.
2. We iteratively update $p_F^{\theta_i^*}$ by minimizing L_{SB} .

$$\theta_{i+1}^*, Z_{i+1}^* = \min_{\theta_{i+1}, Z_{i+1}} L_{\text{SB}}(D_{i+1}, \theta_i^*, Z_i^*, f, \pi)$$

Streaming Bayes GFlowNets

Important.

Streaming Bayes GFlowNets do not require

1. likelihood evaluation on the entire data history;
2. unbounded storage for model snapshots.

Empirical illustration

Example: Linear preference learning with integer-valued features.

Data. $(d_{i1}, d_{i2}, p_i) \in \{1, 0\}^k \times \{1, 0\}^k \times \{1, 0\}$.

$p_i = 1$ means that $d_{i2} \succeq d_{i1}$.

$p_i = 0$ means that $d_{i1} \succeq d_{i2}$.

d_{i1} and d_{i2} are binary feature vectors.

Model. We use a simple logistic model,

$$p(d_{i1} \succeq d_{i2} \mid x) = \sigma(x^T(y_{i1} - y_{i2})).$$

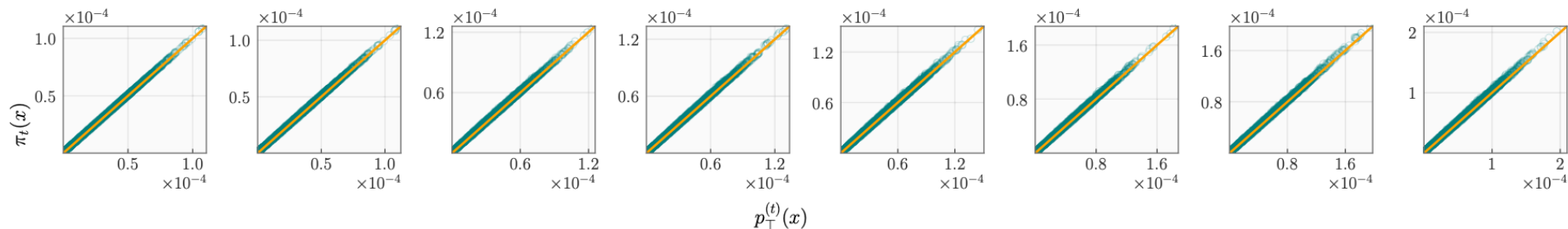
$x \in [[0, u]]^{\{k\}}$ is an integer vector.

We choose a factorized truncated Poisson prior for x .

We observe a (simulated) stream $(D_i)_{i \geq 1}$ of tuples (d_1, d_2, p) .

Empirical illustration

We compare the true posterior (y axis) with our approximation (x axis) for $1 \leq i \leq 8$.



As we can see, Streaming Bayes GFlowNet accurately approximates the streaming posterior.

Take home message

GFlowNets are state-of-the-art models for approximate inference over discrete and compositional distributions.

Traditional approaches to streaming Bayesian inference fail on discrete parameter spaces.

Streaming Bayes GFlowNets are a scalable solution for Bayesian inference in the face of continual data streams.

SB-GFlowNets pave the road for reduced environmental footprint for GFlowNet training via model reuse.