

A BST is a binary tree where each node has a Comparable element and satisfies the restriction that the element in any node is greater than the elements in all nodes in that node's left subtree and lesser than the elements in all nodes in that node's right subtree.

Each node contains an element, a left link, and a right link. The left link points to a BST for items with lesser elements, and the right link points to a BST for items with greater elements, as depicted in the Figure 1.

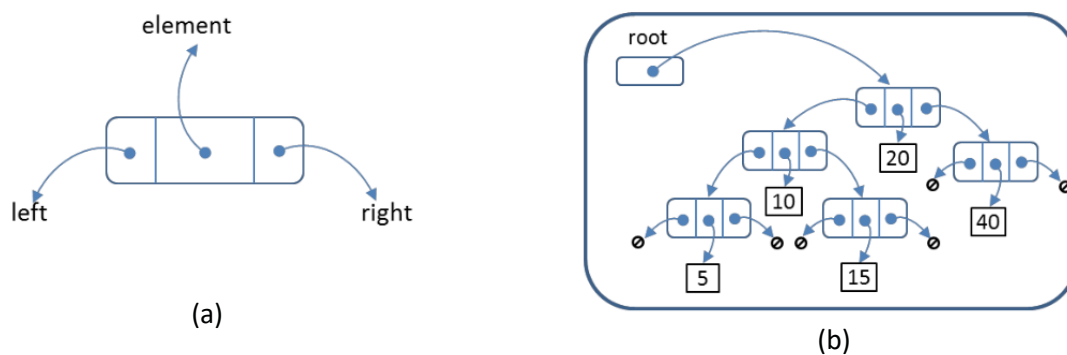


Figure 1 - (a) A single node; (b) binary tree

Download the project PL6_BST_for_students from moodle. The project contains one generic source outer class `BST<E>`, which has one nested class `Node<E>` (already complete) and a text file (xxx.xxx). Three test classes `BSTTest`, `TREETest` and `TREE_WORDSTest`.

Exercise 1: Develop the generic class `BST<E>` with the following public interface:

`BST()`: the BST's constructor.
`boolean isEmpty()`: returns true if the tree is empty, false otherwise.
`int size()`: returns the number of elements in the tree
`void insert(E element)`: inserts (or replaces if already exists) an element in the tree
`void remove(E element)`: removes an element (node) from the tree.
`int height()`: returns the height of the tree
`E smallestElement()`: returns the smallest element within the tree.
`Iterable<E> inOrder()`: returns the sequence of elements resulting from an in-order traversal of the tree
`Iterable<E> preOrder()`: returns the sequence of elements resulting from a pre-order traversal
`Iterable<E> postOrder()`: returns the sequence of elements resulting from an post-order traversal
`Map<Integer,List<E>> nodesByLevel()`: returns a map containing for each tree level a list of nodes that belong to that level

1. Implement all the methods of the BST's interface.
2. Test your implementation running the tests in the `BSTTest` class.

Exercise 2:

Implement a binary search tree from the words of a text file. This tree must store information on the number of occurrences of each word. Admit as valid separators the characters: comma, period, space and line break.

1. Implement the class `TREE_WORDS` to represent a binary search tree with elements of the type `TextWord`;
2. Implement the necessary adjustments in a way that when a word is inserted into the tree the number of its occurrences is updated;
3. Implement the public method `Map<Integer, List<String>> getWordsOccurrences()` that should return a map containing, for each number of occurrences found, the list of words that have the same number of occurrences.

Exercise 3:

Implement a generic method that sorts an unordered `List<E>`.