

CHE 318 L16
Feb-11 2026

We have seen

1) $k_c' \Rightarrow$ simple form to $N_A = k_c'(C_{A1} - C_{A2})$

2) k_c' can be taken from theories

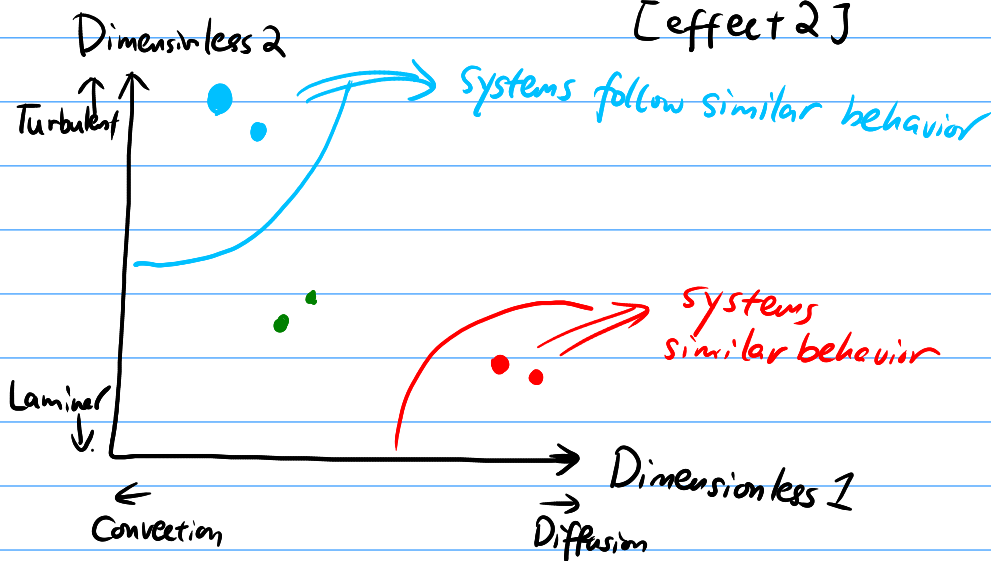
- Film
- Penetration
- Boundary layer

What if

- 1) We're interested in getting accurate k_c'
- 2) Measured k_c' , can we apply to other geometry?

We can use "Dimensionless Analysis"

$$\text{Dimensionless number} = \frac{[\text{effect 1}]}{[\text{effect 2}]}$$



$$N_{Sc} \text{ (Schmidt Nr)} = \frac{\mu}{\rho D_{AB}} = \frac{[\text{momentum diff}]}{[\text{molar diff}]}$$

also $\frac{\delta}{\delta_c} = N_{Sc}^{\frac{1}{3}}$

$$N_{Sh} \text{ (Sherwood Nr)} = \frac{k_c' L}{D_{AB}} = \frac{[\text{conv m.t.}]}{[\text{diff m.t.}]}$$

$$N_{Re} \text{ (Reynolds Nr)} = \frac{U P L}{\mu} = \frac{U L}{(\frac{\mu}{\rho})} = \frac{[\text{kinetic transp}]}{[\text{viscosity transp}]}$$

How do we correlate k_c' ?

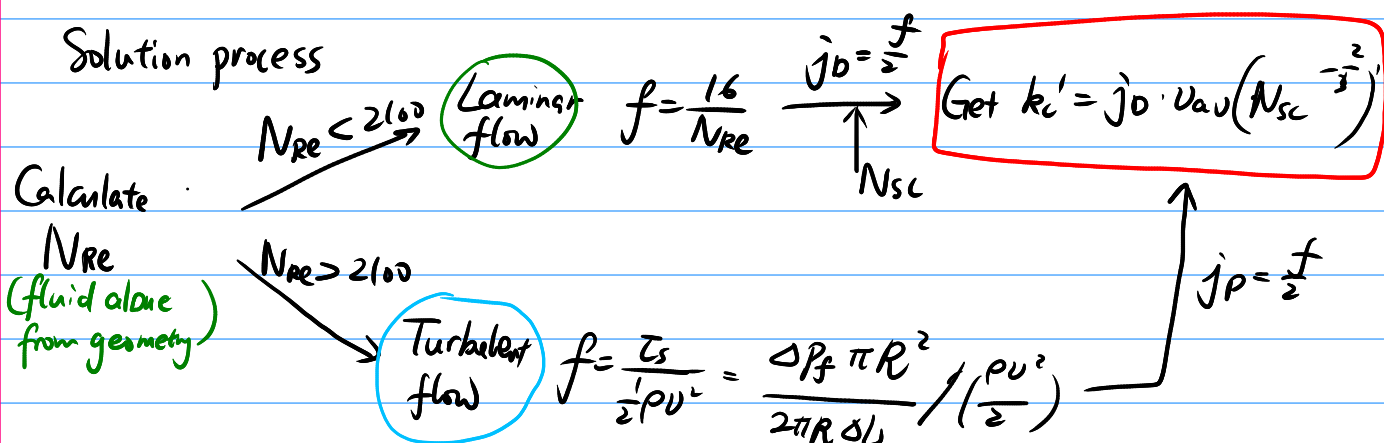
Chilton-Colburn j -factor
(same factor for momentum / heat / mass transfer)

For mass transfer

$$j_D = \frac{k_c'}{U_{av}} (N_{Sc})^{\frac{2}{3}} = \frac{f}{2} \Rightarrow \text{Fanning friction factor}$$

\uparrow average fl. velocity

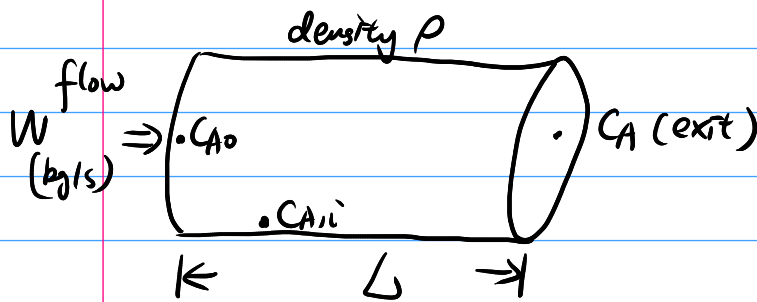
Solution process



More generally

$$j_D = \frac{f}{2} = \frac{N_{Sh}}{N_{Re} N_{Sc}^{\frac{1}{3}}} \rightarrow \text{has } k_c'$$

Pipe Most likely, we use dimensionless analysis on an established chart



$\frac{W}{D_{AB} PL}$ determines exit concentration

$$\frac{W}{D_{AB} PL} = N_{Re} N_{Sc} = \frac{\rho W}{L} \cdot \frac{D}{4} \cdot \frac{\pi}{4}$$

1) Gas (use rod-like flow curve)

2) Liquid $\frac{W}{D_{AB} PL} > 400$ parabolic flow

$$\frac{C_A - C_{A0}}{C_{A,i} - C_{A0}} = 5J \left(\frac{W}{D_{AB} PL} \right)^{-2/3}$$

3) Liquid/Gas turbulent flow

$N_{Re} > 2100$ If $0.6 < N_{Sc} < 3000$

$$N_{Sh} = k_c' \left(\frac{D}{D_{AB}} \right) = 0.023 \left(\frac{\rho D v}{\mu} \right)^{0.83} \left(\frac{\mu}{\rho D_{AB}} \right)^{0.33}$$

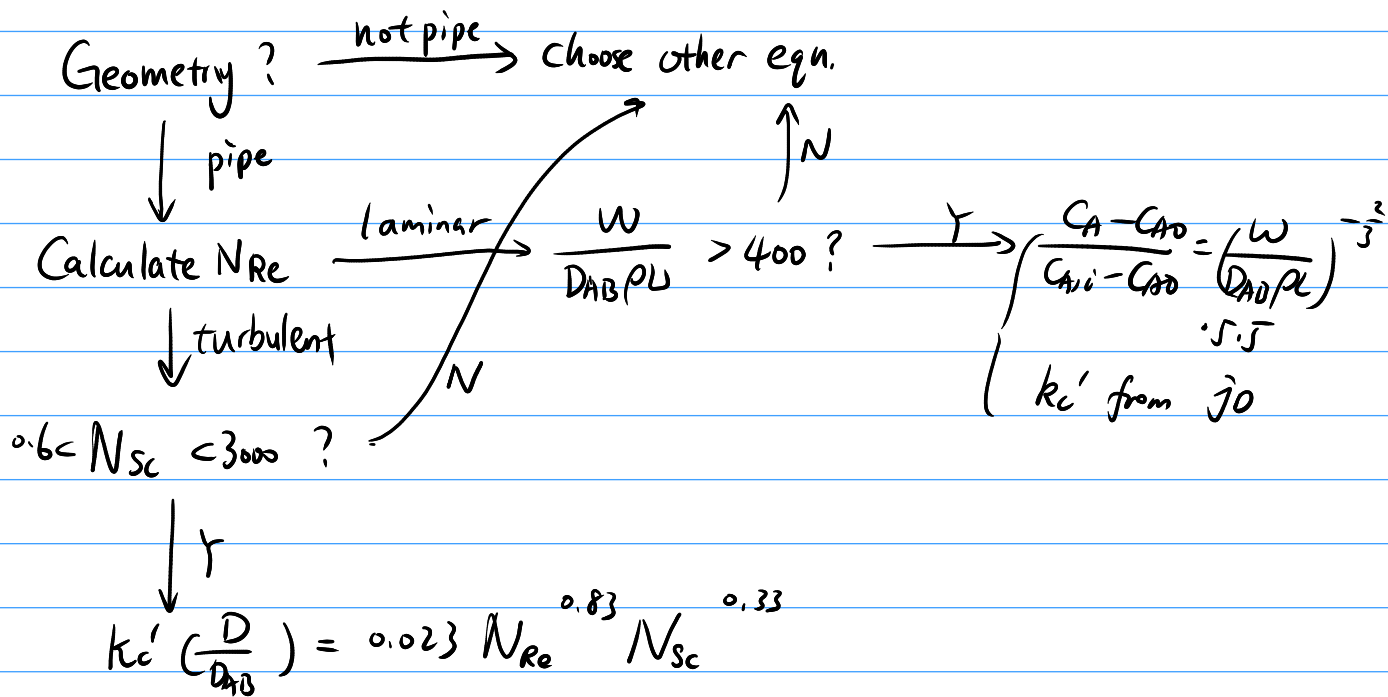
\downarrow $N_{Re,D}$ \downarrow N_{Sc}

1) (very close to the j -D analog)

2) We just need $N_{Re,D}$ $N_{Sc} \Rightarrow k_c'$

3) Only applicable for pipe ! (& N_{Sc} range)

Solution procedure



Case II FI