

CHE318 L03

Jan - 09 2026

Slide 7

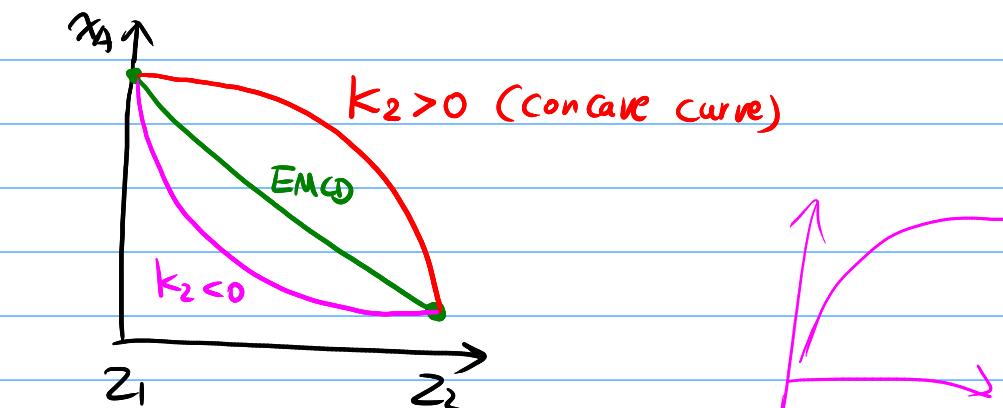
$$N_A = \frac{C_T D_{AB}}{Z_2 - Z_1} \left[ \frac{N_A}{N_A + N_B} \right] \ln \left( \frac{\frac{N_A}{N_A + N_B} - x_{A2}}{\frac{N_A}{N_A + N_B} - x_{A1}} \right)$$
$$= \frac{C_T D_{AB}}{Z_2 - Z_1} \cdot s \cdot \ln \left( \frac{s - x_{A2}}{s - x_{A1}} \right)$$

Stagnant B  $s=1 \Rightarrow$  See L02

Slide 12 General solution of  $x_A(z)$   
See Homework 1

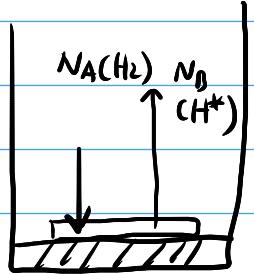
$$x_A = s - k_1 e^{k_2 z}$$

what it looks like



# Slide 14

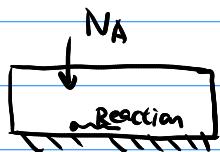
Case I Catalyst at bottom



Mass Balance

Mass Balance

At catalyst surface



$$\text{In} - \text{Out} + \text{Gen} = \text{Acc}$$

$N_A$	0	$-r_{H_2}$	0	for $H_2$
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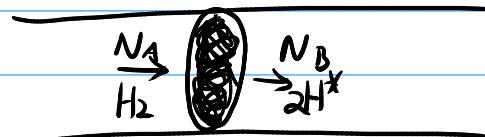
(assumption rate)

0	$N_B$	$r_t = 2r_{H_2}$	for $H^+$
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(generation rate)

$$\begin{aligned} N_A &= r_{H_2} \\ N_B &= -2r_{H_2} \end{aligned} \quad \left\{ \Rightarrow N_B = -2N_A \right.$$

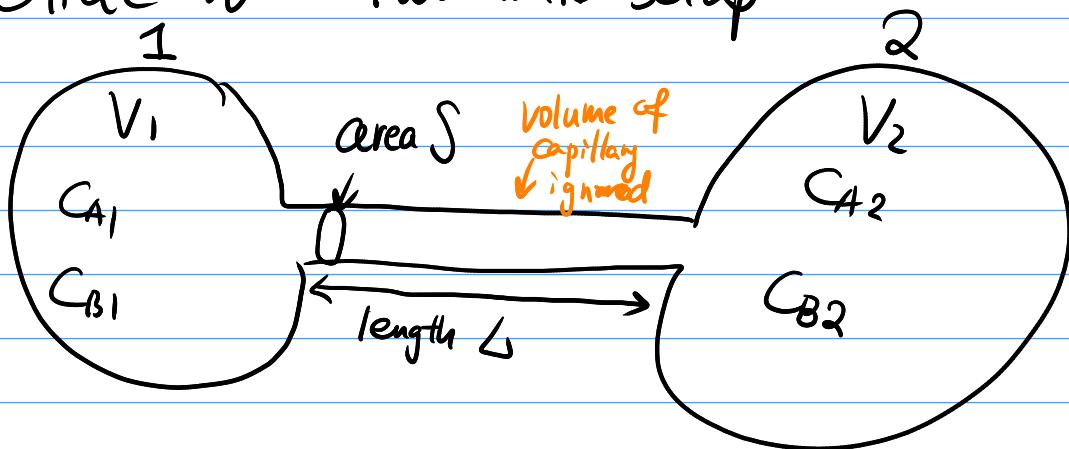
Case 2 Gas pass through porous catalyst in tube



$$\text{Similarly } N_B = 2N_A$$

$N_B / N_A$  ratio must be predetermined  
to solve  $N_A$  !

# Slide 16 Two Bulb setup



Before opening valve

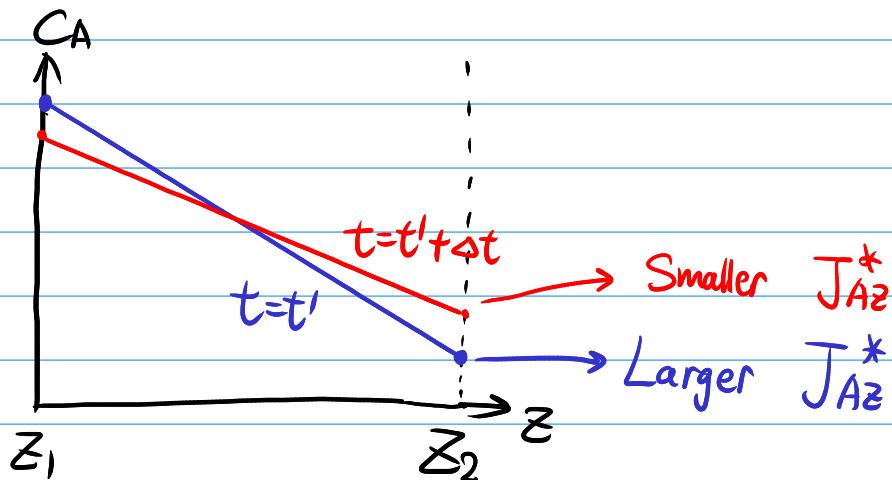
$$C_{A1} = C_A^\circ \quad C_{B1} = C_B^\circ \quad C_{Av} = \frac{V_1 C_A^\circ + V_2 C_A^\circ}{V_1 + V_2}$$

$$= \frac{V_1 C_{A1} + V_2 C_{A2}}{V_1 + V_2}$$

Pseudo-Steady State (P.S.S) *at any time*

At each  $t \Rightarrow C_A(z)$  is linear  $\Rightarrow J_{A2}^* = D_{AB} \frac{C_{A1} - C_{A2}}{L}$

But  $C_{A1}, C_{A2}$  change over time !



## Mass Balance for B

$$\text{In} - \text{Out} + \text{Gen} = \text{Acc}$$

$$S \cdot N_A \quad 0 \quad 0 \quad \frac{dC_{A2}}{dt} \cdot V_2$$

$$S \cdot D_{AB} \frac{C_{A1} - C_{A2}}{L} = \frac{dC_{A2}}{dt} V_2$$

$$\text{Integrate over } t \Rightarrow \ln \left( \frac{C_{A,av} - C_{A2}(t=t_e)}{C_{A,av} - C_{A2}(t=0)} \right) = -D_{AB} \cdot \frac{V_{TS}}{V_1 V_2 L} \cdot t$$

Are we correct? Check unit

$$\ln \left( \boxed{\quad} \right) \rightarrow \text{Dimensionless}$$

$$D_{AB} \cdots \left[ \frac{m^2}{s} \right]$$

$$\frac{V_{TS}}{V_1 V_2 L} \cdots \left[ \frac{m^3 \cdot m^2}{m^3 \cdot m^3 \cdot m} \right] \cdots \left[ \frac{1}{m^2} \right]$$

$$R.H.S \cdots \left[ \frac{m^2}{s} \right] \left[ \frac{1}{m^2} \right] [s] \cdots \text{Dimensionless} \checkmark$$