

CHE318 L03

Jan - 09 2026

Slide 7

$$N_A = \frac{C_T D_{AB}}{z_2 - z_1} \left[\frac{N_A}{N_A + N_B} \right] \ln \left(\frac{\frac{N_A}{N_A + N_B} - x_{A2}}{\frac{N_A}{N_A + N_D} - x_{A1}} \right)$$

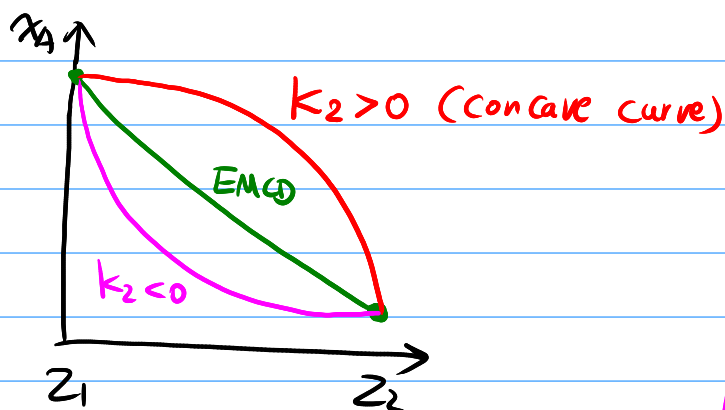
$$= \frac{C_T D_{AB}}{z_2 - z_1} \cdot S \cdot \ln \left(\frac{S - x_{A2}}{S - x_{A1}} \right)$$

Stagnant B $S=1 \Rightarrow$ See L02

Slide 12 General solution of $x_A(z)$
See Homework 1

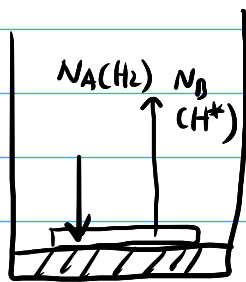
$$x_A = S - K \cdot e^{k_2 z}$$

what it looks like



Slide 14

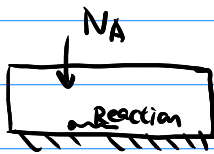
Case 1 Catalyst at bottom



Mass Balance

Mass Balance

At catalyst surface



$$I_n - \text{Out} + \text{Gen} = A_{cc}$$

$$\begin{matrix} N_A & 0 & -r_{H_2} & 0 & \text{for } H_2 \\ & & \text{(assumption rate)} & & \end{matrix}$$

$$\begin{matrix} 0 & N_B & r_H = 2r_{H_2} & & \text{for } H^+ \\ & & \text{(generation rate)} & & \end{matrix}$$

$$\left. \begin{matrix} N_A = r_{H_2} \\ N_B = -2r_{H_2} \end{matrix} \right\} \Rightarrow N_B = -2N_A$$

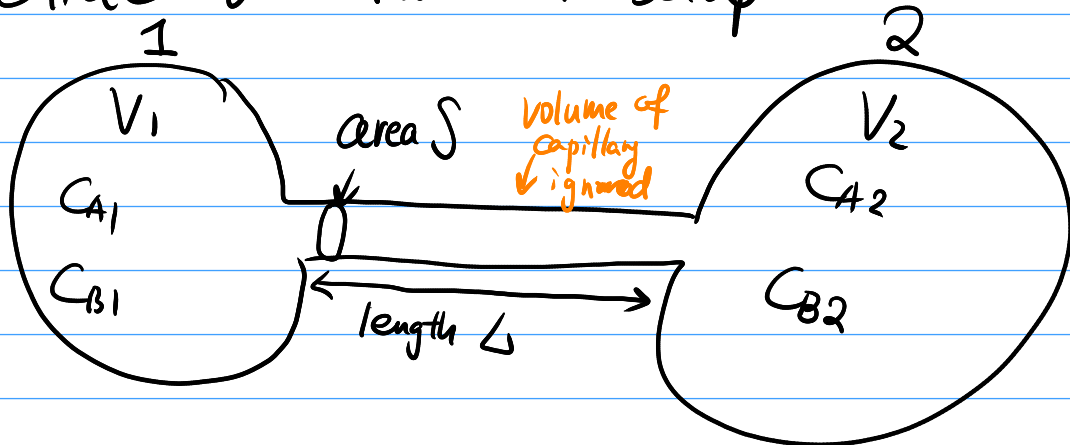
Case 2 Gas pass through porous catalyst in tube



$$\text{Similarly } N_B = 2N_A$$

N_B / N_A ratio must be predetermined to solve N_A !

Slide 16 Two Bulb Setup



Before opening valve

$$C_{A1} = C_A^0$$

$$C_{B1} = C_B^0$$

Average conc

$$C_{AV} = \frac{V_1 C_A^0 + V_2 C_B^0}{V_1 + V_2}$$

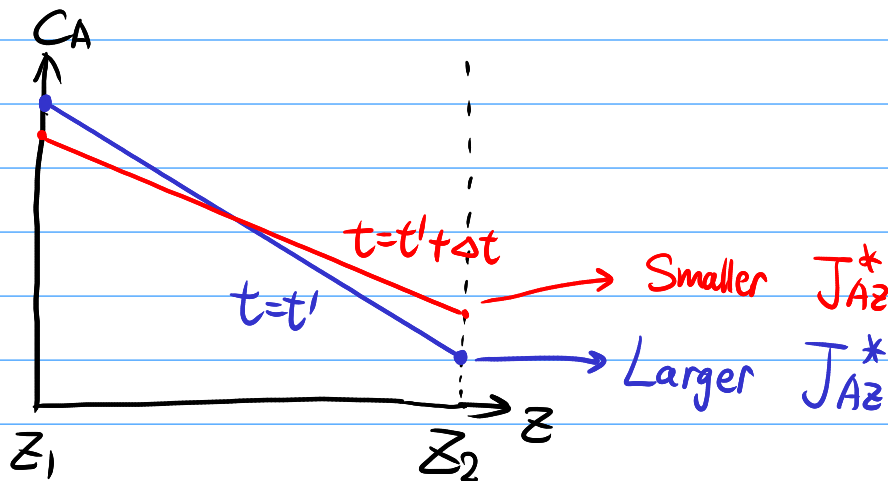
$$= \frac{V_1 C_{A1} + V_2 C_{A2}}{V_1 + V_2}$$

at any time

Pseudo-Steady State (P.S.S)

At each $t \Rightarrow C_A(z)$ is linear $\Rightarrow J_{Az}^* = D_{AB} \frac{C_{A1} - C_{A2}}{L}$

But C_{A1} , C_{A2} change over time!



Mass Balance for B

$$I_n - O_{out} + G_{en} = A_{ce}$$

$$S \cdot N_A \quad 0 \quad 0 \quad \frac{dC_{A2}}{dt} \cdot V_2$$

$$S \cdot D_{AB} \frac{C_{A1} - C_{A2}}{L} = \frac{dC_{A2}}{dt} V_2$$

$$\text{Integrate over } t \Rightarrow \ln \left(\frac{C_{A,av} - C_{A2}(t=t_e)}{C_{A,av} - C_{A2}(t=0)} \right) = -D_{AB} \cdot \frac{V_T S}{V_1 V_2 L} \cdot t$$

Are we correct? Check unit

$$\ln(\boxed{}) \rightarrow \text{Dimensionless}$$

$$D_{AB} \dots \left[\frac{m^2}{s} \right]$$

$$\frac{V_T S}{V_1 V_2 L} \dots \left[\frac{m^3 \cdot m^2}{m^3 \cdot m^3 \cdot m} \right] \dots \left[\frac{1}{m^2} \right]$$

$$\text{R.H.S} \dots \left[\frac{m^2}{s} \right] \left[\frac{1}{m^2} \right] [s] \dots \text{Dimensionless} \checkmark$$