

We have seen

1) k_c' \rightarrow simple form to $N_A = k_c'(C_{A1} - C_{A2})$

2) k_c' can be taken from theories

Film

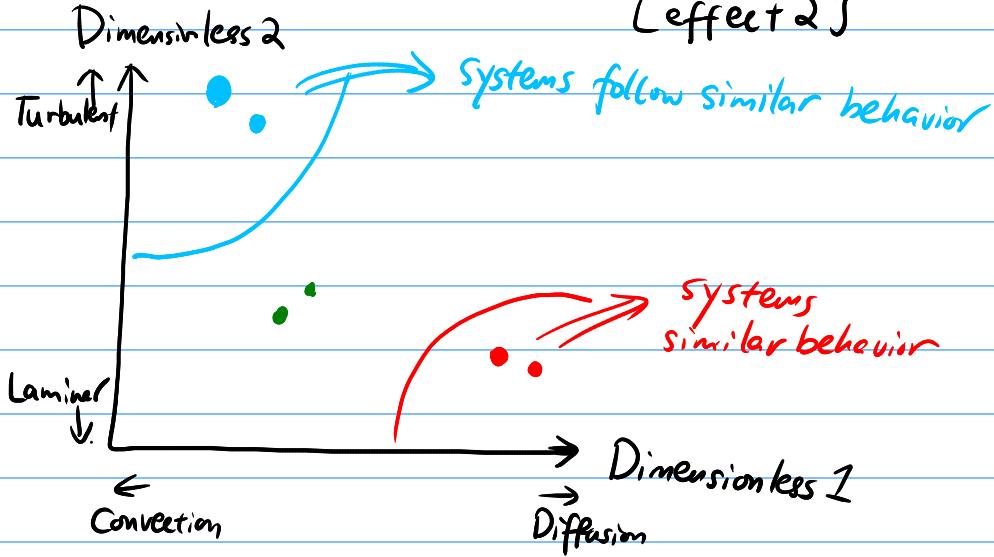
Penetration

Boundary layer

What if 1) We're interested in getting accurate k_c'
2) Measured k_c' , can we apply to other geometry?

We can use "Dimensionless Analysis"

Dimensionless number = $\frac{[\text{effect 1}]}{[\text{effect 2}]}$



$$N_{Sc} \text{ (Schmidt Nr)} = \frac{\mu}{\rho D_{AB}} = \frac{[\text{momentum diff}]}{[\text{molar diff}]} \\ \text{also } \frac{\delta}{Sc} = N_{Sc}^{\frac{1}{3}}$$

$$N_{Sh} \text{ (Sherwood Nr)} = \frac{k_c' L}{D_{AB}} = \frac{[conv \ m.t.]}{[diff \ m.c.]}$$

$$N_{Re} \text{ (Reynolds Nr)} = \frac{\nu P L}{\mu} = \frac{\nu L}{(\frac{M}{\rho})} = \frac{[kinetic \ transp]}{[viscosity \ transp]}$$

How do we correlate k_c' ?

Chilton-Colburn j -factor

(same factor for momentum / heat / mass transfer)

For mass transfer

$$\bar{j}_D = \frac{k_c'}{v_{av}} (N_{Sc})^{\frac{2}{3}} = f \Rightarrow \text{Fanning friction factor}$$

\uparrow
average fl. velocity

Solution process

Calculate

N_{Re}
(fluid alone
from geometry)

$$N_{Re} < 2100$$

Laminar flow

$$f = \frac{16}{N_{Re}} \xrightarrow[N_{Sc}]{} \bar{j}_D = \frac{f}{2}$$

$$\boxed{\text{Get } k_c' = j_D \cdot v_{av} (N_{Sc})^{-\frac{2}{3}}}$$

$$N_{Re} > 2100$$

Turbulent flow

$$f = \frac{C_f}{2 \rho v^2} = \frac{\Delta P_f \pi R^2}{2 \pi R \delta L} / \left(\frac{\rho v^2}{2} \right)$$

$$j_p = \frac{f}{2}$$

More generally

$$\boxed{\bar{j}_D = \frac{f}{2} = \frac{N_{Sh}}{N_{Re} N_{Sc}^{\frac{2}{3}}}}$$

has k_c'

Most likely, we use dimensionless analysis
on an established chart



$$\frac{W}{D_{AB} \rho L} \text{ determines exit concentration}$$

$$\frac{W}{D_{AB} \rho L} = N_{Re} N_{Sc} \cdot \frac{\frac{Ag/s}{m^2 \cdot s \cdot m}}{\frac{D}{4}}$$

1) Gas (use rod-like flow curve)

2) Liquid $\frac{W}{D_{AB} \rho L} > 400$ parabolic flow

A schematic diagram of a pipe with a circular cross-section. Inside the pipe, a curved arrow starts at the bottom left, rises to a peak in the center, and then descends to the bottom right, representing a parabolic flow profile.

$$\frac{C_A - C_{A,0}}{C_{A,i} - C_{A,0}} = S_J \left(\frac{W}{D_{AB} \rho L} \right)^{-2/3}$$

3) Liquid/Gas turbulent flow

$N_{Re} > 2000$ If $0.6 < N_{Sc} < 3000$

$$N_{sh} = k_c' \left(\frac{D}{D_{AB}} \right) = 0.023 \left(\frac{\rho D u}{\mu} \right)^{0.83} \left(\frac{\mu}{\rho D_{AB}} \right)^{0.33}$$

$\underbrace{\qquad}_{N_{Re,D}}$ $\underbrace{\qquad}_{N_{Sc}}$

1) (very close to the j-D analog)

2) We just need $N_{Re,D}$ $N_{Sc} \Rightarrow k_c'$

3) Only applicable for pipe! (& N_{Sc} range)

Solution procedure

Geometry ? $\xrightarrow{\text{not pipe}}$ choose other eqn.

↓ pipe

Calculate N_{Re} $\xrightarrow{\text{laminar}} \frac{W}{D_{AB} \rho U} > 400 ?$ $\xrightarrow{\gamma} \left\{ \begin{array}{l} \frac{C_A - C_{A0}}{C_{Ai} - C_{A0}} = \left(\frac{W}{D_{AB} \rho U} \right)^{-3} \\ \cdot 5.5 \\ k_C' \text{ from } j_0 \end{array} \right.$

↓ turbulent

$0.6 < N_{Sc} < 3000 ?$ $\xrightarrow{\gamma}$

$$k_C' \left(\frac{D}{D_{AB}} \right) = 0.023 N_{Re}^{0.83} N_{Sc}^{0.33}$$

Case II FI