



**BURSA TECHNICAL UNIVERSITY  
INSTITUTE OF NATURAL AND APPLIED SCIENCES  
DEPT. OF MECHANICAL ENGINEERING**

<i>STUDENT NAME:</i>	
<i>COURSE TITLE:</i>	MECH 603 Advanced Mechanical Vibrations
<i>ASSIGNMENT TITLE:</i>	Deriving equations of motion
<i>ASSIGNMENT NUMBER</i>	1

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**DATE** 2013

**SCORE**

**LECTURER NAME:** Assist. Prof. Dr. Hakan Gökdağ **SIGNED:** .....

**DATE:**.....

**Student declaration: (must be signed before submission)**

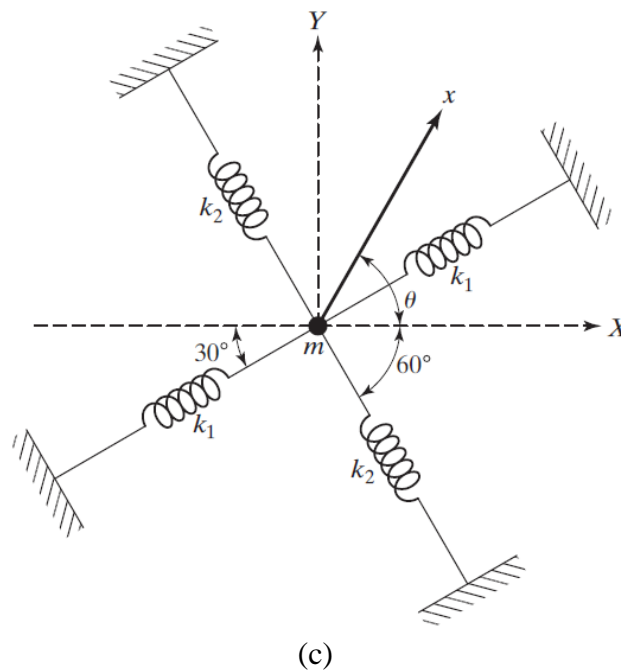
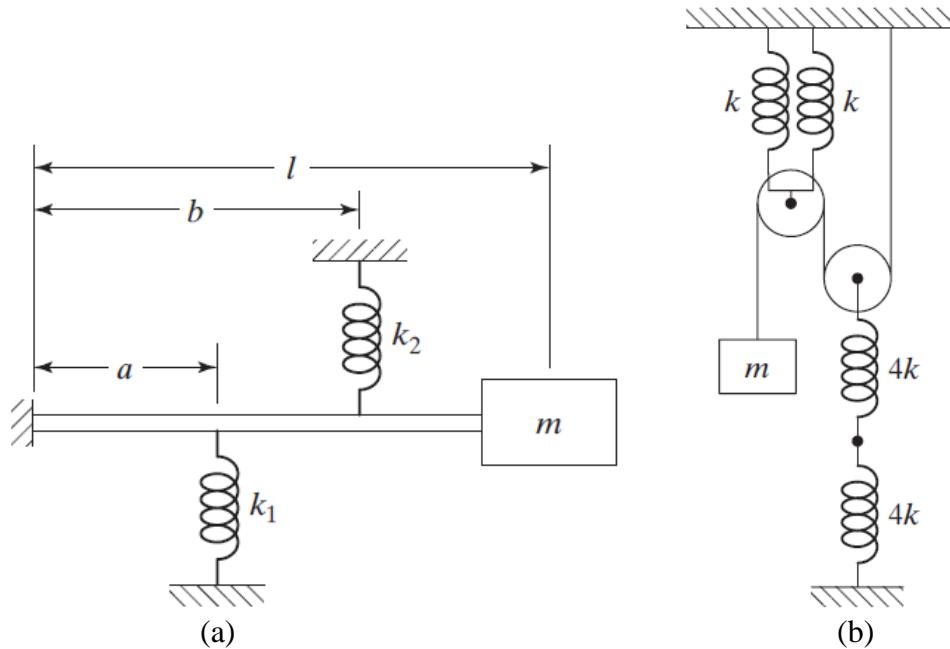
**I declare that this assignment is my own work**

**Student signature:** .....

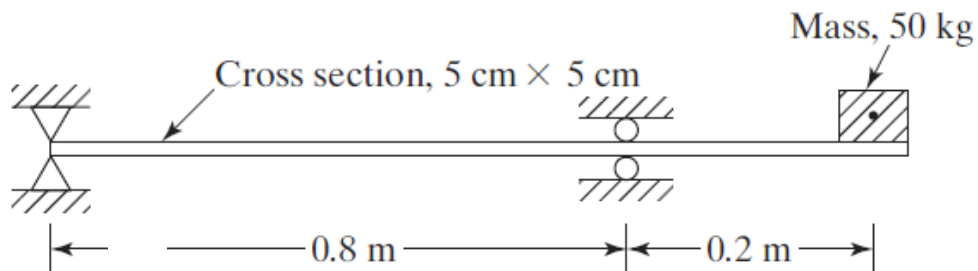
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Please solve the following problems giving sufficient explanations.

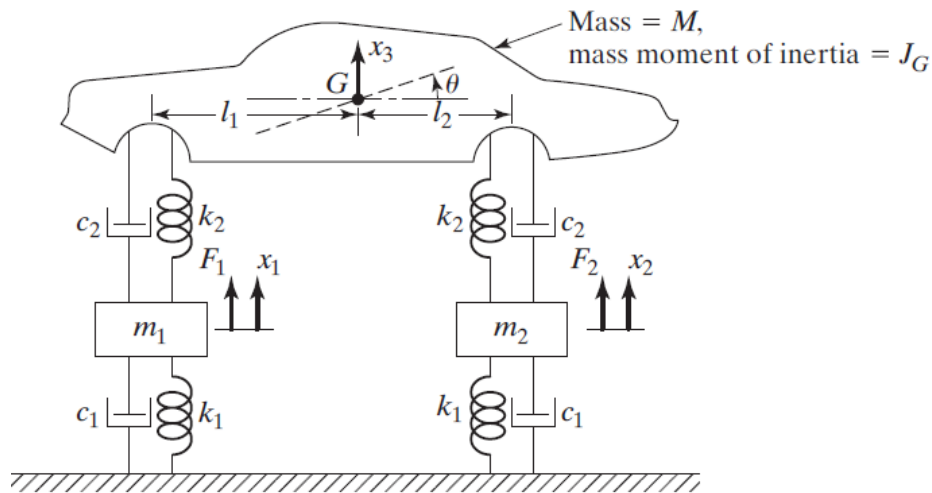
**(1)** Derive the equation of motion, for small displacements, of these single-DOF systems, using: (i) Newton's 2<sup>nd</sup> law of motion, (ii) Lagrange's equations. Note: The masses of rigid rod at (a), and the pulleys at (b) are negligible.



**(2)** A steel beam of length 1 m carries a mass of 50 kg at its free end, as shown in the following figure. Derive equation of motion for vertical motion of the system by modeling it as a single-degree-of-freedom system.



**(3)** Half car model of a vehicle is as shown. Derive equations of motion of the system by (i) Newton's approach, (ii) Lagrange equations.



**(4)** Using Hamilton's principle derive equation of motion for the vertical vibrations of the beam along with suitable boundary conditions. Note that the beam is supported by a torsional spring ( $k_t$ ) at the left end, and a linear spring ( $k$ ) at the right side.

