

Type





```
def getCurrency(country: Country): Option[String] =
  country.value match {
    case "United Kingdom" => Some("GBP")
    case "France" | "Germany" => Some("EUR")
    case _ => None
}
```



```
def getCurrency(country): Option [String] =
  country.value match {
    case "United Kingdom" => Some("GBP")
    case "France" | "Germany" => Some("EUR")
    case _ => None
}
```

```
scala> getCurrency(Country("UK"))
res0: Option[String] = None

scala> getCurrency(Country("GBR"))
res1: Option[String] = None

scala> getCurrency(Country("Royaume-Uni"))
res2: Option[String] = None
```



```
import Country._

def getCurrency(country: Country): String =
   country match {
    case UnitedKingdom => "GBP"
     case France | Germany => "EUR"
   }
```

```
def parseCountry(country: String): Option[Country] = ???
```



```
sealed trait Country
object Country {
    case object UnitedKingdom extends Country
    case object France extends Country
    case object Germany extends Country
}

sealed trait Currency
object Currency {
    case object BritishPound extends Currency
    case object Euro extends Currency
}
```

```
import Country._, Currency._

def getCurrency(country: Country): Currency =
   country match {
    case UnitedKingdom => BritishPound
    case France | Germany => Euro
   }
```



Plan

- What is the cost of misusing types
- How to use ADTs to encode data
- Learn how to measure impact of types and tests
- Explore relationship between types, algebra and logic



Exercise 1: Misused types

exercises.types.TypeExercises.scala



Type should exactly fit business requirements



Imprecise data lead to errors and misleading documentation



How should we encode data?



Algebraic Data Type (ADT)

- OR, a ConfigValue is
 - a String OR
 - o an Int OR
 - Empty
- AND, a User is
 - o an userId AND
 - ∘ a name AND
 - o an address



OR

- a Boolean is true OR false
- an Int is a -10 OR 0 OR 1 OR ...
- a DayOfTheWeek is Monday OR Tuesday OR Wednesday OR ...
- an Option is a Some OR a None
- \bullet a Json is a JsonNumber OR a JsonString OR a JsonArray OR a JsonObject OR ...



How should we encode OR?

A ConfigValue is a String OR an Int OR Empty



OR Encoding

```
object ConfigValue {
  case class ConfigString(value: String) extends ConfigValue
  case class ConfigNumber(value: Double) extends ConfigValue
  case object ConfigEmpty extends ConfigValue
}
```



OR Encoding

```
object ConfigValue {
  case class ConfigString(value: String) extends ConfigValue
  case class ConfigNumber(value: Double) extends ConfigValue
  case object ConfigEmpty extends ConfigValue
}
```

In Scala 3

```
enum ConfigValue {
  case ConfigString(value: String)
  case ConfigNumber(value: Double)
  case ConfigEmpty
}
```



AND

- a User is a userId AND a name AND an address
- a ZonedDateTime is a dateTime AND a timeZone
- a NonEmptyList is a head AND a tail
- a Tuple2 is a _1 AND a _2



How should we encode AND?

A User is a user Id AND a name AND an address



AND Encoding

```
import java.util.UUID

case class User(userId: UUID, name: String, address: Address)

case class Address(streetNumber: Int, streetName: String, postCode: String)
```

scala> User(UUID.randomUUID(), "John Doe", Address(108, "Cannon Street", "EC4N 6EU"))

res3: User = User(080efd71-c292-4827-895c-488f4789c446, John Doe, Address(108, Cannon Street, EC4N 6EU))



Algebraic data types mix AND and OR

```
object Role {
  case class Reader(accountId: Long, premiumUser: Boolean) extends Role
  case class Editor(accountId: Long, favoriteFont: Option[String]) extends Role
  case object Admin extends Role
}
case class User(userId: Long, role: Role, address: Option[Address])
```



Exercise 2: Data Encoding

exercises.types.TypeExercises.scala



Case class and sealed trait map exactly to business language AND and OR

Nested AND and OR form what is called Algebraic Data Types (ADTs)



ADT allow to encode data precisely



How can we compare two encodings?

```
def getCurrency(country: String): Option[String]
```

Is it better to reduce input or reduce output?

```
def getCurrency(country: Country): String

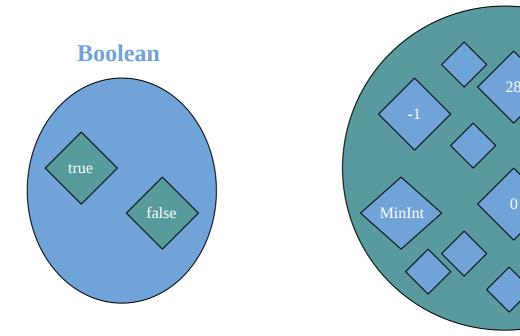
def getCurrency(country: String): Option[Currency]
```

How much better it is to reduce both?

```
def getCurrency(country: Country): Currency
```



Type is a set

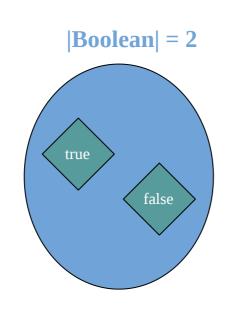


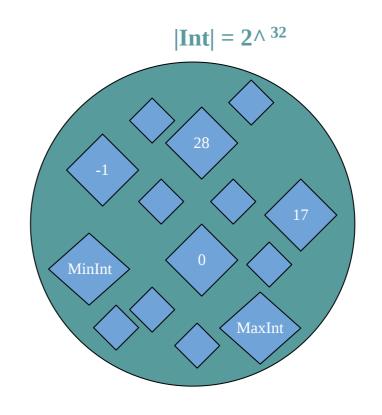
Int

MaxInt



Cardinality







Exercise 3: Cardinality

exercises.types.TypeExercises.scala



Sealed trait

```
case class AnInt(value: Int) extends IntOrBoolean
case class ABoolean(value: Boolean) extends IntOrBoolean
```

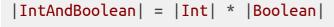
```
AnInt(Int.MinValue) // ~ -2 billion
...
AnInt(0)
AnInt(1)
...
AnInt(Int.MaxValue) // ~ +2 billion
ABoolean(false)
ABoolean(true)
```

```
|IntOrBoolean| = |AnInt| + |ABoolean|
= |Int| + |Boolean|
```



Case class

```
case class IntAndBoolean(i: Int, b: Boolean)
IntAndBoolean(Int.MinValue, false) // ~ -2 billion
IntAndBoolean(0, false)
IntAndBoolean(1, false)
IntAndBoolean(Int.MaxValue, false) // ~ +2 billion
IntAndBoolean(Int.MinValue, true) // ~ -2 billion
IntAndBoolean(0, true)
IntAndBoolean(1, true)
IntAndBoolean(Int.MaxValue, true) // ~ +2 billion
```





A sealed trait is called a sum type

A case class is called a product type



$$|A OR B OR C| = |A| + |B| + |C|$$

$$|A AND B AND C| = |A| * |B| * |C|$$

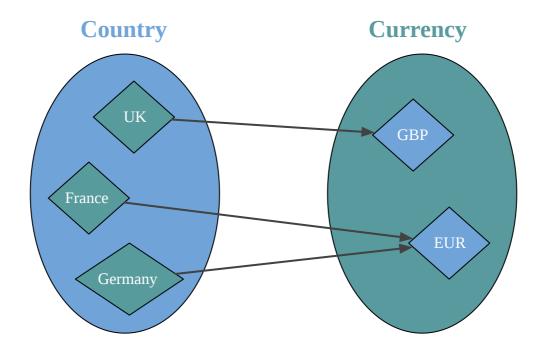


Finish Exercise 3

exercises.types.TypeExercises.scala

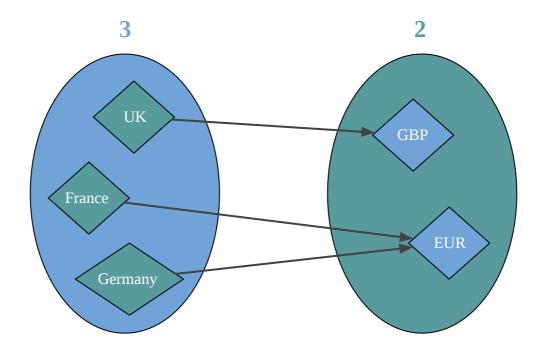


|Country => Currency |



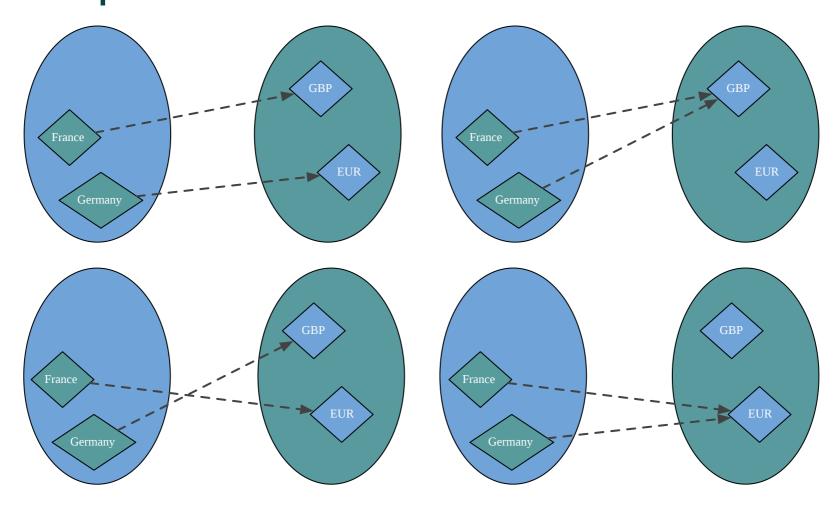


3 => 2



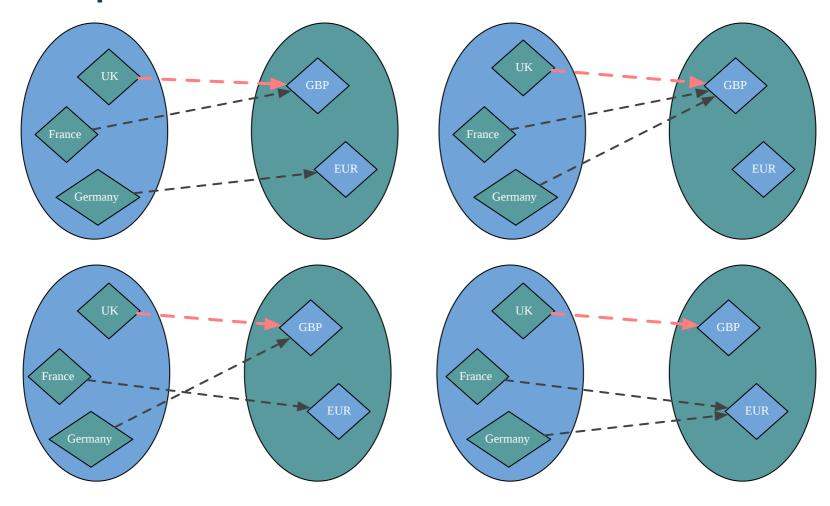


|2 => 2| = 4





3 => 2



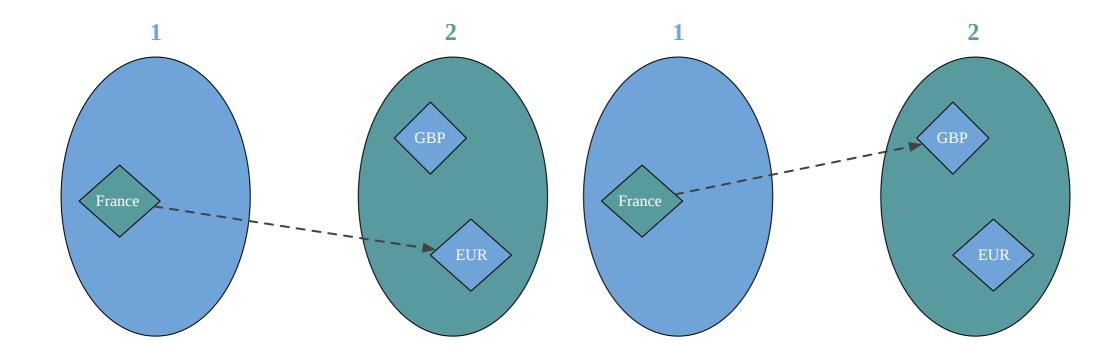








1 => 2 = 2









$$|A => B| = |B| ^ |A|$$

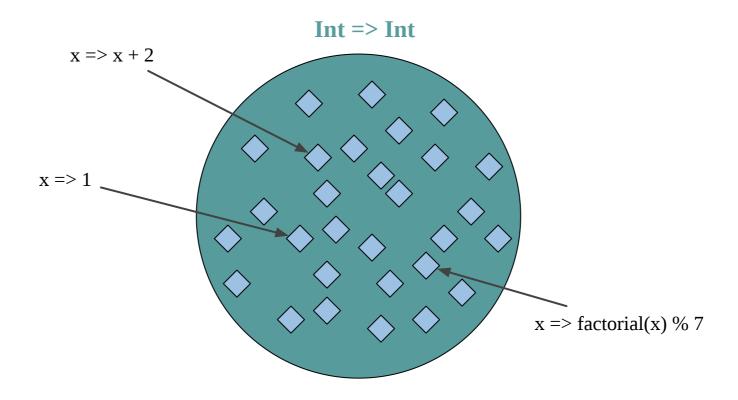


Exercise 4: Parametricity

exercises.types.TypeExercises.scala

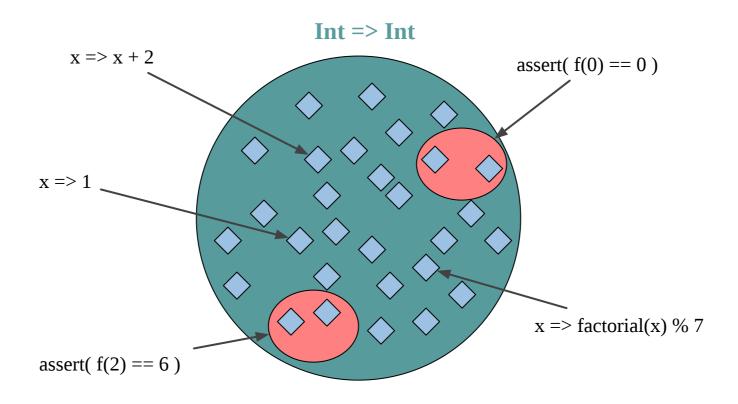


Functions are sets!





Unit tests

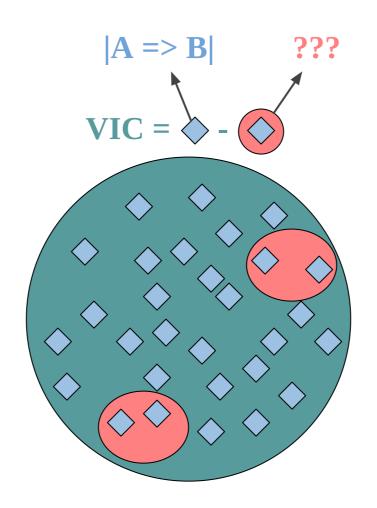




Valid Implementation Count (VIC)

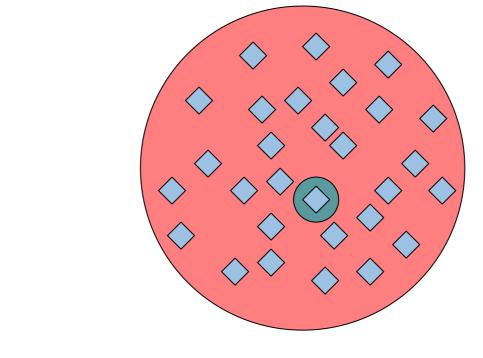








VIC(f) = 1







Exercise 5: Tests

exercises.types.TypeExercises.scala



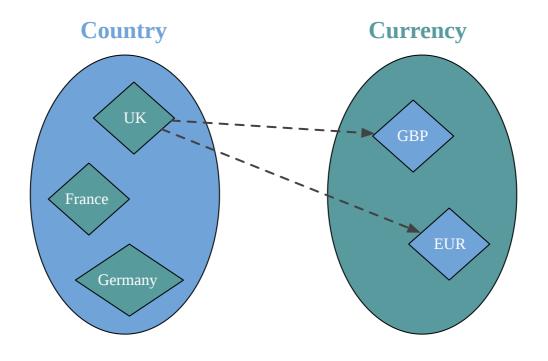
Unit Test

such as

```
assert(getCurrency(France) == EUR)
```

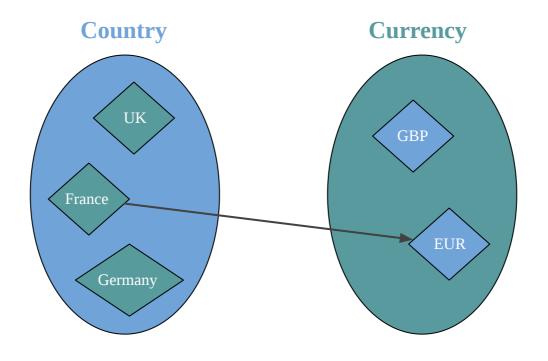


VIC(getCurrency) = 2 * ...



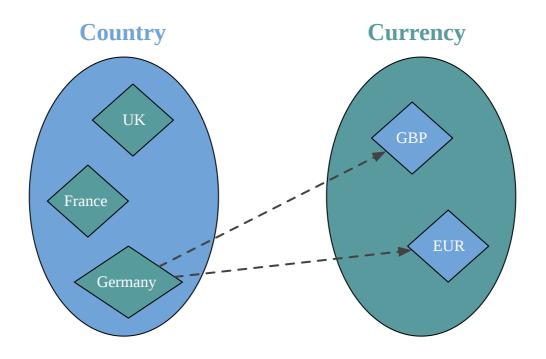


VIC(getCurrency) = 2 * 1 * ...





VIC(getCurrency) = 2 * 1 * 2





$$VIC(f: A => B) = |B| ^ (|A| - n)$$

where n is the number of unit tests



Exercise 6: Type Algebra

exercises.types.TypeExercises.scala



Type Algebra

Туре	Algebra	
Nothing	0	
Unit	1	
Either[A, B]	A + B	
(A, B)	A * B	
A => B	B ^ A	
Isomorphism	A == B	



Curry—Howard isomorphism

Propositions as types from Philip Wadler



Type Algebra Logic

Туре	Algebra	Logic
Nothing	0	\perp
Unit	1	Т
Either[A, B]	A + B	АνВ
(A, B)	A * B	АлВ
A => B	B ^ A	A → B
Isomorphism	A == B	A ⇔ B



Either[A, Nothing] == A



Either[A, Nothing] == A

 $A V \perp \Leftrightarrow A$



(A, Nothing) == Nothing



(A, Nothing) == Nothing

 $A \land \bot \Leftrightarrow \bot$



Find the representation that makes sense to you

```
Either[Int, String] => Boolean <==> (Int => Boolean, String => Boolean)
```



Find the representation that makes sense to you

```
Either[A, B] => C <==> (A => C, B => C)
```



Find the representation that makes sense to you

```
Either[A, B] => C <==> (A => C, B => C)
```

Algebra

Logic

```
Either[A, B] => C = (A V B) \rightarrow C
= (A \rightarrow C) \wedge (B \rightarrow C)
= (A => C, B => C)
```



Summary

- Cardinality of types matters
- Unit tests offer almost no benefit in term of correctness
- VIC(f: A => B) = |B| ^ (|A| n)
- Two techniques to achieve correctness
 - Property based testing
 - Parametric polymorphism



All dynamic languages are static languages with a single type



Any



Any => Any

```
def inc(value: Any): Any = value match {
  case x: Int => x + 1
  case x: Double => x + 1
  case x: Char => x.toString + "1"
  case x: String => x + "1"
}
```



Any => Any

```
def inc(value: Any): Any = value match {
   case x: Int => x + 1
   case x: Double => x + 1
   case x: Char => x.toString + "1"
   case x: String => x + "1"
}
```

```
scala> inc(5)
res4: Any = 6

scala> inc(10.3)
res5: Any = 11.3

scala> inc('c')
res6: Any = c1
```

```
scala> inc(java.time.Instant.ofEpochMilli(0))
scala.MatchError: 1970-01-01T00:00:00Z (of class java.time.Instant)
  at .inc(<console>:2)
  ... 42 elided
```



$$VIC(Any => Any) = |Any| \sim (|Any| - n)$$

where n is the number of unit tests



Resources and further study

- <u>Programming with Algebra</u>: property based testing with storage
- Much Ado About Testing: property based testing best practices and pitfalls
- Choosing properties for property-based testing
- Property-Based Testing in a Screencast Editor
- Property-Based Testing The Ugly Parts: Case Studies from Komposition
- <u>Types vs Tests</u>
- Counting type inhabitants
- Thinking with types: type, algebra, logic
- <u>Propositions as types</u>: Curry–Howard isomorphism



Module 6: Typeclass

