Weaver Spring 2021

## CS 161 Computer Security

Discussion 6

## Midterm Review - Asymmetric Cryptography

What	erm Review - Asymmetric O	ryptograpny
Questic	on 1 True/false	0
Q1.1	True or False: If the discrete-log problem calculate $a$ given $g^a \mod p$ ), ElGamal encry	· · · · · · · · · · · · · · · · · · ·
	O TRUE	O FALSE
Q1.2	TRUE or FALSE: If Eve acquires access to <b>both</b> Alice and Bob's private signature keys, the communication channel is no longer confidential.	
	O TRUE	O FALSE
Q1.3	TRUE or FALSE: To use ElGamal encrypt should break up the message into small bloc ElGamal.	
	O TRUE	O FALSE

then	t to preserve the confidentiality of Alice's bid, but the communication channel between n is insecure. Therefore, they decide to use the ElGamal public key encryption scheme in er to communicate privately.		
Instead of using the traditional version of the ElGamal scheme, Alice and Bob use the following variant. As usual, Bob's private key is $x$ and his public key is $PK = (p, g, h)$ , where $h = g^x \mod p$ . However, to send a message $M$ to Bob, Alice encrypts $M$ as $Enc_{PK}(M) = (s, t)$ , where $s = g^r \mod p$ and $t = g^M \times h^r \mod p$ , for a randomly chosen $r$ .			
Q2.1	Consider two distinct messages $m_1$ and $m_2$ . Let $Enc_{PK}(m_1) = (s_1, t_1)$ and $Enc_{PK}(m_2) = (s_2, t_2)$ . For the given variant of the ElGamal scheme, which of the following is true?		
	$(s_1 + s_2 \mod p,  t_1 + t_2 \mod p)$ is a possible value for $\operatorname{Enc}_{PK}(m_1 + m_2)$ .		
	$(s_1 \times s_2 \mod p,  t_1 \times t_2 \mod p)$ is a possible value for $Enc_{PK}(m_1 + m_2)$ .		
	$(s_1 \times s_2 \mod p,  t_1 \times t_2 \mod p)$ is a possible value for $Enc_{PK}(m_1 \times m_2)$ .		
	$(s_1 + s_2 \mod p,  t_1 + t_2 \mod p)$ is a possible value for $\operatorname{Enc}_{PK}(m_1 \times m_2)$ .		
	O None of these		
Q2.2	2.2 In order to decrypt a ciphertext $(s, t)$ , Bob starts by calculating $q = ts^{-x} \mod p$ . Assume that the message $M$ is between 0 and 1000. How can Bob recover $M$ from $q$ ?		
Q2.3	Explain why Bob cannot efficiently recover $M$ from $q$ if $M$ is randomly chosen such that $0 \le M < p$ .		

Bob wants his pipes fixed and invites independent plumbers to send him bids for their services (*i.e.*, the fees they charge). Alice is a plumber and wants to submit a bid to Bob. Alice and Bob

(15 min)

Question 2 ElGamal and friends

Q2.4 Suppose Alice sends Bob a bid  $M_0 = 500$ , encrypted under Bob's public key. We let  $C_0 = (s, t)$  be the ciphertext here.

Mallory is an active man-in-the-middle attacker who knows Alice's bid is  $M_0 = 500$ . Mallory wants to replace Alice's bid with  $M_1 = 999$ . To do that, Mallory intercepts  $C_0$  and replaces it with another ciphertext  $C_1$ . Mallory wishes that when Bob decrypts  $C_1$ , Bob sees  $M_1 = 999$ .

Describe how Mallory creates  $C_1$  in each of the following situations:

- 1. Mallory didn't obtain  $C_0$ , but knows Bob's public key PK = (p, g, h).
  - ♦ Question: How should Mallory create  $C_1$ ?

- 2. Mallory knows Alice's ciphertext  $C_0$ , but only knows p and g in Bob's public key PK = (p, g, h). (That is to say, Mallory does not know h.)
  - $\diamond$  Question: How should Mallory create  $C_1$ ?