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Part1

"Liker" liked some post of "liked"

Liked(liker, liked):=

 $\Pi_{\text{Likes.liker, Post.pid}}(\sigma_{\textit{Likes.pid}} = Post.pid} \text{ (Likes} \times Post))$

"Viewer" viewed some story of "viewed"

Viewed(viewer, viewed):=

 $\Pi_{Saw.viewerid, Story.sid}(\sigma_{Saw.sid = Story.sid}(Saw \times Story))$

"Uid1" liked some post or viewed some story of "uid2" and

"Uid1" did not followed "uid2"

NotSat(uid1, uid2):=

Liked \cup Viewed $-\Pi_{\text{follower, followed}}$ (Follows)

"Uid" never liked some post or viewed some story of user whom he did not follow

Sat(uid):=

$$\Pi_{uid}(User) - \Pi_{uid1}(NotSat)$$

Report

Result(username, description):=

 $\Pi_{User.name, User.about}(\sigma_{User.uid = Sat.uid}(User \times Sat))$

"Pid" is posted in 2017 along with its posted date and tag

PostTag17(pid, date, tag):=

 $\Pi_{Post.pid, \ when, \ Hashtag.tag}(\sigma_{when.year = \ 2017 \ \land \ Post.pid = \ Hashtag.pid}(Post \times Hashtag))$

Join of all dates and all tags of 2017

All(date, tag):=

 $\Pi_{when.date}(\sigma_{when.year = 2017}(Post)) \times \Pi_{tag}(PostTag17)$

"Tag" was mentioned in 2017 but was not mentioned everyday in 2017

NotEveryday(tag):=

 $\Pi_{tag}(All - \Pi_{date, tag}(PostTag17))$

"Tag" was mentioned everyday in 2017

Everyday(tag):=

 $\Pi_{tag}(PostTag17) - NotEveryday$

"Tag" was mentioned at least 3 times everyday in 2017

result(tag):=

 $\Pi_{\text{Everyday.tag}} \left(\sigma_{(p1.tag = p2.tag = p3.tag = Everyday.tag)} \right. \wedge \left. (p1.tag \neq p2.tag \wedge p1.tag \neq p3.tag \wedge p2.tag \neq p2.tag \right)$

 $\rho_{p3.tag}(\rho_{p1} (PostTag17) \times \rho_{p2} (PostTag17) \times \rho_{p3} (PostTag17) \times Everyday))$

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"Uid1", "uid2" are reciprocal follower and "uid1" > "uid2"
ReciprocalFollower(uid1, uid2):=
\Pi_{\text{fl.followed, fl.follower}} \left( \sigma_{\text{(fl.follower = f2.followed)}} \wedge \text{(fl.followed = f2.follower)} \wedge \text{(fl.follower > f2.followed)} \right)
_{fl.followed)}(\rho_{f2} \text{ (Follows)} \times \rho_{f1} \text{ (Follows))})
"Follower" followed "uid1"
uid1Follower(uid1, uid2, follower):=
\Pi_{\text{uid1. uid2. follower}}(\sigma_{\text{uid1} = \text{followed}}(\text{ReciprocalFollower} \times \text{Follows}))
"Follower" followed "uid2"
uid2Follower(uid1, uid2, follower):=
\Pi_{\text{uid1. uid2. follower}}(\sigma_{\text{uid2} = \text{followed}}(\text{ReciprocalFollower} \times \text{Follows}))
"Uid1", "uid2" are reciprocal follower, "follower" are uncommon
follower of "uid1", "uid2"
UncommonFollower(uid1, uid2, follower):=
(uid1Follower ∪ uid2Follower) − (uid1Follower ∩ uid2Follower)
Report
result(uid1, uid2, follower, name, email):=
\Pi_{uid1,\;uid2,\;follower,\;name,\;email}\left(\sigma_{follower\;=\;uid}\left(UncommonFollower\;\times\;User\right)\right)
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Can not be expressed

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"Uid1", "uid2" are reciprocal follower and "uid1" > "uid2"
ReciprocalFollower(uid1, uid2):=
\Pi_{\text{f1.followed, f1.follower}} \left( \sigma_{\text{(f1.follower = f2.followed)}} \land \text{(f1.followed = f2.follower)} \land \text{(f1.follower > f2.followed)} \right)
_{fl.followed)}(\rho_{f2} \text{ (Follows)} \times \rho_{fl} \text{ (Follows))})
"Liker" liked some post "pid" of "liked"
Liked(liker, liked, pid):=
\Pi_{liker, Post.uid, Post.pid}(\sigma_{Likes.pid = Post.pid}(Likes \times Post))
Join all liker in likes with all (uid, pid) in Post
All(liker, liked, pid):=
\Pi_{liker}(Likes) \times \Pi_{pid, uid}(Post)
"Liker" did not like every post of "liked"
NotLikedEvery(liker, liked):=
All - Liked
"Liker" liked every post of "liked"
LikedEvery(liker, liked):=
\Pi_{liker, liked} (Liked) - \Pi_{liker, liked} (NotLikedEvery)
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"Uid1", "uid2" liked every post of eachother

ReciprocalLiker(uid1, uid2):=

$$\begin{split} &\Pi_{\text{r1.liker, r1.liked}}(\sigma_{\text{r1.liker} = \text{r2.liked} \ \land \text{r1.liked} = \text{r2.liker}} \ (\rho_{\text{r1}} \ (\text{LikedEvery}) \times \rho_{\text{r2}} \\ &(\text{LikedEvery}))) \end{split}$$

"Uid1", "uid2" are backscratchers

Backscratchers(uid1, uid2):=

 $Reciprocal Follower \cap Reciprocal Liker \\$

"When" is the datetime of some activity of "uid"

WhenActivity(uid, when):=

 $\Pi_{uid.when}(Post) \cup \Pi_{uid.when}(Story)$

"When" is datetime of some activity of "followed", who is followed by "follower" with "name"

WhenFollowedActivity(name, follower, followed, when):=

 $\Pi_{User.name,\ User.uid,\ WhenActivity.uid,\ WhenActivity.when} (\sigma_{User.uid} = Follows.follower\ \land\ Follows.followed = WhenActivity.uid} (User \times Follows \times WhenActivity))$

For each "follower" in WhenFollowedActivity, tuple of that follower with most recent "when" is removed

NotMostRecent(name, follower, followed, when):=

$$\begin{split} &\Pi_{\text{r1.name, r1.follower, r1.followed, r1.when}} \left(\sigma_{r1,follower = r2.follower \land r1.when < r2.when} \left(\rho_{\text{r1}}\right) \right) \\ &\left(WhenFollowedActivity\right) \times \rho_{\text{r2}} \left(WhenFollowedActivity\right)\right) \end{split}$$

For each "follower" WhenFollowedActivity, get the tuple of that follower with most recent "when"

MostRecent(name, follower, followed, when):=
WhenFollowedActivity - NotMostRecent

Report user with the most recent user he followed

Result(followerName, followedName, followedEmail, date):=

 $\Pi_{\textit{MostRecent.name, User.name, User.email, MostRecent.when.date}} (\sigma_{\textit{MostRecent.followed = User.uid}}$ (MostRecent \times User))

"LikeDate" is date when "uid" liked some post which was posted on "postDate"

DateLikePost(uid, likeDate, postDate):=

 $\Pi_{Likes.liker,\ Likes.when.date,\ Post.when.date}(\sigma_{Likes.pid=Post.pid}(Likes \times Post))$

"Uid" did not satisfy question requirement:

"users who have always liked posts in the same order as the order in which they were posted"

NotSat(uid):=

$$\begin{split} &\Pi_{r1.uid} \left(\sigma_{(r1.likeDate > r2.likeDate) \ \land \ (r1.postDate < r2.postDate) \ \land \ (r1.uid = r2.uid)} \right. \left(\rho_{r1} \right. \\ &\left. \left(DateLikePost \right) \times \rho_{r2} \left(DateLikePost \right) \right) \end{split}$$

"Uid" satisfied question requirement

Sat(uid):=

 $\Pi_{uid}(User)$ - NotSat

Report

Result(name, email):=

 $\Pi_{\text{name, email}}(\sigma_{\textit{User.uid} = \textit{Sat.uid}}(Sat \times User))$

Can not be expressed

"Sid" was not the last story that "uid" viewed

NotLastStory(viewerid, sid):=

 $\Pi_{s1.viewerid, \ s1.when} \left(\sigma_{(s1.viewerid = \ s2.viewerid)} \wedge_{(s1.when < \ s2.when)} \left(\rho_{s1} \left(Saw \right) \times \rho_{s2} \left(Saw \right) \right) \right)$

"Sid" was the last story that "uid" viewed

LastStory(viewerid, sid):=

 $\Pi_{\text{viewerid. sid}}(Saw) - NotLastStory$

"Sid" was not the first story that "uid" viewed

NotFirstStory(viewerid, sid):=

 $\Pi_{s1.viewerid, \ s1.when} \left(\sigma_{(s1.viewerid = \ s2.viewerid)} \wedge_{(s1.when > \ s2.when)} \left(\rho_{s1} \left(Saw \right) \times \rho_{s2} \left(Saw \right) \right) \right)$

"Sid" was the first story that "uid" viewed

FirstStory(viewerid, sid):=

 $\Pi_{\text{viewerid, sid}}(Saw) - NotFirstStory$

report uid and the id of the first and of the last story he have seen

result(viewerid, firstSid, lastSid):=

 $\Pi_{FirstStory.viewerid, FirstStory.sid, LastStory.sid}$ ($\sigma_{FirstStory.viewerid} = LastStory.viewerid$ (FirstStory × LastStory))

"Pid" has at least 3 different comments

ThreeComments(pid, commentor, when, sentiment):=

$$\begin{split} &\Pi_{c1.pid,\ c1.commentor,\ c1.when,\ sentiment(c1.text)}\left(\sigma_{(c1.pid=c2.pid=c3.pid)}\right. \land \ (c1.commentor \neq c2.commentor) \\ &Vc1.when \neq c2.when) \land \ (c1.commentor \neq c3.commentor) \lor c2.when \neq c3.when) \land \ (c2.commentor \neq c3.commentor) \\ &Vc2.when \neq c3.when) \land \ (\rho_{c1} \ (Comment) \times \rho_{c2} \ (Comment) \times \rho_{c3} \ (Comment))) \end{split}$$

"Pid" in ThreeComments, and pid has comments of at least 2 different "when"

LeastTwoWhen(pid, commentor, when, sentiment):=

$$\begin{split} &\Pi_{\text{r1.pid, p1.commentor, r1.when, r1.sentiment}} \left(\sigma_{\textit{(r1.pid} = \textit{r2.pid)}} \right. \wedge \left. \left(\textit{r1.when} \neq \textit{r2.when}\right) \right. \left(\rho_{\text{r1}} \right. \end{split} \\ &\left. \left(\text{ThreeComments}\right) \times \rho_{\text{r2}} \left(\text{ThreeComments}\right)\right)\right) \end{split}$$

"Pid" in ThreeComments, and pid has comments of at least 3 different "when"

LeastThreeWhen(pid, commentor, when, sentiment):=

$$\begin{split} &\Pi_{\text{r1.pid, p1.commentor, r1.when, r1.sentiment}} \left(\sigma_{\textit{(r1.pid = r2.pid = r3.pid)}} \wedge \text{ (r1.when < r2.when < r3.when)} \right) \left(\rho_{\text{r1}} \right) \\ &\left(\text{ThreeComments}\right) \times \rho_{\text{r2}} \left(\text{ThreeComments}\right) \times \rho_{\text{r3}} \left(\text{ThreeComments}\right) \right) \end{split}$$

"Pid" in ThreeComments, and pid has comments all of the same "when".

These "pid"s can not have shift

OneWhen(pid, commentor, when, sentiment):=
ThreeComments - LeastTwoWhen

OneWhenNoShift:= OneWhen

"Pid" in ThreeComments, and pid has comments of exactly 2 different "when"

TwoWhen(pid, commentor, when, sentiment):=
LeastThreeWhen - LeastTwoWhen

When there are at least 3 different when, get "pid" with no shift LeastThreeWhenNoShift(pid, commentor, when, sentiment):= $\Pi_{r1.pid, \ p1.commentor, \ r1.when, \ r1.sentiment} (\sigma_{(r1.pid = r2.pid = r3.pid)} \wedge (r1.when < r2.when < r3.when) \wedge (r1.sentiment \neq r2.sentiment \wedge r2.sentiment \neq r3.sentiment) (\rho_{r1} (LeastThreeWhen) \times \rho_{r2} (LeastThreeWhen) \times \rho_{r3} (LeastThreeWhen)))$

When there are exactly 2 different when, get "pid" with no shift TwoWhenNoShift(pid, commentor, when, sentiment):= $\Pi_{r1.pid, p1.commentor, r1.when, r1.sentiment} (\sigma_{(r1.pid = r2.pid)} \wedge (r1.when \neq r2.when) \wedge (r1.sentiment = r2.sentiment) (\rho_{r1} (TwoWhen) \times \rho_{r2} (TwoWhen)))$

"Pid" had at least three comments and for which there has been a sentiment shift over time

Shift(pid, commentor, when, sentiment):=
(((ThreeComments - OneWhenNoShift) - TwoWhenNoShift) LeastThreeWhenNoShift)

Report

Result(uid, pid, commentor, date, sentiment):=

 $\Pi_{Post.pid,\ Post.uid,\ Shift.commentor,\ Shift.when.date,\ Shift.sentiment}(\sigma_{Post.pid} = \textit{Shift.pid}\ (Post \times Shift))$

Part2

Q1

 $\sigma_{(Comment.pid = Post.pid) \ \land \ (comment.when \leq Post.when)} \ (Comment \times Post) = \varnothing$

$\mathbf{Q2}$

$$\begin{split} &\sigma_{(s1.uid \ = \ s2.uid) \ \land \ (s1.sid \ \neq \ s2.sid) \ \land \ (s1.current \ = \ true \ \land \ s2.current \ = \ true)} \ (\rho_{s1} \ (Story) \times \rho_{s2} \\ &(Story)) = \varnothing \end{split}$$

Q3

$$\Pi_{\text{pid}}(\text{Post}) - \Pi_{\text{pid}}(\text{PIncludes}) = \varnothing$$

 $\Pi_{\text{sid}}(\text{Story}) - \Pi_{\text{sid}}(\text{SIncludes}) = \varnothing$