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**Part1**

# Q1

“Liker” liked some post of “liked”

Liked(likers, liked):=

$\Pi_{\text{Likes.likers, Post.pid}} (\sigma_{\text{Likes.pid} = \text{Post.pid}} (\text{Likes} \times \text{Post}))$

“Viewer” viewed some story of “viewed”

Viewed(viewer, viewed):=

$\Pi_{\text{Saw.viewerid, Story.sid}} (\sigma_{\text{Saw.sid} = \text{Story.sid}} (\text{Saw} \times \text{Story}))$

“Uid1” liked some post or viewed some story of “uid2” and

“Uid1” did not followed “uid2”

NotSat(uid1, uid2):=

$\text{Liked} \cup \text{Viewed} - \Pi_{\text{follower, followed}} (\text{Follows})$

“Uid” never liked some post or viewed some story of user whom he did not follow

Sat(uid):=

$\Pi_{\text{uid}} (\text{User}) - \Pi_{\text{uid1}} (\text{NotSat})$

Report

Result(username, description):=

$\Pi_{\text{User.name, User.about}} (\sigma_{\text{User.uid} = \text{Sat.uid}} (\text{User} \times \text{Sat}))$

## Q2

“Pid” is posted in 2017 along with its posted date and tag

PostTag17(pid, date, tag):=

$$\Pi_{\text{Post.pid, when, Hashtag.tag}} (\sigma_{\text{when.year} = 2017 \wedge \text{Post.pid} = \text{Hashtag.pid}} (\text{Post} \times \text{Hashtag}))$$

Join of all dates and all tags of 2017

All(date, tag):=

$$\Pi_{\text{when.date}} (\sigma_{\text{when.year} = 2017} (\text{Post})) \times \Pi_{\text{tag}} (\text{PostTag17})$$

“Tag” was mentioned in 2017 but was not mentioned everyday in 2017

NotEveryday(tag):=

$$\Pi_{\text{tag}} (\text{All} - \Pi_{\text{date, tag}} (\text{PostTag17}))$$

“Tag” was mentioned everyday in 2017

Everyday(tag):=

$$\Pi_{\text{tag}} (\text{PostTag17}) - \text{NotEveryday}$$

“Tag” was mentioned at least 3 times everyday in 2017

result(tag):=

$$\Pi_{\text{Everyday.tag}} (\sigma_{(p1.tag = p2.tag = p3.tag = \text{Everyday.tag}) \wedge (p1.tag \neq p2.tag \wedge p1.tag \neq p3.tag \wedge p2.tag \neq p3.tag)} (\rho_{p1} (\text{PostTag17}) \times \rho_{p2} (\text{PostTag17}) \times \rho_{p3} (\text{PostTag17}) \times \text{Everyday}))$$

### Q3

“Uid1”, “uid2” are reciprocal follower and “uid1” > “uid2”

ReciprocalFollower(uid1, uid2):=

$$\Pi_{f1.followed, f1.follower} (\sigma_{(f1.follower = f2.followed) \wedge (f1.followed = f2.follower) \wedge (f1.follower > f2.followed)} (\rho_{f2}(\text{Follows}) \times \rho_{f1}(\text{Follows})))$$

“Follower” followed “uid1”

uid1Follower(uid1, uid2, follower):=

$$\Pi_{uid1, uid2, follower} (\sigma_{uid1 = followed} (\text{ReciprocalFollower} \times \text{Follows}))$$

“Follower” followed “uid2”

uid2Follower(uid1, uid2, follower):=

$$\Pi_{uid1, uid2, follower} (\sigma_{uid2 = followed} (\text{ReciprocalFollower} \times \text{Follows}))$$

“Uid1”, “uid2” are reciprocal follower, “follower” are uncommon follower of “uid1”, “uid2”

UncommonFollower(uid1, uid2, follower):=

$$(\text{uid1Follower} \cup \text{uid2Follower}) - (\text{uid1Follower} \cap \text{uid2Follower})$$

Report

result(uid1, uid2, follower, name, email):=

$$\Pi_{uid1, uid2, follower, name, email} (\sigma_{follower = uid} (\text{UncommonFollower} \times \text{User}))$$

**Q4**

Can not be expressed

## Q5

“U1”, “u2” are reciprocal follower and “u1” > “u2”

ReciprocalFollower(u1, u2):=

$$\Pi_{f1.followed, f1.follower} (\sigma_{(f1.follower = f2.followed) \wedge (f1.followed = f2.follower) \wedge (f1.follower > f2.followed)} (\rho_{f2} (\text{Follows}) \times \rho_{f1} (\text{Follows})))$$

“Liker” liked some post “pid” of “liked”

Liked(liker, liked, pid):=

$$\Pi_{liker, Post.uid, Post.pid} (\sigma_{Likes.pid = Post.pid} (\text{Likes} \times \text{Post}))$$

Join all liker in likes with all (uid, pid) in Post

All(liker, liked, pid):=

$$\Pi_{liker} (\text{Likes}) \times \Pi_{pid, uid} (\text{Post})$$

“Liker” did not like every post of “liked”

NotLikedEvery(liker, liked):=

All - Liked

“Liker” liked every post of “liked”

LikedEvery(liker, liked):=

$$\Pi_{liker, liked} (\text{Liked}) - \Pi_{liker, liked} (\text{NotLikedEvery})$$

“U<sub>id1</sub>”, “u<sub>id2</sub>” liked every post of each other

ReciprocalLiker(u<sub>id1</sub>, u<sub>id2</sub>):=

$$\prod_{r1.liker, r1.liked} (\sigma_{r1.liker = r2.liked \wedge r1.liked = r2.liker} (\rho_{r1} (\text{LikedEvery}) \times \rho_{r2} (\text{LikedEvery})))$$

“U<sub>id1</sub>”, “u<sub>id2</sub>” are backscratchers

Backscratchers(u<sub>id1</sub>, u<sub>id2</sub>):=

ReciprocalFollower  $\cap$  ReciprocalLiker

Report “follower” who followed some pairs of backscratchers

Result(follower):=

$$\prod_{r1.follower} (\sigma_{(r1.follower = r2.follower) \wedge (r1.followed = \text{Backscratchers}.uid1) \wedge (r2.followed = \text{Backscratchers}.uid2)} (\rho_{r1} (\text{Follows}) \times \rho_{r2} (\text{Follows}) \times \text{Backscratchers}))$$

## Q6

“When” is the datetime of some activity of “uid”

WhenActivity(uid, when):=

$\Pi_{uid, when} (Post) \cup \Pi_{uid, when} (Story)$

“When” is datetime of some activity of “followed”, who is followed by “follower” with “name”

WhenFollowedActivity(name, follower, followed, when):=

$\Pi_{User.name, User.uid, WhenActivity.uid, WhenActivity.when} (\sigma_{User.uid = Follows.follower \wedge Follows.followed = WhenActivity.uid} (User \times Follows \times WhenActivity))$

For each “follower” in WhenFollowedActivity, tuple of that follower with most recent “when” is removed

NotMostRecent(name, follower, followed, when):=

$\Pi_{r1.name, r1.follower, r1.followed, r1.when} (\sigma_{r1.follower = r2.follower \wedge r1.when < r2.when} (\rho_{r1} (WhenFollowedActivity) \times \rho_{r2} (WhenFollowedActivity)))$

For each “follower” WhenFollowedActivity, get the tuple of that follower with most recent “when”

MostRecent(name, follower, followed, when):=

WhenFollowedActivity - NotMostRecent



Report user with the most recent user he followed

Result(followerName, followedName, followedEmail, date):=

$\Pi_{MostRecent.name, User.name, User.email, MostRecent.when.date} (\sigma_{MostRecent.followed = User.uid}$   
(MostRecent  $\times$  User))

## Q7

“LikeDate” is date when “uid” liked some post which was posted on  
“postDate”

DateLikePost(uid, likeDate, postDate):=

$\Pi_{\text{Likes.likers, Likes.when.date, Post.when.date}} (\sigma_{\text{Likes.pid} = \text{Post.pid}} (\text{Likes} \times \text{Post}))$

“Uid” did not satisfy question requirement:

“users who have always liked posts in the same order as the order in  
which they were posted”

NotSat(uid):=

$\Pi_{r1.uid} (\sigma_{(r1.likeDate > r2.likeDate) \wedge (r1.postDate < r2.postDate) \wedge (r1.uid = r2.uid)} (\rho_{r1}$   
 $(\text{DateLikePost}) \times \rho_{r2} (\text{DateLikePost})))$

“Uid” satisfied question requirement

Sat(uid):=

$\Pi_{uid} (\text{User}) - \text{NotSat}$

Report

Result(name, email):=

$\Pi_{\text{name, email}} (\sigma_{\text{User.uid} = \text{Sat.uid}} (\text{Sat} \times \text{User}))$

**Q8**

Can not be expressed

## Q9

“Sid” was not the last story that “uid” viewed

NotLastStory(viewerid, sid):=

$$\Pi_{s1.viewerid, s1.when} (\sigma_{(s1.viewerid = s2.viewerid) \wedge (s1.when < s2.when)} (\rho_{s1}(\text{Saw}) \times \rho_{s2}(\text{Saw})))$$

“Sid” was the last story that “uid” viewed

LastStory(viewerid, sid):=

$$\Pi_{viewerid, sid} (\text{Saw}) - \text{NotLastStory}$$

“Sid” was not the first story that “uid” viewed

NotFirstStory(viewerid, sid):=

$$\Pi_{s1.viewerid, s1.when} (\sigma_{(s1.viewerid = s2.viewerid) \wedge (s1.when > s2.when)} (\rho_{s1}(\text{Saw}) \times \rho_{s2}(\text{Saw})))$$

“Sid” was the first story that “uid” viewed

FirstStory(viewerid, sid):=

$$\Pi_{viewerid, sid} (\text{Saw}) - \text{NotFirstStory}$$

report uid and the id of the first and of the last story he have seen

result(viewerid, firstSid, lastSid):=

$$\Pi_{FirstStory.viewerid, FirstStory.sid, LastStory.sid} (\sigma_{FirstStory.viewerid = LastStory.viewerid} (\text{FirstStory} \times \text{LastStory}))$$

# Q10

“Pid” has at least 3 different comments

ThreeComments(pid, commentor, when, sentiment):=

$$\Pi_{c1.pid, c1.commentor, c1.when, sentiment(c1.text)} (\sigma_{(c1.pid = c2.pid = c3.pid) \wedge (c1.commentor \neq c2.commentor} \\ \wedge (c1.when \neq c2.when) \wedge (c1.commentor \neq c3.commentor \wedge (c1.when \neq c3.when) \wedge (c2.commentor \neq c3.commentor \\ \wedge (c2.when \neq c3.when)) (\rho_{c1} (Comment) \times \rho_{c2} (Comment) \times \rho_{c3} (Comment)))$$

“Pid” in ThreeComments, and pid has comments of at least 2 different  
“when”

LeastTwoWhen(pid, commentor, when, sentiment):=

$$\Pi_{r1.pid, p1.commentor, r1.when, r1.sentiment} (\sigma_{(r1.pid = r2.pid) \wedge (r1.when \neq r2.when)} (\rho_{r1} \\ (ThreeComments) \times \rho_{r2} (ThreeComments)))$$

“Pid” in ThreeComments, and pid has comments of at least 3 different  
“when”

LeastThreeWhen(pid, commentor, when, sentiment):=

$$\Pi_{r1.pid, p1.commentor, r1.when, r1.sentiment} (\sigma_{(r1.pid = r2.pid = r3.pid) \wedge (r1.when < r2.when < r3.when)} (\rho_{r1} \\ (ThreeComments) \times \rho_{r2} (ThreeComments) \times \rho_{r3} (ThreeComments)))$$

“Pid” in ThreeComments, and pid has comments all of the same “when”.

These “pid”s can not have shift

OneWhen(pid, commentor, when, sentiment):=

ThreeComments - LeastTwoWhen

“Pid” in ThreeComments, and pid has comments of exactly 2 different “when”

TwoWhen(pid, commentor, when, sentiment):=

LeastThreeWhen - LeastTwoWhen

OneWhenNoShift:= OneWhen

When there are exactly 2 different when, get “pid” with no shift

TwoWhenNoShift(pid, commentor, when, sentiment):=

$$\prod_{r1.pid, p1.commentor, r1.when, r1.sentiment} (\sigma_{(r1.pid = r2.pid) \wedge (r1.when \neq r2.when) \wedge (r1.sentiment = r2.sentiment)} (\rho_{r1} (TwoWhen) \times \rho_{r2} (TwoWhen)))$$

When there are at least 3 different when, get “pid” with no shift

LeastThreeWhenNoShift(pid, commentor, when, sentiment):=

$$\prod_{r1.pid, p1.commentor, r1.when, r1.sentiment} (\sigma_{(r1.pid = r2.pid = r3.pid) \wedge (r1.when < r2.when < r3.when) \wedge (r1.sentiment \neq r2.sentiment \wedge r2.sentiment \neq r3.sentiment)} (\rho_{r1} (LeastThreeWhen) \times \rho_{r2} (LeastThreeWhen) \times \rho_{r3} (LeastThreeWhen)))$$

“Pid” had at least three comments and for which there has been a sentiment shift over time

Shift(pid, commentor, when, sentiment):=

((ThreeComments - OneWhenNoShift) - TwoWhenNoShift) -  
LeastThreeWhenNoShift)

Report

Result(uid, pid, commentor, date, sentiment):=

$\Pi_{\text{Post.pid, Post.uid, Shift.commentor, Shift.when.date, Shift.sentiment}} (\sigma_{\text{Post.pid} = \text{Shift.pid}} (\text{Post} \times \text{Shift}))$

# Part2

## Q1

$$\sigma_{(Comment.pid = Post.pid) \wedge (comment.when \leq Post.when)} (Comment \times Post) = \emptyset$$

## Q2

$$\sigma_{(s1.uid = s2.uid) \wedge (s1.sid \neq s2.sid) \wedge (s1.current = true \wedge s2.current = true)} (\rho_{s1} (Story) \times \rho_{s2} (Story)) = \emptyset$$

## Q3

$$\Pi_{pid} (Post) - \Pi_{pid} (PIncludes) = \emptyset$$

$$\Pi_{sid} (Story) - \Pi_{sid} (SIncludes) = \emptyset$$