

Camera Matrices

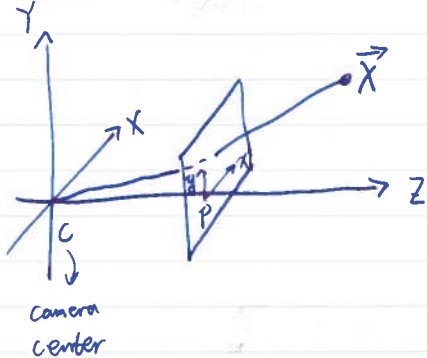
$$X_{cam} = \begin{pmatrix} R & -R\tilde{C}_w \\ 0 & 1 \end{pmatrix} X_w = KR(I - \tilde{C}_w)X_w$$

$\mathbb{R}^{4 \times 4}$ $\mathbb{R}^{4 \times 4}$ \mathbb{H}^3

$\tilde{C}_w \in \mathbb{R}^3$: camera coordinates in world frame

$$M_w^c = \begin{pmatrix} R & -R\tilde{C}_w \\ 0 & 1 \end{pmatrix} \Rightarrow M_c^w = (M_w^c)^{-1} = \begin{pmatrix} R^T & \tilde{C}_w \\ 0 & 1 \end{pmatrix}$$

Intrinsics world-to-cam



$$\begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} \mapsto \begin{pmatrix} fx \\ fy \\ z \\ 1 \end{pmatrix}$$

Note

$$R^T = \begin{pmatrix} \hat{x}_w^{cam} & \hat{y}_w^{cam} & \hat{z}_w^{cam} \end{pmatrix}$$

\hat{x}_w^{cam} = "camera's x-axis in world frame"

Let $M_{Blender}^{OpenGL} \in \mathbb{R}^{3 \times 3}$ s.t.

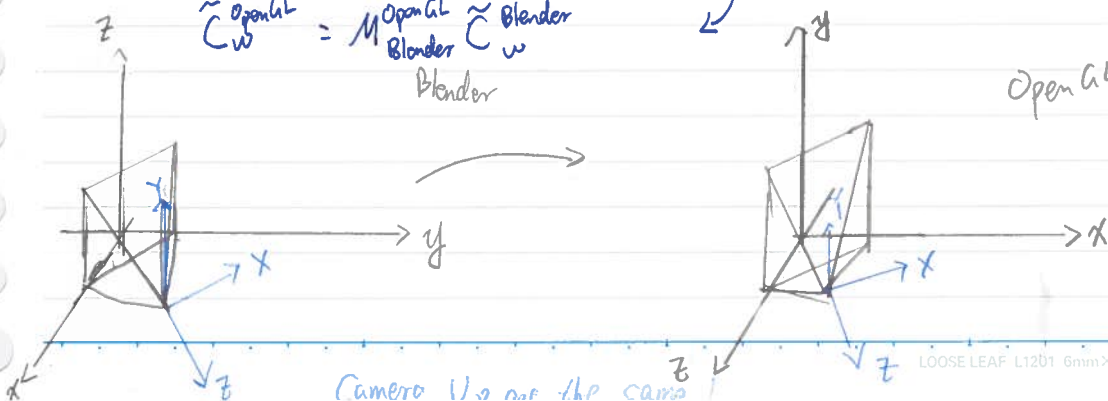
$$X_w^{OpenGL} = M_{Blender}^{OpenGL} X_w^{Blender}$$

$$(R^{OpenGL})^T = M_{Blender}^{OpenGL} \tilde{C}_w^{Blender} (R^{Blender})^T$$

camera-to-world

$$\tilde{C}_w^{OpenGL} = M_{Blender}^{OpenGL} \tilde{C}_w^{Blender}$$

OpenGL



Camera View of the camera

Another Formulation

Note $X^{\text{OpenCL, camera}} = X^{\text{Blender, camera}}$

$$X^{\text{OpenCL, world}} = M_{B,w}^{O,w} X^{B,w}$$

$$X^{O,c} = (R \ t)^{O,w} X^{O,w}$$

$$= (R \ t)^{O,w} M_{B,w}^{O,w} X^{B,w}$$

Also $X^{B,c} = (R \ t)^{B,w} X^{B,w}$

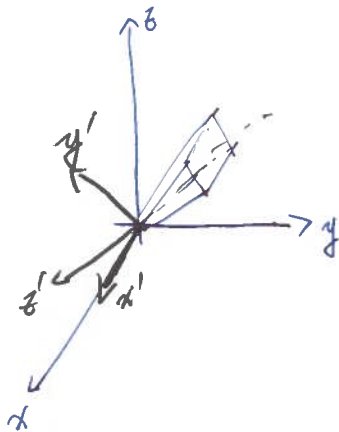
$$\Rightarrow \cancel{(R \ t)^{O,w}} \Rightarrow \cancel{(R \ t)}$$

$$(R \ t)^{O,w} M_{B,w}^{O,w} = (R \ t)^{B,w}$$

$$(R \ t)^{O,w} = (R \ t)^{B,w} M_{O,w}^{B,w}$$

Blender Cameras

(Blender: z-up)



135° rotation ~~on x~~ along x
by y. context. object. matrix - world =

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} & 0 \\ 0 & \frac{\sqrt{2}}{2} & -\frac{\sqrt{2}}{2} & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Camera - to - world

Looking at -z' direction

Intrinsics:

camera.lens = focal length (in mm)

camera.sensor.width (in mm)

$$\frac{\text{lens}}{\text{sensor width}} = \frac{f}{w} = \hat{f}$$

Image Plane



Import OBJ to Blender

"Blender uses y forward, z up; default for obj: y up, -z forward"

