

Question 3:

Generalized scaling matrix:  $M = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ T_x(1-s_x) & T_y(1-s_y) & 1 \end{bmatrix}$

$P = \begin{bmatrix} 2 & 2 & 1 \\ 4 & 2 & 1 \\ 3 & 31 & 1 \end{bmatrix} \Rightarrow P_{\text{final}} = P * M$  with  $s_x=2, s_y=0,5$  and  $T_x=T_y=2$

$$\Rightarrow P_{\text{final}} = \begin{bmatrix} 2 & 2 & 1 \\ 4 & 2 & 1 \\ 3 & 31 & 1 \end{bmatrix} * \begin{bmatrix} 2 & 0 & 0 \\ 0 & 0,5 & 0 \\ 2(1-2) & 2(1-0,5) & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 2 & 1 \\ 4 & 2 & 1 \\ 3 & 31 & 1 \end{bmatrix} * \begin{bmatrix} 2 & 0 & 0 \\ 0 & 0,5 & 0 \\ -2 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 2 & 1 \\ 6 & 2 & 1 \\ 4 & 16,5 & 1 \end{bmatrix}$$

$\Rightarrow$  new 2D coordinates:

$$A'(2;2); B'(6;2); C'(4;16,5)$$