

1           **Identification of plasma environments within the  
2           terrestrial magnetotail and its global structure from  
3           the Magnetospheric Multiscale Mission**

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8           **Key Points:**

- 9
- 10           • Inner-magnetotail environments are statistically identified with background plasma conditions and their global 3D structure is studied.
  - 11           • Warping effects attributed to changes in the Earth's dipole tilt angle leads to an apparent dawn-dusk asymmetry during the summer months.
  - 12           • We utilize a large volume of MMS data with partial plasma moments calculated from low-energy plasma and energetic particle instruments.

15 **Abstract**

16 Using MMS orbits in the Earth's magnetotail from 2017 to 2020, plasma conditions  
 17 and the 3D spatial structure of inner-magnetotail plasma environments (with a focus on  
 18 the plasma sheet) are studied with different approaches. Threshold conditions for dis-  
 19 tinguishing the plasma sheet, plasma sheet boundary layers, and lobes are derived from  
 20 the statistical properties of background plasma parameters. Our results support previ-  
 21 ous studies that employed similar methods using Cluster data. However, stronger cur-  
 22 rents are observed in both the lobes and plasma sheet, likely due to the smaller space-  
 23 craft separation ( $\lesssim 70$  km) that can resolve thin electron-scale currents. Threshold con-  
 24 ditions are used together with magnetic field and electric field measurements to image  
 25 the spatial structure of the plasma sheet. Results are in good agreement with a global  
 26 neutral sheet model based on solar wind conditions and magnetospheric configurations.  
 27 Furthermore, the Earth's dipole tilts towards the Sun around June solstice, which warps  
 28 the magnetotail as much as  $\sim 2\text{--}4 R_E$  in  $Z$  GSM. This warping effect is relaxed towards  
 29 September equinox. Consequently, as MMS travels through the magnetotail from dawn  
 30 to dusk during this period, there is an apparent dawn-dusk asymmetry in plasma con-  
 31 ditions between June and September. Kink-like flapping waves and IMF twisting are other  
 32 mesoscale processes attributed with a few  $R_E$  of flaring near the flanks. These findings  
 33 reveal important insights into the mesoscale structure and dynamics of the magnetotail.

34 **Plain Language Summary**

35 Data from four years of observations by NASA's MMS mission are used to statis-  
 36 tically identify distinctive regions within the Earth's magnetospheric tail. This study re-  
 37 veals insights into the spatial structure of this "magnetotail" and seasonal variations at-  
 38 tributed with changes in the Earth's magnetic field configurations, particularly those of  
 39 the orientation of the Earth's dipole. Our results agree with reported findings from ESA's  
 40 Cluster mission. However, certain aspects unique to MMS lead to some improved mea-  
 41 surements and features relating to MMS orbital design. The presented results are highly  
 42 beneficial to future large statistical studies with MMS data.

## 43 1 Introduction

44 Situated at the nightside of the Earth's magnetosphere, the magnetotail can stretch  
 45 as far as  $\sim 10^3$  Earth radii ( $R_E$ ) (Dungey, 1965; Cowley, 1991) and can exceed  $30 R_E$   
 46 in radius (Coroniti & Kennel, 1972; Shukhtina et al., 2004). Driven by interactions with  
 47 the solar wind and the interplanetary magnetic field (IMF) as well as changes in geo-  
 48 magnetic configurations and plasma conditions, it plays a central role in magnetospheric  
 49 dynamics from global to kinetic scales. Therefore, to understand the multiscale dynam-  
 50 ics within the magnetotail, there has been great interest to identify its complex struc-  
 51 ture and plasma conditions.

52 From global to meso-scales, the magnetotail is subjected to distinct types of de-  
 53 formation, three of which are known as flapping, twisting, and warping (Dayeh et al.,  
 54 2015). Solar wind directional changes can cause it to flap either steadily in the north-  
 55 south direction, or drive kink-like waves propagating towards the flanks (Lui et al., 1978;  
 56 Sergeev et al., 2003; Zhang et al., 2005; Gao et al., 2018). The flapping and the waves  
 57 have periods on the order of 1–10 minutes with wavelengths of 1–4  $R_E$  (Rong et al., 2018;  
 58 Wang et al., 2019). Non-zero IMF  $B_y$  can apply a torque and twist the tail as high as  
 59  $50^\circ$  about the Sun-Earth line (Owen et al., 1995; Tsyganenko, 1998). Due to the  $\sim 11^\circ$   
 60 tilt of the Earth's dipole axis with respect to its rotational axis (Amit & Olson, 2008),  
 61 the magnetotail is periodically displaced  $\sim 1\text{--}2 R_E$  above and below the equatorial plane  
 62 (Hammond et al., 1994) with a hinge radius of  $\sim 10 R_E$  (Tsyganenko & Fairfield, 2004).  
 63 Under these effects, the tail shape is extremely complex and variable on time scales from  
 64 a few minutes to many days and spatial scales up to many Earth radii.

65 There are several distinct plasma environments in the magnetotail. Boundary lay-  
 66 ers at the flanks can bring magnetosheath plasma into the inner magnetosphere via mix-  
 67 ing instabilities (e.g. Otto & Fairfield, 2000; Fairfield et al., 2000; Nykyri et al., 2006;  
 68 Johnson et al., 2014). In the middle of the tail, a plasma sheet (PS), which is a few  $R_E$   
 69 in thickness under normal conditions (Russell & McPherron, 1973; McComas et al., 1986;  
 70 Sanny et al., 1994; Zhou et al., 1997), contains high-beta plasma and low equatorial mag-  
 71 netic field (Baumjohann et al., 1989). To the contrary, the northern and southern lobes  
 72 enclosing the PS are often characterized by low-beta plasma and high equatorial mag-  
 73 netic field, predominantly pointing sunward or antisunward. Separating the PS and the  
 74 lobes, the plasma sheet boundary layers (PSBLs) mix hot and cold plasmas from these

two environments (Eastman et al., 1984) and often display signatures of nonlinear kinetic structures (Cattell et al., 1986; Nakamura et al., 2004; Ergun et al., 2009; Malaspina et al., 2015; Tong et al., 2018). Embedded within the PS is a neutral sheet (NS), often characterized as the null point of the equatorial magnetic field. The NS is the locus of many explosive geomagnetic activities during substorms (Sitnov et al., 2019, and references therein) which include, for example, kinetic instabilities, magnetic reconnection, locally generated turbulence, particle energization, etc (Zimbardo et al., 2010; Sitnov & Schindler, 2010; Liu et al., 2014; Ukhorskiy et al., 2017; Chen et al., 2019; Ergun et al., 2020a, 2020b, 2022; Usanova & Ergun, 2022).

The complex evolution of mesoscale dynamics and kinetic-scale structures often make identifying the various plasma environments a non-trivial task. Previous attempts to identify plasma environments and their spatial variations in the inner magnetotail have included a number of different methods. Combining decades of data, multi-mission studies (Hammond et al., 1994; Tsyganenko & Fairfield, 2004; Dayeh et al., 2015; Xiao et al., 2016) have imaged the neutral sheet under twisting and warping effects by observing the sign of magnetospheric  $B_x$ , from which global models are constructed. Multi-spacecraft missions, e.g. Cluster (Escoubet et al., 2001) and THEMIS (Angelopoulos et al., 2008), allow for timing analysis, often used to study the flapping motion (Runov et al., 2005, 2009). Most commonly, statistical threshold conditions based on averaged background parameters such as the plasma beta, number density, current density, magnetic field and/or plasma flow are used to distinguish the NS, PS, PSBL, and lobe (Baumjohann et al., 1988; Angelopoulos et al., 1994; Åsnes et al., 2008; Boakes et al., 2014). Assuming a certain time scale of the magnetic fluctuations, threshold conditions can also be defined based on magnetometer data alone to distinguish the lobe and PS (Coxon et al., 2016). When the threshold approach fails, the outer layer of the PS and PSBL may be determined on a case-by-case basis by analyzing beam-like populations in the 3D distribution function (Grigorenko et al., 2012) or ionospheric photoelectrons (Pedersen et al., 1985; Baumjohann et al., 1988).

The Magnetospheric Multiscale mission (MMS), launched in 2015, is a NASA four-spacecraft mission (Burch et al., 2016) that targets electron-scale magnetospheric physics, building upon the success of Cluster. Capable of higher time resolution and higher accuracy electromagnetic field and particle measurements, MMS has the potential to reinforce past studies of global models, threshold conditions, and kinetic-scale properties.

108 As apparent from previous experiences, it is challenging to achieve a definitive identi-  
109 fication of the inner-magnetotail plasma environments at any given time. Nevertheless,  
110 knowledge of mesoscale factors and background parameters from MMS data can provide  
111 insights into the magnetotail configuration at various scales. We remark that identify-  
112 ing plasma regions and boundaries is essential to a systematic statistical study of kinetic-  
113 scale magnetotail physics.

114 In this paper, we utilize a large volume of MMS observations to investigate the prop-  
115 erties of magnetotail plasma environments through a few different approaches, with a  
116 focus on the plasma sheet. Statistically, we derive threshold conditions based on back-  
117 ground plasma conditions to distinguish different environments. Results are discussed  
118 in comparison with those from a previous study using Cluster data (Boakes et al., 2014).  
119 Furthermore, the large volume of data allows for enough spatial coverage to image the  
120 global structure of the neutral sheet (i.e. through magnetic field measurements similar  
121 to Tsyganenko & Fairfield, 2004; Xiao et al., 2016). The structure of the NS based on  
122  $B_x$  will be compared with that of the PS identified from the threshold approach, and  
123 the NS model fitted by Xiao et al. (2016). Since the NS is embedded within the PS, we  
124 show that all of these approaches (threshold, imaging, modeling) generally agree, thereby  
125 revealing insights into both the statistical properties of background plasma conditions  
126 and the spatial variations of the NS/PS within the magnetotail. For example, since MMS  
127 always visits the magnetotail from June solstice to September equinox (correspondingly,  
128 from the dawn to dusk sectors in GSM coordinates), observations of the PS spatial struc-  
129 ture reveal that warping effects are prominent around June and insignificant around Septem-  
130 ber, resulting in an apparent dawn-dusk asymmetry in plasma conditions. Our data also  
131 feature the combination of partial plasma moments from low-energy plasma and ener-  
132 getic particle instruments, the technicality and motivation for which are presented in this  
133 paper.

134 This paper is organized as follows. In Section 2, we describe relevant details of MMS  
135 instrumentation. In Section 3, we describe our dataset, which is compiled from a broad  
136 array of MMS instruments measuring fields and particles, where we also present the com-  
137 bined plasma moments and the motivation for their consideration. In Section 4, we dis-  
138 cuss the exclusion of outer magnetotail environments and present the properties of back-  
139 ground plasma conditions in the inner magnetotail. In Section 5, we examine the 3D global  
140 structure of the neutral sheet and plasma sheet using the threshold, imaging, and mod-

<sup>141</sup> eling approaches. Finally, we discuss the implications of these results and provide con-  
<sup>142</sup> cluding remarks in Section 6.

<sup>143</sup> **2 Instrumentation**

<sup>144</sup> A broad array of MMS instruments are used enable and optimize statistical mag-  
<sup>145</sup> netotail studies of the electromagnetic field, particle properties, and their correlation. While  
<sup>146</sup> the present paper only concerns with statistical, mesoscale quantities, we recognize that  
<sup>147</sup> the large volume of data considered here also can be generically advantageous for future  
<sup>148</sup> large-scale studies of kinetic physics in the magnetotail.

<sup>149</sup> The four identical MMS spacecrafts travel in a tetrahedral formation with a highly  
<sup>150</sup> eccentric, near-Earth-equatorial orbit with an initial apogee of  $12 R_E$  and a perigee of  
<sup>151</sup> roughly  $1.2 R_E$  (Fuselier et al., 2016). The natural (inertial) orbital precession is small,  
<sup>152</sup> but as the Earth orbits the Sun, the apogee rotates between the subsolar region and the  
<sup>153</sup> magnetotail in roughly one year. Annually, magnetotail observations occur for MMS pri-  
<sup>154</sup> marily in the summer months between June solstice and September equinox. To max-  
<sup>155</sup> imize encounters with the neutral sheet during these seasons, the night-side apogee was  
<sup>156</sup> raised to  $25 R_E$  in early 2017 and subsequently to  $28 R_E$  in 2019 (Tedla et al., 2018). Through-  
<sup>157</sup> out the magnetotail, MMS instruments operate in two data acquisition rates (fast sur-  
<sup>158</sup>vey and burst). Fast survey data provide continuous coverage, and burst data are se-  
<sup>159</sup>lected short-duration intervals of high time-resolution measurements. In this paper, we  
<sup>160</sup> use fast survey data from 2017 to the end of 2020 to optimize statistical observations of  
<sup>161</sup> magnetotail processes occurring between  $12$  and  $28 R_E$ .

<sup>162</sup> In fast survey mode, the FIELDS investigation provides measurements of the DC  
<sup>163</sup> magnetic field and DC electric field in resolutions of 62.5 ms and 31.25 ms through the  
<sup>164</sup> Fluxgate Magnetometers (FGM) and Electric Double Probes (EDP) instruments (Torbert  
<sup>165</sup> et al., 2016; Russell et al., 2016; Ergun et al., 2016). At apogee, the tetrahedral forma-  
<sup>166</sup> tion is targeted to have a geometric quality factor  $Q \geq 0.7$  ( $Q = 1$  being a perfect tetra-  
<sup>167</sup>hedron) and an average spacecraft separation of 40 km, enabling measurements of field  
<sup>168</sup> gradients on several electron scales (Fuselier et al., 2016). Particularly, the current den-  
<sup>169</sup> sity  $\mathbf{J} = \nabla \times \mathbf{B}/\mu_0$  can be estimated using the curlometer technique (Paschmann & Daly,  
<sup>170</sup> 1998; Dunlop et al., 2021). Simultaneous multi-spacecraft measurements also allow for  
<sup>171</sup> calculations of barycentric quantities so that, for example, plasma dissipation measures

such as  $\mathbf{J} \cdot (\mathbf{E} + \mathbf{u} \times \mathbf{B})$  (Zenitani & Hoshino, 2005; Ergun et al., 2018) or  $(\mathbf{P} \cdot \nabla) \cdot \mathbf{u}$  (Chasapis et al., 2018; Yang et al., 2022) may be examined.

The Fast Plasma Investigation (FPI) samples plasma populations in the low-energy range from 10 eV to 30 keV with time resolutions of 30 ms for electrons and 150 ms for ions (Pollock et al., 2016). FPI instruments utilize top-hat electrostatic analyzers, forming 512 distributed field-of-views (FOVs) over the full  $4\pi$ -sr solid angle, each measuring 32 energy channels. The fast survey FPI data products used in this study are 3D electron and ion distribution functions that are integrated on-board high time-resolution measurements and reduced to 4.5-s resolution. FPI also provides partial plasma moments (associated with its capable energy range) integrated in velocity space from the 4.5-s products.

At the high-energy range, the Energetic Particle Detector (EPD) investigation comprises the Fly's Eye Energetic Particle Sensor (FEEPS) and Energetic Ion Spectrometer (EIS) instruments, utilizing micro-channel plates and solid-state detectors to sample energetic particles in the range of 60–500 keV (Mauk et al., 2016; Blake et al., 2016). For better ion data availability and energetic electron measurements, we utilize FEEPS data in this study. On each spacecraft, two FEEPS instruments are mounted  $180^\circ$  apart on the spin plane, providing 9 electron FOVs (5 operating in fast survey) and 3 ion FOVs, each measuring energy with 16 channels. Although this configuration provides instantaneous measurements of the particle distribution over a  $3\pi$ -sr solid angle, the main data products are electron and ion energy-angle distributions, averaged in 2.5-s resolution by means of rotation. As opposed to the full 3D distribution functions measured by FPI at low energies, the most reliably available of the FEEPS measurements are spin-scanned, omni-directional distribution functions. Therefore, the partial plasma moments that can be calculated from FEEPS data are more limited than those from FPI data.

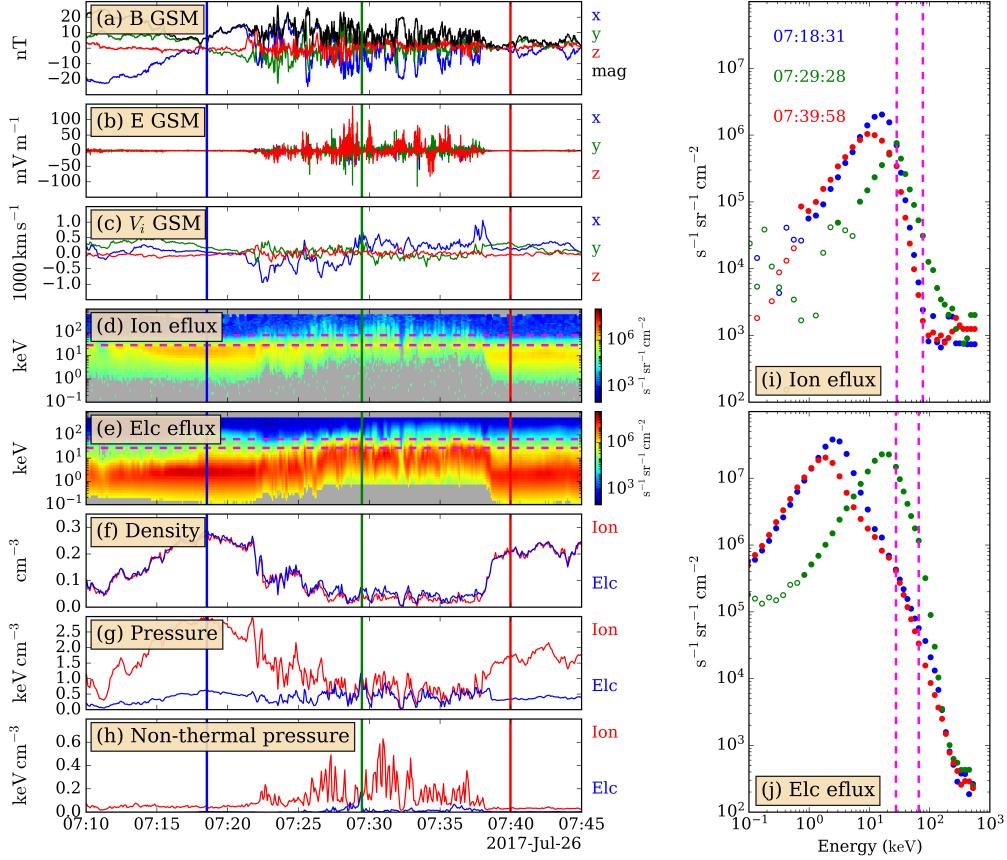
### 3 Methodology and Data

In the previous section, it is clear that low-energy ( $\lesssim 30$  keV) and high-energy ( $\gtrsim 60$  keV) particles are measured by MMS with instruments that have quite distinct techniques (FPI and FEEPS, respectively), resulting in different time resolutions, angular coverages, and an energy-coverage gap of about 30 keV. Therefore, it is not trivial how partial plasma moments may be calculated (in the high-energy range) and combined from

the two instruments. While the combination of partial plasma moments has been applied for previous capable missions such as THEMIS (Angelopoulos et al., 2008; Hietala et al., 2015; Shustov et al., 2019) and Cluster (Haaland et al., 2010), it has not been routinely performed for MMS and is often the constraining factor in previous studies, particularly those investigating ion properties. For example, Artemyev et al. (2021) acknowledges the importance of contributions of 100-keV ions to the plasma moments in the magnetotail, but because of the aforementioned constraint, these contributions are extrapolated using THEMIS data by a scaling argument instead of direct calculations. In the following, we provide another motivation for the necessity of combined plasma moments in the magnetotail through a case study. At the same time, we present a demonstration of our methodology in estimating the contributions of energetic particles to the plasma moments. Technical details of this combination are specific to MMS data products and discussed at length in Appendix A.

Consider a well-documented observation of a strongly turbulent, retreating reconnection X-line in the magnetotail in Fig. 1 (Ergun et al., 2018, 2020a, 2020b). In (a–c), an ion flow reversal occurs around 07:29, together with strong electromagnetic fluctuations persisting about 15 minutes, in which many intermittent structures are found such as double layers, magnetic holes, electron phase-space holes, and thin current sheets. At the same time, increases in energetic ion and electron energy fluxes are observed in (d) and (e). The energy fluxes at some time before, during, and after the turbulent event (denoted in (a–h) with vertical blue, green, and red lines) are also plotted in (i) and (j). The particle distributions in (d–e) and (i–j) are omni-directional and contain both measurements from FPI (below the lower-energy, magenta dashed line) and FEEPS (above the higher-energy dashed line). FEEPS measurements are interpolated to FPI resolution.

From past statistical studies (Huang et al., 2020; Chong et al., 2022), it is reasonable to assume that the plasma bulk flow rarely surpasses FPI capabilities (about 2,000 km/s for ions and 100,000 km/s for electrons). So the contribution from thermal (low-energy) particles to the plasma moments can be calculated from the FPI 3D distribution functions, correctly accounting for drifted particles. Subsequently, the non-thermal contribution may be considered isotropic and calculated from omni-directional distribution functions as detailed in Appendix A. However, this calculation is limited to directionless quantities, such as the number density and scalar pressure. Most clearly seen in (i–j), the energy-



**Figure 1.** Example of FPI-FEEPS combined moment calculations for a strong turbulent reconnection event in the magnetotail. (a) Barycentric magnetic field. (b) Barycentric electric field. The rest of the panels show data from MMS1. (c) Ion velocity. (d) Combined omni-directional ion energy flux. (e) Combined omni-directional electron energy flux. (f) Combined ion (red) and electron (blue) density. (g) Combined ion and electron total pressure. (h) Pressure contribution of non-thermal, energetic (larger than FPI energy threshold) particles. In (a-h), the blue, green, red vertical lines are times before, during, and after the turbulent event. (i) The ion energy flux during vertical snapshots in (a-h). (j) Similarly, snapshots in electron energy flux. Hollow markers are noise-level or background measurements. The dashed magenta lines [horizontal in (d) & (e), vertical in (i) & (j)] denote the extrapolated energy gap between FPI and FEEPS. There are 5 extrapolated points in that gap.

coverage gap (between the dashed lines) may contain a significant contribution to the plasma moments. Thus, we extrapolate the distribution function in this gap from FPI and FEEPS measurements and include its contribution in the non-thermal moment calculations (see Appendix A). In (f–h), we show the total (thermal + non-thermal) number density, total pressure, and non-thermal pressure.

In this event, one significant feature emphasized by the Ergun et al studies is that the reconnection inflow does not resupply particles from the lobe as fast as plasma sheet particles are depleted by the outflow, which results in a density drop in the turbulent region in (f) and the depletion of low-energy particles in (i–j). What we emphasize here is that because of this depletion of low-energy particles, when comparing (g) and (h), the contribution of non-thermal and/or energetic ions to the total pressure (characteristic energy density  $P_s = nk_B T_s$  of species  $s$ ) is on the order of 10 % and can be as high as 50 %. While most electrons are within the thermal (FPI) energy range, there can also be a significant fraction of non-thermal electrons ( $\sim 10\text{--}20\%$  of total electron pressure) in this type of events. Since the frequency of events similar to the one shown in Fig. 1 is not yet established, pressure and temperature calculations solely based on the FPI instrument in the magnetotail may be underestimated for these occurrences. Therefore, it may be crucial for statistical studies of particle energization in the magnetotail to consider plasma moments combined from both FPI and FEEPS.

The calculation of combined plasma moments above requires that there is simultaneous availability from both particle instruments. We also require that electromagnetic field observations (from FGM and EDP) are available to enable future statistical studies of the correlation between field and particle observations. Such a study will be able to establish the statistical occurrence between turbulence, reconnection, and particle energization events such as the example in Fig. 1.

For this study, we have compiled continuous intervals (no significant time gap; duration from minutes to hours) of good availability from the magnetic field, electric field, low-energy plasma, and energetic particle instruments during MMS magnetotail seasons from 2017 to 2020. Additionally, 1-minute averaged solar wind conditions are obtained from the OMNI dataset (King & Papitashvili, 2005), which is used to correlate the magnetotail dynamics with solar wind conditions. In total, there are 437,728,300 field (FGM resolution) and 6,078,827 particle (FPI resolution) data points, amounting to about 316

268 continuous days of observation. Details of compilation of these intervals are highly tech-  
 269 nical and are provided in Vo (2023) together with the source code. The principal con-  
 270 ditions are listed below.

- 271     1.  $X < 0$
- 272     2.  $R \geq 12R_E$
- 273     3.  $Q \geq 0.75$
- 274     4. No periods of thruster firing, EDP probe saturation, shadow spikes, or bad bias  
       settings.
- 275     5. FGM, EDP available from MMS(1–4).
- 276     6. FPI, FEEPS available from MMS1.
- 277     7. Interval at least 1-minute long.

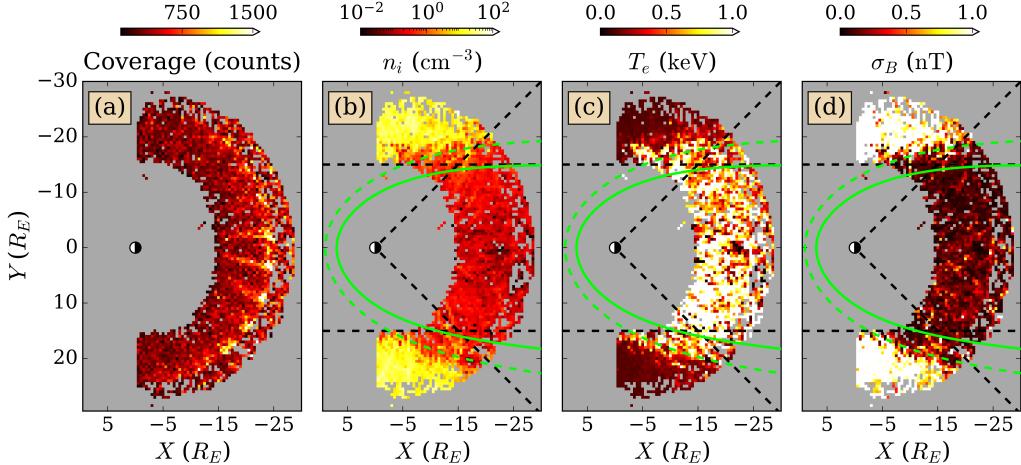
279 Above,  $\mathbf{R} = (X, Y, Z)$  is the spacecraft position in GSM. While most global models of  
 280 the neutral sheet, one of which is later on analyzed and compared, are fitted in aberrated  
 281 GSM (AGSM), we have found little difference between GSM and AGSM in our results.  
 282 Thus, we retain the usage of GSM for all coordinates in subsequent sections. Conditions  
 283 (3) and (5) ensures that the barycentric electromagnetic fields and the curlometer cur-  
 284 rent density may be accurately estimated. (4) ensures intervals of adequate EDP data  
 285 for analysis. (6) ensures the partial plasma moments can always be combined. (7) en-  
 286 forces that the intervals are adequately long for spectral analysis.

## 287 4 Properties of the magnetotail background plasma conditions

288 In this section, we first distinguish the inner magnetotail from the solar wind and  
 289 flank-side boundary layers, the properties of which are outside the scope of the present  
 290 paper. Then, we present the statistical properties of the inner-magnetotail plasma con-  
 291 ditions and compare our results with those in Boakes et al. (2014), hereby referred to  
 292 as B14. Also, as done in B14, threshold conditions for the PS, PSBL, and lobe are de-  
 293 rived based on the statistical properties of the plasma.

### 294 4.1 Exclusion of solar wind and flank-side boundary layers

295 Fig. 2 shows the  $X$ – $Y$  distribution of (a) the coverage of MMS trajectory, (b) the  
 296 ion density  $n_i$ , (c) the electron temperature  $T_e$ , and (d) the standard deviation of the



**Figure 2.** Spatial distribution in the  $X$ - $Y$  plane of (a) MMS coverage during tail seasons in 2017–2020, (b) the ion density  $n_i$ , (c) the electron temperature  $T_e$ , and (d) standard deviation of the magnetic field  $\sigma_B$ . The lime curves are a  $5^\circ$  (clockwise) tilted magnetopause model (Lin et al., 2010) constructed with zero IMF  $B_z$  and total solar wind pressure of 5 nPa (dashed) and 20 nPa (solid). Dashed black lines denote  $|Y| \leq 15 R_E$  and  $|Y| \leq |X|$ . The color scales are chosen to saturate solar wind values to also reveal typical plasma values in the tail.

297 magnetic field  $\sigma_B$  (over a 5-s moving window). In the magnetotail, the electron density  
 298 ( $n_e$ ) measurement is more accurate than  $n_i$ . However, the reverse is true in the solar wind.  
 299 Here, we use  $n_i$  to reveal the differences between the solar wind and the magnetotail.  
 300 Later, we use  $n_e$  when characterizing the magnetotail. 3D histograms are calculated with  
 301  $0.5 R_E \times 0.5 R_E \times 0.5 R_E$  cubic bins then averaged over the  $Z$  direction, except for (a),  
 302 which is summed instead. Hereafter, all data (e.g. the magnetic field, electric field, and  
 303 current density) are averaged over a 5-s moving window and subsequently down-sampled  
 304 to FPI resolution (4.5 s) so that particle and field measurements can be compared. Thus,  
 305 in (a), each count represents a 5-s observation and the total count in each bin represents  
 306 the dwell time of MMS spacecrafts. 3D bins that have lower than 100 counts are excluded  
 307 as they may not be statistically representative.

308 In (a), the dwell time is not uniform. The highly-eccentric orbit has MMS spend  
 309 more time near the apogee to maximize the chance of observing the diffusion region at  
 310 reconnection sites (Fuselier et al., 2016). However, bins that have statistically significant  
 311 counts are distributed over a large and uniform enough area so that the spatial distri-

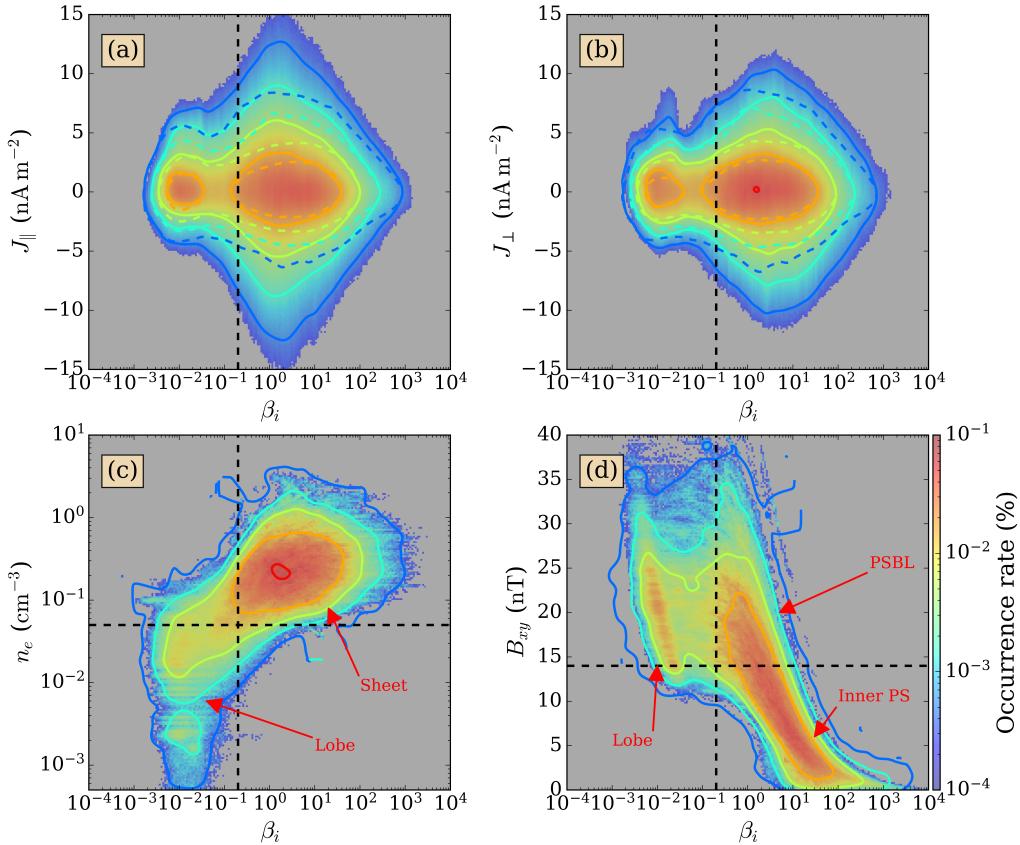
bution of plasma parameters can be studied. Most notably in (b–d), the solar wind is observed (as saturated colors) at  $|Y| \gtrsim 15 R_E$ , where averaged values are  $n_i \sim 10\text{--}100 \text{ cm}^{-3}$ ,  $\sigma_B \sim 1\text{--}5 \text{ nT}$ , and  $T_e \sim 0.01\text{--}0.1 \text{ keV}$ . In contrast, plasma parameters in the inner magnetotail are generally 1–2 orders of magnitude smaller, where  $n_i \sim 0.1\text{--}1 \text{ cm}^{-3}$ ,  $\sigma_B \sim 0.1\text{--}0.5 \text{ nT}$ , and  $T_e \sim 1 \text{ keV}$ . Fig. 2 shows that in general, background plasma parameters such as the density, temperature, and magnetic field fluctuations are distinctive between the inner and outer magnetotail. Thus, we can use these differences to statistically exclude regions more likely associated with the solar wind or flank-side boundary layers.

OMNI solar wind observations during MMS magnetotail seasons indicate average IMF  $B_z \sim 0$  and total pressure  $P_{\text{sw}} \sim 1\text{--}5 \text{ nPa}$ . We use these parameters to construct an asymmetric magnetopause model (Lin et al., 2010), plotted as dashed ( $P_{\text{sw}} = 5 \text{ nPa}$ ) and solid ( $P_{\text{sw}} = 20 \text{ nPa}$ ) lime curves in (b–d). Details about the average OMNI observations and the Lin10 model are provided in Appendix B. The dashed curve agrees well with the change in plasma parameters. Thus, to be conservative when eliminating boundary layers, we define the inner magnetotail as the region bounded by the solid lime curve. In subsequent sections, all statistical results are obtained with data located strictly within this region.

For comparison, previous statistical studies have typically constrained the inner magnetotail region either with (i)  $|Y| \leq |X|$  (Ergun et al., 2015) or (ii) with a threshold  $|Y| \leq Y_0$  (Boakes et al., 2014; Chong et al., 2022). These two constraints are plotted as dashed black lines in (b–d). On a closer look, they are all somewhat equivalent conditions. (i) tends to work for smaller radial distances  $R \leq 12 R_E$ , and (ii) is good for small enough threshold  $Y_0$ , although the popular choice  $Y_0 = 15 R_E$  may include some mixed plasma data.

## 4.2 Identification of inner tail plasma environments

Fig. 3 shows the statistical profile of background plasma parameters in terms of the ion beta  $\beta_i = P_i/(B^2/2\mu_0)$ , where  $P_i$  is the ion pressure. For comparison, it is plotted in the same format as Figure 1 in B14. (a) and (b) show the current density components parallel ( $J_{\parallel}$ ) and perpendicular ( $J_{\perp}$ ) to the background magnetic field. (c) shows the electron density  $n_e$ , and (d) shows the equatorial magnetic field  $B_{xy}$ . Due to the solenoidal condition ( $\nabla \cdot \mathbf{B} = 0$ ), the noise level of the curlometer currents in (a–b) can be estimated



**Figure 3.** Occurrence rates of (a) the parallel current density  $J_{\parallel}$ , (b) the perpendicular current density  $J_{\perp}$  (in the cross-tail direction,  $\hat{\mathbf{z}} \times \mathbf{B}$ ), (c) the electron density  $n_e$ , and (d) the equatorial magnetic field  $B_{xy}$  in terms of the ion plasma beta  $\beta_i$ . Solid lines are contours of the colored distributions. In (a) and (b), the overplotted colored dashed lines are contours of the noise estimation of the curlometer current,  $\nabla \cdot \mathbf{B}/\mu_0$ . In all panels, the vertical dashed line denotes  $\beta_i = 0.2$ . In (c), the horizontal dashed line is the FPI 1-count level  $n_e = 0.05 \text{ cm}^{-3}$ . In (d), the horizontal dashed line denotes  $B_{xy} = 14 \text{ nT}$ .

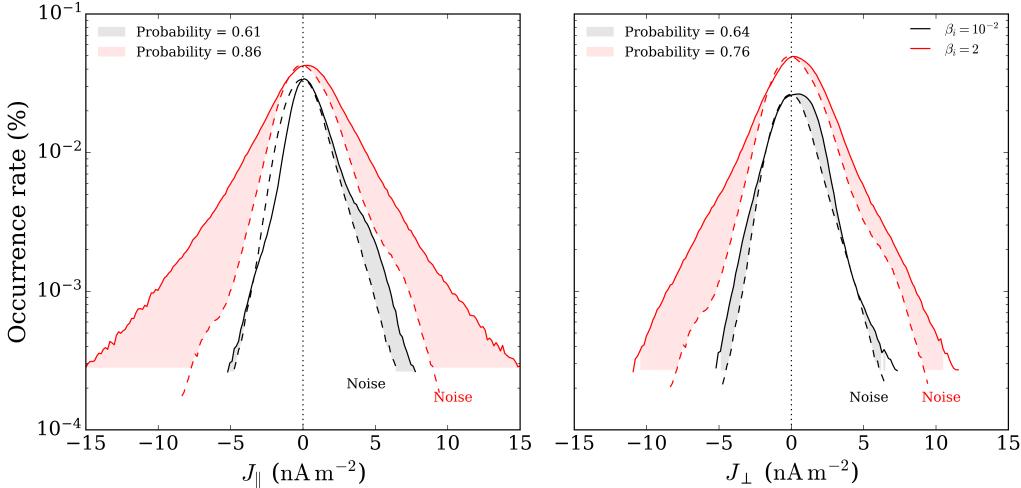
**Table 1.** Threshold conditions distinguishing tail plasma environments derived from Fig. 3.

Plasma environment	Condition
Lobe	$\beta_i < 0.2$
Plasma sheet	$\beta_i \geq 0.2 \text{ \& } B_{xy} \leq 14 \text{ nT}$
Plasma sheet boundary layer	$\beta_i \geq 0.2 \text{ \& } B_{xy} > 14 \text{ nT}$

as  $J_{\text{noise}} = \nabla \cdot \mathbf{B}/\mu_0$ . In these panels, we have overplotted the contours of  $J_{\text{noise}}$  for comparison with the current amplitude. At a given color, currents larger than noise are measured if the solid line is wider than the dashed line.

In general, the features in this plot are consistent with the Cluster study. Most clearly in all panels, there are two distinct populations separated by  $\beta_i$ . The lobe-like population has low density ( $n_e \sim 0.01 \text{ cm}^{-3}$ ), low beta ( $\beta_i \sim 0.01$ ), and high equatorial magnetic field ( $B_{xy} \sim 20 \text{ nT}$ ). In contrast, the plasma sheet-like population has high density ( $n_e \sim 0.1 \text{ cm}^{-3}$ ), high beta ( $\beta_i \sim 1$ ), and low field ( $B_{xy} \sim 5 \text{ nT}$ ). One note of caution is the region of low electron density. The FPI instrument has a large uncertainty if the electron density is below  $0.05 \text{ cm}^{-3}$  [horizontal dashed line in (c)]. However, noise and background in the combined FPI-FEEPS distribution function has been treated carefully in the low-density region such that the accuracy is improved (see Appendix A for details). In subsequent sections, the threshold conditions for the plasma sheet are the main subject of study, where the density is typically higher than the FPI threshold.

To systematically determine the thresholds, B14 used changes in the current and electron densities with respect to  $\beta_i$  to define the PS/lobe separation and similarly, the statistical spread in  $B_{xy}$  to distinguish between the PSBL and the outer/inner regions of the plasma sheet. The threshold conditions were then reported annually. However, we deem it unnecessary for that level of detail in this study. It suffices to define by visual inspection the threshold conditions as tabulated in Table 1 and annotated in Fig. 3. We also make no attempt to distinguish the inner PS from the outer PS as done in B14. In general, our thresholds are all consistent with averages from the yearly results in B14. The beta threshold is slightly higher (by a factor of 2), most probably due to the usage of combined plasma moments (only partial moments with energies  $\lesssim 40 \text{ keV}$  were used in the B14 study).



**Figure 4.** Vertical cuts of the statistical distribution of the currents in Fig. 3(a–b) at  $\beta_i = 10^{-2}$  (in black) and  $\beta_i = 2$  (in red). The corresponding dashed lines with the same colors are the noise estimation  $J_{\text{noise}}$ . The shaded areas are those where more occurrence is observed at a given amplitude than the noise estimation. The probability of these observations based on the shown conditional distribution functions (on  $\beta_i$ ) is provided in the legends (shaded area versus total area under the solid lines).

368 In (a) and (b), the average current amplitude in the PS is consistent with results  
 369 in B14 ( $0.5\text{--}2\text{ nA/m}^2$ ). However, a difference among our results is in the lobe (low-beta  
 370 region). B14 only observed noise in this region ( $J \sim 0.5\text{ nA/m}^2$ ). But the wider (green/blue)  
 371 contours than  $J_{\text{noise}}$  show that there are detections of statistically significant lobe cur-  
 372 rents above the noise level. To better visualize this difference, Fig. 4 shows vertical cuts  
 373 of these panels at  $\beta_i = 10^{-2}$  (black) and  $\beta_i = 2$  (red). The occurrence rate of high-beta  
 374 currents is higher than those with low  $\beta_i$ . The shaded regions indicate that there are “wings”  
 375 in the probability distribution functions (PDFs) that is more significant than the statis-  
 376 tics of noise (dashed lines). At any occurrence rate below  $2 \times 10^{-3}\%$  for low  $\beta_i$ , the de-  
 377 tected current amplitudes are higher than the estimated noise, which means wider con-  
 378 tours in Fig. 3. Finally, to show the partition between noise-level currents (in the “core”  
 379 of the PDFs) and non-noise currents (in the wings), we calculate the probability of the  
 380 latter (see the figure legends) and discover that more than half of the observations are  
 381 not noise. That said, the low overall occurrence rate indicates that their detection is not  
 382 common.

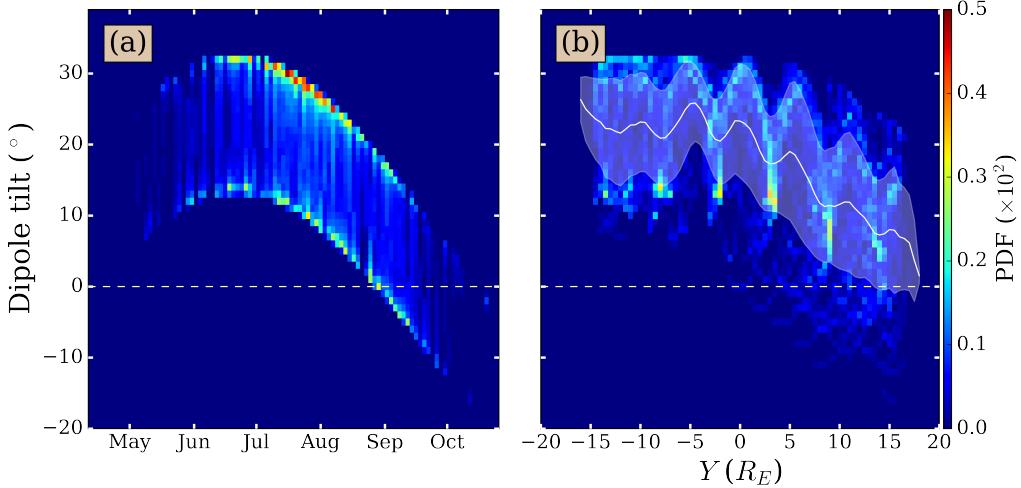
383 In the magnetotail, the typical Cluster spacecraft separation is 1000s of km (Escoubet  
 384 et al., 2001), which is comparable to the average ion inertial length. About  $\sqrt{m_i/m_e} \sim 40$   
 385 times smaller, the typical electron inertial length is  $\sim 20$  km. Since the target of MMS  
 386 is electron physics, 97 % of the dataset has spacecraft separation  $\leq 70$  km (not shown).  
 387 As a result, intense electron-scale currents are resolved in MMS data, but may be un-  
 388 derestimated in Cluster data due to the linear spatial interpolation in the curlometer tech-  
 389 nique (Paschmann & Daly, 1998). Therefore, we hypothesize that the presence of sig-  
 390 nificant lobe currents in our statistics is due to the smaller spacecraft separation. Fu-  
 391 ture studies are necessary to reveal their origin and properties. Overall, these results still  
 392 provide strong support of Cluster observations from the MMS mission, with an improve-  
 393 ment on current density measurements.

## 394 5 Global structure of the magnetotail plasma sheet

395 In this section, we investigate the three-dimensional global structure of the plasma  
 396 sheet. As mentioned in Section 1, the magnetotail is influenced by processes such as flap-  
 397 ping, twisting, and warping. Therefore, the plasma sheet may be highly deformed on mesoscales.  
 398 In that case, it is interesting to study the spatial variations of the background plasma  
 399 conditions, based on which the PS threshold condition is established in Table 1. From  
 400 solar wind observations in Appendix B, the average IMF  $B_y$  is around 2 nT with near-  
 401 zero IMF  $B_z$ , suggesting that the twisting angle should not be significant for radial dis-  
 402 tances smaller than  $30 R_E$  (Tsyganenko & Fairfield, 2004), which leaves flapping and warp-  
 403 ing as the main deforming factors during MMS magnetotail seasons.

404 To investigate the warping of the magnetotail plasma sheet, we consider the Earth's  
 405 dipole tilt angle  $\Psi$  obtained from the MMS Magnetic Ephemerides Coordinates (MEC)  
 406 dataset generated by Henderson et al. (2018). In GSM coordinates,  $\Psi$ , constrained in  
 407 the  $X-Z$  plane, is the angle between the Earth's dipole tilt axis and the  $Z$  axis, which  
 408 is positive when the Earth tilts toward the Sun and negative away from the Sun. Due  
 409 to the daily Earth rotation,  $\Psi$  varies almost sinusoidally with an amplitude of about  $10^\circ$   
 410 and a period of about 1 day (not shown). Fig. 5 shows the distribution of  $\Psi$  with respect  
 411 to (a) the time of year and (b) the concurrent MMS spacecraft position in  $Y$ .

412 In (a), there are two peaks separated by  $\sim 20^\circ$  due to the daily variation of  $\Psi$  and  
 413 the seasonal variation of the dipole tilt ( $\Psi$  is lower in October). The daily variation is

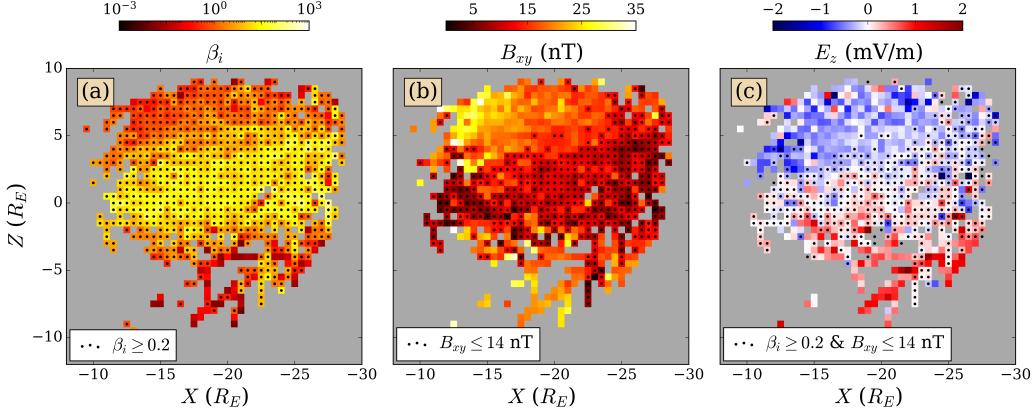


**Figure 5.** Distribution of the dipole tilt angle  $\Psi$  (a) in time and (b) in  $Y$ . The average  $\Psi$  is plotted as the solid white line in (b). The shaded area is 1 standard deviation.

also seen in panel (b). However, (b) also shows that  $\Psi$  is lower at higher  $Y$ . The correlation between  $\Psi$  and  $Y$  is due to low natural precession of the MMS orbit, which causes MMS to visit the magnetotail only in the summer months. In these seasons, MMS enters the magnetotail from the dawn-side flank ( $Y \sim -15 R_E$ ) around May when  $\Psi$  is high and exits to the dusk-side flank ( $Y \sim 15 R_E$ ) around October when  $\Psi$  is low. The solid white line in (b) shows the average value of  $\Psi$  in terms of  $Y$ , which is around  $20^\circ$  in the dawn sector ( $Y < 0$ ) and gradually decreases to zero in the dusk sector ( $Y > 0$ ). The difference in average  $\Psi$  between these two sectors can lead to significant variations as a function of  $Y$  due to dipole tilt warping effects.

Using the same bin size as that in Fig. 2 ( $0.5 R_E$ ), Fig. 6 shows the ( $Y$  averaged) spatial structure of (a) the ion plasma beta  $\beta_i$ , (b) the equatorial magnetic field  $B_{xy}$ , and (c) the normal electric field  $E_z$ . Similarly, Fig. 7 shows the ( $X$  averaged) spatial structure of (a)  $B_x$  and (b)  $\Psi$ . The structures of these parameters altogether provide a 3D picture of the plasma sheet, with the tilt angle  $\Psi$  indicating the degree of warping.

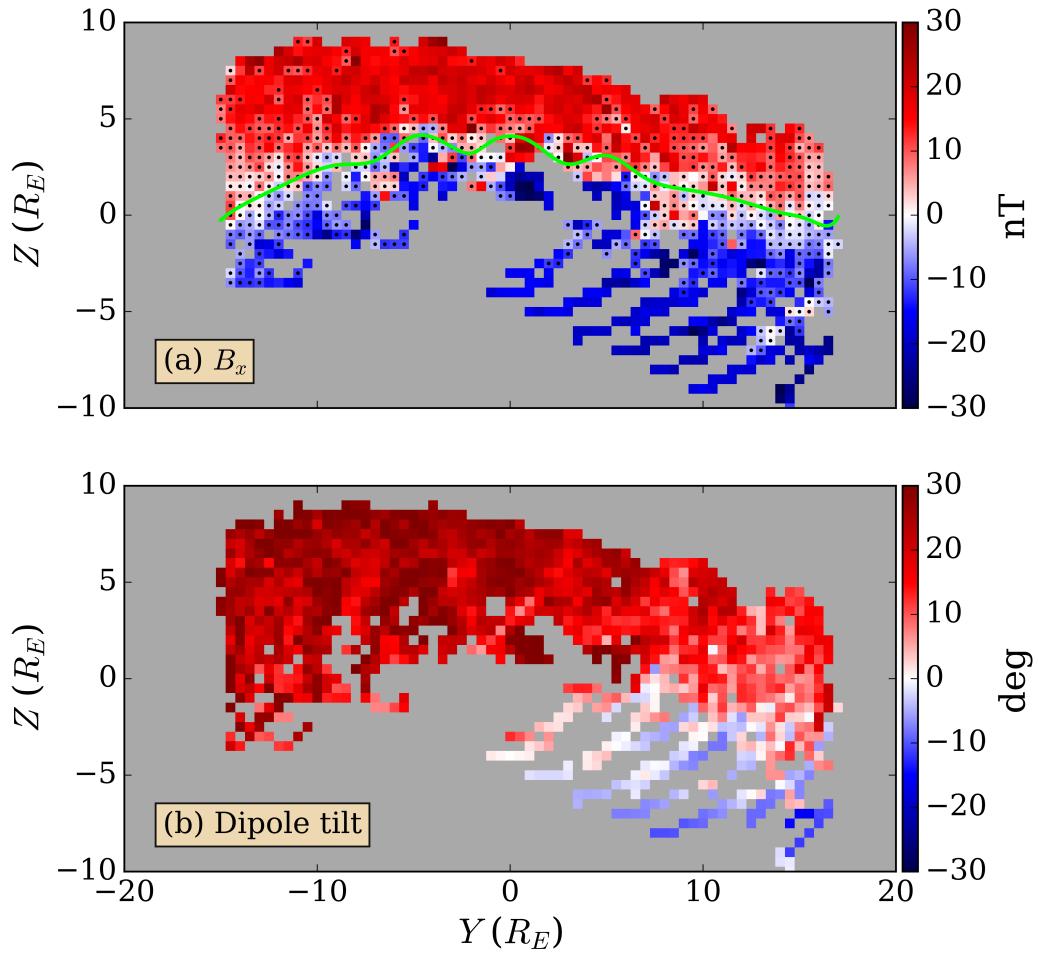
In Fig. 6 from (a) to (c), the bins are marked with a dot if they satisfy the beta condition, the magnetic field condition, and both (the plasma sheet condition in Table 1), respectively. The features in this figure correspond one-to-one with those discussed in Table 1. First, in Fig. 6(a), while constraining  $\beta_i$  to high values mostly excludes envi-



**Figure 6.** Spatial distribution in the  $X$ - $Z$  plane of (a)  $\beta_i$ , (b)  $B_{xy}$ , and (c)  $E_z$ . In (a), marked bins (those with a circle marker at the center) satisfy the PS beta condition  $\beta_i \geq 0.2$  in Table 1. Similarly, the marked bins satisfy the PS field condition  $B_{xy} \leq 14$  nT in (b). Those in (c) satisfy both, the full PS condition.

environments consistent with the lobe, the PSBL and PS can extend widely in  $Z$ . So the beta condition does not reveal much about the spatial extent. In Fig. 6(b), the magnetic field condition excludes the PSBL regions, leaving the remaining PS, which is more narrow along  $Z = 0$ . In Fig. 6(c), the normal electric field  $E_z$  that supports the cross-tail drift current  $J_y \propto -E_z B_x$  also roughly follows this spatial structure. This electric field always points towards the inner PS (negative/positive in the northern/southern lobe) and tends to zero at the NS. This plot shows that the PS threshold condition agrees with the spatial structure of the PS, as drawn out by the normal electric field ( $E_z$ ) and equatorial magnetic field ( $B_{xy}$ ).

The spatial extent of  $E_z$  in the  $Z$  direction seemingly flares up to  $\sim 8\text{--}10 R_E$  beyond  $|X| \gtrsim 20 R_E$ , while at closer distances, its structure is mainly located within  $5 R_E$  of the equator. This flaring in the  $Z$  direction of the plasma sheet can be explained with variations in the  $Y$  direction caused by the dipole tilt. In Fig. 7(a), the two lobes are clearly distinguishable, with  $B_x > 0$  indicating the northern hemisphere and  $B_x < 0$  indicating the southern hemisphere. The null point  $B_x \sim 0$  is the location of the neutral sheet. In (b), the distribution of  $\Psi$  also reflects the aforementioned dawn-dusk asymmetry in Fig. 5, where  $\Psi$  varies between  $10^\circ$  and  $30^\circ$  in the dawn sector ( $Y < 0$ ) and between  $-10^\circ$  and  $10^\circ$  in the dusk sector ( $Y > 0$ ).



**Figure 7.** Spatial distribution in the  $Y$ - $Z$  plane of (a)  $B_x$  and (b) the dipole tilt angle  $\Psi$ . The solid lime line in (a) is a global tail neutral sheet model (Xiao et al., 2016) dependent on  $\Psi$  and the average solar wind pressure  $P_{\text{sw}} = 2 \text{ nPa}$ . Similar to Fig. 6(c), the marked bins satisfy the plasma sheet condition (plotted in the same format).

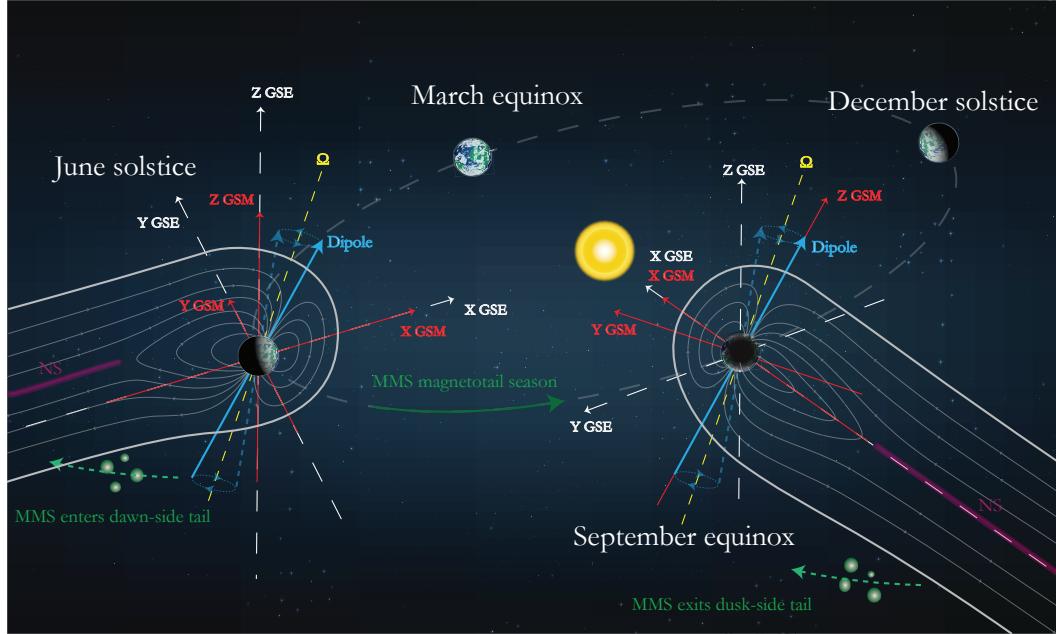
450       Bins marked with a dot in Fig. 7(a) indicate the region satisfying the PS condition  
 451       in Table 1. The reversal of  $B_x$  shows that the neutral sheet is located within the  
 452       marked plasma sheet. The lime curve is a global NS model from Xiao et al. (2016), de-  
 453       pendent on the dipole tilt angle and the solar wind pressure (see Appendix B). We use  
 454       the average value of  $\Psi$  obtained from Fig. 5(b) (solid white line) for the former, and av-  
 455       erage OMNI observations  $P_{\text{sw}} = 2 \text{ nPa}$  for the latter. The small variations in this model  
 456       are highly dependent on those in  $\Psi$ , which in turn is affected by the spacecraft apogee.  
 457       However, its average shows a remarkable agreement with the  $B_x$  reversal.

458       In Fig. 7(b), the high values of  $\Psi$  in the dawn sector causes the magnetotail to be  
 459       warped to  $\sim 2\text{--}4 R_E$  in  $Z$ , while in the dusk sector, there is little warping. The combi-  
 460       nation of warping in the dusk sector with no warping in the dawn sector contributes to  
 461       the apparent flaring in  $X\text{--}Z$  seen in Fig. 6, as the  $Y$  direction is averaged in that figure.  
 462       The plasma sheet extent around the neutral sheet in Fig. 7(a) seems to increase towards  
 463       the flanks ( $\sim 2\text{--}3 R_E$ ). This increase may be explained by kink-like flapping waves that  
 464       are commonly observed in these regions (Gao et al., 2018). As the magnetic field con-  
 465       dition is more strictly constrained to lower threshold, the outer PS is excluded and will  
 466       result in a spatial distribution that follow the NS more closely.

## 467       6 Discussions and Conclusions

468       In summary, using a large volume of MMS data with combined plasma moments  
 469       from the low-energy plasma and energetic particle instruments, we have investigated the  
 470       background plasma conditions and the 3D spatial structure of the magnetotail plasma  
 471       sheet using the threshold, imaging, and modeling approaches. Consequently, we have sta-  
 472       tistically distinguished inner-magnetotail environments corresponding to the plasma sheet,  
 473       plasma sheet boundary layers, and lobes. We find that these methods are in good agree-  
 474       ments, showing that the neutral sheet is embedded within a thick region of the plasma  
 475       sheet, and they are both highly warped in the dawn sector and less deformed in the dusk  
 476       sector.

477       This asymmetry is attributed to changes in the dipole tilt angle as the Earth or-  
 478       bits the Sun (see Figs. 5 and 7). But this observation is, in part, also specific to MMS,  
 479       since the mission always visits the magnetotail in the summer months due to its orbital  
 480       design. Fig. 8 provides a schematic of the Earth's magnetospheric configurations dur-



**Figure 8.** Schematic of Earth’s magnetospheric configurations during an MMS magnetotail season. The Earth’s rotational axis ( $\Omega$ , dashed yellow) is constant. The magnetic dipole moment (solid blue arrow) rotates around this axis once a day, warping the magnetotail up and down in  $Z$  GSM. Around June solstice, MMS (green dots) enters the magnetotail from the dawn side. During this period, GSM (red) coincides with GSE (white) coordinates whenever the moment lies in the XZ plane. The tilt angle is large, resulting in a highly warped magnetotail in the positive  $Z$  direction. Towards September equinox, MMS exits the magnetotail from the dusk side. During this period, whenever the moment lies in the YZ plane, the  $Z$  axis of GSM coordinate is parallel with the dipole moment. The small tilt angle results in a relaxed magnetotail.

481 ing these periods. As MMS enters the magnetotail from the dawn-side flank around June  
 482 solstice, the Earth’s dipole on average tilts around  $20^\circ$  towards the Sun, resulting in a  
 483 highly warped neutral sheet at  $Z \sim 2\text{--}4 R_E$  [see Fig. 7(a)]. But when it exits the mag-  
 484 netotail from the dusk-side flank around September equinox, the average tilt angle is zero,  
 485 leading to a less deformed and displaced neutral sheet.

486 While we have demonstrated that the deformation of the magnetotail mainly comes  
 487 from warping, there remains flaring effects due to kink-like flapping waves or IMF twist-  
 488 ing near the flanks that are not discussed in details in this paper. Future studies may  
 489 need to consider smaller-scale evolution and utilize timing analysis to investigate prop-  
 490 erties of the flapping in further details. However, the insights about the plasma sheet

491 spatial variations reported in this paper will be useful for future MMS magnetotail stud-  
 492 ies when considering its configuration and the state of the plasma sheet.

493 The threshold conditions in Fig. 3 and Table 1 are also in good agreement with a  
 494 previous Cluster study (Boakes et al., 2014). The average current amplitude in the PS  
 495 agrees with Cluster observations. However, lobe currents with amplitude comparable to  
 496 those in the PS are also detected, albeit their occurrence rate is lower [Fig. 3(a–b), Fig. 4].  
 497 One interpretation of their presence is that thin electron-scale currents are resolved in  
 498 the curlometer calculation due to MMS mission design with smaller average spacecraft  
 499 separation in the magnetotail (Paschmann & Daly, 1998; Dunlop et al., 2021). While small-  
 500 scale current systems have been observed with Cluster via the particle distribution func-  
 501 tion (Teste et al., 2007), its larger average separation inherently leads to underestima-  
 502 tion of electron-scale currents via the curlometer technique. Finally, the ion plasma beta  
 503 condition is slightly higher (by a factor of 2), probably due to the additional contribu-  
 504 tion of energetic (60–500 keV) ions to the total pressure. However, the threshold is still  
 505 on the same order as that reported by B14, so our results are still consistent. Neverthe-  
 506 less, this might also be a demonstration that the combined plasma moments (discussed  
 507 in Fig. 1) are important for studies of the magnetotail, especially those involving ion prop-  
 508 erties. While the difference in large statistical averages is small, that on a case-by-case  
 509 basis might be significant. Finally, the region of interest (inner magnetotail) is more me-  
 510 thodically defined, well-separated from solar wind data and mixed plasma regions near  
 511 the flank-side boundary layers.

512 To perform the statistical analysis in this paper, we utilize around 316 continuous  
 513 days of magnetotail observations by MMS (about 400 million field measurements and  
 514 6 million particle measurements), with data from a broad array of field and particle in-  
 515 struments. The dataset compiled in this study is useful not only for studying background  
 516 plasma properties, but also for kinetic-scale dynamical evolution. Particularly, the in-  
 517 tervals in our data contain continuous high-quality electric field measurements from EDP  
 518 of at least 1 minute. Combined with accurate spatial gradient calculations, spectral anal-  
 519 ysis, and particle measurements, this enables future statistical studies of field fluctua-  
 520 tions, particle energization, and their correlation. Further investigations of this data will  
 521 reveal insights in the frequency of events such as the one in Fig. 1, and the properties  
 522 and spatial variations of plasma turbulence and reconnection in the inner magnetotail.

523 **Availability Statement**

524 The MMS dataset, including ephemerides MEC data, is publicly available at the  
 525 MMS Science Data Center (<https://lasp.colorado.edu/mms/sdc/public/>). Data are an-  
 526 alyzed using the SPEDAS software package (<http://spedas.org/blog/>). All figures are  
 527 generated with matplotlib, a Python visualization package (<https://matplotlib.org/>).

528 **Acknowledgments**

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 532 instruments and data products, S. Schwartz for suggesting the number-energy flux con-  
 533 version table in the ISSI/ESA report, and P. Reiff for helpful comments on the sketch  
 534 in Figure 8.

535 **Appendix A FPI-FEEPS combined plasma moments**

536 In this section, we describe the technical details pertaining to the combined FPI  
 537 and FEEPS moment calculations. Since the data products for the distribution function  
 538 from each instrument and their limitations are different, their combination is non-trivial.  
 539 Every instrument is constrained within a certain energy range. So the derived plasma  
 540 moments from the distribution function are only partial contributions. However, the main  
 541 moments of interest for this study, the number density and scalar pressure, are additive  
 542 scalars. So it is possible to sum the low- and high-energy contributions to get a total par-  
 543 tial plasma moments. In the following, “low-energy” refers to the FPI measurements, while  
 544 “high-energy” contains both the FEEPS measurements and the extrapolated energy-coverage  
 545 gap between the two instruments.

546 At the low energy range, the FPI instrument provides a 3D distribution function  
 547  $f(E, \varphi, \theta)$  in spherical coordinates with the energy  $E = (1/2)mv^2$  measured at 32 dif-  
 548 ferent channels from 6.32 eV to 27.5 keV for electrons and from 2.16 eV to 28.3 keV for  
 549 ions (Pollock et al., 2016).  $m$  is the mass of the particle species. Averaged over a solid  
 550 angle  $d\Omega = d(\cos \theta)d\varphi$ , the differential energy flux, defined as (Larsen et al., 2022)

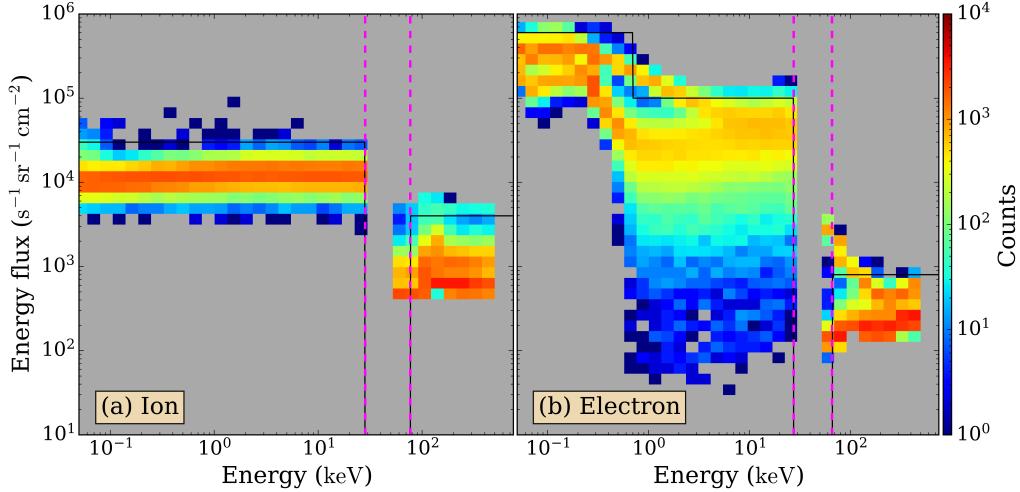
**Table A1.** Periods of lobe observations used for background estimation.

	Start	Stop
1	2017-07-04/04:50	2017-07-04/05:20
2	2017-07-07/02:30	2017-07-07/03:20
3	2017-07-10/07:20	2017-07-10/09:20
4	2017-07-13/09:30	2017-07-13/10:10
5	2017-07-15/15:20	2017-07-15/16:40

$$\frac{d\mathcal{F}}{dE} = \frac{v^4}{2} \frac{\int d\Omega f(E, \varphi, \theta)}{\int d\Omega}, \quad (\text{A1})$$

is solely a function of energy, provided in the FPI data products as an energy-angle spectrogram. While FPI also provides partial moments calculated from the full 3D distribution function (which undergoes multiple conditioning and processing steps by default for integration such as spin-tone correction, penetrating radiation removal, etc, while the energy flux does not), those moments are not reliable when there is significant cold ( $\sim 10\text{-}100\text{ eV}$ ) plasma contribution. In particular, the ion energy flux can be contaminated with background radiation (energetic electrons) up to keV energies, and the electron distribution is often contaminated with photoelectrons due to spacecraft charging effects (up to  $\sim 100\text{ eV}$ ). Thus, as a rule of thumb, caution to the plasma moments is needed when the density is below  $0.05\text{ cm}^{-3}$ .

To push the limits of FPI in our combined moments calculation, we apply the usual processing steps to the omni-directional energy flux with an addition of a background removal. Fig. A1 shows the average energy fluxes of ions and electrons during 5 nominally quiet lobe periods in July 2017 (selected by eyes, see Table A1). In (a), the ion distribution shows two constant background populations for the FPI and FEEPS energy ranges, respectively. In (b), there are a cold photoelectron background up to about 1 keV, and a variable population throughout the remaining FPI range. In our dataset, we remove these populations using the displayed step functions (solid black). The resulting omni-directional energy flux is used in conjunction with FEEPS data to calculate a combined spectrum, as shown in Fig. 1(d–e).

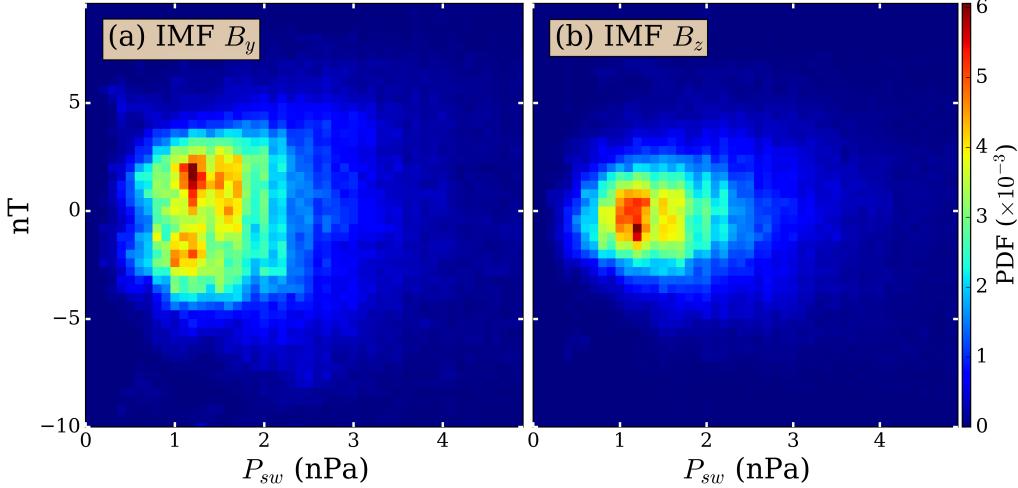


**Figure A1.** Average values of the (a) ion and (b) electron energy fluxes during nominal lobe periods. The step functions (in black) are used to remove background populations in the data used in this study.

At the high energy range, the FEEPS instrument provides a coarse instantaneous all-sky view of electrons and ions, whose angular coverage can be refined by means of rotation (Blake et al., 2016; Mauk et al., 2016). While the design of the field-of-view is different for each particle species, the all-sky measurements can be combined into an omnidirectional number flux spectrogram, which is related to the energy flux (see Table D.2 of Wüest et al., 2007) by

$$\frac{dN}{dE} = \frac{1}{E} \frac{dF}{dE}, \quad (\text{A2})$$

with  $E$  measured from 33.2 keV to 509.2 keV for electrons and from 57.9 keV to 558.6 keV for ions. The lowest-energy channel in FEEPS is excluded due to noise. In Fig. 1(d–e), the FEEPS number flux has been converted to energy flux with Eq. (A2) in the combined spectrogram. Five data points are linearly extrapolated to cover the energy gap between the two instruments. While a linear extrapolation might not be adequate to estimate the missing data in the gap, we note that this method of extrapolation does not add false data and only underestimate the contribution of missing data in the gap.



**Figure B1.** Distribution of (a) the IMF  $B_y$  and (b) the IMF  $B_z$  with respect to total (dynamical and magnetic) solar wind pressure during MMS magnetotail observations.

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It is reasonable to assume that the bulk flow rarely surpasses the FPI energy range. Therefore, the omni-directional, high-energy contribution to the partial number density and scalar pressure can be integrated as (see also Mauk et al., 2004)

$$n_{hi} = 4\pi \sqrt{\frac{m}{2}} \int (\sqrt{E} dE) \left( \frac{1}{E} \frac{dN}{dE} \right), \quad \text{and} \quad P_{hi} = 4\pi \sqrt{\frac{m}{2}} \int (\sqrt{E} dE) \frac{dN}{dE}, \quad (A3)$$

587

where  $\sqrt{E} dE \sim v^2 dv$  and from Eqs. (A1) and (A2),  $(1/E)dN/dE \sim f$ . The energy range in above integrals covers both the extrapolated range and FEEPS range. Finally, the total number density and scalar pressure, shown in Fig. 1(f-g), are  $n_{total} = n_{lo} + n_{hi}$  and  $P_{total} = P_{lo} + P_{hi}$ . Potentially, these considerations can also be extended to other quantities such as the isotropic parts of the temperature and the heat flux. In general, the resulting ion and electron densities calculated with the steps as laid out above preserve charge quasi-neutrality very well, even during periods of low FPI density (see Fig. 1f), which provides confidence in the statistical analyses discussed in the main text.

595

## Appendix B Solar wind and IMF conditions during MMS magnetotail observations and global magnetospheric models

597

The OMNI dataset (King & Papitashvili, 2005) provides 1-minute averaged solar wind and interplanetary magnetic field (IMF) conditions. From this dataset, we plot in

599 Fig. B1 the distribution of (a) the IMF  $B_y$  and (b) the IMF  $B_z$  with respect to the to-  
 600 tal solar wind pressure (including magnetic field pressure and dynamical pressure) dur-  
 601 ing the magnetotail seasons constrained by the criteria in Section 3. Different from the  
 602 counting statistics discussed in the main text, each count here represents a 1-min obser-  
 603 vation. From this figure,  $B_y$  averages around 1–2 nT, while  $B_z$  averages around zero. The  
 604 total solar wind pressure averages around 1–2 nPa, with the most extreme pressure around  
 605 4–5 nPa.

606 In this study, two global magnetospheric models are utilized for our analysis of MMS  
 607 observations. Lin et al. (2010) used a database of magnetopause crossings (observed from  
 608 1994 to 2008) from Cluster, Geotail, GOES, IMP 8, Interball, LANL, Polar, TC1, and  
 609 THEMIS, together with solar wind conditions from ACE and Wind to construct an asym-  
 610 metric 3D magnetopause model in aberrated GSM coordinates. This model (see Equa-  
 611 tions (19–20) in their paper) depends on the IMF  $B_z$ , the total solar wind pressure, and  
 612 the Earth’s dipole tilt angle  $\Psi$ . since the average  $\Psi$  changes between the dawn and dusk  
 613 sectors [see Figs. 5 and 7], we set  $\Psi = 0$  and use average values in Fig. B1(b) for the  
 614 magnetopause shapes in Fig. 2(b–d). The models also need to be tilted 5° clockwise to  
 615 better fit the changes in background plasma conditions between the solar wind and in-  
 616 ner magnetotail. This rotation is needed due to either the seasonal variations of  $\Psi$ , or  
 617 the usage of GSM coordinates throughout the paper.

618 Xiao et al. (2016) used magnetic field data from Cluster, Geotail, TC-1, and THEMIS  
 619 from 1995 to 2013 to fit the average shape and position of the magnetotail neutral sheet.  
 620 Their model (see Equations (4–7) in their paper) is consistent with that in Tsyganenko  
 621 and Fairfield (2004) and depends on the  $Y$  coordinate, the Earth’s dipole tilt angle  $\Psi$ ,  
 622 and scaling parameters normalized for a downtail distance of  $20R_E$  and solar wind pres-  
 623 sure of 2 nPa. This pressure is typical from OMNI observations in Fig. B1. We use the  
 624 average value of  $\Psi$  in terms of  $Y$  from Fig. 5(b) so that this NS model, as shown in Fig. 7(a),  
 625 is only dependent on the  $Y$  coordinate. In our analysis, we have also found little vari-  
 626 ations of the results for different  $X$  downtail distance, so the scaling parameters normal-  
 627 ized for  $X = -20 R_E$  are reasonable.

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