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1060. Missing Element in Sorted Array [□] (/problems /missing-element-in-sorted-array/)

June 12, 2019 | 15.3K views

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Given a sorted array A of **unique** numbers, find the K-th missing number starting from the leftmost number of the array.

Example 1:

Input: A = [4,7,9,10], K = 1

Output: 5 **Explanation:**

The first missing number is 5.

Example 2:

Input: A = [4,7,9,10], K = 3

Output: 8 **Explanation:**

The missing numbers are [5,6,8,...], hence the third missing number is 8.

Example 3:

Input: A = [1,2,4], K = 3

Output: 6 **Explanation:**

The missing numbers are $[3,5,6,7,\ldots]$, hence the third missing number is 6.

Note:

- 1. 1 <= A.length <= 50000
- 2. 1 <= A[i] <= 1e7
- 3. 1 <= K <= 1e8

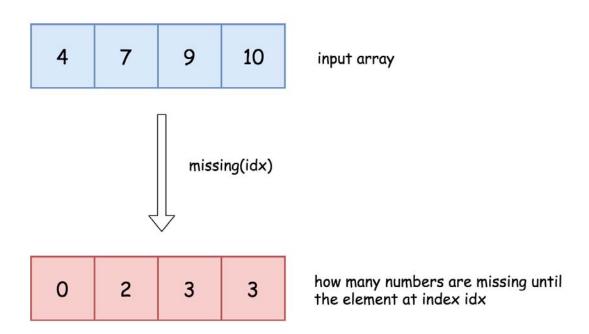
Solution

Approach 1: One Pass

Intuition

The problem is similar to First Missing Positive (https://leetcode.com/articles/first-missing-positive/) and the naive idea would be to solve it in a similar way by one pass approach.

Let's first assume that one has a function missing(idx) that returns how many numbers are missing until the element at index idx.

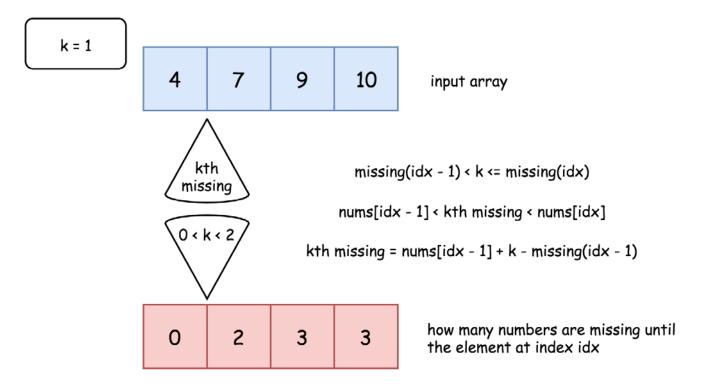


With the help of such a function the solution is straightforward:

• Find an index such that missing(idx - 1) < k <= missing(idx). In other words, that means that kth missing number is in-between nums[idx - 1] and nums[idx].

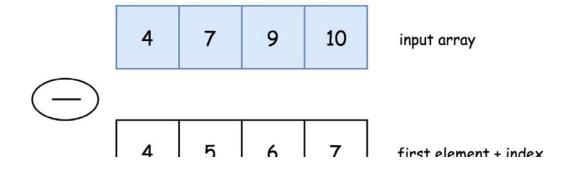
One even could compute a difference between kth missing number and nums[idx - 1]. First, there are missing(idx - 1) missing numbers until nums[idx - 1]. Second, all k - missing(idx - 1) missing numbers from nums[idx - 1] to kth missing are consecutive ones, because all of them are less than nums[idx] and hence there is nothing to separate them. Together that means that kth smallest is larger than nums[idx - 1] by k - missing(idx - 1).

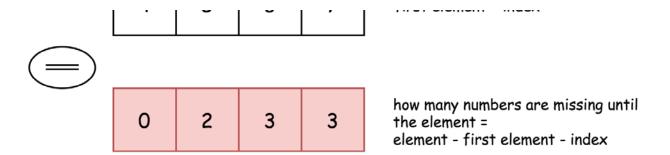
• Return kth smallest nums[idx - 1] + k - missing(idx - 1).



The last thing to discuss is how to implement missing(idx) function.

Let's consider an array element at index idx. If there is no numbers missing, the element should be equal to nums[idx] = nums[0] + idx. If k numbers are missing, the element should be equal to nums[idx] = nums[0] + idx + k. Hence the number of missing elements is equal to nums[idx] - nums[0] - idx.





Algorithm

- Implement missing(idx) function that returns how many numbers are missing until array element with index idx. Function returns nums[idx] nums[0] idx.
- Find an index such that missing(idx 1) < k <= missing(idx) by a linear search.
- Return kth smallest nums[idx 1] + k missing(idx 1).

Implementation

```
Copy
Java
       Python
1
    class Solution:
2
        def missingElement(self, nums: List[int], k: int) -> int:
3
            # Return how many numbers are missing until nums[idx]
            missing = lambda idx: nums[idx] - nums[0] - idx
4
5
            n = len(nums)
6
7
            # If kth missing number is larger than
8
            # the last element of the array
9
            if k > missing(n - 1):
10
                return nums[-1] + k - missing(n - 1)
11
12
            idx = 1
13
            # find idx such that
14
            # missing(idx - 1) < k <= missing(idx)</pre>
15
            while missing(idx) < k:
16
                idx += 1
17
18
            # kth missing number is greater than nums[idx - 1]
19
            # and less than nums[idx]
20
            return nums[idx - 1] + k - missing(idx - 1)
```

Complexity Analysis

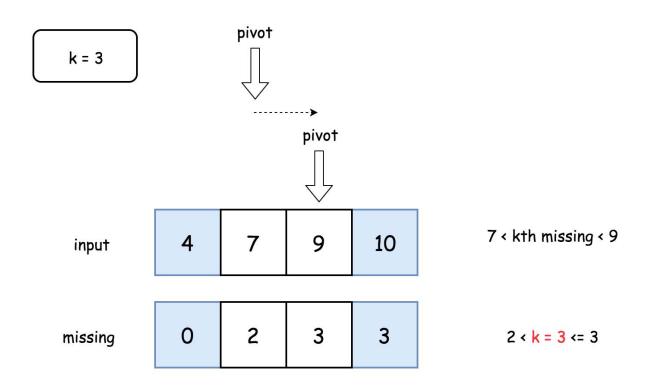
- ullet Time complexity: $\mathcal{O}(N)$ since in the worst case it's one pass along the array.
- Space complexity: $\mathcal{O}(1)$ since it's a constant space solution.

Approach 2: Binary Search

Intuition

Approach 1 uses the linear search and doesn't profit from the fact that array is *sorted*. One could replace the linear search by a binary one (https://leetcode.com/articles/binary-search/) and reduce the time complexity from $\mathcal{O}(N)$ down to $\mathcal{O}(\log N)$.

The idea is to find the leftmost element such that the number of missing numbers until this element is less or equal to k.



Algorithm

- Implement missing(idx) function that returns how many numbers are missing until array element with index idx. Function returns nums[idx] nums[0] idx.
- Find an index such that missing(idx 1) < k <= missing(idx) by a binary search.
- Return kth smallest nums[idx 1] + k missing(idx 1).

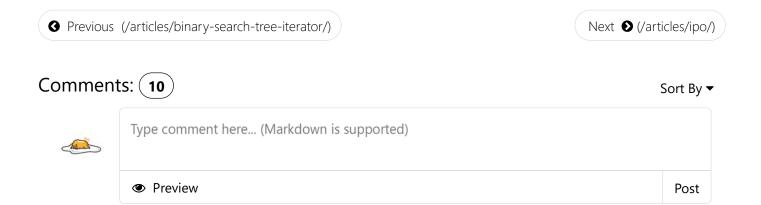
Implementation

```
♣ Copy
Java
       Python
1
    class Solution:
2
        def missingElement(self, nums: List[int], k: int) -> int:
3
            # Return how many numbers are missing until nums[idx]
 4
            missing = lambda idx: nums[idx] - nums[0] - idx
5
            n = len(nums)
7
            # If kth missing number is larger than
8
            # the last element of the array
9
            if k > missing(n - 1):
                return nums[-1] + k - missing(n - 1)
10
11
12
            left, right = 0, n - 1
            # find left = right index such that
13
            # missing(left - 1) < k <= missing(left)</pre>
14
15
            while left != right:
                pivot = left + (right - left) // 2
16
17
18
                if missing(pivot) < k:</pre>
19
                     left = pivot + 1
20
                else:
21
                     right = pivot
22
23
            # kth missing number is greater than nums[left - 1]
24
            # and less than nums[left]
25
            return nums[left - 1] + k - missing(left - 1)
```

Complexity Analysis

- ullet Time complexity: $\mathcal{O}(\log N)$ since it's a binary search algorithm in the worst case when the missing number is less than the last element of the array.
- ullet Space complexity : $\mathcal{O}(1)$ since it's a constant space solution.

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bhushan55 (/bhushan55) ★ 93 ② July 28, 2019 9:36 PM

the time complexity is not constant, you should only put for the worst case here.

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ywen1995 (/ywen1995) ★ 318 ② August 11, 2019 8:25 PM

The constant complexity is very misleading (or over simplified) here.



ilkercankaya (/ilkercankaya) ★ 89 ② December 20, 2019 9:21 AM

(/ilkercankaya)

Time Complexity is calculated by taking the worst-case into account. Saying that it is O(1) is extremely misleading for a lot of people. Please change it!

6 ∧ ∨ © Share ¬ Reply



nlackx (/nlackx) ★ 71 ② November 15, 2019 11:55 PM

The idea is to find the leftmost element such that the number of missing numbers until this element is **smaller** or equal to k.

should be greater



montabano1 (/montabano1) ★ 2 ② April 21, 2020 10:52 AM

I think using the phrase that approach 1 "doesn't profit from the fact that array is sorted." is wrong. If the array wasnt sorted we would not be able to find what numbers were missing?

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civabhusal (/civabhusal) 🖈 2 🧿 April 3, 2020 9:28 AM

How does the second approach take O(logN) time when missing(idx) takes O(N) time? Could you please kindly clarify?

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Prashanth_123 (/prashanth_123) ★ 0 ② April 21, 2020 5:27 PM

```
public int missingElement(int[] nums, int k) {
    int temp = k, index = Integer.MIN_VALUE, numMissingElements
= 0;
```

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pbu (/pbu) ★ 261 ② March 4, 2020 5:57 AM java, one pass:

```
class Solution {
   public int missingElement(int[] nums, int k) {
     int n = nums.length:
```

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letsGo99 (/letsgo99) ★4 ② March 16, 2020 11:38 PM

The time complexity is O(n). You use the lambda function which would iterate n times through the list before the binary search

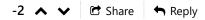
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FishFly (/fishfly) ★ -2 ② March 13, 2020 12:54 AM

The time complexity of lambda func is already O(N)...



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