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231. Power of two (/problems/power-of-two/)

Aug. 17, 2019 | 17.5K views

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Given an integer, write a function to determine if it is a power of two.

Example 1:

Input: 1

Output: true

Explanation: $2^{0} = 1$

Example 2:

Input: 16

Output: true

Explanation: $2^4 = 16$

Example 3:

Input: 218
Output: false

Solution

Overview

We're not going to discuss here an obvious $\mathcal{O}(\log N)$ time solution

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```

```
Copy
Java
      Python
   class Solution(object):
2
       def isPowerOfTwo(self, n):
3
           if n == 0:
4
                return False
5
            while n % 2 == 0:
6
               n /= 2
7
            return n == 1
```

Instead, the problem will be solved in $\mathcal{O}(1)$ time with the help of bitwise operators. The idea is to discuss such bitwise tricks as

- How to get / isolate the rightmost 1-bit: x & (-x).
- How to turn off (= set to 0) the rightmost 1-bit: x & (x 1).

These tricks are often used as something obvious in more complex bit-manipulation solutions, like for N Queens problem (https://leetcode.com/articles/n-queens-ii/), and it's important to recognize them to understand what is going on.

Intuition

The idea behind both solutions will be the same: a power of two in binary representation is one 1-bit, followed by some zeros:

```
1 = (00000001)_2
```

$$2 = (00000010)_2$$

$$4 = (00000100)_2$$

$$8 = (00001000)_2$$

A number which is not a power of two, has more than one 1-bit in its binary representation:

```
3 = (00000011)_2
```

$$5 = (00000101)_2$$

$$6 = (00000110)_2$$

$$7 = (00000111)_2$$

The only exception is 0, which should be treated separately.

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Approach 1: Bitwise Operators : Get the Rightmost 1-bit

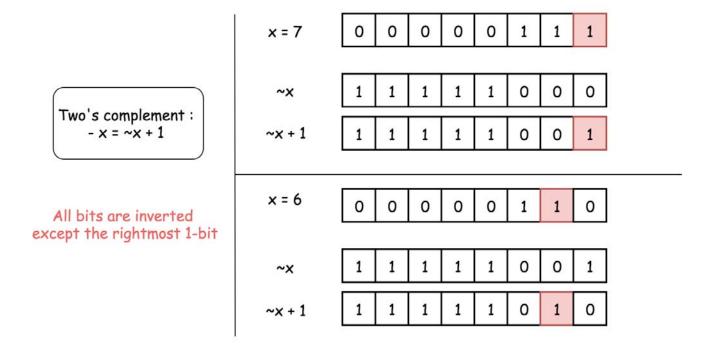
Get/Isolate the Rightmost 1-bit

Let's first discuss why x & (-x) is a way to keep the rightmost 1-bit and to set all the other bits to 0.

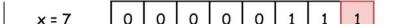
Basically, that works because of two's complement (https://en.wikipedia.org /wiki/Two%27s_complement). In two's complement notation -x is the same as $\neg x+1$. In other words, to compute -x one has to revert all bits in x and then to add 1 to the result.

Adding 1 to $\neg x$ in binary representation means to carry that 1-bit till the rightmost 0-bit in $\neg x$ and to set all the lower bits to zero. Note, that the rightmost 0-bit in $\neg x$ corresponds to the rightmost 1-bit in x.

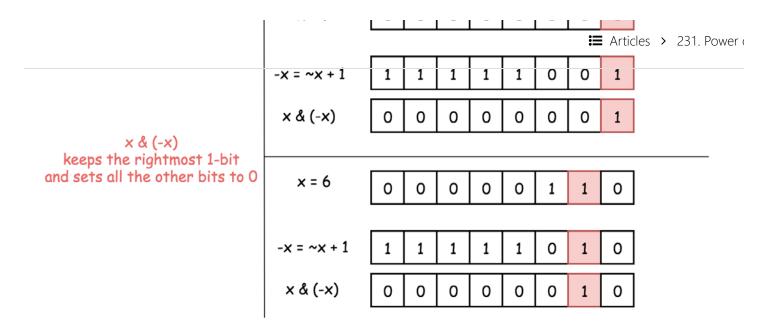
In summary, -x is the same as $\neg x+1$. This operation reverts all bits of x except the rightmost 1-bit.



Hence, x and -x have just one bit in common - the rightmost 1-bit. That means that x & (-x) would keep that rightmost 1-bit and set all the other bits to 0.



3 of 8

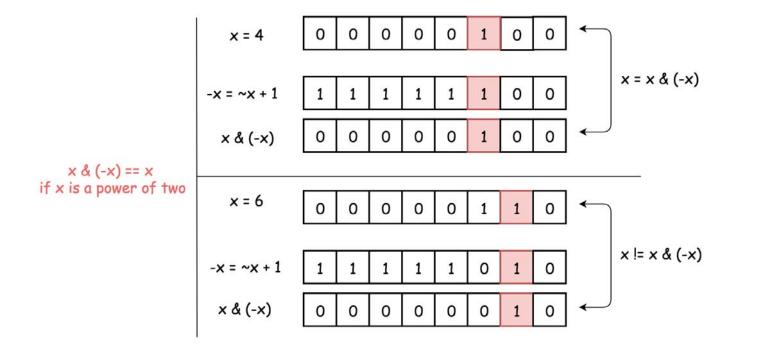


Detect Power of Two

So let's do x & (-x) to keep the rightmost 1-bit and to set all the others bits to zero. As discussed above, for the power of two it would result in x itself, since a power of two contains just one 1-bit.

Other numbers have more than 1-bit in their binary representation and hence for them x & (-x) would not be equal to x itself.

Hence a number is a power of two if x & (-x) == x.



Implementation

Complexity Analysis

- Time complexity : $\mathcal{O}(1)$.
- Space complexity : $\mathcal{O}(1)$.

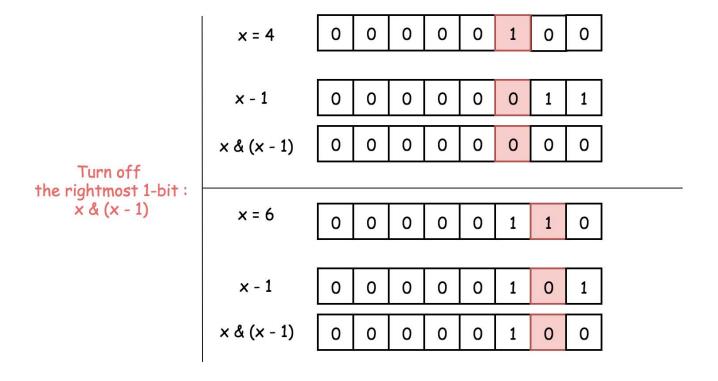
Approach 2: Bitwise operators: Turn off the Rightmost 1-bit

Turn off the Rightmost 1-bit

Let's first discuss why x & (x - 1) is a way to set the rightmost 1-bit to zero.

To subtract 1 means to change the rightmost 1-bit to 0 and to set all the lower bits to 1.

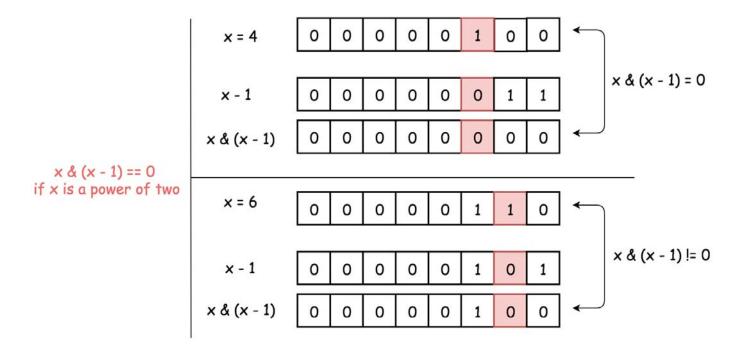
Now AND operator: the rightmost 1-bit will be turned off because 1 & 0 = 0, and all the lower bits as well.



Detect Power of Two

The solution is straightforward:

- 1. Power of two has just one 1-bit.
- 2. x & (x 1) sets this 1-bit to zero, and hence one has to verify if the result is zero x & (x 1) == 0.



Implementation

Complexity Analysis

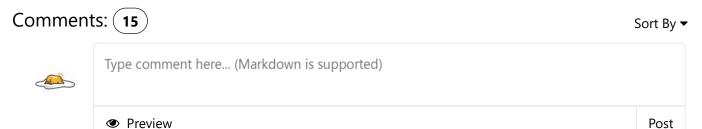
- ullet Time complexity : $\mathcal{O}(1)$.
- Space complexity : $\mathcal{O}(1)$.

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yendoan007 (/yendoan007) \bigstar 4 ② August 17, 2019 9:23 PM Great solution and explanation.



MartinPayne (/martinpayne) ★ 2 ② 2 days ago

Great explanation, maybe add a part that explains why you need to cast to long (I'm sure overflow but having pictures for that too would be helpful).

2 A V C Share Reply



nits2010 (/nits2010) \bigstar 572 • August 20, 2019 9:16 AM sir x = 8 binary is 1000 there are 3 zero at the end, not 2 zero.

and x = 8-1 = 7 has binary 111 not 011

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mjolewis (/mjolewis) ★ 2 ② August 18, 2019 11:22 AM Amazing solution.

2 A V C Share Reply



franklinqin0 (/franklinqin0) ★ 13 ④ March 26, 2020 6:55 AM

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The C and C++ solutions for approach 1 should've been for approach 2.

(/franklinqin0)

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maroochydore (/maroochydore) ★ 1 ② September 10, 2019 8:43 AM

I took granted that number is always integer type. but computer already deals with number as binary format. Handling number with bitwise gives me huge inspiration always.

1 ∧ ∨ ☑ Share ← Reply



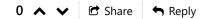
zzznotsomuch (/zzznotsomuch) ★ 27 ② 2 days ago

Today I learned! Great Post!



UMN-HKC (/umn-hkc) ★ 249 ② 2 days ago

you can just return false when $n \le 0$, why do you have to convert to long first?



(/umn hkc)

(1)2)

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