

### Assignment 1 Part 1

1.

$$A: p = 2i_A + (-2)j_A$$

$$B: p = 3i_B + 0.5j_B$$

$$C: p = -4i_C + 3j_C$$

2.

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.

```
modelMatrix.setAsIdentity();
modelMatrix *= Translate(1,1,1);
modelMatrix *= Scale(1,1,2);
```

4.

$$[0.5 \ 2.5 \ 2]^T$$

5.

$$A: \begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 0 & 0 & 3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad B: \begin{bmatrix} 0 & 0 & 1 & 2 \\ 0 & 1 & 0 & 3 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad C: \begin{bmatrix} 0 & 0 & 1 & 2 \\ 0 & 0.5 & 0 & 3.5 \\ -1 & 0 & 0 & -1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad D: \begin{bmatrix} 0 & 0 & 1 & 2 \\ 0 & 1 & 0 & 3 \\ -2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

6.

**For arbitrary tilted line  $y = mx + b$**

$$M = \begin{bmatrix} 1 & 0 & 0 & \cos\theta & -\sin\theta & 0 \\ 0 & 1 & b & \sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 \end{bmatrix} \quad \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad \begin{bmatrix} \cos\theta & \sin\theta & 0 \\ -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -b \\ 0 & 0 & 1 \end{bmatrix} M = \text{Translate}(0,b,0) * \text{RotateX}(\theta) * \text{Scale}(1,-1,1) * \text{RotateX}(-\theta) * \text{Translate}(0,-b,0)$$

**For arbitrary tilted line  $y = x - 1$  and  $\theta = 45$**

In OpenGL Shader code:

```

modelMatrix.setAsIdentity();
modelMatrix *= Translate(0,b,0);
modelMatrix *= RotateX( $\theta$ );
modelMatrix *= Scale(1,-1,1);
modelMatrix *= RotateX(- $\theta$ );
modelMatrix *= Translate(0,-b,0);

```

**For arbitrary tilted line  $y = x - 1$  and  $\theta = 45$**

M =

1	0	0		$\cos 45$	$-\sin 45$	0	1	0	0		$\cos 45$	$\sin 45$	0	1	0	0		
0	1	-1	*	$\sin 45$	$\cos 45$	0	*	0	-1	0	*	$-\sin 45$	$\cos 45$	0	*	0	1	1
0	0	1		0	0	1	0	0	1		0	0	1	0	0	1		

M =

0	1	1
1	0	-1
0	0	1

**For arbitrary tilted line  $y = x - 1$**

In OpenGL Shader code:

```

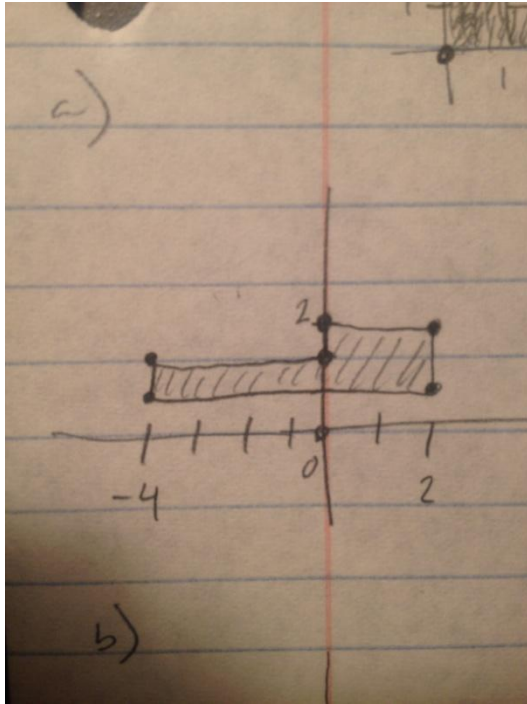
modelMatrix.setAsIdentity();
modelMatrix *= Translate(0,-1,0);
modelMatrix *= RotateX(45);
modelMatrix *= Scale(1,-1,1);
modelMatrix *= RotateX(-45);
modelMatrix *= Translate(0,1,0);

```

7.

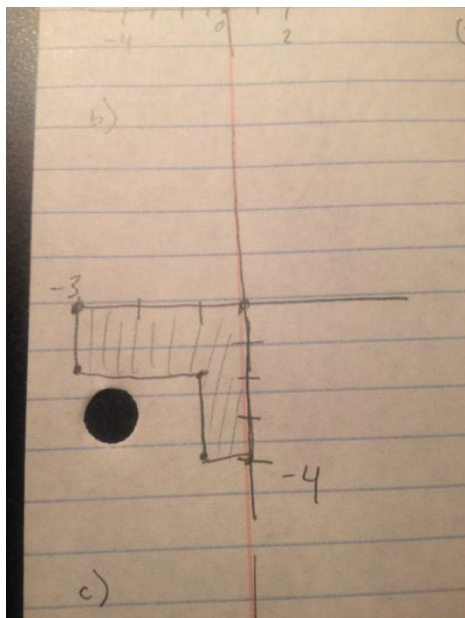
a)  $L' = ABCL$

```
modelMatrix *= Scale(2,1,1);  
modelMatrix *= Translate(1,1,0);  
modelMatrix *= RotateZ(90);  
drawL();
```

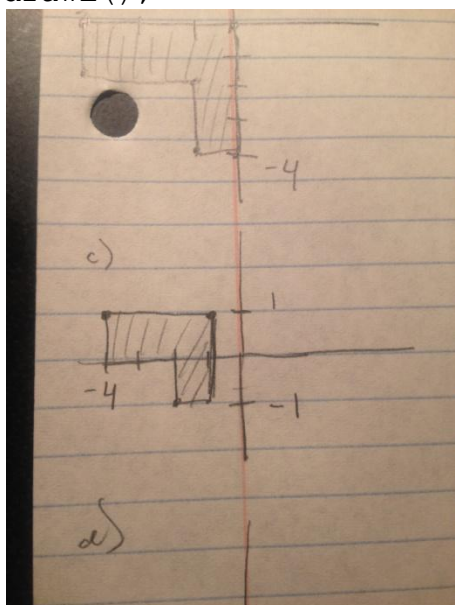


b)  $L' = CADL$

```
modelMatrix = matrixStack.pop();  
matrixStack.push(modelMatrix); //saves for part c  
modelMatrix *= RotateZ(90);  
modelMatrix *= Scale(2,1,1);  
modelMatrix *= Scale(-1,1,1);  
drawL();
```



c)  $L' = \text{CDDL}$   
`modelMatrix = matrixStack.pop();`  
`matrixStack.push(modelMatrix); //saves for part d`  
`modelMatrix *= RotateZ(90);`  
`modelMatrix *= Translate(1,1,0);`  
`modelMatrix *= Scale(-1,1,1);`  
`drawL();`



d)  $L' = \text{DCCADL}$   
`modelMatrix = matrixStack.pop();`  
`modelMatrix *= Scale(-1,1,1);`  
`modelMatrix *= RotateZ(90);`  
`modelMatrix *= RotateZ(90);`

```
modelMatrix *= Scale(2,1,1);  
modelMatrix *= Scale(-1,1,1);  
drawL();
```

