

assignment_2

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Problem 1. Regression

```
data <- read.csv("qsar_aquatic_toxicity.csv", sep = ";", header = FALSE)
names(data) <- c(
  "TPSA",
  "SAacc",
  "H050",
  "MLOGP",
  "RDCHI",
  "GATS1p",
  "nN",
  "C040",
  "LC50"
)

head(data)
```

```
##      TPSA    SAacc H050 MLOGP RDCHI GATS1p nN C040  LC50
## 1    0.00    0.000   0 2.419 1.225  0.667  0    0 3.740
## 2    0.00    0.000   0 2.638 1.401  0.632  0    0 4.330
## 3    9.23   11.000   0 5.799 2.930  0.486  0    0 7.019
## 4    9.23   11.000   0 5.453 2.887  0.495  0    0 6.723
## 5    9.23   11.000   0 4.068 2.758  0.695  0    0 5.979
## 6  215.34  327.629   3 0.189 4.677  1.333  0    4 6.064
```

a. Dataset splitting

Split the data into a training and a test set, with approximately 2/3 and 1/3 of the observations, respectively.

```
# Use 70% of dataset as training set and remaining 30% as testing set
set.seed(123)
sample <- sample.split(data$LC50, SplitRatio = 2/3)
train  <- subset(data, sample == TRUE)
test   <- subset(data, sample == FALSE)
```

```
cat("Dimension of Training Set:", paste(dim(train), collapse = "x"), "\nDimension of Test Set:", paste(
```

```
## Dimension of Training Set: 364x9
## Dimension of Test Set: 182x9
```

(i) Original Model

Model each of them directly as a linear effect

```
train_i = train
test_i = test
```

```
# Fit linear regression model on training data
model <- lm(LC50 ~ ., data=train_i)
```

```
summary(model)
```

```
##
## Call:
## lm(formula = LC50 ~ ., data = train_i)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8548 -0.8166 -0.1830  0.6771  4.8867
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.629264   0.312580   8.411 1.00e-15 ***
## TPSA         0.027092   0.003336   8.121 7.74e-15 ***
## SAacc        -0.015959   0.002652  -6.017 4.42e-09 ***
## H050         -0.003879   0.076369  -0.051 0.959522
## MLOGP         0.400783   0.081760   4.902 1.45e-06 ***
## RDCHI         0.654990   0.177787   3.684 0.000265 ***
## GATS1p        -0.589994   0.195299  -3.021 0.002702 **
## nN           -0.199466   0.059602  -3.347 0.000906 ***
## C040          -0.046002   0.091165  -0.505 0.614156
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.219 on 355 degrees of freedom
## Multiple R-squared:  0.5024, Adjusted R-squared:  0.4912
## F-statistic: 44.8 on 8 and 355 DF, p-value: < 2.2e-16
```

```
# Predict on training and test datasets
pred_train <- predict(model, newdata=train_i)
pred_test  <- predict(model, newdata=test_i)
```

```
# Adding predictions columns to the datasets
train_i$predicted_LC50 <- pred_train
test_i$predicted_LC50  <- pred_test
```

```
# Evaluate model: calculate MSE, RMSE, and R-squared for training and test sets
mse_train <- mean((train_i$LC50 - train_i$predicted_LC50)^2)
rmse_train <- sqrt(mse_train)
r2_train <- 1 - (sum((train_i$LC50 - train_i$predicted_LC50)^2) / sum((train_i$LC50 - mean(train_i$LC50))^2))

mse_test <- mean((test_i$LC50 - test_i$predicted_LC50)^2)
```

```
rmse_test <- sqrt(mse_test)
r2_test <- 1 - (sum((test_i$LC50 - test_i$predicted_LC50)^2) / sum((test_i$LC50 - mean(test_i$LC50))^2))
```

```
cat(paste0(
  "Training Metrics:\n",
  "MSE (Train): ", mse_train, "\n",
  "RMSE (Train): ", rmse_train, "\n",
  "R-squared (Train): ", r2_train, "\n\n",

  "Test Metrics:\n",
  "MSE (Test): ", mse_test, "\n",
  "RMSE (Test): ", rmse_test, "\n",
  "R-squared (Test): ", r2_test, "\n"
))
```

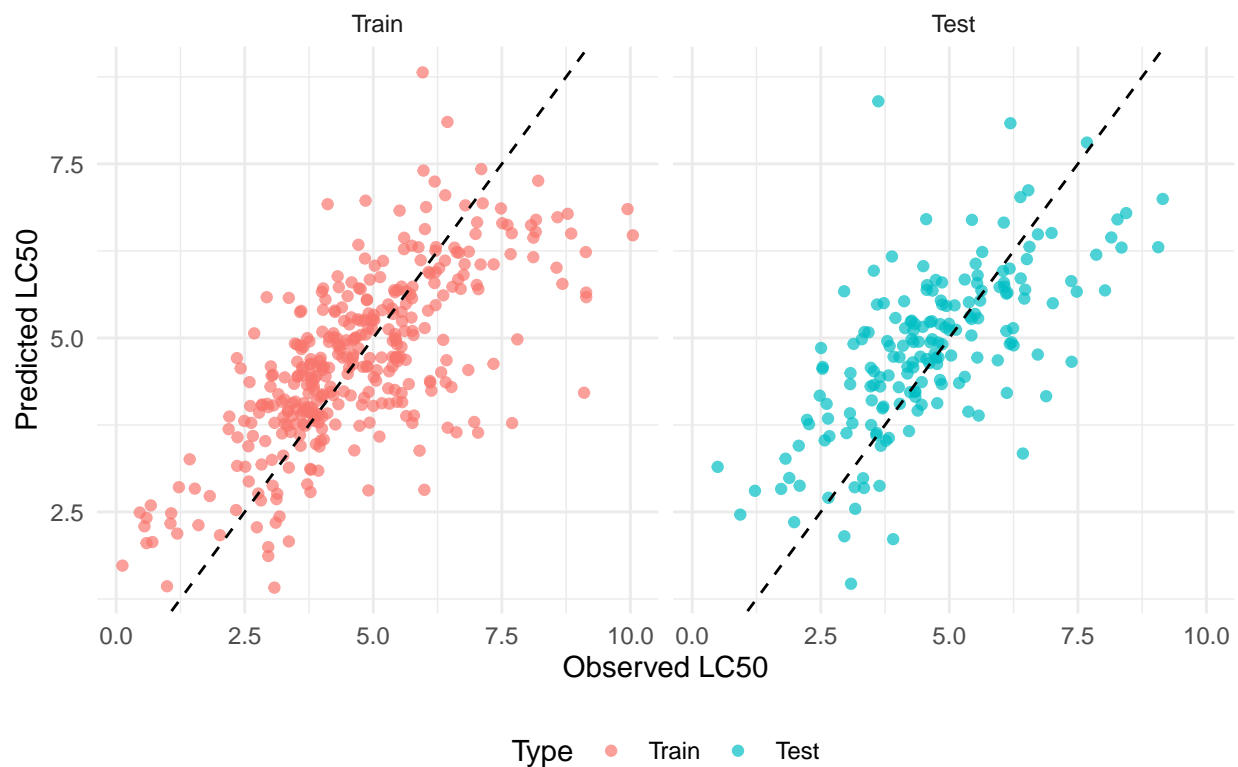
```
## Training Metrics:
## MSE (Train): 1.44990640082018
## RMSE (Train): 1.20412059230801
## R-squared (Train): 0.502397645581479
##
## Test Metrics:
## MSE (Test): 1.40224882922927
## RMSE (Test): 1.18416587910194
## R-squared (Test): 0.433587696937759
```

```
# Combine data for plotting
train_i$Type <- 'Train'
test_i$Type <- 'Test'
combined_data <- rbind(train_i, test_i)

combined_data$Type <- factor(combined_data$Type, levels = c('Train', 'Test'))

# Plotting observed vs predicted LC50 values
ggplot(combined_data, aes(x = LC50, y = predicted_LC50, color = Type)) +
  geom_point(alpha = 0.7) +
  geom_abline(intercept = 0, slope = 1, linetype = "dashed") +
  labs(title = "Observed vs Predicted LC50", x = "Observed LC50", y = "Predicted LC50") +
  theme_minimal() +
  facet_wrap(~Type) +
  theme(legend.position = "bottom")
```

Observed vs Predicted LC50



(ii). Dummy encoding

Transform 3 count variables (H050, nN, C040) using a 0/1 dummy encoding where 0 represents absence of the specific atom and 1 represents presence of the specific atoms.

```
# To make sure we use the same split in (i)
train_ii = train
test_ii = test

# Transform 3 count variables (H050, nN, C040) into 0/1 in train and test datasets

train_ii$H050 <- ifelse(train_ii$H050 > 0, 1, 0)
train_ii$nN <- ifelse(train_ii$nN > 0, 1, 0)
train_ii$C040 <- ifelse(train_ii$C040 > 0, 1, 0)

test_ii$H050 <- ifelse(test_ii$H050 > 0, 1, 0)
test_ii$nN <- ifelse(test_ii$nN > 0, 1, 0)
test_ii$C040 <- ifelse(test_ii$C040 > 0, 1, 0)

head(train_ii)
```

```
##      TPSA   SAacc H050 MLOGP RDCHI GATS1p nN C040  LC50
## 1    0.00   0.000   0  2.419  1.225  0.667  0   0  3.740
## 3    9.23  11.000   0  5.799  2.930  0.486  0   0  7.019
```

```
## 6 215.34 327.629 1 0.189 4.677 1.333 0 1 6.064
## 7 9.23 11.000 0 2.723 2.321 1.165 0 0 7.337
## 9 0.00 0.000 0 2.067 1.800 1.250 0 0 3.941
## 10 0.00 0.000 0 2.746 1.667 1.400 0 0 3.809
```

```
# Fit linear regression model on transformed training data
model_transform_dummy <- lm(LC50 ~ ., data = train_ii)

summary(model_transform_dummy)
```

```
##
## Call:
## lm(formula = LC50 ~ ., data = train_ii)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.0873 -0.8306 -0.1303  0.6571  5.0526
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.693545   0.315949   8.525 4.44e-16 ***
## TPSA         0.023267   0.003365   6.914 2.20e-11 ***
## SAacc        -0.014731   0.002407  -6.121 2.46e-09 ***
## H050         -0.090233   0.161558  -0.559  0.57684
## MLOGP         0.436885   0.082632   5.287 2.18e-07 ***
## RDCHI         0.553158   0.180181   3.070  0.00231 **
## GATS1p        -0.539057   0.190296  -2.833  0.00488 **
## nN            0.018072   0.156479   0.115  0.90812
## C040         -0.124928   0.169094  -0.739  0.46051
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.239 on 355 degrees of freedom
## Multiple R-squared:  0.4864, Adjusted R-squared:  0.4749
## F-statistic: 42.03 on 8 and 355 DF, p-value: < 2.2e-16
```

```
# Predict on training and test datasets
pred_train_transform_dummy <- predict(model, newdata=train_ii)
pred_test_transform_dummy <- predict(model, newdata=test_ii)
```

```
# Adding predictions columns to the datasets
train_ii$predicted_LC50 <- pred_train_transform_dummy
test_ii$predicted_LC50 <- pred_test_transform_dummy
```

```
# Evaluate model: calculate MSE, RMSE, and R-squared for training and test sets
mse_train_transform_dummy <- mean((train_ii$LC50 - train_ii$predicted_LC50)^2)
rmse_train_transform_dummy <- sqrt(mse_train_transform_dummy)
r2_train_transform_dummy <- 1 - (sum((train_ii$LC50 - train_ii$predicted_LC50)^2) / sum((train_ii$LC50 - mean(train_ii$LC50))^2))

mse_test_transform_dummy <- mean((test_ii$LC50 - test_ii$predicted_LC50)^2)
rmse_test_transform_dummy <- sqrt(mse_test_transform_dummy)
r2_test_transform_dummy <- 1 - (sum((test_ii$LC50 - test_ii$predicted_LC50)^2) / sum((test_ii$LC50 - mean(test_ii$LC50))^2))
```

```

cat(paste0(
  "Training Metrics:\n",
  "MSE (Train): ", mse_train_transform_dummy, "\n",
  "RMSE (Train): ", rmse_train_transform_dummy, "\n",
  "R-squared (Train): ", r2_train_transform_dummy, "\n\n",

  "Test Metrics:\n",
  "MSE (Test): ", mse_test_transform_dummy, "\n",
  "RMSE (Test): ", rmse_test_transform_dummy, "\n",
  "R-squared (Test): ", r2_test_transform_dummy, "\n"
))

```

```

## Training Metrics:
## MSE (Train): 1.53935201233042
## RMSE (Train): 1.24070625545711
## R-squared (Train): 0.471700252387877
##
## Test Metrics:
## MSE (Test): 1.53043849004967
## RMSE (Test): 1.23710892408457
## R-squared (Test): 0.381807870490008

```

```

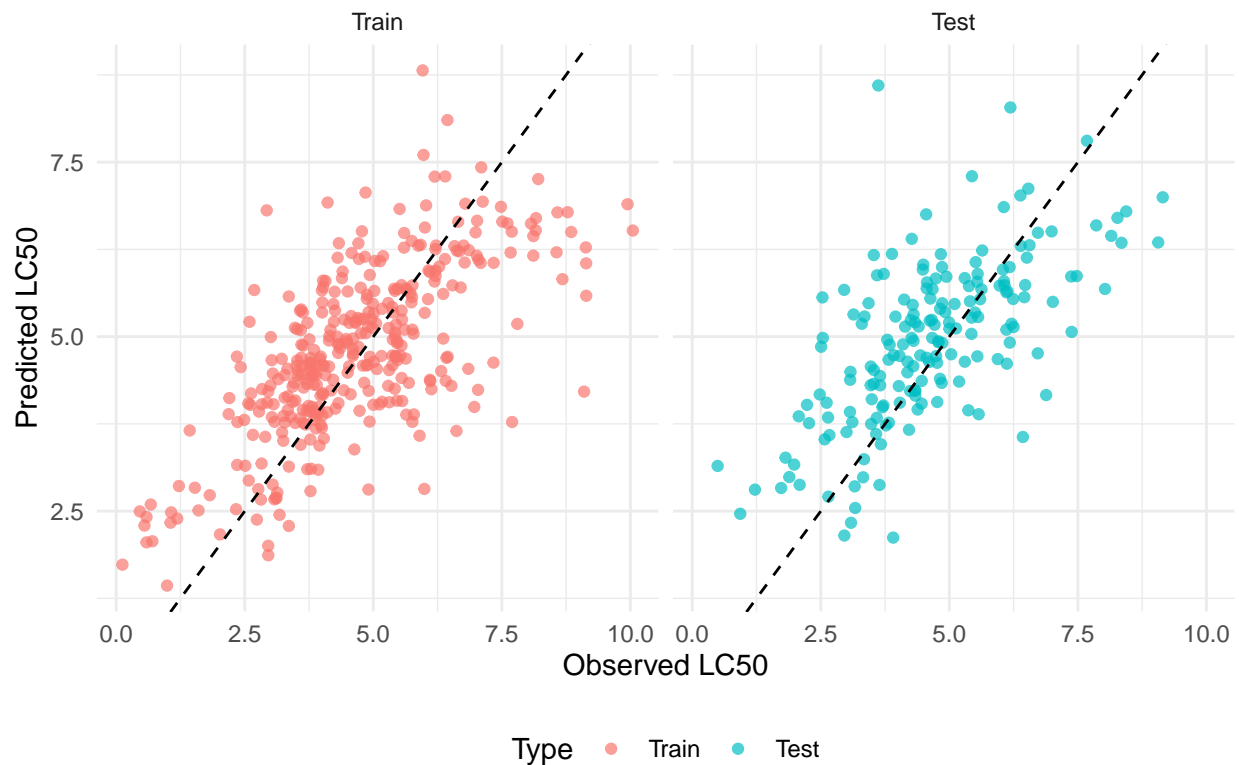
# Combine data for plotting
train_ii$Type <- 'Train'
test_ii$Type <- 'Test'
combined_data <- rbind(train_ii, test_ii)

combined_data$Type <- factor(combined_data$Type, levels = c('Train', 'Test'))

# Plotting observed vs predicted LC50 values
ggplot(combined_data, aes(x = LC50, y = predicted_LC50, color = Type)) +
  geom_point(alpha = 0.7) +
  geom_abline(intercept = 0, slope = 1, linetype = "dashed") +
  labs(title = "Dummy Encoding: Observed vs Predicted LC50", x = "Observed LC50", y = "Predicted LC50")
  theme_minimal() +
  facet_wrap(~Type) +
  theme(legend.position = "bottom")

```

Dummy Encoding: Observed vs Predicted LC50



```
# Prepare combined data
train_combined <- train_i[, c("LC50", "predicted_LC50")]
train_combined$Method <- 'Original'
train_combined$Type <- 'Train'
train_ii_combined <- train_ii[, c("LC50", "predicted_LC50")]
train_ii_combined$Method <- 'Dummy'
train_ii_combined$Type <- 'Train'
train_combined_all <- rbind(train_combined, train_ii_combined)
test_combined <- test_i[, c("LC50", "predicted_LC50")]
test_combined$Method <- 'Original'
test_combined$Type <- 'Test'
test_ii_combined <- test_ii[, c("LC50", "predicted_LC50")]
test_ii_combined$Method <- 'Dummy'
test_ii_combined$Type <- 'Test'
test_combined_all <- rbind(test_combined, test_ii_combined)
# Convert 'Method' and 'Type' to factors
train_combined_all$Method <- factor(train_combined_all$Method, levels = c('Original', 'Dummy'))
test_combined_all$Method <- factor(test_combined_all$Method, levels = c('Original', 'Dummy'))
# Function to draw regression lines
add_regression_lines <- function(df, original_model, dummy_model) {
  ggplot(df, aes(x = LC50, y = predicted_LC50, color = Method)) +
    geom_point(alpha = 0.7) +
    geom_smooth(method = "lm", formula = y ~ x, se = FALSE,
    aes(linetype = Method),
    data = df[df$Method == 'Original', ],
    color = 'blue') +
```



```

geom_smooth(method = "lm", formula = y ~ x, se = FALSE,
aes(linetype = Method),
data = df[df$Method == 'Dummy', ],
color = 'red') +
geom_abline(intercept = 0, slope = 1, linetype = "dashed") +
labs(x = "Observed LC50", y = "Predicted LC50", title = df$Type[1]) +
theme_minimal() +
theme(legend.position = "bottom")
}

# Plot training data with both regression lines
train_plot <- add_regression_lines(train_combined_all, model, model_transform_dummy)
train_plot <- train_plot + labs(title = "Training Data")
# Plot testing data with both regression lines
test_plot <- add_regression_lines(test_combined_all, model, model_transform_dummy)
test_plot <- test_plot + labs(title = "Testing Data")
# Display plots side by side
grid.arrange(train_plot, test_plot, ncol = 2)

```



b. Repeating the procedure 200 times

Procedure

- Randomly splitting training/test (70%/30%).
- Fit the models with 2 options (i) Original model and (ii) Dummy encoding.

- Record the test errors (MSE/RMSE/ R^2).

```
# Initialize vectors to store test errors
mse_test_errors_i <- numeric(200)
rmse_test_errors_i <- numeric(200)
r2_test_errors_i <- numeric(200)
mse_test_errors_ii <- numeric(200)
rmse_test_errors_ii <- numeric(200)
r2_test_errors_ii <- numeric(200)

# Repeat the procedure 200 times
set.seed(2)
for (i in 1:200) {
  # Split the data
  sample <- sample.split(data$LC50, SplitRatio = 2/3)
  train <- subset(data, sample == TRUE)
  test <- subset(data, sample == FALSE)

  # Option (i): Original model
  model <- lm(LC50 ~ ., data=train)
  pred_test_i <- predict(model, newdata=test)
  mse_test_i <- mean((test$LC50 - pred_test_i)^2)
  rmse_test_i <- sqrt(mse_test_i)
  r2_test_i <- 1 - (sum((test$LC50 - pred_test_i)^2) / sum((test$LC50 - mean(test$LC50))^2))

  # Option (ii): Dummy encoding
  train$H050 <- ifelse(train$H050 > 0, 1, 0)
  train$nN <- ifelse(train$nN > 0, 1, 0)
  train$C040 <- ifelse(train$C040 > 0, 1, 0)

  test$H050 <- ifelse(test$H050 > 0, 1, 0)
  test$nN <- ifelse(test$nN > 0, 1, 0)
  test$C040 <- ifelse(test$C040 > 0, 1, 0)

  model_ii <- lm(LC50 ~ ., data = train)
  pred_test_ii <- predict(model_ii, newdata = test)
  mse_test_ii <- mean((test$LC50 - pred_test_ii)^2)
  rmse_test_ii <- sqrt(mse_test_ii)
  r2_test_ii <- 1 - (sum((test$LC50 - pred_test_ii)^2) / sum((test$LC50 - mean(test$LC50))^2))

  # Record the test errors
  mse_test_errors_i[i] <- mse_test_i
  rmse_test_errors_i[i] <- rmse_test_i
  r2_test_errors_i[i] <- r2_test_i

  mse_test_errors_ii[i] <- mse_test_ii
  rmse_test_errors_ii[i] <- rmse_test_ii
  r2_test_errors_ii[i] <- r2_test_ii
}
```

Make a plot that illustrates the empirical distributions of the test error for each modelling option and compare the average test error. What is the point of repeating the experiment in this way before drawing any conclusions? Try to explain why one often obtains, like in this case, a worse result by using option (ii).

Initials insight:

- Method 1: performs better in term of MSE
- Method 2: better in reduce over fitting

```
# Calculate and print average test errors
average_test_error_i <- mean(mse_test_errors_i)
average_rmse_error_i <- mean(rmse_test_errors_i)
average_r2_error_i <- mean(r2_test_errors_i)

average_test_error_ii <- mean(mse_test_errors_ii)
average_rmse_error_ii <- mean(rmse_test_errors_ii)
average_r2_error_ii <- mean(r2_test_errors_ii)

cat(paste0(
  "Average Test Errors (Original Model):\n",
  "MSE: ", average_test_error_i, "\n",
  "RMSE: ", average_rmse_error_i, "\n",
  "R-squared: ", average_r2_error_i, "\n\n",

  "Average Test Errors (Dummy Model):\n",
  "MSE: ", average_test_error_ii, "\n",
  "RMSE: ", average_rmse_error_ii, "\n",
  "R-squared: ", average_r2_error_ii, "\n"
))

## Average Test Errors (Original Model):
## MSE: 1.47708146772242
## RMSE: 1.21330895603276
## R-squared: 0.460485255063669
##
## Average Test Errors (Dummy Model):
## MSE: 1.52752950559007
## RMSE: 1.23398478875802
## R-squared: 0.442128799570138

# Create data frames for plotting
errors_df_mse <- data.frame(
  Error = c(mse_test_errors_i, mse_test_errors_ii),
  Metric = 'MSE',
  Model = factor(rep(c("Original", "Dummy"), each = 200))
)
errors_df_rmse <- data.frame(
  Error = c(rmse_test_errors_i, rmse_test_errors_ii),
  Metric = 'RMSE',
  Model = factor(rep(c("Original", "Dummy"), each = 200))
)
errors_df_r2 <- data.frame(
  Error = c(r2_test_errors_i, r2_test_errors_ii),
  Metric = 'R-squared',
  Model = factor(rep(c("Original", "Dummy"), each = 200))
)
errors_df <- rbind(errors_df_mse, errors_df_rmse, errors_df_r2)

# Ensure the 'Metric' factor has the correct level order
```

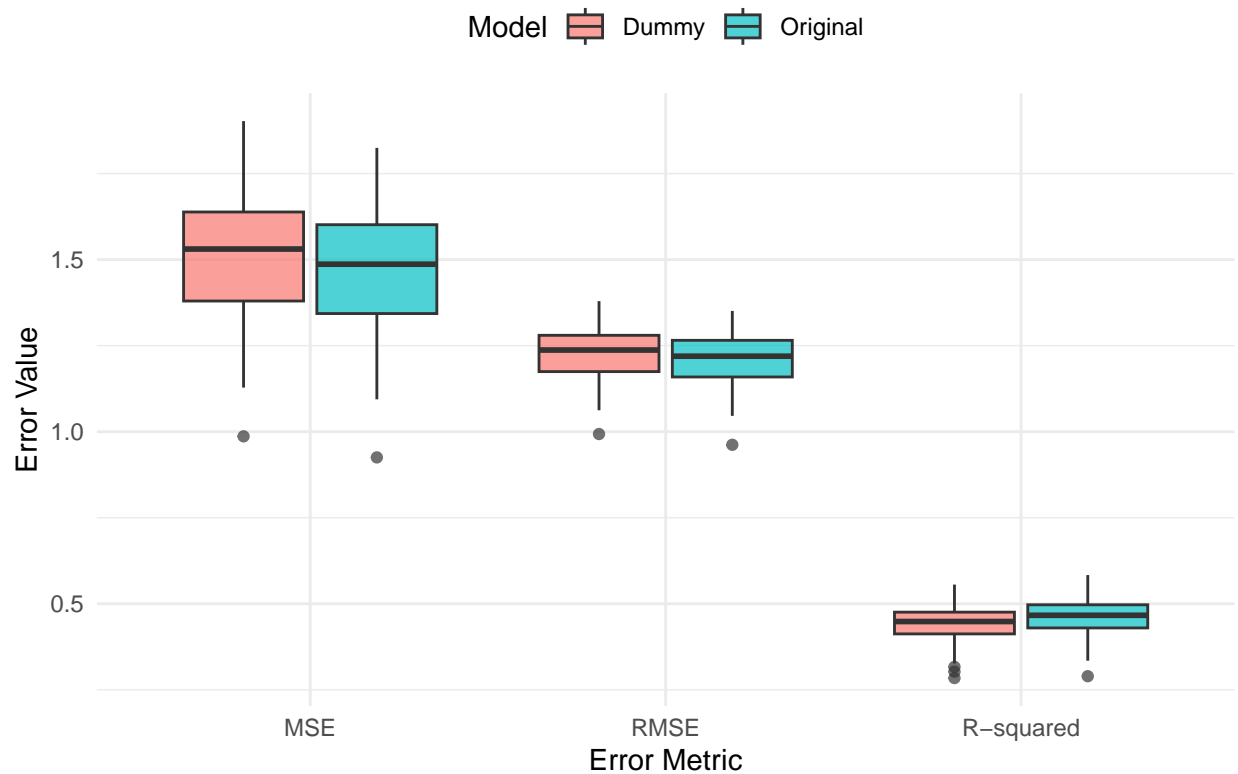
```
errors_df$Metric <- factor(errors_df$Metric, levels = c('MSE', 'RMSE', 'R-squared'))

# Plot the empirical distributions of the test errors
ggplot(errors_df, aes(x = Error, fill = Model)) +
  geom_density(alpha = 0.5) +
  facet_wrap(~ Metric, scales = "free") +
  labs(title = "Empirical Distributions of Test Errors", x = "Test Error", y = "Density") +
  theme_minimal()
```



```
# Plot the empirical distributions of the test errors using boxplots
ggplot(errors_df, aes(x = Metric, y = Error, fill = Model)) +
  geom_boxplot(alpha = 0.7) +
  labs(title = "Boxplots of Test Errors", x = "Error Metric", y = "Error Value") +
  theme_minimal() +
  theme(legend.position = "top")
```

Boxplots of Test Errors



c. Variable selection procedures

(at least backward elimination and forward selection) with different stopping criteria (at least AIC and BIC) and compare the results. Do you obtain the same model?

```
# Split the data into training (2/3) and test (1/3) sets
set.seed(123)
sample <- sample.split(data$LC50, SplitRatio = 2/3)
train <- subset(data, sample == TRUE)
test <- subset(data, sample == FALSE)

# Set up full and null model
full.model <- lm(LC50 ~ ., data = train)
null.model <- lm(LC50 ~ 1, data = train)

# Set up target and number of variables
y <- train$LC50
num_vars <- ncol(train) - 1 # exclude the response variable column
```

Forward Selection

```
# With AIC
model.forward.aic <- stepAIC(null.model, scope = list(lower = null.model, upper = full.model), direction="both")
summary(model.forward.aic)
```

```
##
## Call:
## lm(formula = LC50 ~ MLOGP + TPSA + SAacc + nN + RDCHI + GATS1p,
##     data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8194 -0.8018 -0.1737  0.6654  4.8981
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.653540   0.285743   9.286 < 2e-16 ***
## MLOGP        0.404067   0.078544   5.144 4.44e-07 ***
## TPSA         0.027138   0.003284   8.265 2.78e-15 ***
## SAacc        -0.016185   0.002177  -7.435 7.84e-13 ***
## nN           -0.201305   0.058114  -3.464 0.000597 ***
## RDCHI         0.639082   0.174662   3.659 0.000291 ***
## GATS1p        -0.589921   0.183821  -3.209 0.001452 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.216 on 357 degrees of freedom
## Multiple R-squared:  0.502, Adjusted R-squared:  0.4937
## F-statistic: 59.98 on 6 and 357 DF, p-value: < 2.2e-16
```

```
# With BIC
# If we set it to k = log(n), the function considers the BIC.

model.forward.bic <- stepAIC(null.model, scope = list(lower = null.model, upper = full.model), direction="both")
summary(model.forward.bic)
```

```
##
## Call:
## lm(formula = LC50 ~ MLOGP + TPSA + SAacc + nN + RDCHI + GATS1p,
##     data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8194 -0.8018 -0.1737  0.6654  4.8981
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.653540   0.285743   9.286 < 2e-16 ***
## MLOGP        0.404067   0.078544   5.144 4.44e-07 ***
## TPSA         0.027138   0.003284   8.265 2.78e-15 ***
## SAacc        -0.016185   0.002177  -7.435 7.84e-13 ***
## nN           -0.201305   0.058114  -3.464 0.000597 ***
## RDCHI         0.639082   0.174662   3.659 0.000291 ***
## GATS1p        -0.589921   0.183821  -3.209 0.001452 **
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.216 on 357 degrees of freedom
## Multiple R-squared:  0.502, Adjusted R-squared:  0.4937
## F-statistic: 59.98 on 6 and 357 DF,  p-value: < 2.2e-16
```

Backward Elimination

```
# With AIC
model.backward.aic <- stepAIC(full.model, direction = 'backward', trace = FALSE)
summary(model.backward.aic)
```

```
##
## Call:
## lm(formula = LC50 ~ TPSA + SAacc + MLOGP + RDCHI + GATS1p + nN,
##     data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8194 -0.8018 -0.1737  0.6654  4.8981
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.653540   0.285743   9.286 < 2e-16 ***
## TPSA         0.027138   0.003284   8.265 2.78e-15 ***
## SAacc        -0.016185   0.002177  -7.435 7.84e-13 ***
## MLOGP         0.404067   0.078544   5.144 4.44e-07 ***
## RDCHI         0.639082   0.174662   3.659 0.000291 ***
## GATS1p        -0.589921   0.183821  -3.209 0.001452 **
## nN            -0.201305   0.058114  -3.464 0.000597 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.216 on 357 degrees of freedom
## Multiple R-squared:  0.502, Adjusted R-squared:  0.4937
## F-statistic: 59.98 on 6 and 357 DF,  p-value: < 2.2e-16
```

```
# With BIC
model.backward.bic <- stepAIC(full.model, direction = 'backward', k = log(nrow(train)), trace = FALSE)
summary(model.backward.bic)
```

```
##
## Call:
## lm(formula = LC50 ~ TPSA + SAacc + MLOGP + RDCHI + GATS1p + nN,
##     data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8194 -0.8018 -0.1737  0.6654  4.8981
##
```

```
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.653540   0.285743   9.286 < 2e-16 ***
## TPSA         0.027138   0.003284   8.265 2.78e-15 ***
## SAacc        -0.016185   0.002177  -7.435 7.84e-13 ***
## MLOGP         0.404067   0.078544   5.144 4.44e-07 ***
## RDCHI         0.639082   0.174662   3.659 0.000291 ***
## GATS1p        -0.589921   0.183821  -3.209 0.001452 **
## nN           -0.201305   0.058114  -3.464 0.000597 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.216 on 357 degrees of freedom
## Multiple R-squared:  0.502, Adjusted R-squared:  0.4937
## F-statistic: 59.98 on 6 and 357 DF, p-value: < 2.2e-16
```

Stepwise Selection

With AIC

```
model.stepwise.aic <- stepAIC(null.model, scope = list(lower = null.model, upper = full.model), direction = "both")
summary(model.stepwise.aic)
```

```
##
## Call:
## lm(formula = LC50 ~ MLOGP + TPSA + SAacc + nN + RDCHI + GATS1p,
##     data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8194 -0.8018 -0.1737  0.6654  4.8981
##
## Coefficients:
##           Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.653540   0.285743   9.286 < 2e-16 ***
## MLOGP         0.404067   0.078544   5.144 4.44e-07 ***
## TPSA         0.027138   0.003284   8.265 2.78e-15 ***
## SAacc        -0.016185   0.002177  -7.435 7.84e-13 ***
## nN           -0.201305   0.058114  -3.464 0.000597 ***
## RDCHI         0.639082   0.174662   3.659 0.000291 ***
## GATS1p        -0.589921   0.183821  -3.209 0.001452 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.216 on 357 degrees of freedom
## Multiple R-squared:  0.502, Adjusted R-squared:  0.4937
## F-statistic: 59.98 on 6 and 357 DF, p-value: < 2.2e-16
```

With BIC

```
model.stepwise.bic <- stepAIC(null.model, scope = list(lower = null.model, upper = full.model), direction = "both")
summary(model.stepwise.bic)
```

```
##
```



```
## Call:
## lm(formula = LC50 ~ MLOGP + TPSA + SAacc + nN + RDCHI + GATS1p,
##     data = train)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.8194 -0.8018 -0.1737  0.6654  4.8981
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  2.653540   0.285743   9.286  < 2e-16 ***
## MLOGP        0.404067   0.078544   5.144 4.44e-07 ***
## TPSA         0.027138   0.003284   8.265 2.78e-15 ***
## SAacc        -0.016185   0.002177  -7.435 7.84e-13 ***
## nN           -0.201305   0.058114  -3.464 0.000597 ***
## RDCHI         0.639082   0.174662   3.659 0.000291 ***
## GATS1p        -0.589921   0.183821  -3.209 0.001452 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.216 on 357 degrees of freedom
## Multiple R-squared:  0.502, Adjusted R-squared:  0.4937
## F-statistic: 59.98 on 6 and 357 DF, p-value: < 2.2e-16
```

Model Comparison

```
# Predict on the test set using all models
test$pred_backward_aic <- predict(model.backward.aic, newdata = test)
test$pred_forward_aic <- predict(model.forward.aic, newdata = test)
test$pred_stepwise_aic <- predict(model.stepwise.aic, newdata = test)
test$pred_backward_bic <- predict(model.backward.bic, newdata = test)
test$pred_forward_bic <- predict(model.forward.bic, newdata = test)
test$pred_stepwise_bic <- predict(model.stepwise.bic, newdata = test)

# Calculate MSE, RMSE, and R-squared for each model
mse <- function(actual, predicted) mean((actual - predicted)^2)
rmse <- function(actual, predicted) sqrt(mse(actual, predicted))
r2 <- function(actual, predicted) 1 - (sum((actual - predicted)^2) / sum((actual - mean(actual))^2))

metrics <- data.frame(
  Model = c("Backward AIC", "Forward AIC", "Stepwise AIC", "Backward BIC", "Forward BIC", "Stepwise BIC"),
  MSE = c(
    mse(test$LC50, test$pred_backward_aic),
    mse(test$LC50, test$pred_forward_aic),
    mse(test$LC50, test$pred_stepwise_aic),
    mse(test$LC50, test$pred_backward_bic),
    mse(test$LC50, test$pred_forward_bic),
    mse(test$LC50, test$pred_stepwise_bic)
  ),
  RMSE = c(
    rmse(test$LC50, test$pred_backward_aic),
    rmse(test$LC50, test$pred_forward_aic),
    rmse(test$LC50, test$pred_stepwise_aic),
    rmse(test$LC50, test$pred_backward_bic),
    rmse(test$LC50, test$pred_forward_bic),
    rmse(test$LC50, test$pred_stepwise_bic)
  ),
  R2 = c(
    r2(test$LC50, test$pred_backward_aic),
    r2(test$LC50, test$pred_forward_aic),
    r2(test$LC50, test$pred_stepwise_aic),
    r2(test$LC50, test$pred_backward_bic),
    r2(test$LC50, test$pred_forward_bic),
    r2(test$LC50, test$pred_stepwise_bic)
  )
)
```

```

rmse(test$LC50, test$pred_stepwise_aic),
rmse(test$LC50, test$pred_backward_bic),
rmse(test$LC50, test$pred_forward_bic),
rmse(test$LC50, test$pred_stepwise_bic)
),
R2 = c(
  r2(test$LC50, test$pred_backward_aic),
  r2(test$LC50, test$pred_forward_aic),
  r2(test$LC50, test$pred_stepwise_aic),
  r2(test$LC50, test$pred_backward_bic),
  r2(test$LC50, test$pred_forward_bic),
  r2(test$LC50, test$pred_stepwise_bic)
)
)
print(metrics)

```

```

##           Model      MSE      RMSE      R2
## 1 Backward AIC 1.398176 1.182445 0.4352328
## 2 Forward AIC 1.398176 1.182445 0.4352328
## 3 Stepwise AIC 1.398176 1.182445 0.4352328
## 4 Backward BIC 1.398176 1.182445 0.4352328
## 5 Forward BIC 1.398176 1.182445 0.4352328
## 6 Stepwise BIC 1.398176 1.182445 0.4352328

```

d. Ridge Regression

```

set.seed(123)
sample <- sample.split(data$LC50, SplitRatio = 2/3)
train <- subset(data, sample == TRUE)
test <- subset(data, sample == FALSE)

x_train <- as.matrix(train[, -9])
y_train <- train$LC50
x_test <- as.matrix(test[, -9])
y_test <- test$LC50

```

Cross Validation

```

# Reference: https://bookdown.org/ssjackson300/Machine-Learning-Lecture-Notes/choosing-lambda.html

# Define a grid of lambda values
lambda_grid <- 10^seq(10, -2, length = 100)

# Perform cross-validation for ridge regression
cv_ridge <- cv.glmnet(x_train,
  y_train,
  alpha = 0,
  lambda = lambda_grid,
  standardize = TRUE
)

```

```

    )
best_lambda_cv <- cv_ride$lambda.min
print(paste("Best Lambda from Cross-Validation:", best_lambda_cv))

## [1] "Best Lambda from Cross-Validation: 0.0174752840000768"

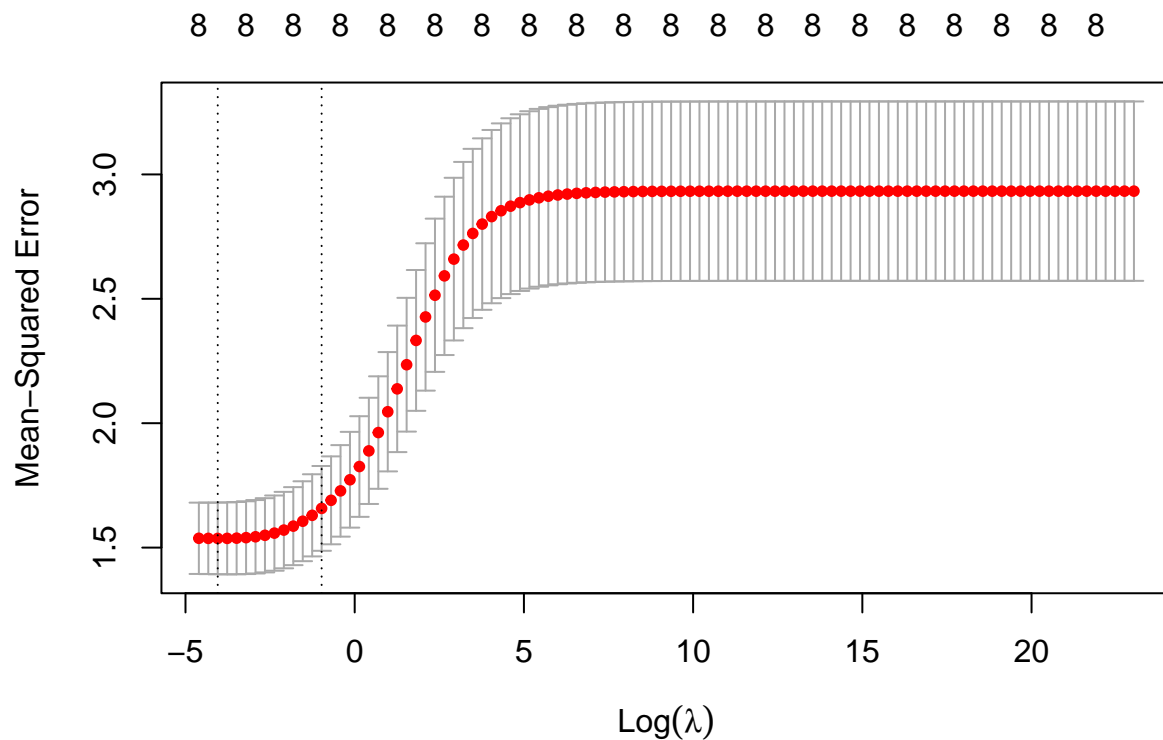
# Predict and evaluate on test data
ridge_pred_cv <- predict(cv_ride, s = best_lambda_cv, newx = x_test)
mse_cv <- mean((ridge_pred_cv - y_test)^2)
rmse_cv <- sqrt(mse_cv)
r2_cv <- 1 - (sum((ridge_pred_cv - y_test)^2) / sum((y_test - mean(y_test))^2))

cat(paste0(
  "MSE: ", mse_cv, "\n",
  "RMSE (Test): ", rmse_cv, "\n",
  "R-squared (Test): ", r2_cv, "\n"
))

## MSE: 1.39984196703498
## RMSE (Test): 1.18314917361885
## R-squared (Test): 0.434559904102569

plot(cv_ride)

```



Bootstrap Procedure

Reference: https://pages.stat.wisc.edu/~kdlevin/teaching/Fall2022/STAT340/lects/L13_bootstrap.html

```
# Define ridge regression function for bootstrap
ridge_bootstrap <- function(data, lambda, B = 100) {
  n <- nrow(data) # number of observations
  boot_mses <- numeric(B)

  for (i in 1:B) {
    resample_indices <- sample(1:n, n, replace = TRUE)

    # resampled_data <- fin_pairs[resample_indices,] fin_pairs = [X, Y]
    resampled_data <- data[resample_indices, ]

    x_boot <- as.matrix(resampled_data[, -9])
    y_boot <- resampled_data$LC50

    # Apply ridge regression and predict in this resampling data set
    ridge_model <- glmnet(x_boot, y_boot, alpha = 0, lambda = lambda, standardize = TRUE)
    boot_pred <- predict(ridge_model, s = lambda, newx = as.matrix(data[, -9]))
    boot_mses[i] <- mean((boot_pred - data$LC50)^2)
  }

  return(mean(boot_mses))
}

# Perform bootstrap for ridge regression
set.seed(1)
boot_results <- sapply(lambda_grid, function(lambda) {
  ridge_bootstrap(train, lambda, B = 100)
})

# Find the optimal lambda
best_lambda_bootstrap <- lambda_grid[which.min(boot_results)]
print(paste("Best Lambda from Bootstrap:", best_lambda_bootstrap))
```

```
## [1] "Best Lambda from Bootstrap: 0.0132194114846603"
```

```
# Predict and evaluate on test data
ridge_pred_bootstrap <- predict(cv_ridge, s = best_lambda_bootstrap, newx = x_test)
mse_bootstrap <- mean((ridge_pred_bootstrap - y_test)^2)
rmse_bootstrap <- sqrt(mse_bootstrap)
r2_bootstrap <- 1 - (sum((ridge_pred_bootstrap - y_test)^2) / sum((y_test - mean(y_test))^2))

cat(paste0(
  "MSE: ", mse_bootstrap, "\n",
  "RMSE (Test): ", rmse_bootstrap, "\n",
  "R-squared (Test): ", r2_bootstrap, "\n"
))
```

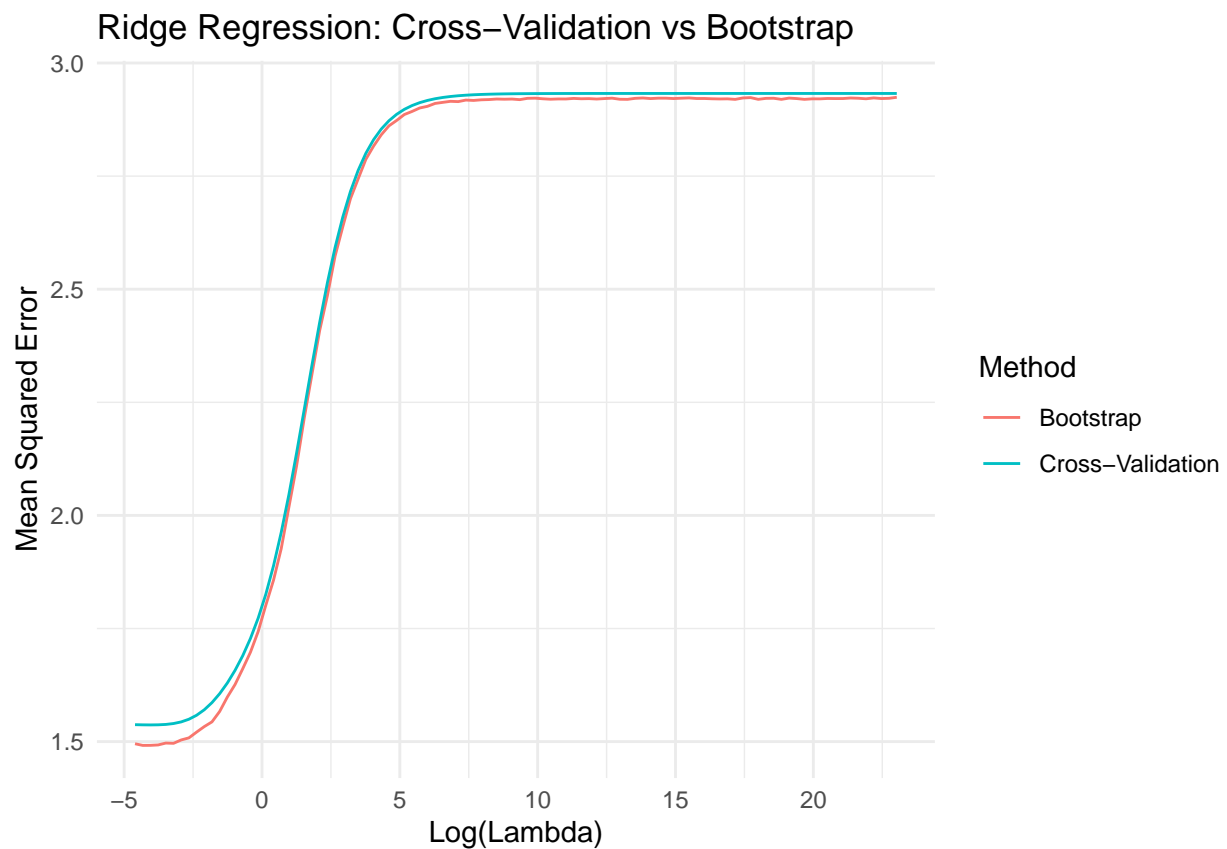
```
## MSE: 1.39995494236231
```

```
## RMSE (Test): 1.18319691613962
## R-squared (Test): 0.434514269822825
```

Cross Validation vs Bootstrap Comparison

```
# Create comparison data frame
comparison_df <- data.frame(
  Lambda = rep(lambda_grid, 2),
  MSE = c(cv_ridge$cvm, boot_results),
  Method = rep(c("Cross-Validation", "Bootstrap"), each = length(lambda_grid))
)

# Plot the results
ggplot(comparison_df, aes(x = log(Lambda), y = MSE, color = Method)) +
  geom_line() +
  labs(title = "Ridge Regression: Cross-Validation vs Bootstrap",
       x = "Log(Lambda)",
       y = "Mean Squared Error") +
  theme_minimal()
```



e. Generalised Additive Model (GAM)

```
summary(train)
```

```
##          TPSA          SAacc          H050          MLOGP
## Min.    : 0.00   Min.    : 0.00   Min.    : 0.0000   Min.    : -5.199
## 1st Qu.: 16.05   1st Qu.: 13.13   1st Qu.: 0.0000   1st Qu.: 1.139
## Median : 40.46   Median : 42.92   Median : 0.0000   Median : 2.226
## Mean    : 48.02   Mean    : 58.75   Mean    : 0.9313   Mean    : 2.273
## 3rd Qu.: 70.14   3rd Qu.: 78.20   3rd Qu.: 1.0000   3rd Qu.: 3.455
## Max.    :336.43   Max.    :551.10   Max.    :16.0000   Max.    : 9.148
##          RDCHI          GATS1p          nN          C040
## Min.    :1.000   Min.    :0.2880   Min.    : 0.000   Min.    : 0.0000
## 1st Qu.:1.946   1st Qu.:0.7578   1st Qu.: 0.000   1st Qu.: 0.0000
## Median :2.329   Median :1.0485   Median : 1.000   Median : 0.0000
## Mean    :2.469   Mean    :1.0682   Mean    : 1.025   Mean    : 0.3654
## 3rd Qu.:2.913   3rd Qu.:1.2902   3rd Qu.: 2.000   3rd Qu.: 0.0000
## Max.    :6.439   Max.    :2.3530   Max.    :11.000   Max.    :11.0000
##          LC50
## Min.    : 0.122
## 1st Qu.: 3.603
## Median : 4.516
## Mean    : 4.666
## 3rd Qu.: 5.637
## Max.    :10.047
```

Lower Complexity (k = 4)

```
# Fit GAM with smoothing splines (lower complexity)
gam_model_1 <- gam(LC50 ~ s(TPSA, k = 4) + s(SAacc, k = 4) + s(H050, k = 4) +
  s(MLOGP, k = 4) + s(RDCHI, k = 4) + s(GATS1p, k = 4) +
  s(nN, k = 4) + s(C040, k = 4), data = train)

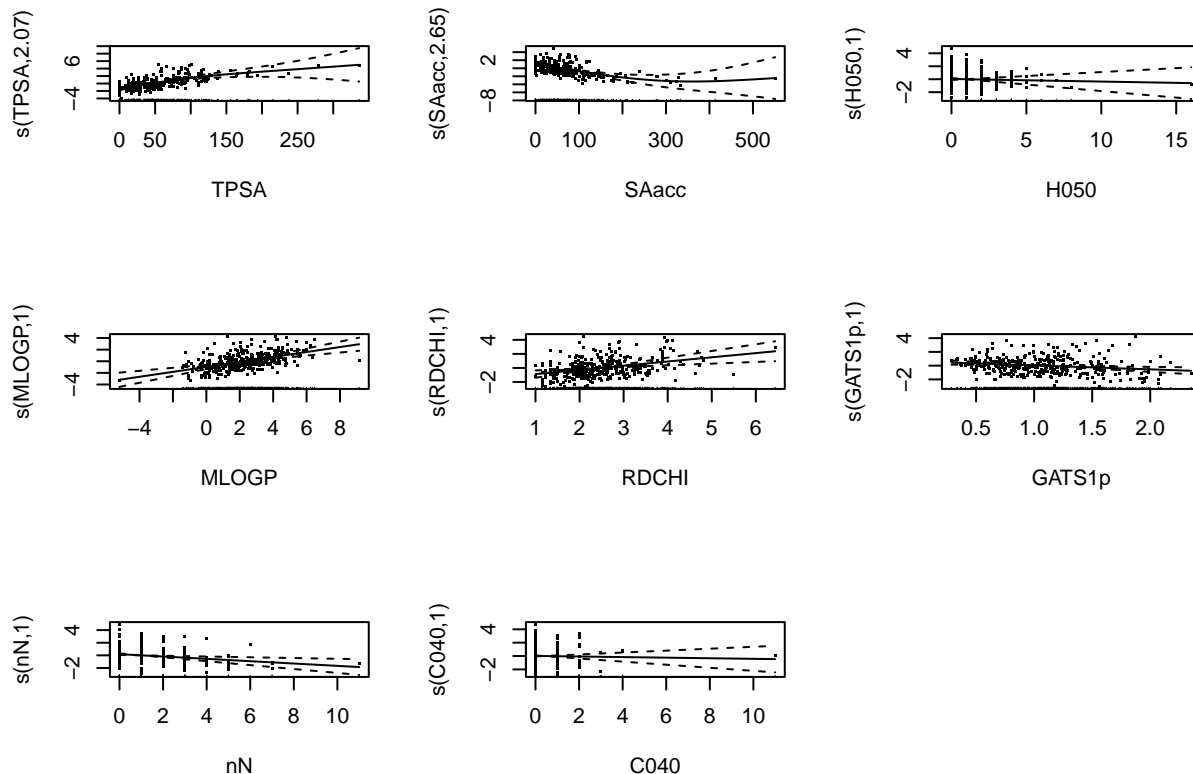
# Summarize models
summary(gam_model_1)
```

```
##
## Family: gaussian
## Link function: identity
##
## Formula:
## LC50 ~ s(TPSA, k = 4) + s(SAacc, k = 4) + s(H050, k = 4) + s(MLOGP,
##      k = 4) + s(RDCHI, k = 4) + s(GATS1p, k = 4) + s(nN, k = 4) +
##      s(C040, k = 4)
##
## Parametric coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.66605    0.06325   73.77  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Approximate significance of smooth terms:
##      edf Ref.df      F p-value
## s(TPSA)  2.070  2.398 29.935 < 2e-16 ***
## s(SAacc)  2.653  2.839 13.121 1.57e-07 ***
## s(H050)   1.000  1.000  0.243 0.622164
## s(MLOGP)  1.000  1.000 26.936 6.42e-07 ***
## s(RDCHI)  1.000  1.000 11.284 0.000867 ***
## s(GATS1p) 1.000  1.000  8.847 0.003138 **
## s(nN)     1.000  1.000  8.832 0.003164 **
## s(C040)   1.000  1.000  0.216 0.642396
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) =  0.502   Deviance explained = 51.6%
## GCV = 1.5049   Scale est. = 1.4564      n = 364
```

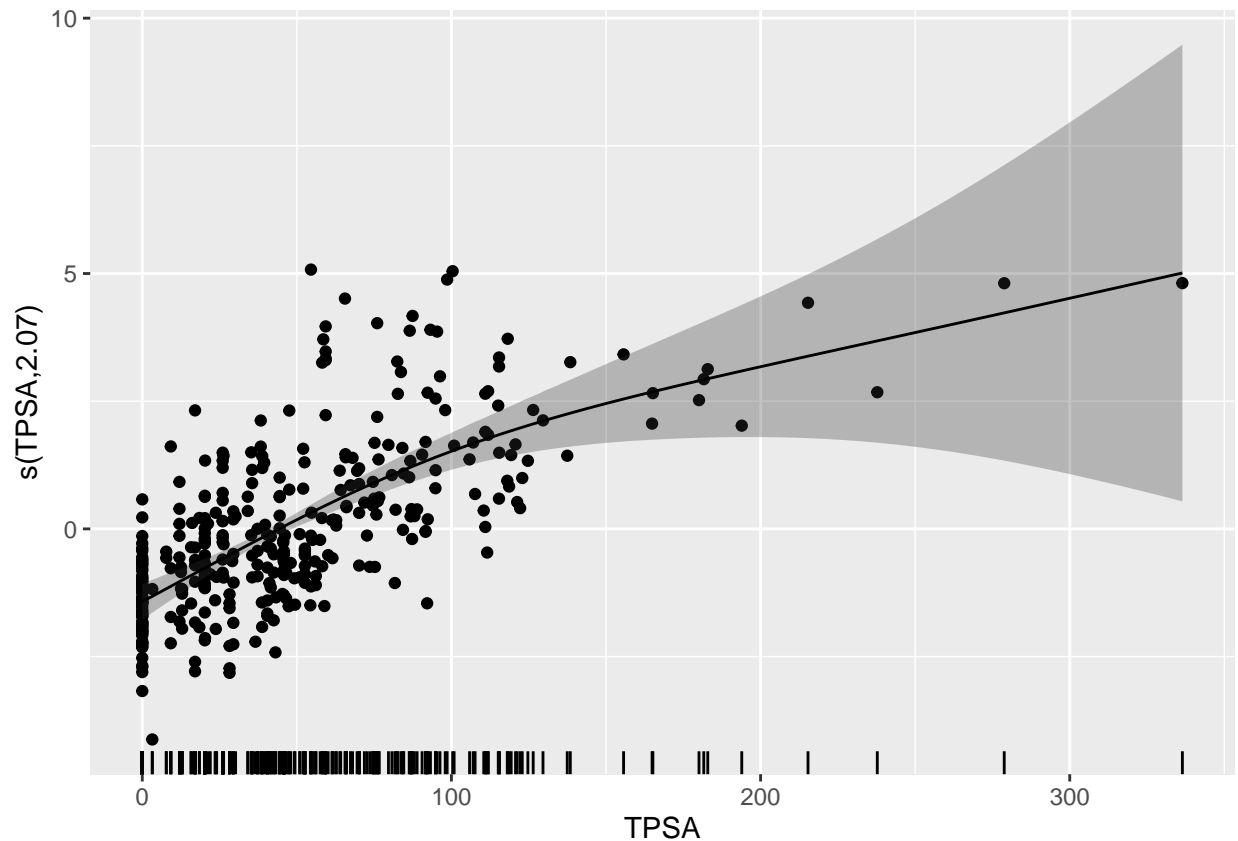
reference: <https://stackoverflow.com/questions/67077306/plotting-output-of-gam-model>

```
p_obj <- plot(gam_model_1, residuals = TRUE, pages = 1, scale = 0)
```



```
p_obj <- p_obj[[1]] # just one smooth so select the first component
sm_df <- as.data.frame(p_obj[c("x", "se", "fit")])
data_df <- as.data.frame(p_obj[c("raw", "p.resid")])
```

```
## plot
ggplot(sm_df, aes(x = x, y = fit)) +
  geom_rug(data = data_df, mapping = aes(x = raw, y = NULL),
    sides = "b") +
  geom_point(data = data_df, mapping = aes(x = raw, y = p.resid)) +
  geom_ribbon(aes(ymin = fit - se, ymax = fit + se, y = NULL),
    alpha = 0.3) +
  geom_line() +
  labs(x = p_obj$xlabel, y = p_obj$ylabel)
```



```
gam_pred_1 <- predict(gam_model_1, newdata = test)
gam_mse_1 <- mean((gam_pred_1 - y_test)^2)
gam_rmse_1 <- sqrt(gam_mse_1)
gam_r2_1 <- 1 - (sum((gam_pred_1 - y_test)^2) / sum((y_test - mean(y_test))^2))

cat(paste0(
  "MSE: ", gam_mse_1, "\n",
  "RMSE (Test): ", gam_rmse_1, "\n",
  "R-squared (Test): ", gam_r2_1, "\n"
))
```

```
## MSE: 1.40582163542459
## RMSE (Test): 1.18567349444296
## R-squared (Test): 0.432144528404967
```

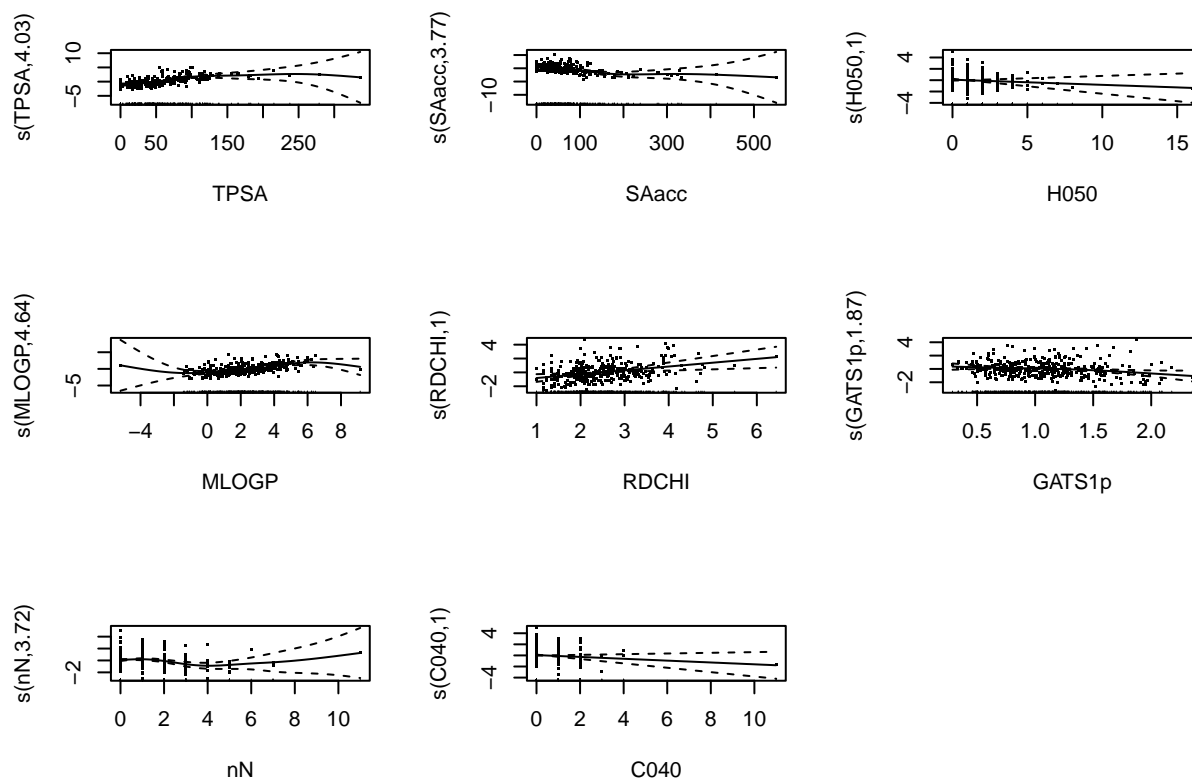

Higher Complexity (k = 6)

```
# Fit GAM with smoothing splines (higher complexity)
gam_model_2 <- gam(LC50 ~ s(TPSA, k = 6) + s(SAacc, k = 6) + s(H050, k = 6) +
  s(MLOGP, k = 6) + s(RDCHI, k = 6) + s(GATS1p, k = 6) +
  s(nN, k = 6) + s(C040, k = 6), data = train)

# Summarize models
summary(gam_model_2)

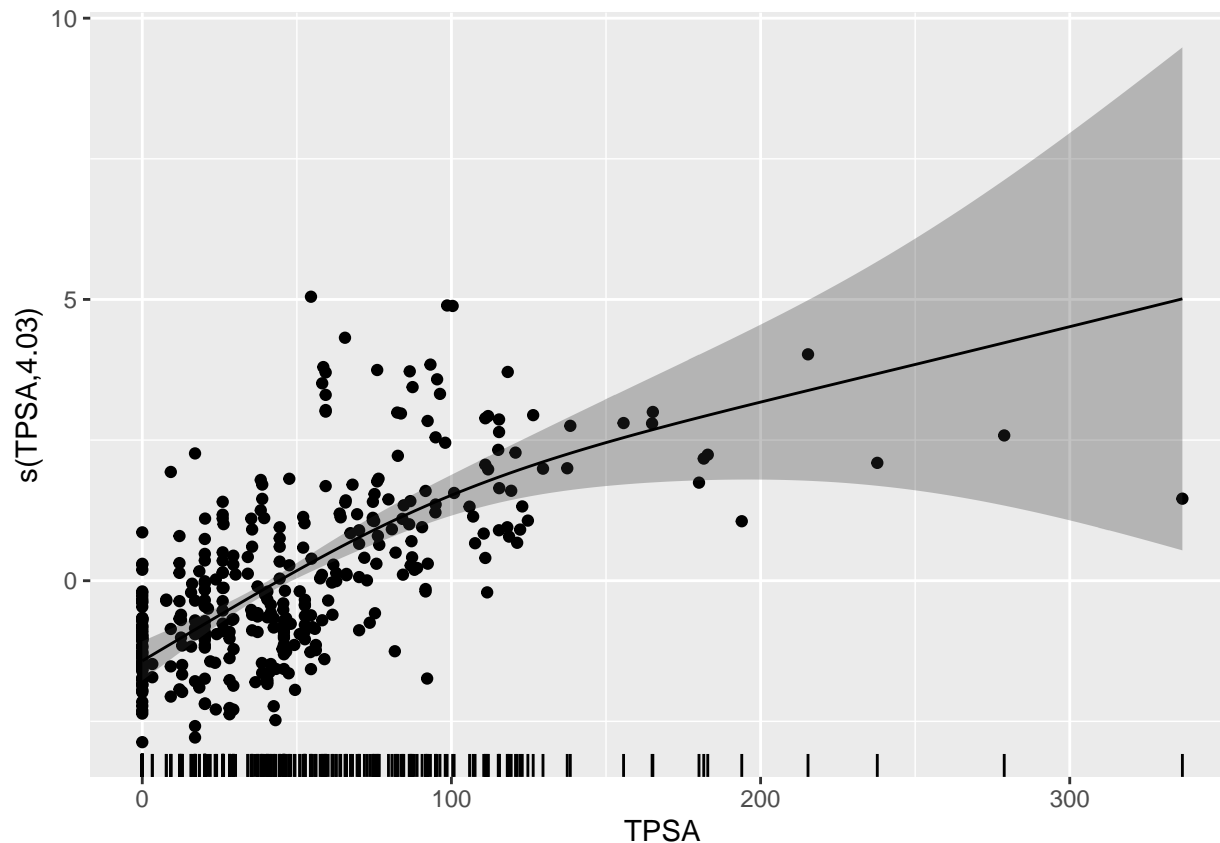
##
## Family: gaussian
## Link function: identity
##
## Formula:
## LC50 ~ s(TPSA, k = 6) + s(SAacc, k = 6) + s(H050, k = 6) + s(MLOGP,
##      k = 6) + s(RDCHI, k = 6) + s(GATS1p, k = 6) + s(nN, k = 6) +
##      s(C040, k = 6)
##
## Parametric coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  4.66605    0.06113   76.33  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
##              edf Ref.df      F  p-value
## s(TPSA)      4.026  4.425 18.481 < 2e-16 ***
## s(SAacc)     3.775  4.260  9.769 5.29e-07 ***
## s(H050)      1.000  1.000  1.095 0.29606
## s(MLOGP)     4.643  4.865  7.208 2.61e-06 ***
## s(RDCHI)     1.000  1.000  8.520 0.00375 **
## s(GATS1p)    1.871  2.363  3.643 0.01718 *
## s(nN)        3.721  4.295  3.602 0.00821 **
## s(C040)      1.000  1.000  2.129 0.14545
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) =  0.534   Deviance explained = 56.1%
## GCV = 1.4478   Scale est. = 1.3601    n = 364

p_obj_2 <- plot(gam_model_2, residuals = TRUE, pages = 1, scale = 0)
```



```
p_obj_2 <- p_obj_2[[1]] # just one smooth so select the first component
sm_df_2 <- as.data.frame(p_obj_2[c("x", "se", "fit")])
data_df_2 <- as.data.frame(p_obj_2[c("raw", "p.resid")])

## plot
ggplot(sm_df, aes(x = x, y = fit)) +
  geom_rug(data = data_df_2, mapping = aes(x = raw, y = NULL),
    sides = "b") +
  geom_point(data = data_df_2, mapping = aes(x = raw, y = p.resid)) +
  geom_ribbon(aes(ymin = fit - se, ymax = fit + se, y = NULL),
    alpha = 0.3) +
  geom_line() +
  labs(x = p_obj_2$xlabel, y = p_obj_2$ylabel)
```



```
gam_pred_2 <- predict(gam_model_2, newdata = test)
gam_mse_2 <- mean((gam_pred_2 - y_test)^2)
gam_rmse_2 <- sqrt(gam_mse_2)
gam_r2_2 <- 1 - (sum((gam_pred_2 - y_test)^2) / sum((y_test - mean(y_test))^2))

cat(paste0(
  "MSE: ", gam_mse_2, "\n",
  "RMSE (Test): ", gam_rmse_2, "\n",
  "R-squared (Test): ", gam_r2_2, "\n"
))
```

```
## MSE: 1.3585368150292
## RMSE (Test): 1.16556287476446
## R-squared (Test): 0.451244351105306
```

f. Regression Tree with Cost-Complexity Pruning

```
# Fit a regression tree model
tree_model <- rpart(LC50 ~ ., data = train, method = "anova", control = rpart.control(cp = 0.001))
printcp(tree_model) # Display the cost complexity pruning table
```

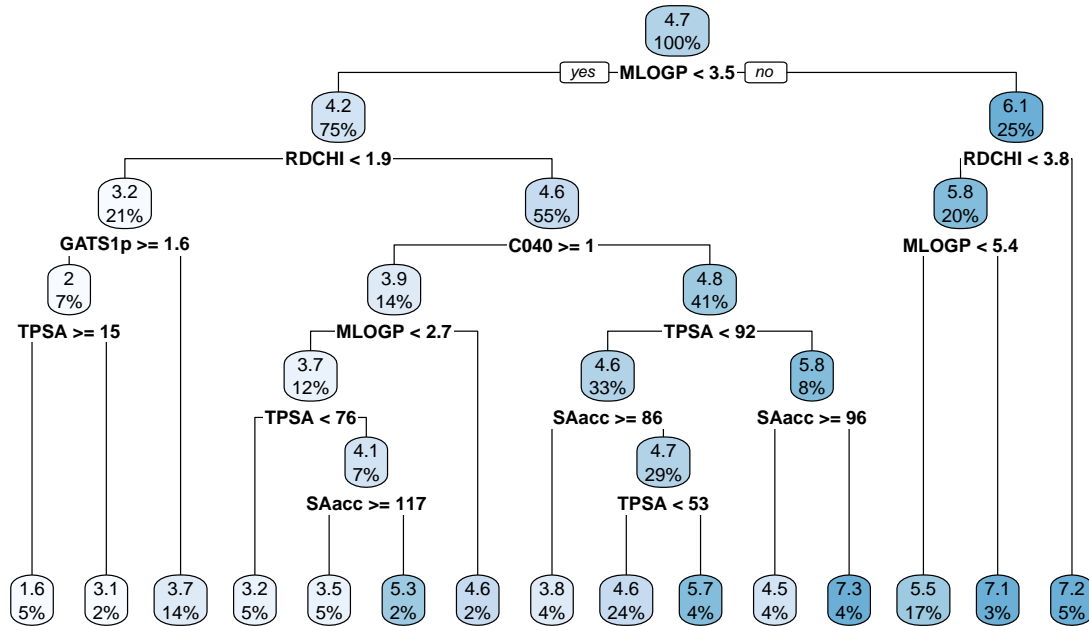
```
##
## Regression tree:
```

```
## rpart(formula = LC50 ~ ., data = train, method = "anova", control = rpart.control(cp = 0.001))
##
## Variables actually used in tree construction:
## [1] C040   GATS1p H050   MLOGP  RDCHI  SAacc  TPSA
##
## Root node error: 1060.6/364 = 2.9138
##
## n= 364
##
##      CP nsplit rel error  xerror   xstd
## 1  0.2198608      0  1.00000 1.00582 0.083377
## 2  0.1015513      1  0.78014 0.85037 0.073595
## 3  0.0470255      2  0.67859 0.73790 0.061890
## 4  0.0384187      3  0.63156 0.67470 0.059262
## 5  0.0282925      6  0.51631 0.66571 0.059021
## 6  0.0225187      7  0.48801 0.66047 0.058312
## 7  0.0132815      8  0.46550 0.65154 0.056470
## 8  0.0109658     10  0.43893 0.60906 0.054135
## 9  0.0094706     11  0.42797 0.60140 0.053811
## 10 0.0086901     14  0.39955 0.59657 0.052692
## 11 0.0066615     15  0.39086 0.61671 0.053956
## 12 0.0063800     16  0.38420 0.63467 0.055231
## 13 0.0039482     17  0.37782 0.63634 0.058081
## 14 0.0038386     18  0.37387 0.62956 0.057522
## 15 0.0031083     19  0.37004 0.63425 0.057628
## 16 0.0027054     20  0.36693 0.63142 0.057532
## 17 0.0021546     21  0.36422 0.63076 0.058458
## 18 0.0019759     22  0.36207 0.62731 0.058474
## 19 0.0014224     23  0.36009 0.62838 0.058471
## 20 0.0014058     24  0.35867 0.63024 0.058550
## 21 0.0010000     26  0.35586 0.62934 0.058560

# Prune the tree
optimal_cp <- tree_model$cptable[which.min(tree_model$cptable[, "xerror"]), "CP"]
pruned_tree <- prune(tree_model, cp = optimal_cp)

# Visualize the tree
rpart.plot(pruned_tree, main = "Pruned Regression Tree")
```

Pruned Regression Tree



```

# Predict and evaluate on test data
tree_pred <- predict(pruned_tree, newdata = test)
tree_mse <- mean((tree_pred - y_test)^2)
tree_rmse <- sqrt(tree_mse)
tree_r2 <- 1 - (sum((tree_pred - y_test)^2) / sum((y_test - mean(y_test))^2))

cat(paste0(
  "MSE: ", tree_mse, "\n",
  "RMSE (Test): ", tree_rmse, "\n",
  "R-squared (Test): ", tree_r2, "\n"
))

```

```

## MSE: 1.55285972999018
## RMSE (Test): 1.24613792574906
## R-squared (Test): 0.372751228125619

```

g. Compare all the models implemented

[TBD]

- Linear Regression (Original)
- Linear Regression model by Dummy Encoding Method (Dummy Encoding)
- Ridge Regression with Cross Validation (Ridge CV)
- Ridge Regression with Bootstrapping ("Ridge Bootstrap")

- Generalized Additive Model with lower complexity (GAM k=4)
- Generalized Additive Model with higher complexity (GAM k=6)
- Regression Tree with Cost-Complexity Pruning (Tree)

```
# Create a comprehensive metrics data frame
all_models_metrics <- data.frame(
  Model = c("Original", "Dummy Encoding", "Variable Selection", "Ridge CV", "Ridge Bootstrap", "GAM k=4", "GAM k=6", "Tree"),
  MSE = c(mse_test, mse_test_transform_dummy, metrics$MSE[metrics$Model == "Forward AIC"], mse_cv, mse_lm, gam_mse_2, tree_mse),
  RMSE = c(rmse_test, rmse_test_transform_dummy, metrics$RMSE[metrics$Model == "Forward AIC"], rmse_cv, rmse_lm, gam_rmse_2, tree_rmse),
  R2 = c(r2_test, r2_test_transform_dummy, metrics$R2[metrics$Model == "Forward AIC"], r2_cv, r2_bootstrap, gam_r2_2, tree_r2)
)

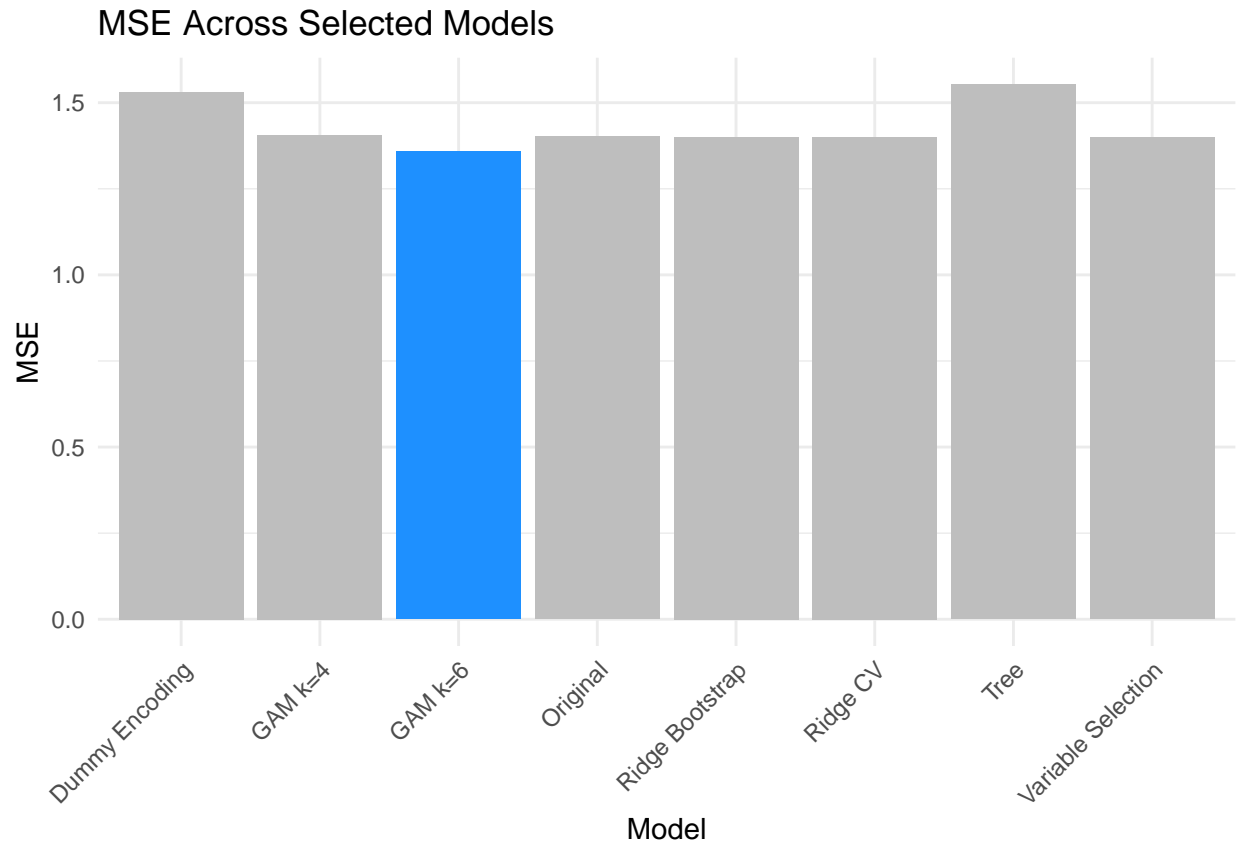
# Print the all models metrics
print(all_models_metrics)
```

##	Model	MSE	RMSE	R2
## 1	Original	1.402249	1.184166	0.4335877
## 2	Dummy Encoding	1.530438	1.237109	0.3818079
## 3	Variable Selection	1.398176	1.182445	0.4352328
## 4	Ridge CV	1.399842	1.183149	0.4345599
## 5	Ridge Bootstrap	1.399955	1.183197	0.4345143
## 6	GAM k=4	1.405822	1.185673	0.4321445
## 7	GAM k=6	1.358537	1.165563	0.4512444
## 8	Tree	1.552860	1.246138	0.3727512

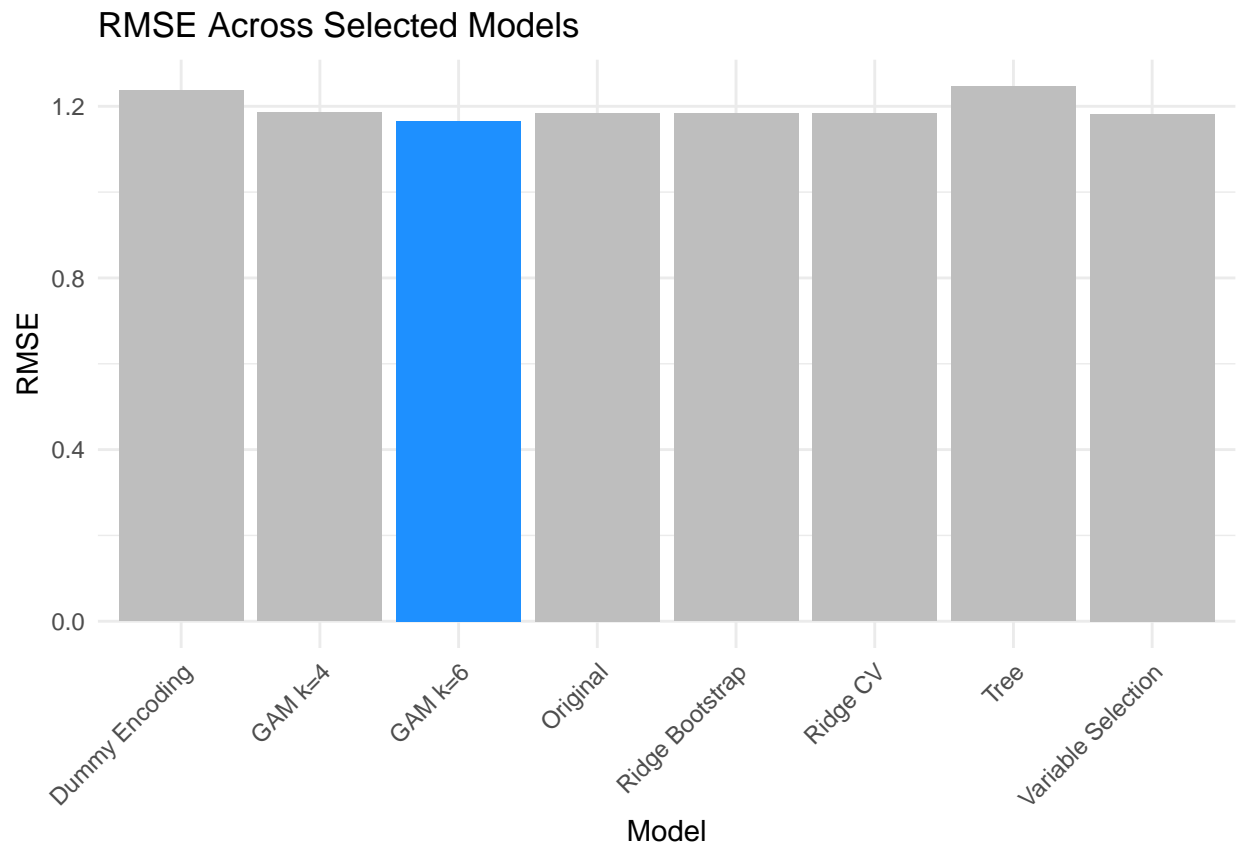
Visualization of Model Comparisons

```
# Identify the model with the minimum MSE, RMSE and maximum R-squared
best_mse_model <- all_models_metrics$Model[which.min(all_models_metrics$MSE)]
best_rmse_model <- all_models_metrics$Model[which.min(all_models_metrics$RMSE)]
best_r2_model <- all_models_metrics$Model[which.max(all_models_metrics$R2)]

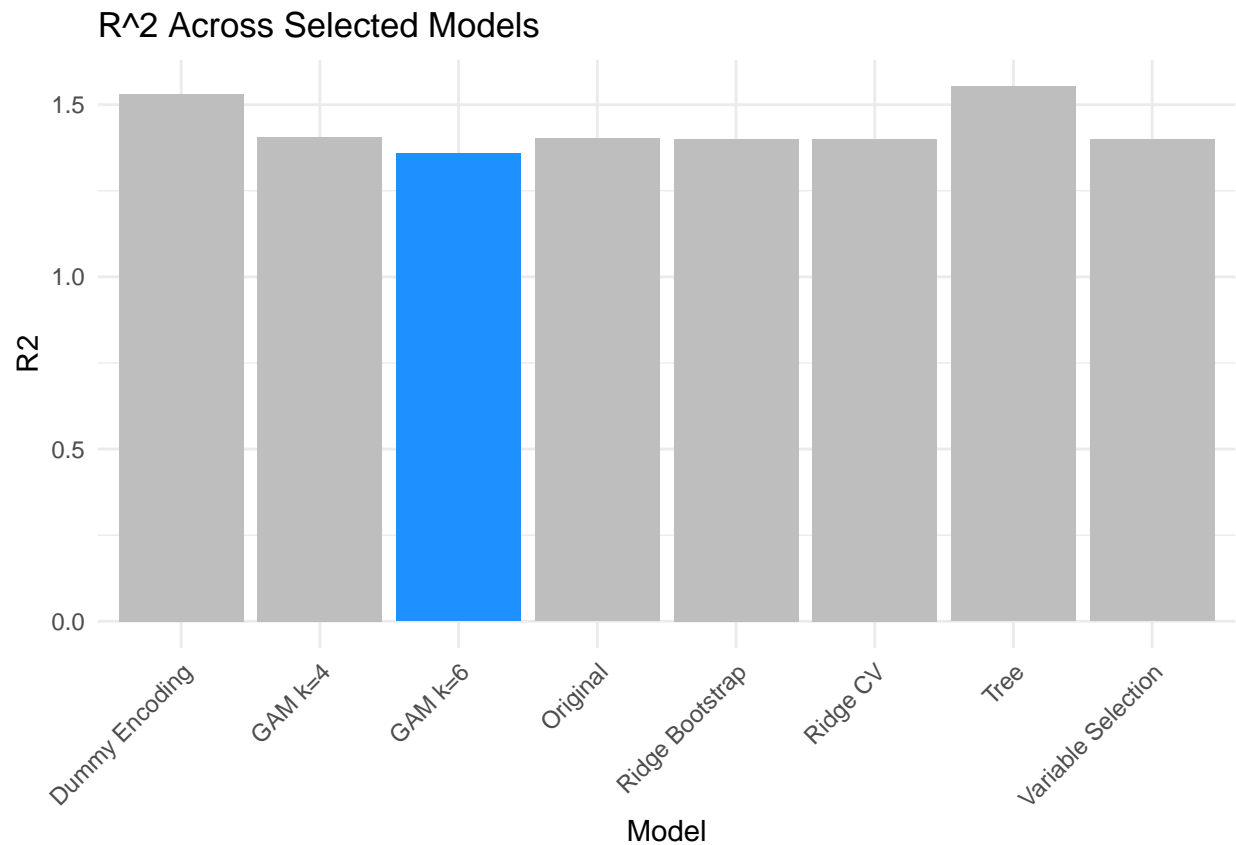
# Plot MSE across selected models
ggplot(all_models_metrics, aes(x = Model, y = MSE, fill = Model == best_mse_model)) +
  geom_bar(stat = "identity") +
  scale_fill_manual(values = c("gray", "dodgerblue"), guide = "none") +
  theme_minimal() +
  labs(title = "MSE Across Selected Models", x = "Model", y = "MSE", fill = "Best Model") +
  theme(axis.text.x = element_text(angle = 45, hjust = 1))
```



```
# Plot RMSE across selected models
ggplot(all_models_metrics, aes(x = Model, y = RMSE, fill = Model == best_mse_model)) +
  geom_bar(stat = "identity") +
  scale_fill_manual(values = c("gray", "dodgerblue"), guide = "none") +
  theme_minimal() +
  labs(title = "RMSE Across Selected Models", x = "Model", y = "RMSE", fill = "Best Model") +
  theme(axis.text.x = element_text(angle = 45, hjust = 1))
```



```
# Plot RMSE across selected models
ggplot(all_models_metrics, aes(x = Model, y = MSE, fill = Model == best_mse_model)) +
  geom_bar(stat = "identity") +
  scale_fill_manual(values = c("gray", "dodgerblue"), guide = "none") +
  theme_minimal() +
  labs(title = "R^2 Across Selected Models", x = "Model", y = "R2", fill = "Best Model") +
  theme(axis.text.x = element_text(angle = 45, hjust = 1))
```

Problem 2. Classification

```
library(mlbench)
data("PimaIndiansDiabetes2")
```

```
data <- PimaIndiansDiabetes2
head(data)
```

```
##   pregnant glucose pressure triceps insulin mass pedigree age diabetes
## 1         6    148      72     35      NA  33.6   0.627  50      pos
## 2         1     85     66     29      NA  26.6   0.351  31      neg
## 3         8    183     64     NA      NA  23.3   0.672  32      pos
## 4         1     89     66     23     94  28.1   0.167  21      neg
## 5         0    137     40     35    168  43.1   2.288  33      pos
## 6         5    116     74     NA      NA  25.6   0.201  30      neg
```

```
# Checking missing value
sapply(data, function(x) sum(is.na(x)))
```

```
## pregnant glucose pressure triceps insulin mass pedigree age
##         0         5      35      227      374      11         0
## diabetes
##         0
```

```
# Remove rows with missing values
data <- na.omit(data)
head(data)
```

```
##      pregnant glucose pressure triceps insulin mass pedigree age diabetes
## 4           1      89       66      23      94 28.1    0.167 21      neg
## 5           0     137       40      35     168 43.1    2.288 33      pos
## 7           3      78       50      32      88 31.0    0.248 26      pos
## 9           2     197       70      45     543 30.5    0.158 53      pos
## 14          1     189       60      23     846 30.1    0.398 59      pos
## 15          5     166       72      19     175 25.8    0.587 51      pos
```

```
summary(data)
```

```
##      pregnant      glucose      pressure      triceps
## Min.   : 0.000   Min.   : 56.0   Min.   : 24.00   Min.   : 7.00
## 1st Qu.: 1.000   1st Qu.: 99.0   1st Qu.: 62.00   1st Qu.:21.00
## Median : 2.000   Median :119.0   Median : 70.00   Median :29.00
## Mean   : 3.301   Mean   :122.6   Mean   : 70.66   Mean   :29.15
## 3rd Qu.: 5.000   3rd Qu.:143.0   3rd Qu.: 78.00   3rd Qu.:37.00
## Max.   :17.000   Max.   :198.0   Max.   :110.00   Max.   :63.00
##      insulin      mass      pedigree      age      diabetes
## Min.   : 14.00   Min.   :18.20   Min.   :0.0850   Min.   :21.00   neg:262
## 1st Qu.: 76.75   1st Qu.:28.40   1st Qu.:0.2697   1st Qu.:23.00   pos:130
## Median :125.50   Median :33.20   Median :0.4495   Median :27.00
## Mean   :156.06   Mean   :33.09   Mean   :0.5230   Mean   :30.86
## 3rd Qu.:190.00   3rd Qu.:37.10   3rd Qu.:0.6870   3rd Qu.:36.00
## Max.   :846.00   Max.   :67.10   Max.   :2.4200   Max.   :81.00
```

```
# Checking how balance is with the dependent variable
prop.table(table(data$diabetes))
```

```
##
##      neg      pos
## 0.6683673 0.3316327
```

Randomly split the dataset into a training set (approximately 2/3 of the sample size) and a test set, such that the class distributions (i.e. the empirical distribution of diabetes) is similar in the two sets.

```
set.seed(123)
```

```
sample <- sample.split(data$diabetes, SplitRatio = 2/3)
train <- subset(data, sample == TRUE)
test <- subset(data, sample == FALSE)
```

```
# Class distribution in the training set
prop.table(table(train$diabetes))
```

```
##
##      neg      pos
## 0.6679389 0.3320611
```

```
# Class distribution in the testing set
prop.table(table(test$diabetes))
```

```
##
##      neg      pos
## 0.6692308 0.3307692
```

```
cat("Dimension of Training Set:", paste(dim(train), collapse = "x"), "\nDimension of Test Set:", paste(
```

```
## Dimension of Training Set: 262x9
## Dimension of Test Set: 130x9
```

a. k-NN classifier

```
library(class)
library(caret)
```

```
## Loading required package: lattice
```

```
##
## Attaching package: 'lattice'
```

```
## The following object is masked from 'package:boot':
##
##      melanoma
```

```
library(FNN)
```

```
## Warning: package 'FNN' was built under R version 4.3.3
```

```
##
## Attaching package: 'FNN'
```

```
## The following objects are masked from 'package:class':
##
##      knn, knn.cv
```

```
X_train <- train[, -ncol(train)]
y_train <- train$diabetes
```

```
X_test <- test[, -ncol(test)]
y_test <- test$diabetes
```

```
accuracy = function(actual, predicted) {
  mean(actual == predicted)
}
```

```
set.seed(42)
k_to_try = 1:100
acc_k = rep(0, length(k_to_try))

# Loop over values of k
for (i in seq_along(k_to_try)) {
  pred <- knn(
    train = scale(X_train),
    test = scale(X_test),
    cl = y_train,
    k = k_to_try[i]
  )
  acc_k[i] <- accuracy(y_test, pred)
}
```

```
ex_seq = seq(from = 1, to = 100, by = 5)
seq_along(ex_seq)
```

```
## [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
```

```
ex_storage = rep(x = 0, times = length(ex_seq))
for(i in seq_along(ex_seq)) {
  ex_storage[i] = mean(rnorm(n = 10, mean = ex_seq[i], sd = 1))
}
```

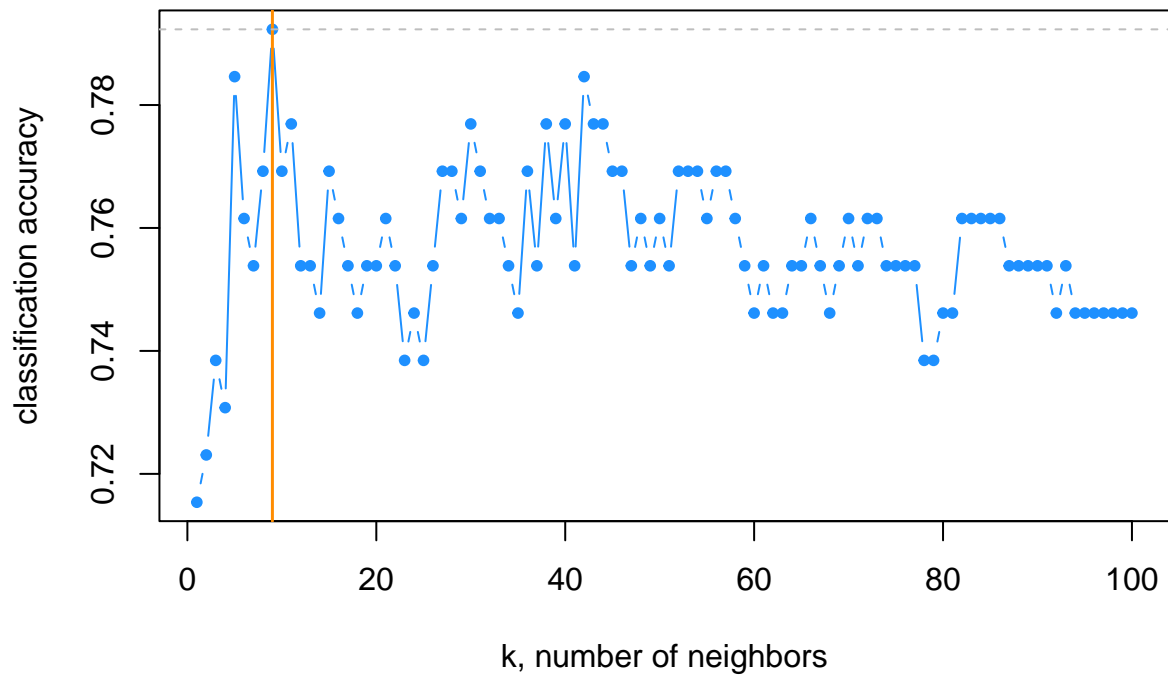
```
ex_storage
```

```
## [1] 1.547297 5.836543 10.821920 15.636096 20.979785 26.018394 31.539077
## [8] 35.782125 41.251106 45.912805 51.229248 55.801428 60.205034 66.210242
## [15] 70.797793 75.754132 81.101802 86.093609 90.743936 96.187940
```

```
# Reference: https://davidalpiaz.github.io/r4sl/k-nearest-neighbors.html
```

```
# plot accuracy vs choice of k
plot(acc_k, type = "b", col = "dodgerblue", cex = 1, pch = 20,
      xlab = "k, number of neighbors", ylab = "classification accuracy",
      main = "Accuracy vs Neighbors")
# add lines indicating k with best accuracy
abline(v = which(acc_k == max(acc_k)), col = "darkorange", lwd = 1.5)
# add line for max accuracy seen
abline(h = max(acc_k), col = "grey", lty = 2)
# add line for prevalence in test set
abline(h = mean(y_test == "No"), col = "grey", lty = 2)
```

Accuracy vs Neighbors



```
max(acc_k)
```

```
## [1] 0.7923077
```

```
max(which(acc_k == max(acc_k)))
```

```
## [1] 9
```

Using 5-fold

```
# 5-fold cross-validation using caret
train_control <- trainControl(method = "cv", number = 5)
train_knn <- train(diabetes ~ .,
  data = train,
  method = "knn",
  trControl = train_control,
  tuneGrid = expand.grid(k = k_to_try))

## plot(train_knn)

cv_results <- train_knn$results

head(cv_results)
```

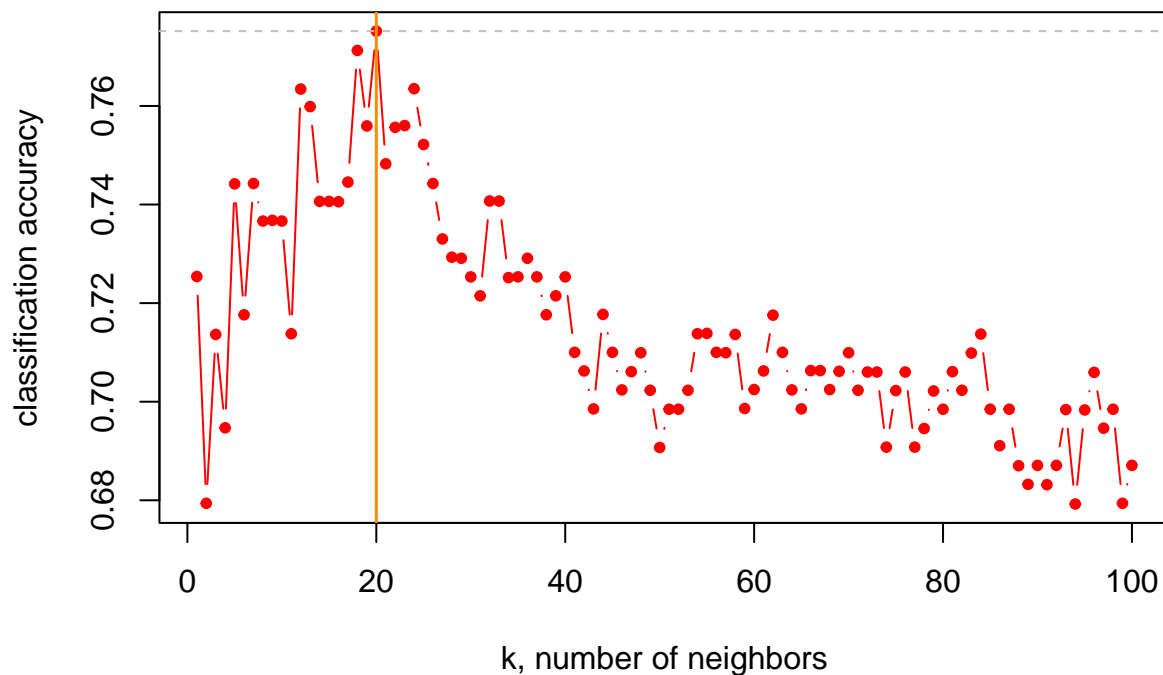
```
##   k Accuracy      Kappa AccuracySD      KappaSD
## 1 1 0.7253991 0.3853807 0.04199871 0.1010289
## 2 2 0.6793904 0.2899952 0.06339646 0.1503705
## 3 3 0.7136430 0.3261247 0.05242032 0.1384865
## 4 4 0.6947025 0.2954201 0.05140217 0.1233151
## 5 5 0.7441945 0.4223798 0.05806649 0.1303848
## 6 6 0.7176343 0.3517014 0.06971643 0.1419173
```

```
# Plot the 5-fold CV accuracy vs choice of k
```

```
plot(cv_results$k, cv_results$Accuracy, type = "b", col = "red", cex = 1, pch = 20,
     xlab = "k, number of neighbors", ylab = "classification accuracy",
     main = "5-fold CV Accuracy vs Neighbors")
#legend("bottomright", legend = "5-fold CV Accuracy", col = "red", pch = 19, lty = 1)

# Add lines indicating k with best accuracy
abline(v = cv_results$k[which.max(cv_results$Accuracy)], col = "darkorange", lwd = 1.5)
# Add line for max accuracy seen
abline(h = max(cv_results$Accuracy), col = "grey", lty = 2)
```

5-fold CV Accuracy vs Neighbors



```
max(cv_results$Accuracy)
```

```
## [1] 0.7751814
```

```
cv_results$k[which.max(cv_results$Accuracy)]
```

```
## [1] 20
```

Using leave-one-out cross-validation

```
# leave-one-out cross-validation using caret
train_control_loocv <- trainControl(method = "LOOCV")
train_knn_loocv <- train(diabetes ~ .,
                        data = train,
                        method = "knn",
                        trControl = train_control_loocv,
                        tuneGrid = expand.grid(k = k_to_try))

cv_results_loocv <- train_knn_loocv$results

head(cv_results_loocv)
```

```
##   k Accuracy      Kappa
## 1 1 0.7480916 0.4353817
## 2 2 0.6984733 0.3337411
## 3 3 0.7061069 0.3197788
## 4 4 0.6793893 0.2644877
## 5 5 0.7061069 0.3157181
## 6 6 0.7290076 0.3764832
```

```
# Plot the LOOCV accuracy vs choice of k
```

```
plot(cv_results_loocv$k, cv_results_loocv$Accuracy, type = "b", col = "red", cex = 1, pch = 20,
     xlab = "k, number of neighbors", ylab = "classification accuracy",
     main = "LOOCV Accuracy vs Neighbors")
```

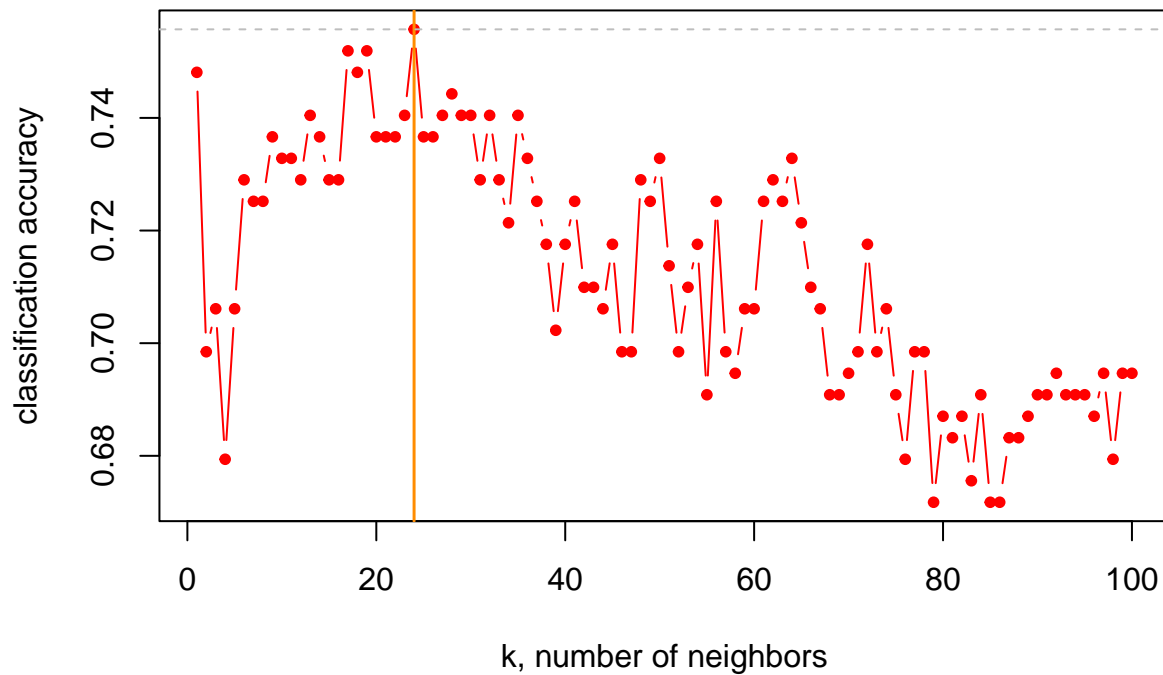
```
# Add lines indicating k with best accuracy
```

```
abline(v = cv_results_loocv$k[which.max(cv_results_loocv$Accuracy)], col = "darkorange", lwd = 1.5)
```

```
# Add line for max accuracy seen
```

```
abline(h = max(cv_results_loocv$Accuracy), col = "grey", lty = 2)
```

LOOCV Accuracy vs Neighbors



```
max(cv_results_loocv$Accuracy)
```

```
## [1] 0.7557252
```

```
cv_results$k[which.max(cv_results_loocv$Accuracy)]
```

```
## [1] 24
```

b. Generalized Additive Model (GAM)

```
# Fit a GAM with automatic smoothness selection
gam_model <- gam(
  diabetes ~ s(glucose) + s(pressure) + s(insulin) + s(mass) + s(pedigree) + s(age) + s(pregnant),
  data = train,
  family = binomial(link = 'logit'),
  select = TRUE,
  method= "REML")
```

In the `summary(model)` output, the Approximate significance of smooth terms table shows an estimated degrees of freedom (edf) and Chi square score (Chi.sq) close to zero, with a p-value > 0.05:


```
summary(gam_model)
```

```
##
## Family: binomial
## Link function: logit
##
## Formula:
## diabetes ~ s(glucose) + s(pressure) + s(insulin) + s(mass) +
##          s(pedigree) + s(age) + s(pregnant)
##
## Parametric coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.1305      0.1918  -5.895 3.75e-09 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
##              edf Ref.df Chi.sq  p-value
## s(glucose)    9.761e-01     9 36.884 < 2e-16 ***
## s(pressure)   1.297e-05     9  0.000 0.832820
## s(insulin)    5.976e-06     9  0.000 0.697822
## s(mass)       1.889e+00     9 10.598 0.001791 **
## s(pedigree)   8.059e-01     9  3.887 0.027410 *
## s(age)        2.127e+00     9 12.199 0.000871 ***
## s(pregnant)   1.798e+00     9  4.837 0.047140 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) =  0.421   Deviance explained = 39.2%
## -REML = 114.77   Scale est. = 1           n = 262
```

Reference: <https://osf.io/wgc4f/wiki/mgcv:%20model%20selection/>

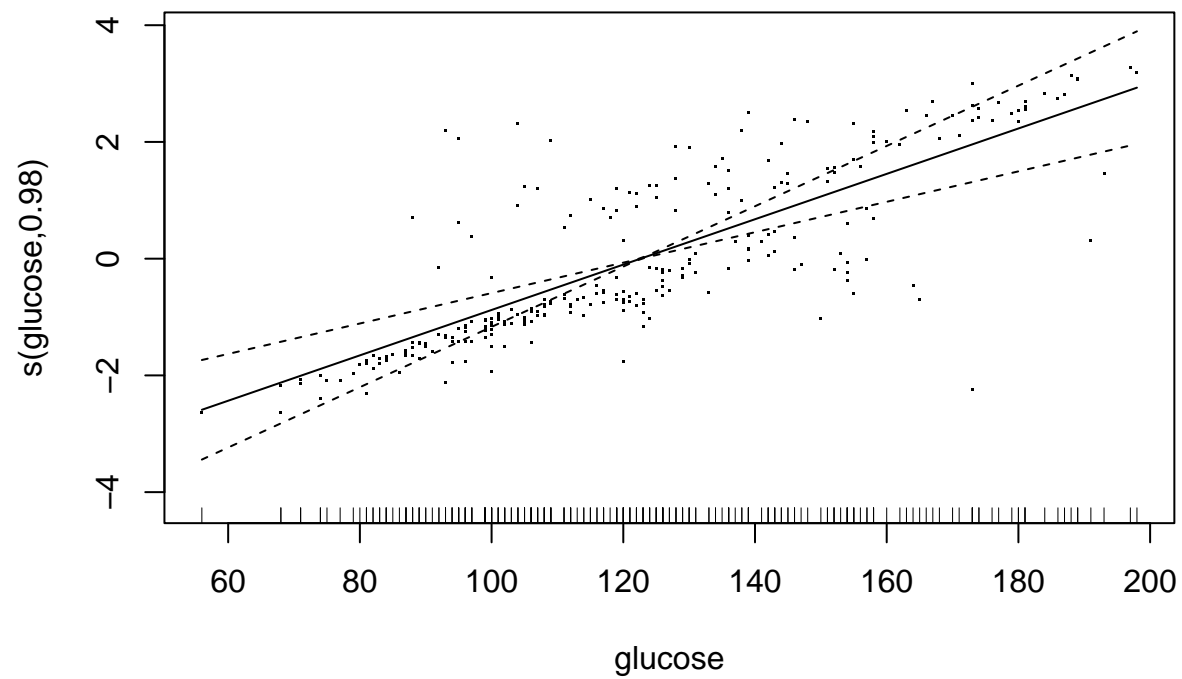
[TBD] You can use these statistics to detect a shrunk term. It is usually sufficient to check for p-values > 0.05:

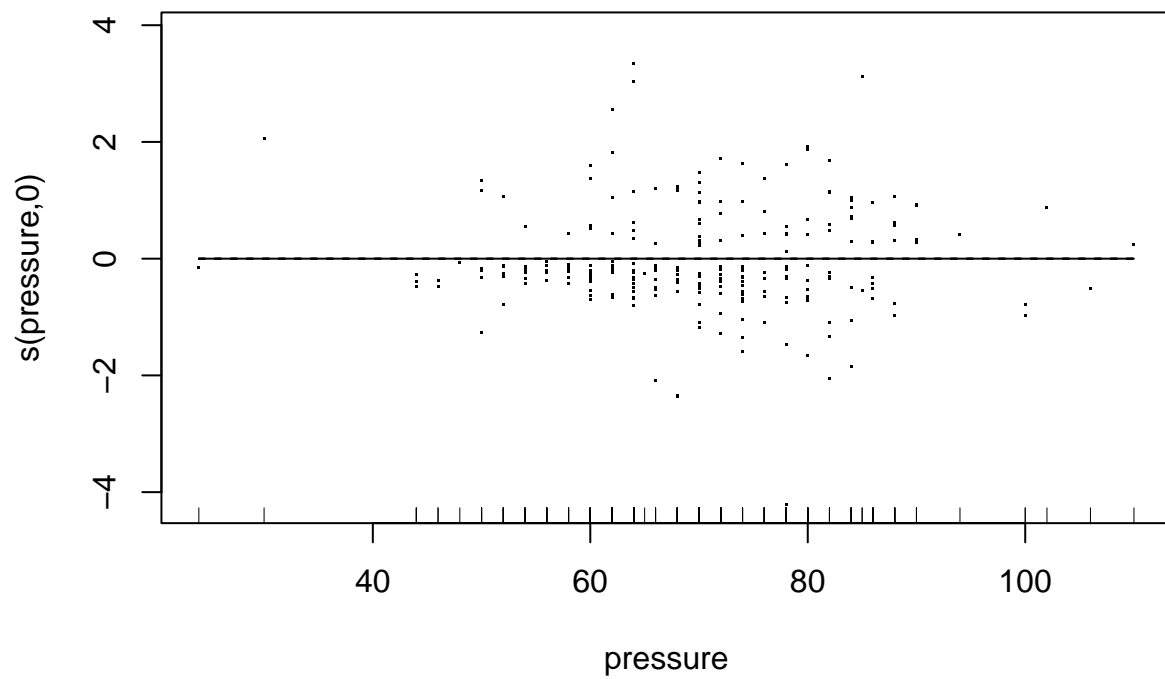
```
summary(gam_model)$s.pv
```

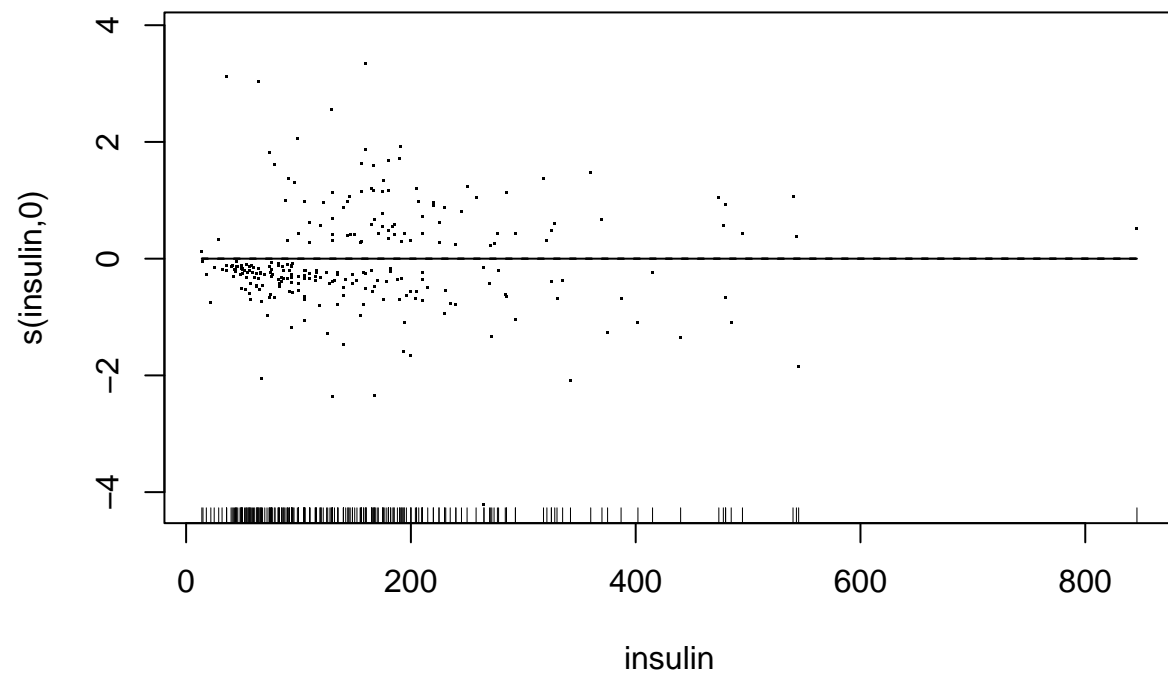
```
## [1] 0.0000000000 0.8328200945 0.6978222967 0.0017906665 0.0274097259
## [6] 0.0008710921 0.0471395990
```

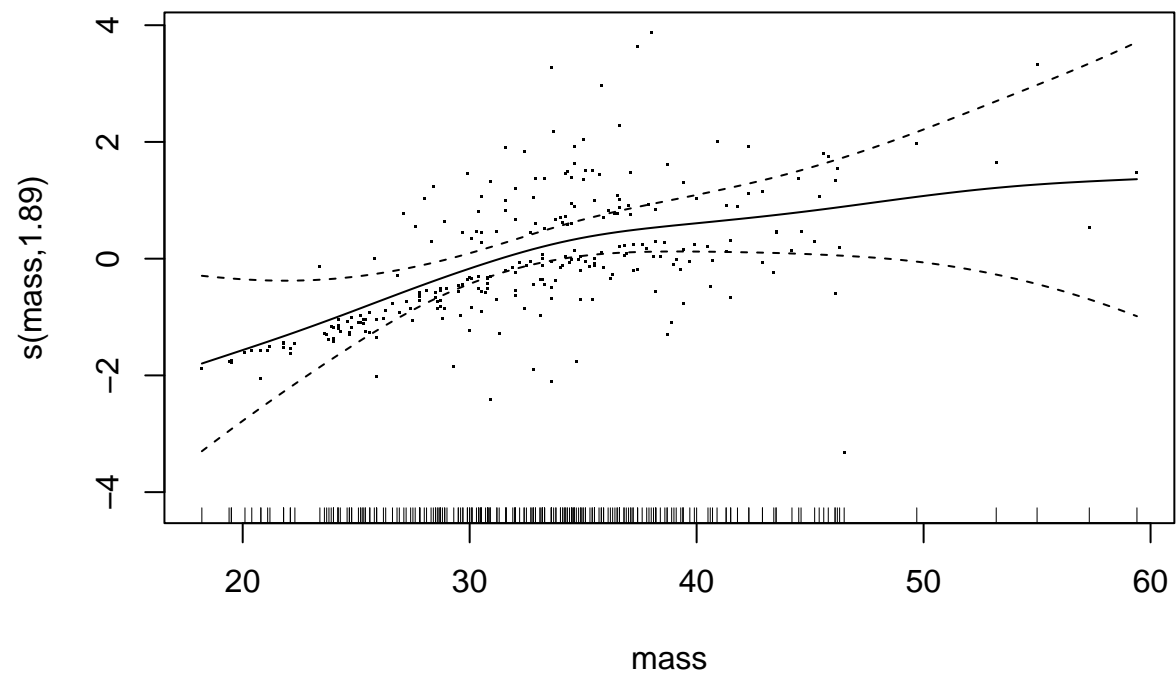
We can see that the glucose and pedigree is a shrunk term

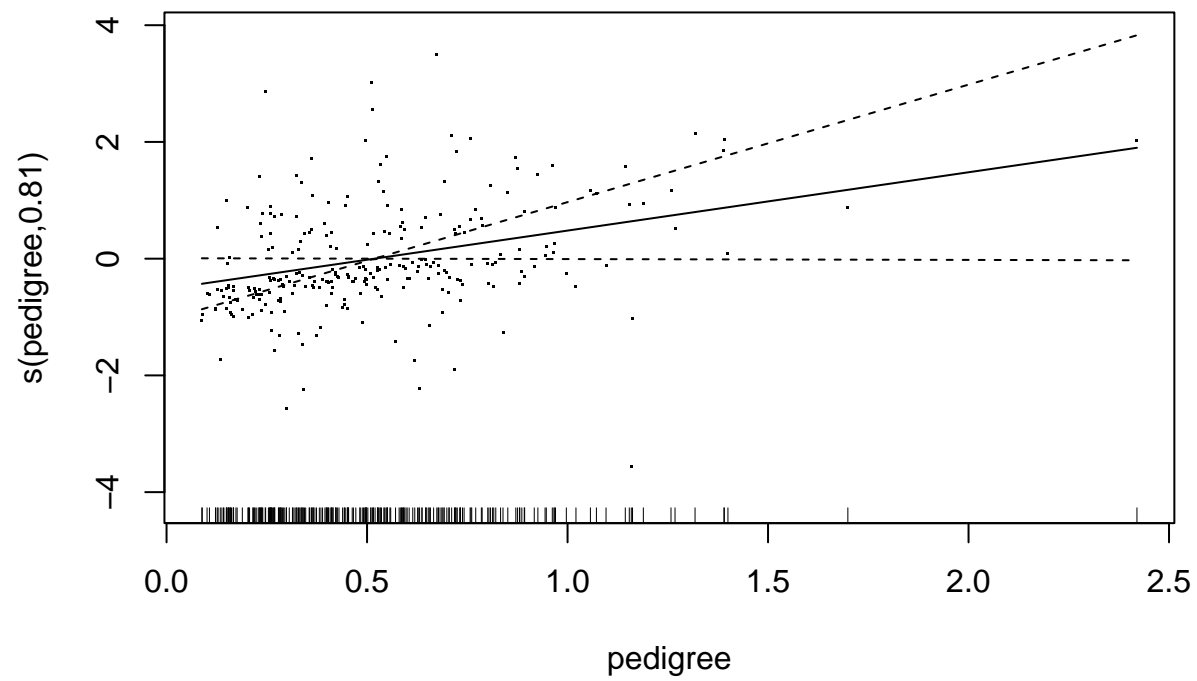
```
p_obj <- plot(gam_model, residuals = TRUE)
```

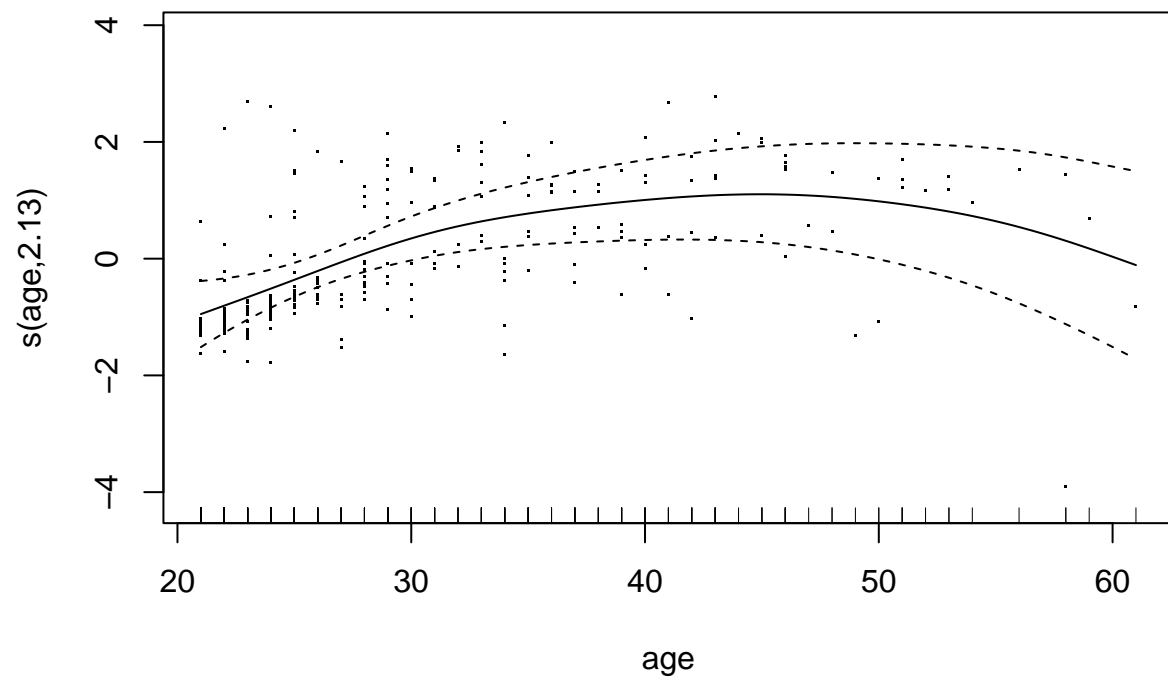


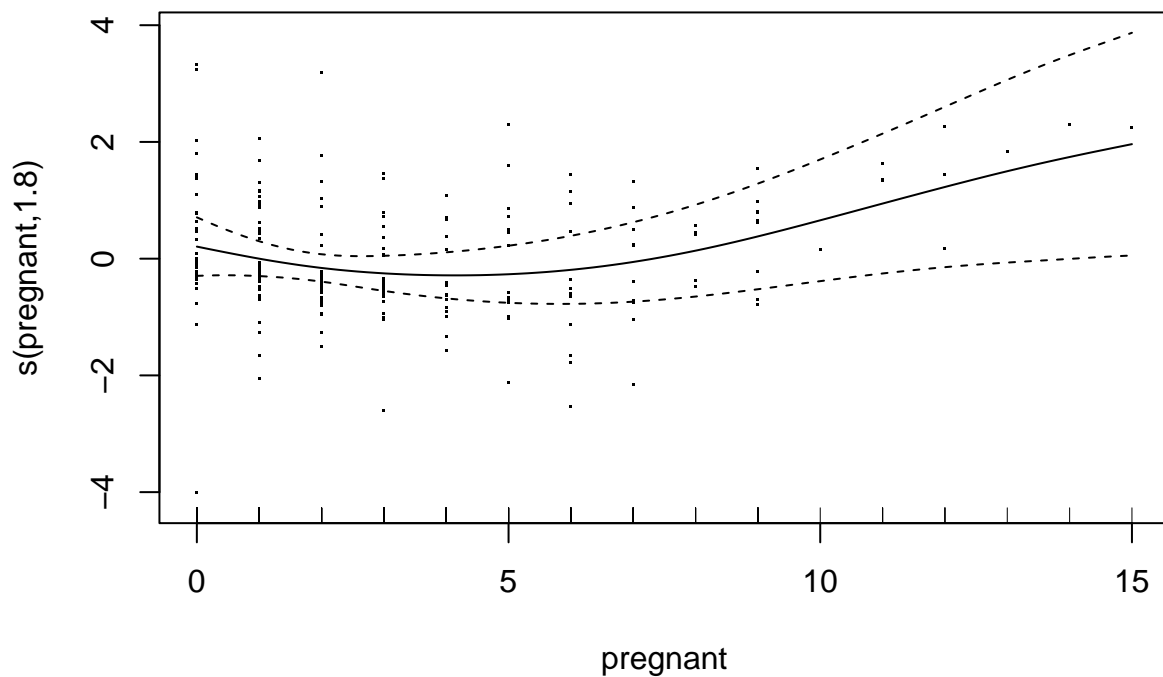






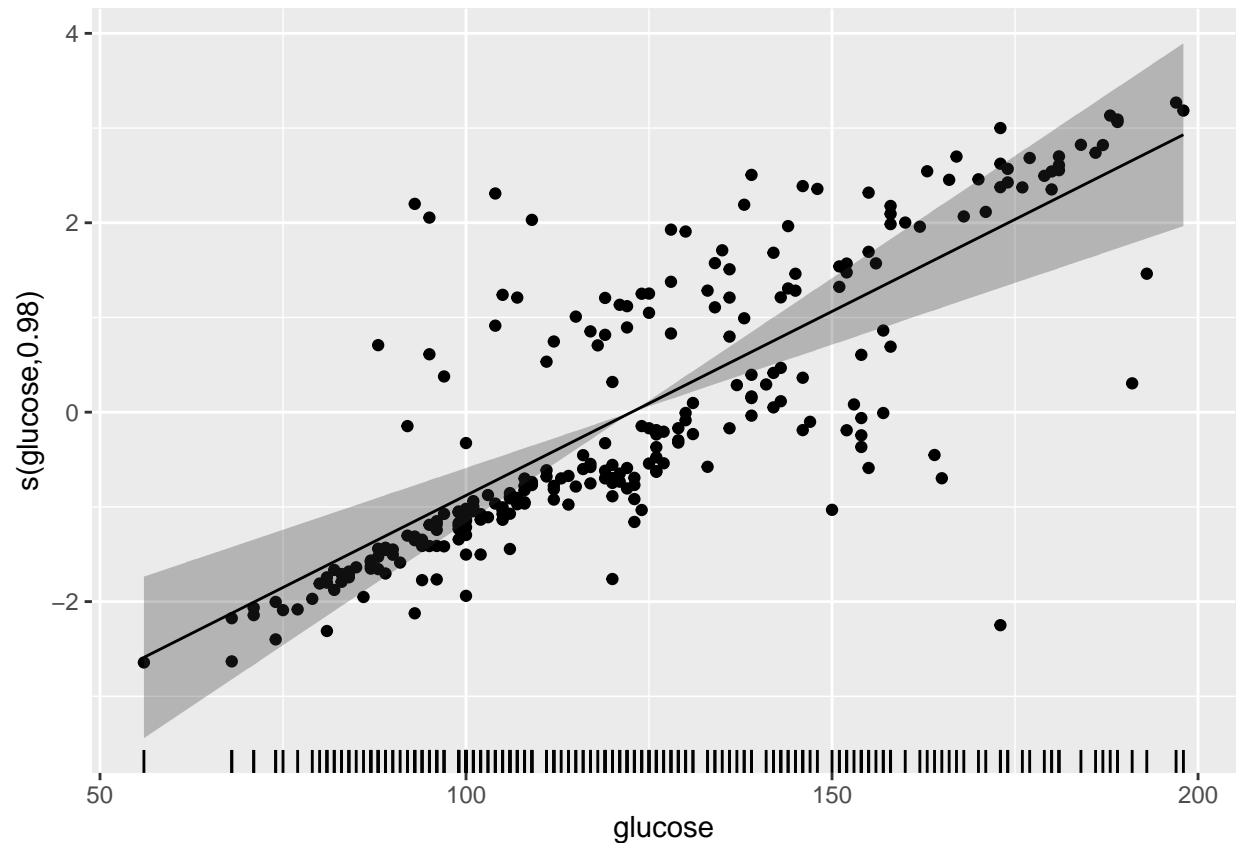






```
p_obj <- p_obj[[1]] # just one smooth so select the first component
sm_df <- as.data.frame(p_obj[c("x", "se", "fit")])
data_df <- as.data.frame(p_obj[c("raw", "p.resid")])

## plot
ggplot(sm_df, aes(x = x, y = fit)) +
  geom_rug(data = data_df, mapping = aes(x = raw, y = NULL),
    sides = "b") +
  geom_point(data = data_df, mapping = aes(x = raw, y = p.resid)) +
  geom_ribbon(aes(ymin = fit - se, ymax = fit + se, y = NULL),
    alpha = 0.3) +
  geom_line() +
  labs(x = p_obj$xlab, y = p_obj$ylab)
```

c. Tree-based methods

Setting up the k-fold cross validation $k = 10$ cross-validation folds. Reference: https://quantdev.ssri.psu.edu/sites/qdev/files/09_EnsembleMethods_2017_1127.html

```
library(rpart)           # For trees
library(rpart.plot)      # Enhanced tree plots
library(party)           # Alternative decision tree algorithm
```

```
## Warning: package 'party' was built under R version 4.3.3
```

```
## Loading required package: grid
```

```
## Loading required package: mvtnorm
```

```
## Warning: package 'mvtnorm' was built under R version 4.3.3
```

```
## Loading required package: modeltools
```

```
## Loading required package: stats4
```

```
## Loading required package: strucchange
```

```

## Warning: package 'strucchange' was built under R version 4.3.3

## Loading required package: zoo

##
## Attaching package: 'zoo'

## The following objects are masked from 'package:base':
##
##      as.Date, as.Date.numeric

## Loading required package: sandwich

## Warning: package 'sandwich' was built under R version 4.3.3

library(partykit)                # Convert rpart object to BinaryTree

## Warning: package 'partykit' was built under R version 4.3.3

## Loading required package: libcoin

##
## Attaching package: 'partykit'

## The following objects are masked from 'package:party':
##
##      cforest, ctree, ctree_control, edge_simple, mob, mob_control,
##      node_barplot, node_bivplot, node_boxplot, node_inner, node_surv,
##      node_terminal, varimp

library(pROC)                    # For ROC curves

## Type 'citation("pROC")' for a citation.

##
## Attaching package: 'pROC'

## The following objects are masked from 'package:stats':
##
##      cov, smooth, var

set.seed(1234)

# Setting up cross-validation
cvcontrol <- trainControl(method="repeatedcv",
                          number = 10,
                          allowParallel=TRUE)

```

(i) Classification tree

```

train.tree <- train(as.factor(diabetes) ~ .,
                    data=train,
                    method="ctree",
                    trControl=cvcontrol,
                    tuneLength = 10)
train.tree

```

```

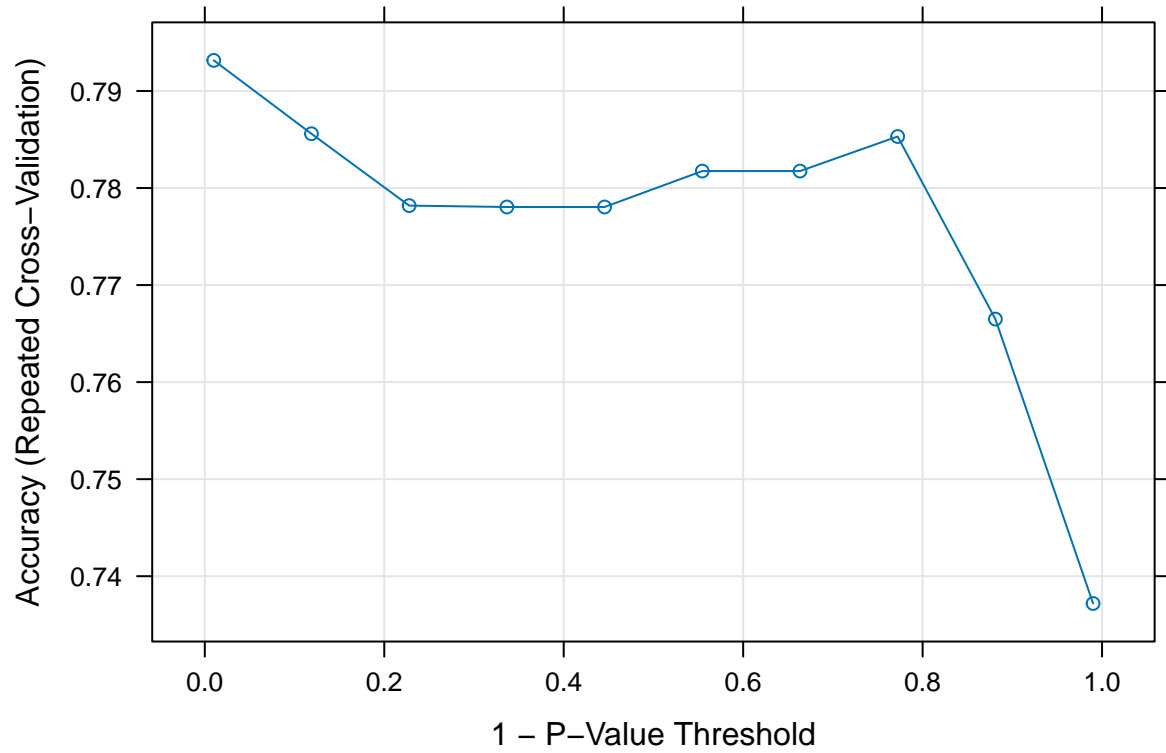
## Conditional Inference Tree
##
## 262 samples
## 8 predictor
## 2 classes: 'neg', 'pos'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 1 times)
## Summary of sample sizes: 235, 236, 235, 236, 235, 237, ...
## Resampling results across tuning parameters:
##
##   mincriterion  Accuracy  Kappa
##   0.0100000     0.7931567  0.5294069
##   0.1188889     0.7855954  0.4963222
##   0.2277778     0.7781880  0.4816163
##   0.3366667     0.7780456  0.4835965
##   0.4455556     0.7780456  0.4835965
##   0.5544444     0.7817493  0.4930560
##   0.6633333     0.7817493  0.4930560
##   0.7722222     0.7853105  0.4941199
##   0.8811111     0.7664957  0.4422783
##   0.9900000     0.7371852  0.3930795
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was mincriterion = 0.01.

```

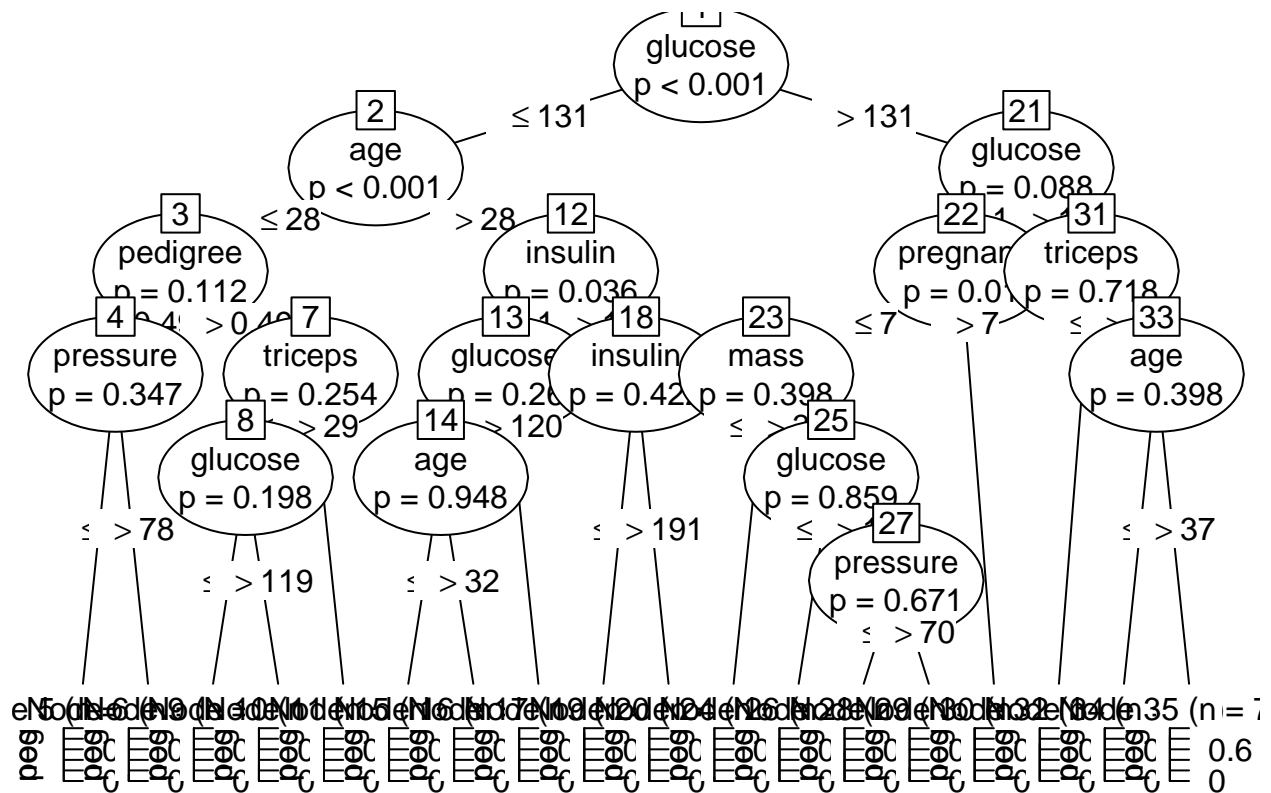
```

plot(train.tree)

```



```
plot(train.tree$finalModel)
```



```
# obtaining class predictions for training
tree.classTrain <- predict(train.tree, type="raw")

# Check accuracy and confusion matrix for training set
confusionMatrix(train$diabetes, tree.classTrain)
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction neg pos
##          neg 164  11
##          pos  24  63
##
##              Accuracy : 0.8664
##              95% CI : (0.8191, 0.9052)
##          No Information Rate : 0.7176
##          P-Value [Acc > NIR] : 7.327e-09
##
##              Kappa : 0.6871
##
##  Mcnemar's Test P-Value : 0.04252
##
##              Sensitivity : 0.8723
##              Specificity : 0.8514
##          Pos Pred Value : 0.9371
##          Neg Pred Value : 0.7241
```

```
##           Prevalence : 0.7176
##           Detection Rate : 0.6260
##           Detection Prevalence : 0.6679
##           Balanced Accuracy : 0.8618
##
##           'Positive' Class : neg
##
```

Accuracy of training set is 86.64%

```
# Obtaining class predictions for test set
tree.classTest <- predict(train.tree,
                          newdata = test,
                          type="raw")

# Check accuracy and confusion matrix for training set
confusionMatrix(test$diabetes, tree.classTest)
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction neg pos
##           neg  74  13
##           pos  18  25
##
##           Accuracy : 0.7615
##           95% CI : (0.6789, 0.8319)
##           No Information Rate : 0.7077
##           P-Value [Acc > NIR] : 0.1034
##
##           Kappa : 0.4451
##
##           McNemar's Test P-Value : 0.4725
##
##           Sensitivity : 0.8043
##           Specificity : 0.6579
##           Pos Pred Value : 0.8506
##           Neg Pred Value : 0.5814
##           Prevalence : 0.7077
##           Detection Rate : 0.5692
##           Detection Prevalence : 0.6692
##           Balanced Accuracy : 0.7311
##
##           'Positive' Class : neg
##
```

Accuracy of test set is 76.15%

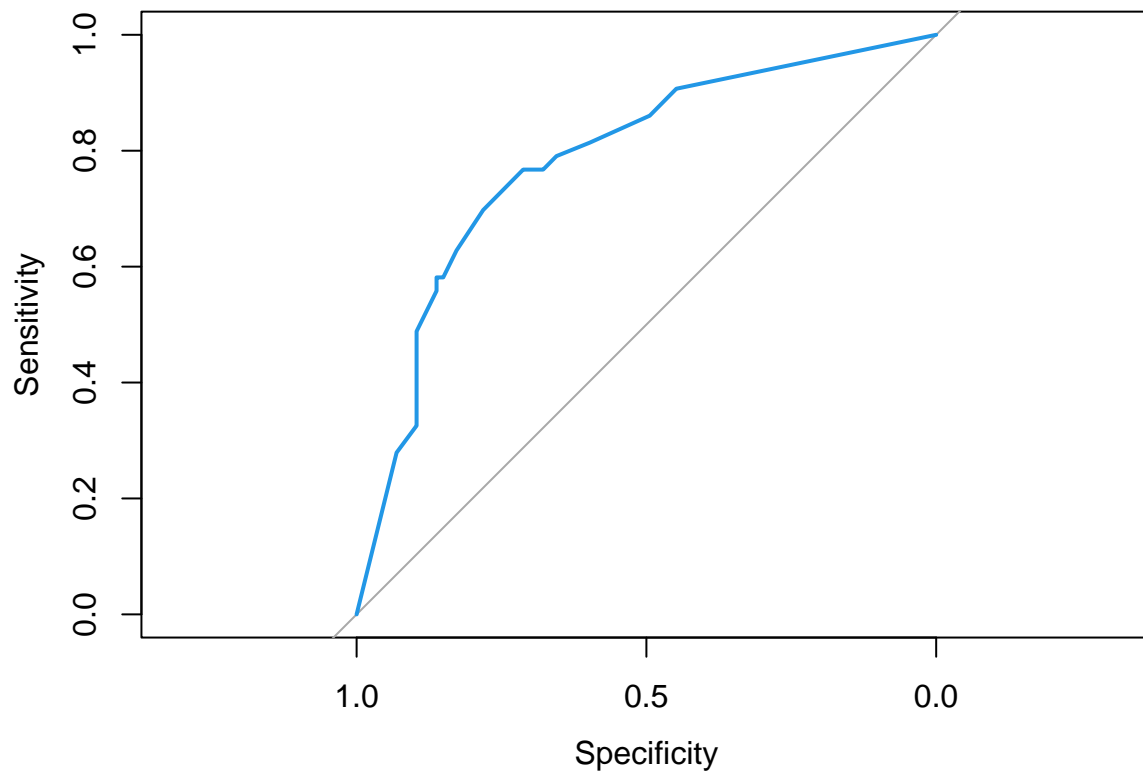
```
#Obtaining predicted probabilities for Test data
tree.probs=predict(train.tree,
                   newdata=test,
                   type="prob")
```

```
#Calculate ROC curve
rocCurve.tree <- roc(test$diabetes,tree.probs[, "neg"])
```

```
## Setting levels: control = neg, case = pos
```

```
## Setting direction: controls > cases
```

```
#plot the ROC curve
plot(rocCurve.tree,col=c(4))
```



```
#calculate the area under curve (bigger is better)
auc(rocCurve.tree)
```

```
## Area under the curve: 0.7848
```

(ii) Ensemble of bagged trees

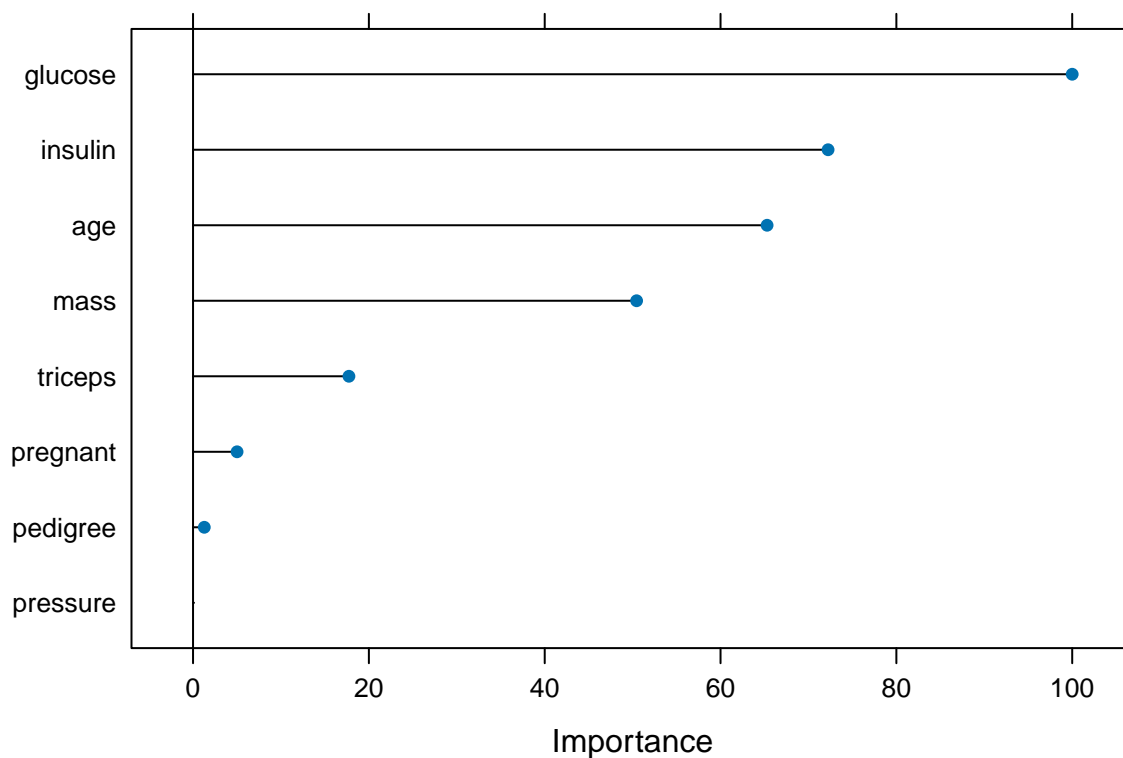
```
#Using treebag
train.bagg <- train(as.factor(diabetes) ~ .,
  data=train,
  method="treebag",
  trControl=cvcontrol,
```

```
importance=TRUE)
```

```
train.bagg
```

```
## Bagged CART
##
## 262 samples
## 8 predictor
## 2 classes: 'neg', 'pos'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 1 times)
## Summary of sample sizes: 235, 237, 235, 235, 236, 236, ...
## Resampling results:
##
## Accuracy   Kappa
## 0.7817721  0.4906951
```

```
plot(varImp(train.bagg))
```



```
#obtaining class predictions
bagg.classTrain <- predict(train.bagg, type="raw")

confusionMatrix(train$diabetes, bagg.classTrain)
```



```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction neg pos
##      neg 175   0
##      pos   0  87
##
##           Accuracy : 1
##           95% CI : (0.986, 1)
##      No Information Rate : 0.6679
##      P-Value [Acc > NIR] : < 2.2e-16
##
##           Kappa : 1
##
##  McNemar's Test P-Value : NA
##
##      Sensitivity : 1.0000
##      Specificity : 1.0000
##      Pos Pred Value : 1.0000
##      Neg Pred Value : 1.0000
##      Prevalence : 0.6679
##      Detection Rate : 0.6679
##      Detection Prevalence : 0.6679
##      Balanced Accuracy : 1.0000
##
##      'Positive' Class : neg
##
```

```
bagg.classTest <- predict(train.bagg,
                           newdata = test,
                           type="raw")

confusionMatrix(test$diabetes, bagg.classTest)
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction neg pos
##      neg  74  13
##      pos  17  26
##
##           Accuracy : 0.7692
##           95% CI : (0.6872, 0.8386)
##      No Information Rate : 0.7
##      P-Value [Acc > NIR] : 0.04933
##
##           Kappa : 0.4662
##
##  McNemar's Test P-Value : 0.58388
##
##      Sensitivity : 0.8132
##      Specificity : 0.6667
##      Pos Pred Value : 0.8506
##      Neg Pred Value : 0.6047
```

```
##           Prevalence : 0.7000
##           Detection Rate : 0.5692
##           Detection Prevalence : 0.6692
##           Balanced Accuracy : 0.7399
##
##           'Positive' Class : neg
##
```

```
#Obtaining predicted probabilities for Test data
```

```
bagg.probs=predict(train.bagg,
                   newdata=test,
                   type="prob")
```

```
#Calculate ROC curve
```

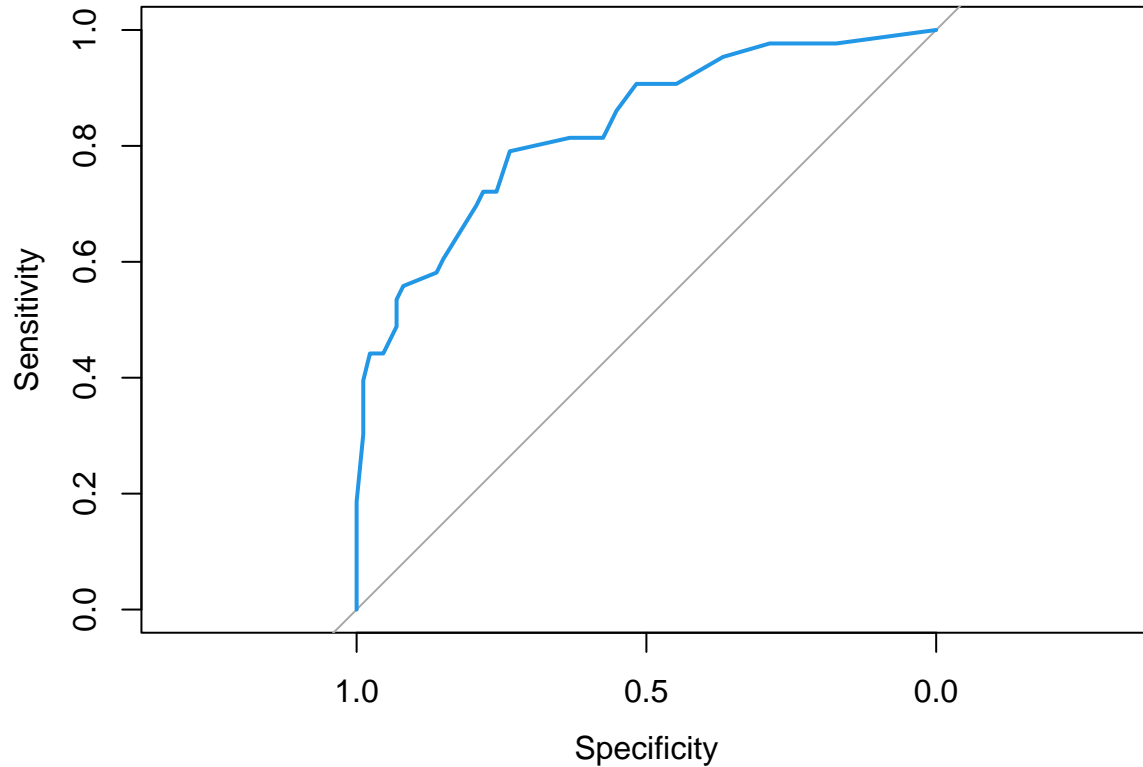
```
rocCurve.bagg <- roc(test$diabetes, bagg.probs[, "neg"])
```

```
## Setting levels: control = neg, case = pos
```

```
## Setting direction: controls > cases
```

```
#plot the ROC curve
```

```
plot(rocCurve.bagg,col=c(4))
```



```
#calculate the area under curve (bigger is better)
auc(rocCurve.bagg)
```

```
## Area under the curve: 0.8311
```

(iii) Random Forest

```
#Using treebag
train.rf <- train(as.factor(diabetes) ~ .,
                  data=train,
                  method="rf",
                  trControl=cvcontrol,
                  importance=TRUE)

train.rf
```

```
## Random Forest
##
## 262 samples
## 8 predictor
## 2 classes: 'neg', 'pos'
##
## No pre-processing
## Resampling: Cross-Validated (10 fold, repeated 1 times)
## Summary of sample sizes: 235, 235, 235, 236, 235, 236, ...
## Resampling results across tuning parameters:
##
##  mtry  Accuracy  Kappa
##  2     0.7938917 0.5193219
##  5     0.8014416 0.5417510
##  8     0.7898917 0.5141065
##
## Accuracy was used to select the optimal model using the largest value.
## The final value used for the model was mtry = 5.
```

```
#obtaining class predictions
rf.classTrain <- predict(train.rf, type="raw")

confusionMatrix(train$diabetes, rf.classTrain)
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction neg pos
##      neg 175   0
##      pos   0  87
##
##           Accuracy : 1
##           95% CI : (0.986, 1)
##      No Information Rate : 0.6679
```

```
##      P-Value [Acc > NIR] : < 2.2e-16
##
##              Kappa : 1
##
## Mcnemar's Test P-Value : NA
##
##      Sensitivity : 1.0000
##      Specificity : 1.0000
##      Pos Pred Value : 1.0000
##      Neg Pred Value : 1.0000
##      Prevalence : 0.6679
##      Detection Rate : 0.6679
##      Detection Prevalence : 0.6679
##      Balanced Accuracy : 1.0000
##
##      'Positive' Class : neg
##
```

```
rf.classTest <- predict(train.rf,
                        newdata = test,
                        type="raw")

confusionMatrix(test$diabetes, rf.classTest)
```

```
## Confusion Matrix and Statistics
##
##      Reference
## Prediction neg pos
##      neg  73  14
##      pos  16  27
##
##      Accuracy : 0.7692
##      95% CI : (0.6872, 0.8386)
##      No Information Rate : 0.6846
##      P-Value [Acc > NIR] : 0.02154
##
##      Kappa : 0.4725
##
## Mcnemar's Test P-Value : 0.85513
##
##      Sensitivity : 0.8202
##      Specificity : 0.6585
##      Pos Pred Value : 0.8391
##      Neg Pred Value : 0.6279
##      Prevalence : 0.6846
##      Detection Rate : 0.5615
##      Detection Prevalence : 0.6692
##      Balanced Accuracy : 0.7394
##
##      'Positive' Class : neg
##
```

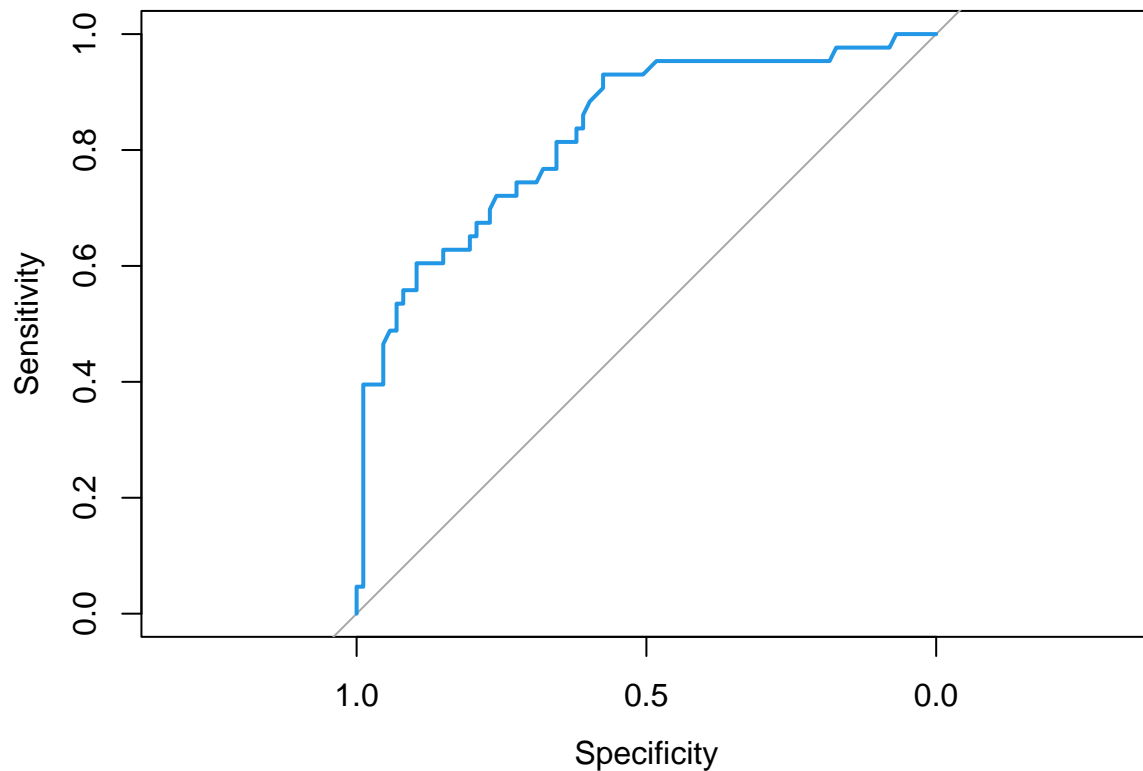
```
#Obtaining predicted probabilities for Test data
rf.probs=predict(train.rf,
                 newdata=test,
                 type="prob")

#Calculate ROC curve
rocCurve.rf <- roc(test$diabetes, rf.probs[, "neg"])
```

```
## Setting levels: control = neg, case = pos
```

```
## Setting direction: controls > cases
```

```
#plot the ROC curve
plot(rocCurve.rf,col=c(4))
```

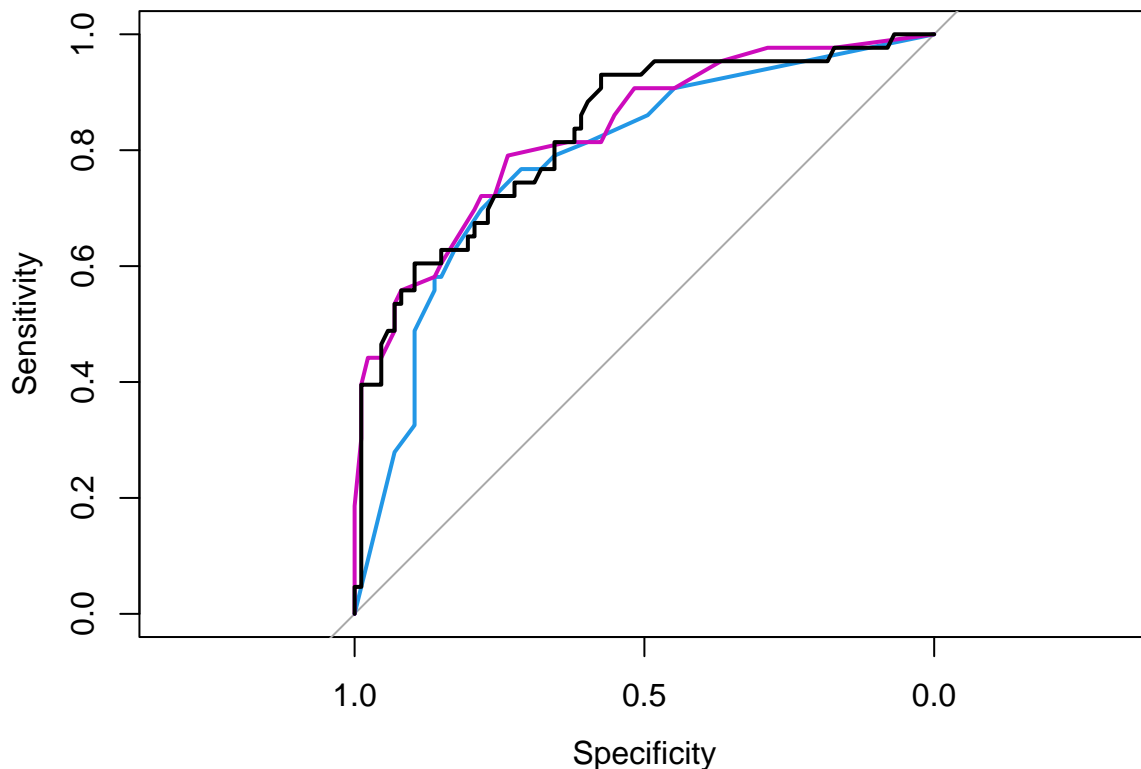


```
#calculate the area under curve (bigger is better)
auc(rocCurve.rf)
```

```
## Area under the curve: 0.8292
```

Tree-based models comparison

```
plot(rocCurve.tree,col=c(4))
plot(rocCurve.bagg,add=TRUE,col=c(6)) # color magenta is bagg
plot(rocCurve.rf,add=TRUE,col=c(1)) # color black is rf
```



d. Neural Network

```
library(tidyverse)

## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr      1.1.4      v readr      2.1.5
## v forcats    1.0.0      v stringr    1.5.1
## v lubridate  1.9.3      v tibble     3.2.1
## v purrr      1.0.2      v tidyr      1.3.1
## -- Conflicts ----- tidyverse_conflicts() --
## x stringr::boundary() masks strucchange::boundary()
## x dplyr::collapse()   masks nlme::collapse()
## x dplyr::combine()    masks gridExtra::combine()
## x tidyr::expand()     masks Matrix::expand()
## x dplyr::filter()     masks stats::filter()
## x dplyr::lag()        masks stats::lag()
## x purrr::lift()       masks caret::lift()
## x tidyr::pack()       masks Matrix::pack()
```

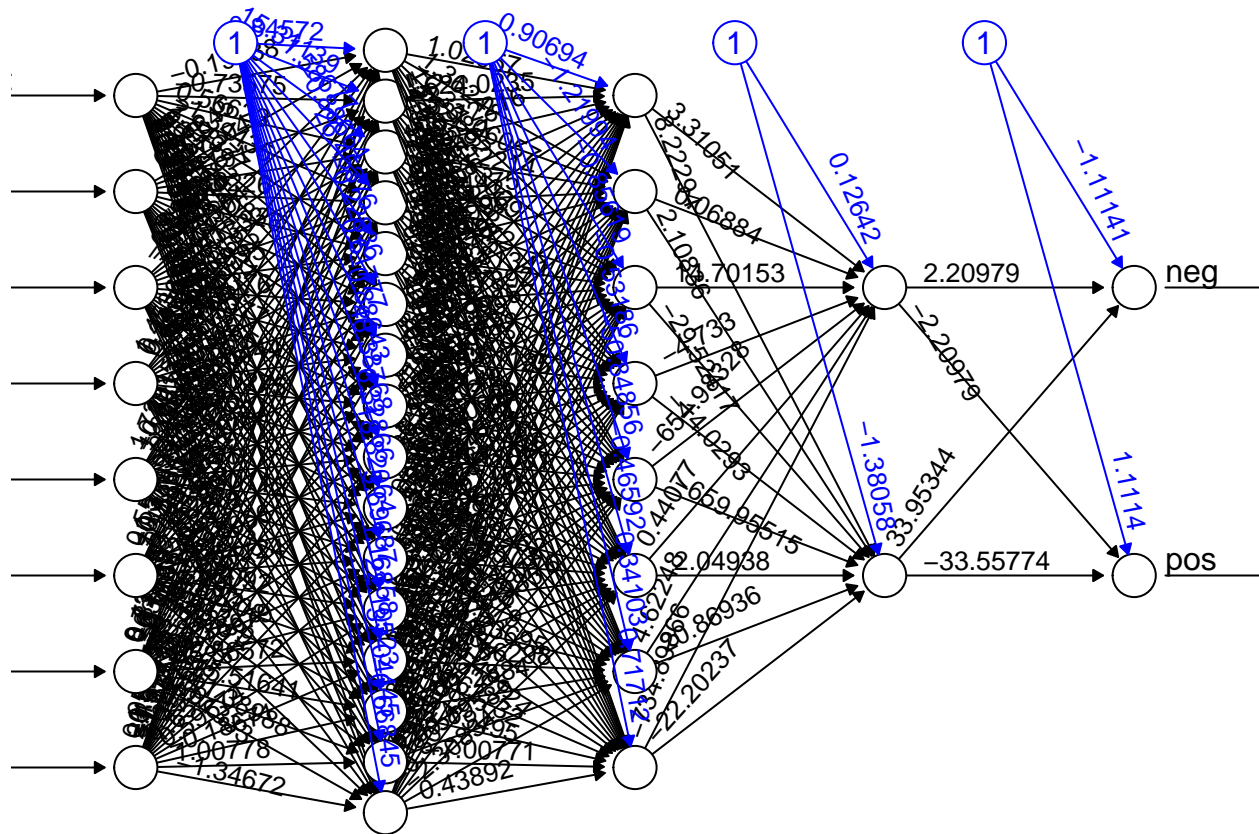
```
## x dplyr::select()      masks MASS::select()
## x tidyr::unpack()     masks Matrix::unpack()
## x dplyr::where()      masks party::where()
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
library(neuralnet)
```

```
##
## Attaching package: 'neuralnet'
##
## The following object is masked from 'package:dplyr':
##
##   compute
```

```
nn_model = neuralnet(
  diabetes~.,
  data=train,
  hidden=c(16,8,2),
  linear.output = FALSE
)
```

```
plot(nn_model, rep = "best")
```



```

pred <- predict(nn_model, test)
labels <- c("neg", "pos")

prediction_label <- data.frame(max.col(pred)) %>%
mutate(pred=labels[max.col.pred.]) %>%
select(2) %>%
unlist()

table(test$diabetes, prediction_label)

```

```

##      prediction_label
##      neg pos
## neg  59  28
## pos  19  24

```

```

check = as.numeric(test$diabetes) == max.col(pred)
accuracy = (sum(check)/nrow(test))*100
print(accuracy)

```

```
## [1] 63.84615
```

e. Compare all models