ECSE 543A NUMERICAL METHODS IN ELECTRICAL ENGINEERING Assignment 3

Set: 13-Nov-2017 Due: 07-Dec-2017

- 1. You are given a list of measured BH points for M19 steel (Table 1), with which to construct a continuous graph of B versus H.
 - (a) Interpolate the first 6 points using full-domain Lagrange polynomials. Is the result plausible, i.e. do you think it lies close to the true B versus H graph over this range?
 - (b) Now use the same type of interpolation for the 6 points at B = 0, 1.3, 1.4, 1.7, 1.8, 1.9. Is this result plausible?
 - (c) An alternative to full-domain Lagrange polynomials is to interpolate using cubic Hermite polynomials in each of the 5 subdomains between the 6 points given in (b). With this approach, there remain 6 degrees of freedom the slopes at the 6 points. Suggest ways of fixing the 6 slopes to get a good interpolation of the points.
- 2. The magnetic circuit of Figure 1 has a core made of MI9 steel, with a cross-sectional area 1 cm². $L_c = 30$ cm and $L_a = 0.5$ cm. The coil has N = 1000 turns and carries a current I = 8 A.
 - (a) Derive a (nonlinear) equation for the flux ψ in the core, of the form $f(\psi) = 0$.
 - (b) Solve the nonlinear equation using Newton-Raphson. Use a piecewise-linear interpolation of the data in Table 1. Start with zero flux and finish when

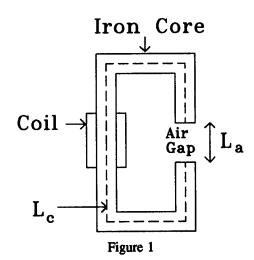
$$|f(\psi)/f(0)| < 10^{-6}$$

Record the final flux, and the number of steps taken.

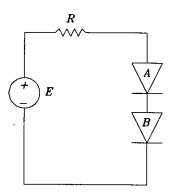
(c) Try solving the same problem with successive substitution. If the method does not converge, suggest and test a modification of the method that does converge.

в (Т)	H (A/m)
0.0	0.0
0.2	14.7
0.4	36.5
0.6	71.7
0.8	121.4
1.0	197.4
$\overline{1.1}$	256.2
1.2	348.7
1.3	540.6
1.4	1062.8
1.5	2318.0
1.6	4781.9
1.7	8687.4
1.8	13924.3
1.9	22650.2
1.9	44030.4

Table 1: BH Data for M19 Steel



- 3. In the circuit shown below, the DC voltage E is 220 mV, the resistance R is 500 Ω , the diode A reverse saturation current I_{sA} is 0.6 μ A, the diode B reverse saturation current I_{sB} is 1.2 μ A, and assume kT/q to be 25 mV.
 - (a) Derive nonlinear equations for a vector of nodal voltages, \mathbf{v}_n , in the form $\mathbf{f}(\mathbf{v}_n) = 0$. Give \mathbf{f} explicitly in terms of the variables I_{SA} , I_{SB} , E, R and \mathbf{v}_n .
 - (b) Solve the equation $\mathbf{f} = 0$ by the Newton-Raphson method. At each step, record \mathbf{f} and the voltage across each diode. Is the convergence quadratic? [Hint: define a suitable error measure ε_k].



- 4.
- (a) Integrate the function cos(x) on the interval x=0 to x=1, by dividing the interval into N equal segments and using one-point Gauss-Legendre integration for each segment. Plot $log_{10}(E)$ versus $log_{10}(N)$ for N=1, 2, ..., 20, where E is the absolute error in the computed integral. Comment on the result.
- (b) Repeat part (a) for the function $log_e(x)$, only this time plot for N=10, 20,...200. Comment on the result.
- (c) An alternative to dividing the interval into equal segments is to use smaller segments in more difficult parts of the interval. Experiment with a scheme of this kind, and see how accurately you can integrate $log_e(x)$ using only 10 segments.