Karma Computer

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1 Architecture

Karma is a computer with a Von Neumann architecture having an address space of 2²⁰ cells, one 32-bit machine word each.

The processor has 16 one-word (32 bits each) registers r0-r15, as well as an additional flags register (also one-word). Their usage is described in Table 1.

Table 1: Usage of Karma processor registers

r0-r13	Free usage
r14	Stack head pointer
r15	Instruction pointer
flags	Comparison operation result

The usage of the r14 register is described in the Stack-related commands section, the aim of the r15 register is discussed in the Function calls section, and the usage of the flags register is detailed in the Comparisons and jumps section.

2 Karma assembler standard

2.1 Command formats

Each command takes up *exactly one* word, 8 high bits of which specify the operation code and the use of the rest 24 bits is command-specific. With respect to the operation code each command may be of one of the following formats:

Table 2: Karma processor command formats

		8 bits	4 bits	4 bits	16 bits	Syntax sample
Register-memory	RM		register	memory	address	load r0, 12956
Register-register	RR	command	receiver register	source register	source modifier	mov r1, r2, -0xa21
Register-immediate	RI	code	register	immedia	ate value	ori r2, 64
Jump	J		ignored	memory	address	calli 01547

The *memory address* operand for RM and J commands is interpreted as an unsigned integer representing the number of a memory cell (in 0-indexing). The bit size of the operand (20 bits) allows it to represent any memory cell (there are 2^{20} of them).

For RM and J commands the memory address operand in the assembler code may be represented as:

- A decimal number (non-prefixed, not starting with 0)
- An octal number (with a 0 prefix)
- A hexadecimal number (with a 0x or a 0x prefix)

The same applies to the *source modifier* and *immediate value* operands for RR and RI commands respectively. If the operand is negative, in octal and hexadecimal representations the minus sign is placed before the prefix.

For the sake of not overcomplicating matters all arguments of any command are required. When using an RR command, if one does not wish to modify the value represented by the source modifier, the *source modifier* should be specified as 0.

2.2 Types

2.2.1 Basic types

There are three architecture-defined basic types in the Karma assembler:

- uint32 is a one-word unsigned integral type
- uint 64 is a two-word unsigned integral type
- double is a two-word real-valued type

The two-word types (i.e. uint64 and double) are represented by two consecutive memory cells or registers. The low 32 bits are placed in the first memory cell/register and the high 32 bits – in the subsequent one. When referring to a two-word type value in commands, the specified memory cell/register is *always* considered to be the first one (i.e. the one containing the low 32 bits of the value).

2.2.2 Source modifier and immediate value: two's complement

The RR and RI commands both accept a signed integral operand, which cannot be straightforwardly represented using the basic types (because there are no signed integral basic types).

The signed integral values always have the two's complement representation (see Wiki for details). Such a representation is dependent on the bit size of the type that holds the value. Therefore, in the binary representation of a command, the same value may be represented differently if it is a source modifier versus an immediate value. That occurs iff the value is negative.

Before usage, both the source modifier and the immediate value are transformed to uint 32 using the 32-bit two's complement representation for the same value. E.g. if a source modifier was -5 (written in 16-bit two's complement representation), it will be converted to the same -5 value, but in the 32-bit representation.

The two's complement representation of signed values is designed so that it produces intuitive additive operations results (see explanation). Therefore, when specifying the source modifier, one does not need to think about the signed integral values representation, and may simply assume that the signed source modifier value is added to the unsigned source register value in a purely mathematical sense of things, after which the resulting value is taken modulo 2^{32} .

Note, that the addition of the source modifier to the source register value always happens before the main operation (unless, of course, the command's documentation states that the source modifier is ignored). Therefore, all RI commands that do not ignore the source modifier effectively accept two uint32 operands.

2.3 Command set

2.3.1 System commands

Table 3: System commands

Code	Name	Format	Syntax sample	Description
0	halt	RI	halt r1 0	Stop processor
1	syscall	RI	syscall r0 100	System call

halt

The halt command sends an interruption signal to the CPU, which halts it until the next external signal is received, after which the execution is continued. The immediate value operand is ignored.

syscall

The syscall command's immediate operand specifies the call code. The semantics of those codes is described in Table 4:

Table 4: System call codes

Code	Name	Description	Register operand
0	EXIT	Finish execution without error	Ignored
100	SCANINT	Get a uint32 from stdin	Receiver
101	SCANDOUBLE	Get a double value from stdin	Low bits receiver
102	PRINTINT	Output a uint32 to stdout	Source
103	PRINTDOUBLE	Output double value to stdout	Low bits source
104	GETCHAR	Get a single ASCII character from stdin	Receiver
105	PUTCHAR	Output a single ASCII character from stdout	Source

Specifying a value for the syscall immediate operand not listed in the table above leads to an error during compilation or execution (depending on whether such a value was originally specified in an assembler code or in a handcrafted executable file).

If the source register for the PUTCHAR system call contains a value greater than 255 (that is, not representing an ASCII character), an execution error will occur.

2.3.2 Integer arithmetic operators

Table 5: Integer arithmetic operators

Code	Name	Format	Syntax sample	Description
2	add	RR	add r1 r2 -3	r1 += r2 - 3
3	addi	RI	addi r4 10	r4 += 10
4	sub	RR	sub r3 r5 5	r3 -= r5 + 5
5	subi	RI	subi r4 1	r4 -= 1
6	mul	RR	mul r3 r7 -2	(r4,r3) = r3 * (r7 - 2)
7	muli	RI	muli r5 100	(r6, r5) = r5 * 100
8	div	RR	div r3 r8 5	tmp = $(r4, r3)$ r3 = tmp / (r8 + 5) r4 = tmp % (r8 + 5)
9	divi	RI	divi r6 7	tmp = $(r7, r6)$ r6 = tmp / 7 r7 = tmp % 7

add, addi, sub, subi

These commands take two uint32 values obtained from the specified operands (see the respective section for details) and produce a uint32 value as a result.

In the mathematical sense of things, for the unsigned (as-is) interpretation of the operands the arithmetic is simply performed modulo 2^{32} . E.g. if r0 contained 0, after subi r0 1, the value in r0 will be $2^{32} - 1$.

At the same time, if both terms of each operation were to be interpreted as *signed* integral values in the 32-bit two's complement representation, the result, if interpreted as a *signed* integral value in the same representation, would be mathematically correct. That is provided by the two's complement representation of the signed operands (see explanations for addition and subtraction).

mul, muli

These commands multiply two uint32 values obtained from the specified operands (see the respective section for details), produce a uint64 value and store it into the two registers starting from the specified receiver register (see here for details).

Unlike additive operations, these operations would not produce the correct results if the factors were to interpreted as *signed* integral values in the 32-bit two's complement representation. That is because in order to produce valid results in such a case, the factors must first be *extended* to the size of the destination type, i.e. rewritten in the 64-bit two's complement representation (see explanation). However, if we were to perform such an extension, we would block the opportunity to multiply two big *unsigned* values (because we would have interpreted them as *signed* values and added non-zero bits to the right of the original representation when extending, thus producing an incorrect result for this case).

Overall, one must be cautious when specifying the source modifier and the immediate value in these operations, and bear in mind that if those produce negative factors, they will firstly be converted to uint 32 by being taken modulo 2^{32} .

div, divi

These commands accept a uint64 dividend from the two registers starting from the specified receiver register (see here for storage details) and a uint32 divisor obtained in the common manner and perform an integral division. The quotient is then placed into the receiver register and the remainder – into the next register.

If the quotient does not fit into a register, a quotient overflow execution error occurs.

Like the mul and muli commands, these command only work with *unsigned* operands and would not produce valid results if the operands were to be interpreted as *signed* integral values.

2.3.3 Bitwise operators

Table 6: Bitwise operators

Code	Name	Format	Syntax sample	Description
10	not	RI	not r1 0	r1 =~ r1
11	shl	RR	shl r1 r2 1	r1 ≪= r2 + 1
12	shli	RI	shli r1 2	r1 ≪= 2
13	shr	RR	shr r1 r2 -4	r1 ≫= r2 - 4
14	shri	RI	shri r1 2	r1 ≫= 2
15	and	RR	and r4 r6 3	r4 &= r6 + 3
16	andi	RI	andi r5 2	r5 &= 2
17	or	RR	or r3 r2 -2	r3 = r2 - 2
18	ori	RI	ori r6 100	r6 = 100
19	xor	RR	xor r1 r5 0	r1 ^= r5
20	xori	RI	xori r1 127	r1 ^= 127

not

The immediate value is ignored, but per our agreement must be present for simplicity.

Other bitwise operators

All other bitwise operators take two uint32 values obtained from the specified operands in the common manner and produce a uint32 value as a result. The right hand side operand must be less than the size of a machine word (i.e. no more than 31), otherwise an execution error occurs.

2.3.4 Real-valued operators

Table 7: Real-valued operators

Code	Name	Format	Syntax sample	Description
21	itod	RR	itod r2 r5 5	(r3, r2) = double(r5 + 5)
22	dtoi	RR	dtoi r2 r5 0	r2 = uint32((r6, r5))
23	addd	RR	addd r2 r5 0	(r3,r2) += (r6,r5)
24	subd	RR	subd r1 r6 0	(r2,r1) = (r7,r6)
25	muld	RR	muld r0 r2 0	(r1,r0) *= (r3,r2)
26	divd	RR	divd r1 r3 0	(r2,r1) /= (r4,r3)

For the double values storage please refer to this section. For the double values representation please refer to Wiki, specifically to the Overview and Internal representation sections.

itod

The source modifier is added to the source register in the common manner, after which the resulting uint32 value is converted to double and stored into the two registers starting from the specified receiver register.

dtoi

The source modifier is ignored, but per our agreement must be present for simplicity.

The double value obtained from the two registers starting from the source register is converted to uint 32 and stored into the receiver register. If the value obtained after conversion does not fit into uint 32, an execution error occurs.

Real-valued arithmetic operators

The source modifier is ignored for all real-valued arithmetic operators, but per our agreement must be present for simplicity.

2.3.5 Comparisons and jumps

Table 8: Comparisons and jumps

Code	Name	Format	Syntax sample	Description
27	cmp	RR	cmp r0 r1 2	r0 <=> r1 + 2
28	cmpi	RI	cmpi r0 0	r0 <=> 0
29	cmpd	RR	cmpd r1 r4 0	(r2,r1) <=> (r5,r4)
30	jmp	J	jmp Oxffa	Unconditional jump
31	jne	J	jne 0xd471	Jump if not equal
32	jeq	J	jeq 05637	Jump if equal
33	jle	J	jle 1234	Jump if less or equal
34	jl	J	jl 0X1e4b	Jump if less
35	jge	J	jge 29834	Jump if greater or equal
36	jg	J	jg 03457	Jump if greater

Flags register

To allow for basic execution branching, an additional flags register is supported. It holds the result of the latest comparison. Only the lowest 6 bits of this register are used. The semantics of those bits is described in Table 9.

Table 9: flags register bits semantics (low-to-high, 0-indexed)

0	Equal
1	Not equal
2	Greater
3	Less
4	Greater or equal
5	Less or equal

Several bits may be simultaneously filled. For example, if the latest comparison resulted in equality, the value of the flags register will be 110001₂, because equality causes the 'less/greater or equal' conditions to also be true.

cmp, cmpi, cmpd

These are comparison operators. They compare the two values provided by the operands and store the result to the flags register according to the flags register bits semantics described above. These are the only commands that store values in the flags register.

The cmp and cmpi command compare the uint32 value from the receiver register to the uint32 value obtained from the operands in the common manner.

The cmpd command ignores the immediate value operand and compares the two double values specified by the receiver and the source register operands. For the double values storage please refer to this section.

Jump commands

These commands implement execution branching. All of them, except for the jmp command, do nothing unless the condition mentioned in the table above is satisfied, that is, if the respective bit (according to the flags register bits semantics) is filled in the flags register. The jmp command is performed unconditionally.

If one of these commands take effect, the next executed instruction will be the one stored in the provided memory address operand (because the Karma computer has a Von Neumann architecture, the instructions' binaries are stored in the common address space).

These are the only commands that read the value stored in the flags register.

2.3.6 Stack-related commands

Table 10: Stack operators and function calls

Code	Name	Format	Syntax sample	Description
37	push	RI	push r0 255	*(r14) = r0 + 255
38	pop	RI	pop r3 3	r3 = *(+ + r14) + 3

These commands work directly with the stack, putting uint32 values into it (push) and extracting them afterwards (pop).

For the push command, the immediate value operand is added to the value from the specified source register before it is pushed to the stack. Similarly, for the pop command, the immediate value operand is added to the value retrieved (popped) from the stack before it is stored in the specified receiver register. The additions happen according to the common rules.

The r14 register is the stack head pointer (as stated here). It always points to the memory cell, in which the data will be put on push operation, that is, one memory cell 'ahead' of the latest pushed value. The stack grows *backwards*, i.e. the next pushed value is stored in the *previous* memory cell from the latest one.

2.3.7 Data transfer commands

Table 11: Data transfer commands

Code	Name	Format	Syntax sample	Description
39	lc	RI	lc r7 123	r7 = 123
40	la	RM	la r5 0xab1f	r5 = 0xab1f
41	mov	RR	mov r0 r3 10	r0 = r3 + 10
42	load	RM	load r3 0xffc2	r3 = *(0xffc2)
43	load2	RM	load2 r4 13224	r4 = *(13224) r5 = *(13225)
44	store	RM	store r1 057123	*(057123) = r1
45	store2	RM	store2 r0 0X15fc	*(0X15fc) = r0 *(0X15fd) = r1
46	loadr	RR	loadr r8 r1 15	r8 = *(r1 + 15)
47	loadr2	RR	loadr2 r2 r0 12	r2 = *(r0 + 12) r3 = *(r0 + 13)
48	storer	RR	storer r2 r3 3	*(r3+3) = r2
49	storer2	RR	storer2 r5 r2 13	*(r2+13) = r5 *(r3+14) = r6

1c, la, mov

These commands store the uint 32 value obtained from the operands in the common manner to the specified receiver register. The la command is similar to lc, but allows for labels usage (see Labels section for details).

Register-memory data transfer

All the other commands are used to transfer data between the registers and the memory.

Those of them which have the RR format treat the uint32 value obtained from the operands in the common manner as a memory address. If this value does not represent a valid address, i.e. is greater or equal to 2^{20} , an execution error occurs. Note that the storer and the storer2 commands treat the receiver register operand as the opposite, i.e. as the *source* for a value to be stored into the memory. These are the only two RR commands with such behaviour.

For the RM format commands the memory cell is specified by the 20-bit *unsigned* memory address operand. Since any 20-bit unsigned value represents a valid memory address, an execution error at this stage cannot occur in this case.

The commands with a '2' suffix perform the same action as the respective commands without the suffix twice: once with the register and the memory cell specified by the operands and then with the next register and the next memory cell. Therefore, the specified register cannot be r15 and the specified memory cell cannot be 0xfffff (there are no next ones for them). If such a situation does occur, it results in an execution error.

Table 12: Function call comands

Code	Name	Format	Syntax sample	Description
50	call	RR	call r0 r5 2	Call the function located at the address r5 + 2
51	calli	J	calli 21913	Call the function located at the address 21913
52	ret	J	ret 3	Return and clear 3 arguments

This section defines the rules by which the execution of one part of the code (the *caller*) can be delayed until another part (the *callee*) is executed. The callee is often also referred to as a *subprogram* or a *function*, and the delay process is called a *function* call. The function call commands extensively use the r15 register. Its usage is described below.

r15 register

The r15 register always contains the address of the next instruction to be executed. When executing the binary code, the Karma executor consecutively checks the r15 register and executes the command, whose address is stored there. If at any point the r15 register is corrupted and does not store a valid memory address (i.e. if the value stored in the r15 register is greater or equal to 2^{20}), an execution error occurs.

Calling convention

For the functions to be meaningful they need to accept *arguments*, i.e. values passed from the caller to the callee for the latter to perform computations dependant on these values. The arguments can be passed in a number of ways, e.g. be saved to some predefined registers or a preallocated part of the address space to then be retrieved from there by the caller. Alternatively, the arguments may be passed via the stack. For all programs to be understandable and intuitive to a code reader, some sort of agreement has to be established. This agreement is often called the *calling convention*.

Note that a calling convention is exactly that – a convention. Nothing on the architecture or the syntax level prevents one from not following it during their code development. However, that is considered a bad practice as it can lead to confusion and unexpected results for the code user.

By the Karma assembler calling convention, the arguments are passed to a function via the stack last-to-first, that is, the semantically first argument is the last one to be pushed to the stack.

call, calli

These commands perform the transfer of control from the caller to the callee.

For the call command the address of the next instruction to be executed is obtained from the specified operands in the common manner. If this value does not represent a valid address, i.e. is greater or equal to 2^{20} , an execution error occurs.

For the calli command the address of the next instruction to be executed is specified by the 20-bit *unsigned* memory address operand. Since any 20-bit unsigned value represents a valid memory address, no execution error can occur in this case.

Both these command do the following:

- Push the value obtained from the r15 register (i.e. the address of the instruction that would be executed next if the current command did not interrupt the consecutive execution, the return point) to the stack (as if with the push command)
- Store the address obtained by the operands (as described above) in the r15 register (to be executed next)

The call command additionally stores a copy of the return point address into the provided receiver register.

ret

This command performs the transfer of control from the callee back to the caller. It pops a value from the stack into the r15 register (as if with the pop command), after which it increments the value stored in r14 (the stack head pointer) by a value specified by its operand.

This is the only J command, for which the memory address operand does **not** in fact represent a memory cell. Instead, it specifies the number of additional (to the return point address) values that should be popped from the stack (without storing them anywhere). It is used to clear the stack from the function arguments. It is the user's responsibility to make sure that the number of additional values popped from the stack equals the number of the function arguments, i.e. the executor has no way of checking that condition, and specifying the wrong value as the ret command operand may lead to unexpected stack contents.

2.4 Constants

One can define a constant of any basic type as well as of two additional types: char and string.

Syntax sample: uint32 123

For consistent disassembling purposes any constant's memory representation is preceded with a one-word unique type identifier.

uint32, uint64

These values may be represented in all the same ways as command operands.

The negative values are processed in the common manner, i.e. using the two's complement representation for the bit size of the respective type. The values of uint 32 type constants which are greater or equal to 2^{32} , but are less than 2^{64} , are taken modulo 2^{32} . If the specified value does not fit into uint 64, a compile error occurs.

For storage details see the respective section.

double

A double constant may be represented either in a decimal or a hexadecimal formats. Both these formats are described with the std::stod function of the C++ standard.

For storage details see the respective section.

char

A char constant value must be surrounded with single quotes.

There are a number of escape sequences representing certain special ASCII characters. One of those is the '\#' escape sequence, used to represent a single '#' character (the hash sign, ASCII code 35). This escape sequence allows to resolve the confusion between a hash sign at the start of a comment (see Comments section for details). The rest of the supported escape sequences are listed in the Simple escape sequences table of the C++ standard.

A char constant value is stored as a uint 32 from 0 to 255 inclusively in ASCII encoding.

string

A string constant value must be surrounded with double quotes. Such a value represents a sequence of char values. In particular, that means that all the same escape sequences are used.

A string value is represented in memory as the respective char values stored in consecutive memory cells followed by an additional zero character (ASCII code 0). The zero character indicates the end of a string.

2.5 Labels

Before a command or a constant either on the same or on a separate line one may place a *label*, which can be used later on in the assembler code to indicate the memory address of the command or constant it is placed before.

Syntax:

- A label must consist only of lowercase latin letters, digits, underscores and dots
- A label must not start with a digit
- A label must be followed by a colon
- A label must be the first word in its line (it may be the only word of the line)
- A label must not conflict with predefined words (i.e. command names, directives, etc.)
- The next word after the label must be a command name
 In particular, that means that there cannot be two consecutive labels pointing to the same command
- The labels must be unique (i.e. label redefinition is not allowed)

Usage:

- A label usage may precede its definition
- A label must be defined somewhere in the code to be used, there are no predefined labels
- A label may only be used as a memory address, i.e. only as an operand of a command of either RM or J type Note: this means that, when used, a label is always the last word in its line (see Command formats section)

2.6 Directives

2.6.1 include directive

An assembler file may have several include directives at the beginning. An include directive must be followed by an unquoted string representing a relative (to the original file) path to another assembler file.

If such directives are present, the files specified by them are compiled with the code from the original file as if their contents were copied to the beginning of the original file in the order of inclusion. In particular, that means that the code from the original file may use the labels defined in the included files. Therefore the labels must be unique throughout all the included files as well as the original file.

All include statements must appear before the code. If an include directive is encountered after the first command (or label, whichever occurs first) of the file or if the relative path specified by the directive is invalid for any reason (not a relative path, no such file exists, etc.), a compilation error occurs.

2.6.2 end directive

An assembler program must have *exactly one* end directive, which must be in *the last* line of the program. It has one operand which indicates the address of the first instruction (or a label).

2.7 Comments

Each line may contain a hash sign (#). If it does, everything after the hash sign is considered a comment and is not compiled into the executable file. Multiline comments are not allowed.

Note that if hash sign is preceded with a backslash (\) it is not considered a comment start. This allows for using a hash sign in string or char constants (see Constants section for details).

2.8 Notes

- The Karma processor has a RISC architecture, which means that there is no way to operate directly on memory cells, all data has to be loaded to the registers before modifications and the results have to be explicitly stored back to the memory if necessary (see Data transfer commands for details)
- A Von Neumann architecture of the Karma computer implies that both the machine code of the program and the stack are
 inside the global address space. The former is placed at its beginning, and the latter starts at its end and grows backwards
- The stack is *unbounded*, i.e. it does not have any size limits besides the address space size
- Our system allows to write data to any memory cells, including the ones occupied by the machine code itself Therefore, theoretically, a program might overwrite itself during runtime, although such behaviour is considered a bad practice
- The same applies to the registers: any register, except for flags, may be passed as an operand to any command (that accepts a register operand). That includes the r14 and r15 registers, which are meant for utility purposes. Manually modifying the values of these registers, while allowed, is considered a bad practice and can lead to unexpected results

3 Karma executable file

To run a program on a Karma computer one needs to generate an executable file which contains meta-information about the machine code and the code itself. The executable file is stored in a remote storage (e.g. a hard drive or an SSD) as a byte sequence. The header of the executable file takes up exactly 512 bytes. The format of the executable file is described in Table 5.

Table 13: Karma executable file format

Bytes	Contents		
015	ASCII string "ThisIsKarmaExec"		
1619	Program code size		
2023	Program constants size		
2831	Address of the first instruction		
3235	Initial stack pointer value		
3639	ID of the target processor		
512	Code segment		
	Constants segment		

Notes:

- The ASCII string at the beginning of the executable file contains 15 explicit characters and an implicit '\0' at the end
- The code, constants and data segments sizes are denoted in bytes (as opposed to in machine words)
- The execution of the program starts from the instruction whose address is specified in the executable file header. This is the initial value of the r15 register
- The header also specifies the initial stack head address This is the initial value of the r14 register
- Currently a Karma executable file can run on only one processor that with ID 239
- The code, constants and data segments are loaded into the Karma computer consecutively, starting from the very first memory cell (i.e. the one with the 0 address)

4 Code samples

4.1 Hello world!

```
hello_world:
                                       # define the string to print
     string "Hello, world!\n"
main:
                                       # load the address of the string to r0
     la r0 hello_world
                                       # a while loop
     loop:
          loadr r1 r0 0
                                      # load the current character of the string into r1
                                      \# check if the current character is '\0'
          cmpi r1 0
          jeg out
                                      # if we have encountered the '\0' character, break the cycle
                                      # print the current character from r1 to stdout
          syscall r1 105
                                      # proceed to the next character
          addi r0 1
                                      # continue the loop
          jmp loop
                                      # out of the while loop
     out:
          lc r0 0
                                       # clear r0
                                      \# exit the program with code 0
          syscall r0 0
                                      # start execution from label main
end main
```

4.2 Calculate the square of a number without functions

```
main:
     syscall r0 100
                                      # read an integer from stdin to r0
     mov r2 r0 0
                                      \# copy from r0 to r2
                                      # a pair of registers (r0, r1) contains the square
    mul r0 r2 0
                                      # print from r0 to stdout (i.e. the lower bits)
     syscall r0 102
     lc r0 10
                                      # store the constant 10 ('\n') to r0
     syscall r0 105
                                      # print '\n' from r0 to stdout
     lc r0 0
                                      # clear r0
                                      # exit the program with code 0
     syscall r0 0
                                      # start execution from label main
end main
```

4.3 Calculate the square of a number with functions

```
# a function calculating the square with one argument on the stack
sqr:
                                      # load the first (and only) argument to r0
     loadr r0 r14 2
                                      # copy from r0 to r2
     mov r2 r0 0
    mul r0 r2 0
                                      # a pair of registers (r0, r1) contains the square
                                      \# return from function and remove the argument from the stack
     ret 1
intout:
                                      \# a function printing its argument and '\n'
     load r0 r14 1
                                      # load the first (and only) argument to r0
     syscall r0 102
                                      # print r0 to stdout
     lc r0 10
                                      # store the constant 10 ('\n') to r0
                                      # print '\n' from r0 to stdout
     syscall r0 105
                                      # return from function and remove the argument from the stack
     ret 1
main:
     syscall r0 100
                                      # read an integer from stdin to r0
                                      # put r0+0 to the stack as the sqr argument
     push r0 0
                                      # call sqr, the function will put the result to r0
     calli sqr
     push r0 0
                                      # prepare the result of sqr to be passed to intout
     calli intout
                                      # call intout with the prepared argument
     lc r0 0
                                      # clear r0
                                      # exit the program with code 0
     syscall r0 0
end main
                                      # start execution from label main
```

4.4 Calculate the factorial of a number using a loop

```
\# a non-recursive function calculating the factorial of its argument
fact:
     loadr r0 r14 2
                                       # load the first (and only) argument to r0
     mov r2 r0 0
                                      \# copy the argument to r2
     lc r0 1
                                       \# initialise the result with 1
                                       # a while loop
     loop:
                                      \# compare r2 to 1
          cmpi r2 1
          jle out
                                      # if the next factor is less or equal to 1, break the cycle
                                      # multiply the current result by the next factor
          mul r0 r2 0
          subi r2 1
                                      # decrement r2 by 1
                                      # continue the loop
          jmp loop
                                       # out of the while loop
     out:
                                       # return from function and remove the argument from the stack
          ret 1
main:
     syscall r0 100
                                      # read an integer from stdin to r0
                                      # put r0+0 to the stack as the fact argument
     push r0 0
                                      # call fact, the function will put the result to r0
     calli fact
                                      # print r0 to stdout
     syscall r0 102
     lc r0 10
                                      # store the constant 10 ('\n') to r0
     syscall r0 105
                                      # print '\n' from r0 to stdout
     lc r0 0
                                      # clear r0
                                       # exit the program with code 0
     syscall r0 0
                                      # start execution from label main
end main
```

4.5 Calculate the factorial of a number using recursion

```
fact:
                                       # a recursive function calculating the factorial of its argument
     loadr r0 r14 2
                                       # load the first (and only) argument to r0
     cmpi r0 1
                                       \# compare r0 to 1
                                       # if the argument is greater that 1, recurse
     jg skip0
                                       # else store 1 (the result for this case, 1! = 1) to r0
     lc r0 1
     ret 1
                                       # return from function and remove the argument from the stack
skip0:
                                       \# a supplemental function providing recursion
     push r0 0
                                       # push the current value to the stack (\star)
     subi r0 1
                                       # decrement the current value by 1
     push r0 0
                                       # push the decremented value to stack as the fact argument
                                       # r0 contains the result for the decremented value
     calli fact
                                       # pop the value stored during the (\star) push to r2
     pop r2 0
                                       # multiply the result for the decremented value by the current value
     mul r0 r2 0
                                       \# return from function and remove the argument from the stack
     ret 1
main:
     syscall r0 100
                                       # read an integer from stdin to r0
                                       # put r0+0 to the stack as the fact argument
     push r0 0
     calli fact
                                       # call fact, the function will put the result to r0
     syscall r0 102
                                       # print r0 to stdout
     lc r0 10
                                       # store the constant 10 ('\n') to r0
     syscall r0 105
                                       # print '\n' from r0 to stdout
                                       # clear r0
     lc r0 0
                                       \# exit the program with code 0
     syscall r0 0
                                       # start execution from label main
end main
```