



# **Deep Learning for Detecting Amphoras in Ancient Shipwrecks**

by

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Bachelor Thesis in Computer Science

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# 1 Introduction

## 1.1 Motivation

### 1.1.1 Relevance of Amphoras

The name *amphora* is derived from the Greek word *amphoreus*, which literally means "two-handled" [1, 2]. It is the combination of two linguistic roots: *amphi* (on both sides) and *phoreus* (bearer) [1, 2]. Amphoras (or amphorae) were commercially used from 1500 B.C.E. to 500 C.E. to ship products throughout the Mediterranean, supplying the ancient Greek and Roman empires [2]. Amphoras were designed to ship large quantities of liquid (wine, olives, and oils) and dry products (grain, nuts, and salted fish) [2].

Like many measures that are named after the packages, amphoras were also a semi-standard unit of liquid measure [2]. A cargo ship's capacity was measured by the number of amphoras it could carry instead of by weight [2, 3].

The structurally strong egg-like shape and the high volume-to-weight ratio made amphoras very efficient packages [2]. Amphoras were by far the most common cargo type in Mediterranean shipwreck analysis; more than half of the ships only carried amphoras [2, 4].

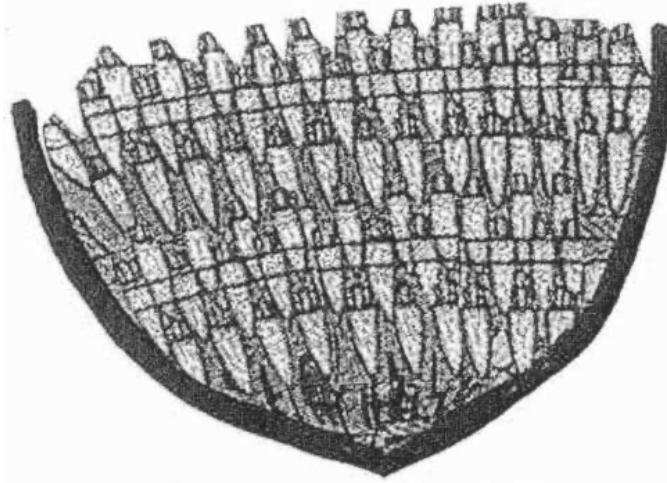


Figure 1: The egg-like shape enabled amphoras to interlock and minimize the waste of space on a ship. Source: [2].

Amphoras' various shapes and markings - which changed by time, region, producer, contents, and brand identity - were used to identify the package status and the different products inside [2].

Amphoras have great significance in archaeology. They can be used as evidence for the trade patterns throughout the Mediterranean [2]. As they were usually discarded at the destination of a trade and have been found in shipwrecks, archaeologists have been using them to recreate the transit routes [2]. Furthermore, researchers have been able to classify different amphoras, which also helps to date ruins and shipwrecks [2].



Figure 2: Amphoras have various shapes. Source: [5].

### 1.1.2 Computer Vision for Underwater Archaeology

Computer vision is the science of perceiving and understanding the world through images and videos [6]. There have been multiple exciting applications of computer vision, including image classification [7], object detection and localization [8, 9], art generation (neural style transfer) [10], image creation with Generative Artificial Networks (GAN) [11], face recognition [12], action and activity recognition [13], human pose estimation [14], and image recommendation system [15].

However, there is still limited research for the application of computer vision and machine learning in archaeology, especially underwater archaeology, compared to other domains [16, 17]. Computer vision, instead of visual inspection, could be used to automate the detection, assessment, and classification of artifacts [16].

Underwater computer vision has proven to be challenging, largely due to: 1) the distortion and attenuation caused by light propagation in water, 2) the unrestricted natural environment with the abundance of marine life and suspended particles, and 3) underwater objects are often broken [17, 18, 19, 20].

Despite the challenges, computer vision has lower cost [18] compared to sonar imagery [21] and laser scanning [22]. Plus, the increasingly abundant visual data obtained through autonomous underwater vehicles (AUVs), unmanned underwater vehicles (UUVs) [19, 23], and seafloor cabled observatories [17] enables us to utilize deep learning.

Furthermore, the research for deep-water shipwrecks is even more limited, mostly due to the lack of information and accessibility [24]. However, the need to study deep-water sites are in high demand, as the threats to these sites are increasing [24]. One major threat is the new forms of trawling that destroy the surface of these sites and interfere with the readability [24]. This means that many shipwrecks are likely to be damaged before they

can be studied [24]. It is thus crucial to implement efficient, accessible, and accurate techniques like deep learning based computer vision to study deep-water shipwrecks.

## 1.2 Deep Learning

Machine learning is the class of algorithms that allow computers to learn and improve from data instead of being explicitly programmed [25, 26]. And deep learning is the subfield of machine learning that builds artificial neural networks with more than one layer between the input and output layers [26, 27, 28]. Deep learning constructs complex representations by combining simpler ones from the previous layers [29].

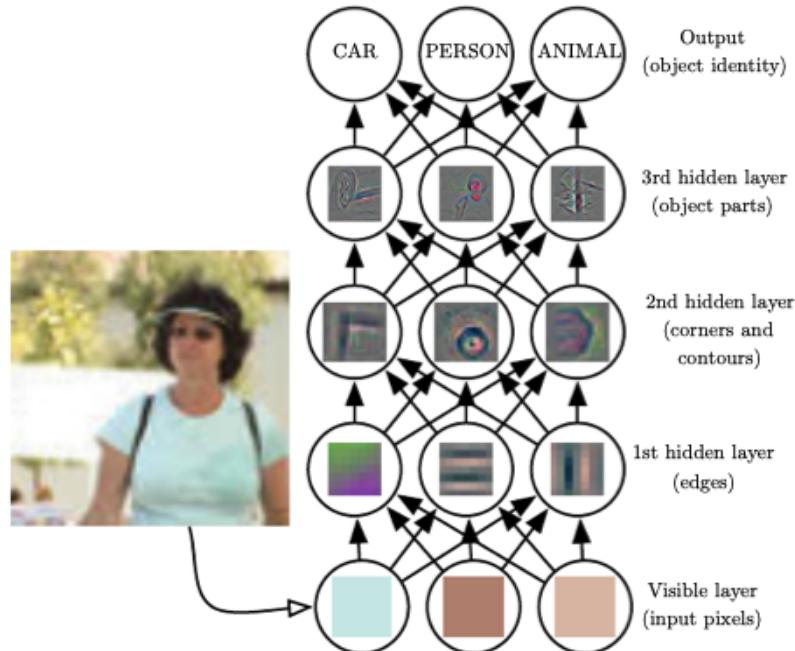


Figure 3: A deep learning system that learns the representations of a person. This is achieved by combining simpler features like corners and contours, which are further expressed by combining simpler features like edges.  
Source: [29].

### 1.2.1 Artifical Neural Networks (ANNs)

Inspired by the biological neuron, artificial neural networks (ANNs) were first introduced in 1943 using propositional logic [30]. The artificial neuron activates its single binary output when the number of active binary inputs reaches the activation threshold, which enables us to build networks that can perform any logical computation [26, 30].

Then the Perceptron was introduced in 1957, which is based on a different artificial neuron called threshold logic unit (TLU) or linear threshold unit (LTU) [31]. The inputs and outputs are numbers instead of binary values, and each input has a weight. TLU computes the weighted sum of the inputs and then applies a step function like the Heaviside

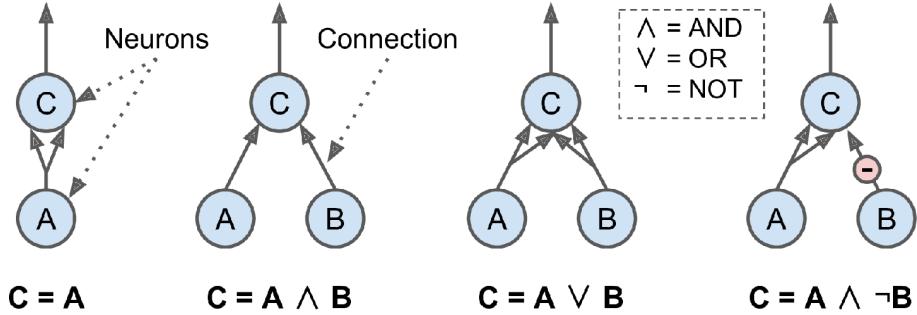


Figure 4: ANNs performing logical computations with the activation threshold of 2. Source: [26].

$$\text{function } \text{heaviside}(x) = \begin{cases} 0 & x \leq 0 \\ 1 & x \geq 0 \end{cases} \quad [26, 31].$$

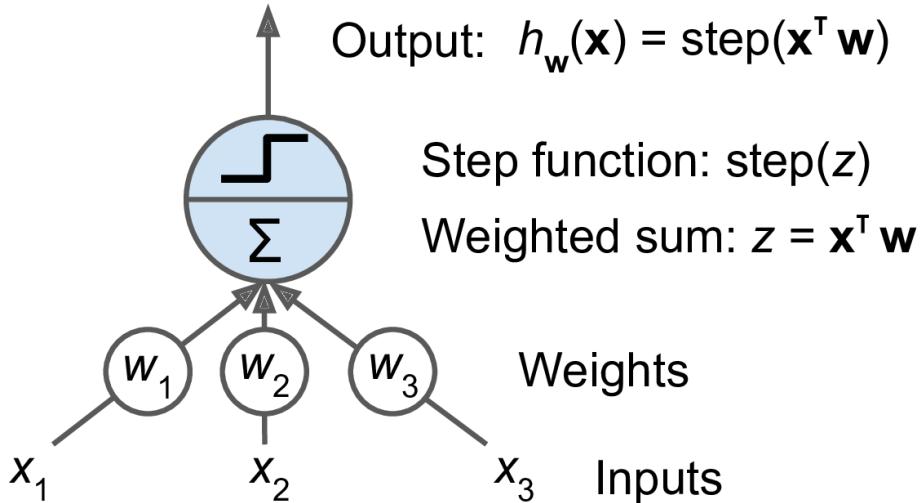


Figure 5: Threshold logic unit. Source: [26].

A single TLU can be used for simple linear binary classification, while a layer of TLUs plus a bias neuron form a Perceptron capable of multi-output classification [26].

The outputs of a fully connected layer is computed as follows, where  $\mathbf{X}$ ,  $\mathbf{W}$ ,  $\mathbf{b}$ , and  $\phi$  are respectively the input matrix, weight matrix, bias vector, and activation function:

$$h_{\mathbf{W}, \mathbf{b}}(\mathbf{X}) = \phi(\mathbf{X}\mathbf{W} + \mathbf{b})$$

The Perceptron is trained using a variant of the Herbb's rule [32], which is famously summarized as "neurons wire together if they fire together [33]" [26]. However, the Perceptron can not learn complex patterns due the linear decision boundary of the output neurons, and it can only make predictions based on a hard threshold instead of outputting a class probability [26]. To address these limitations, the Multilayer Perceptron (MLP) was introduced by stacking multiple Perceptrons.

Backpropagation [34] is used to train the MLP, which first makes a prediction and measures the error in the forward pass, then measures the error contribution from each connection in the reverse pass, and finally tweaks the connection weights to reduce the error.

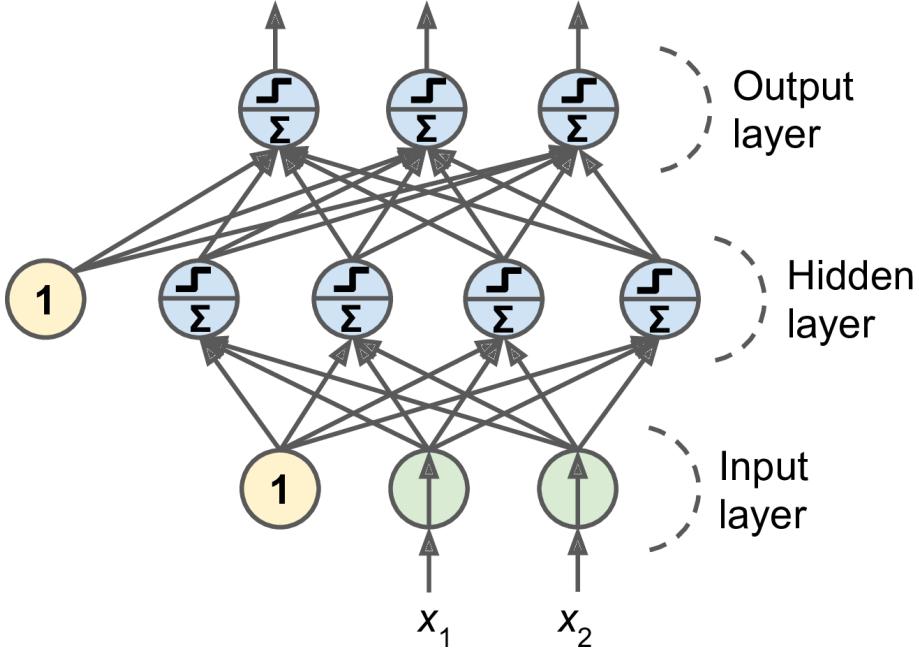


Figure 6: A Multilayer Perceptron with one hidden layer. Source: [26].

error in the Gradient Descent [35] step [26]. Activation functions like Rectified Linear Unit  $ReLU(x) = \max(0, x)$  are used to add nonlinearity, which theoretically gives a large enough deep neural network the ability to approximate any continuous function [26].

### 1.2.2 Convolutional Neural Networks (CNNs)

Convolutional Neural Networks (CNNs) were inspired by the brain's visual cortex, and they have been used in computer vision since the 1980s [26]. We can not simply use a deep neural network with fully connected layers for computer vision, as it breaks down for large images due to the huge number of parameters it requires [26]. CNNs also have successful applications in other domains like recommender systems [36] and natural language processing (NLP) [37].

Hubel et al. [38, 39, 40] found that many biological neurons have a small receptive field, which means they only react to visual stimuli in a limited region of the visual field [26]. Some neurons only react to horizontal lines, while others only react to lines with different orientations [26]. Some neurons have larger receptive fields, and they react to more complex patterns formed by lower-level patterns [26].

Neurons in the first convolutional layer are only connected to pixels in their receptive fields, and neurons in the second convolutional layer are only connected to the neurons in a small receptive field in the first layer [26]. This allows the CNN to concentrate on lower-level features in the first hidden layer, then combine them into higher-level features in the second hidden layer, and so on [26].

The filters or convolution kernels, which are learned during training, are neurons' weights that can be presented as small images the size of receptive fields [26]. For example, a black square with a horizontal white line in the middle (a matrix full of 0s except for the central row with 1s) is a filter that only reacts to the central row in the receptive field. A



Figure 7: CNN layers with rectangular receptive fields. Source: [26].

layer of neurons with the same filter outputs a feature map, which highlights the parts of an image that activate the filter the most [26].

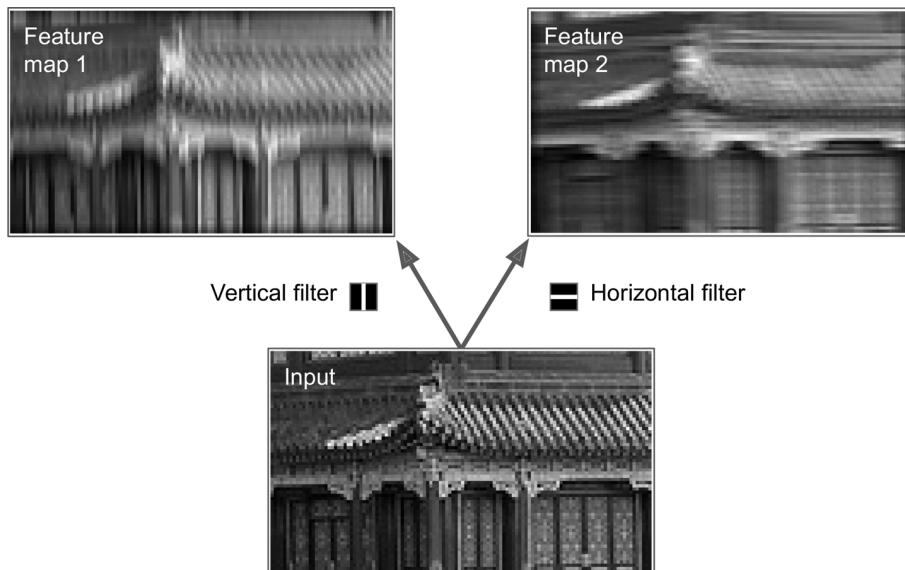


Figure 8: Two feature maps obtained by applying two different filters. Source: [26].

The pooling layers subsample (i.e. shrink) the input image to reduce the computational load and the number of parameters, which also reduces overfitting [26]. Plus, pool layers can bring some invariance to small translations, rotations, and scaling [26].

The typical CNN architecture involves the aforementioned convolutional layers, pooling layers, and fully connected layers. Some well-established CNN architectures are LeNet-5 [41], AlexNet [42], GoogLeNet [43], VGGNet [44], ResNet (Residual Network) [45], Xception (Extreme Inception) [46], MobileNet [47, 48], and SENet (Squeeze-and-Excitation Network) [49].



Figure 9: A max pooling layer with a  $2 \times 2$  kernel and stride 2. Only the max value from each receptive field gets passed to the next layer. Source: [26].



Figure 10: Max pooling layer's invariance to small translations. Source: [26].

Here we give ResNet a more in-depth introduction, as it's the backbone network of the model we use to detect amphoras. Resnet adds skip connections (or shortcut connections), which means the input signal of a layer is also added to the ouput of a higher up layer [26, 45]. Skip connections help speed up the training considerably, since: 1) the network preconditions the problem to be the identify function, which is often close to the target function, and 2) the network can start making progress even if some layers have not started learning yet [26, 45]. Batch normalization [50] is used after each convolution, which zero-centers and normalizes each input to reduce the vanishing gradient problem [51] and the need for other regularization techniques like dropout [52] [26, 45]. The global average pooling layer at the end of the network is another type of pooling layer that gets the mean of the entire feature map [26, 45]. Softmax is used in the output layer to ensure that all probabilities add up to 1 [26, 45].



Figure 11: The typical CNN architecuture. Source: [26].



Figure 12: ResNet architecture. Source: [26].

### 1.3 Deep Learning vs. Traditional Computer Vision

The increasingly abundant visual data and the improvements of deep learning algorithms, computing power, and image resolution have enabled deep learning to achieve state-of-the-art performance in many computer vision tasks, including image classification, object detection, and semantic segmentation [17, 53, 54].

Traditionally, computer vision requires the manual feature selection and engineering step, which relies on domain knowledge to produce high-quality features [6, 8, 54]. These handcrafted features are further procesed by a machine learning classifier like a support vector machine (SVM) [6, 8, 54]. However, manual feature extraction becomes more and more complex as the number of classes increases [54]. Besides, conventional machine learning algorithms' ability to generalize saturates quickly as the size of training data grows [17].

In deep learning, the manual feature extraction step is no longer needed, and neural networks can be trained end-to-end as a feature extractor plus a classifier [6, 54]. Thus, deep learning requires less domain knowledge, it and provides more flexibility as the models can be re-trained with a custom dataset for any specific use case [54].

However, deep learning does not make traditional computer vision obsolete. Techniques like Scale Invariant Feature Transform (SIFT) [55], Speeded Up Robust Features (SURF) [56], and Features from Accelerated Segment Test (FAST) [57] are still useful in improving performance for computer vision tasks [54]. And deep learning's performance depends

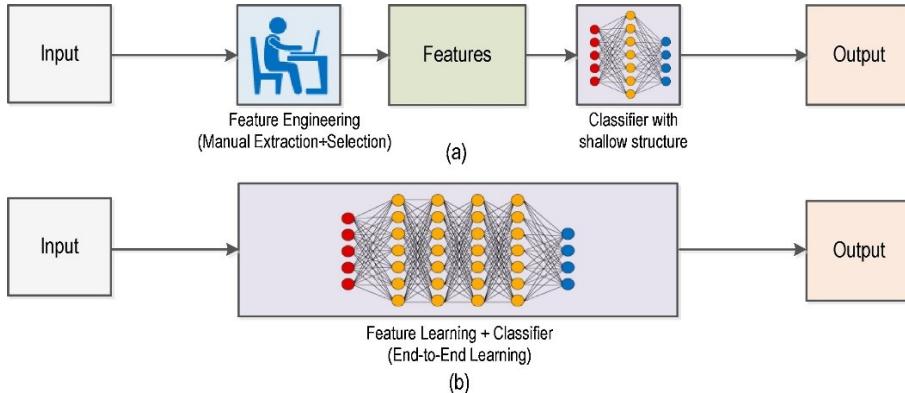


Figure 13: (a) Traditional computer vision workflow. (b) Deep learning workflow. Source: [54].

on obtaining large datasets with high image resolution [54]. Some popular public datasets like PASCAL Visual Object Classes (VOC) [58], ImageNet [59], and Microsoft Common Objects in Context (COCO) [60] have respectively 500 thousand, 14 million, and 328 thousand images.

## 1.4 Object Detection

Object detection is the computer vision task that localizes and classifies objects in an image [6, 8, 9, 26]. Object detection remains to be one of the most challenging problems in computer vision, as it can be considered as both a regression task (localization by predicting the bounding box) and a classification task (predicting the object class in each bounding box) [6, 61, 26]. Plus, the large variations in viewpoints, poses, occlusions, and lighting conditions make it even more difficult to perform perfect object detection [8, 9].

The traditional sliding window approach is to train a CNN to classify and locate a single object, and then slide it across the image [26, 62, 61, 63]. This approach slides the CNN multiple times with different window sizes to detect objects with various sizes, which causes it to be quite slow [26].

Luckily, many object detection frameworks based on fully convolutional network (FCN) [64] have been introduced. FCNs contain only convolutional layers and pooling layers and only need to process each image once, which means they are faster and the input images can have arbitrary sizes [6, 26, 64]. Here we summarize three well-established and influential object detection framework families: Region-Based Convolutional Neural Networks (R-CNN) [61, 65, 66], Single Shot Detector (SSD) [67], and You Only Look Once (YOLO) [63, 68, 69, 70, 71].

### 1.4.1 General Object Detection Framework Components

Before we dive into specific object detection frameworks, it's worth understanding the four high-level components of general object detection frameworks [6].



Figure 14: The sliding window approach for object detection. Source: [54].

**Region Proposal** The region proposal algorithm finds regions of interest (RoIs) that are further processed by the framework by discarding regions with low objectness score [6]. The objectness score indicates the probability of the region containing an object instead of the background, and it is the class probability for a single-class object detection task [6].

**Network Predictions** A pretrained CNN is used as the backbone for feature extraction and makes the bounding-box prediction and class prediction for each region [6]. The bounding-box prediction is the tuple  $(x, y, w, h)$ , where  $x$  and  $y$  are the coordinates of the center and  $w, h$  are the width and the height [6].

**Non-Maximum Suppression (NMS)** The backbone network typically produces multiple overlapping bounding boxes for one object, thus NMS finds the box with the maximum class probability and suppresses the rest [6]. The steps include [6]:

1. Discard boxes with predictions less than the tunable confidence threshold.
2. Select the box with the highest probability.
3. Compute the overlap - intersection over union (IoU) - of the boxes that have the same class prediction. Boxes with high IoU are averaged together.
4. Suppress boxes with an IoU less than the tunable NMS threshold.

**Metrics** The two main metrics for object detection are frames per second (FPS) and mean average precision (mAP) [6, 9, 26, 72]. To understand mAP, we need to understand first the aforementioned intersection over union (IoU) and the precision-recall curve (PR



Figure 15: NMS. Source: [6].

curve). The IoU is also known as the Jaccard index, which is used to measure similarity between two sets [72]. The IoU can be mathematically formulated as follows [6, 72]:

$$IoU = \frac{B_{ground\ truth} \cap B_{prediction}}{B_{ground\ truth} \cup B_{prediction}}$$



Figure 16: IOU. Source: [6].

We say that the prediction is a true positive (TP) if the predicted class is the same as the ground truth and the IoU value is more than the tunable threshold, otherwise it is a false positive (FP) [9, 6, 72]. A false negative (FN) is a ground truth that does not have a prediction [72]. Then we can define precision and recall as follows [27, 73]:

$$Precision = \frac{TP}{TP + FP}$$

$$Recall = \frac{TP}{TP + FN}$$

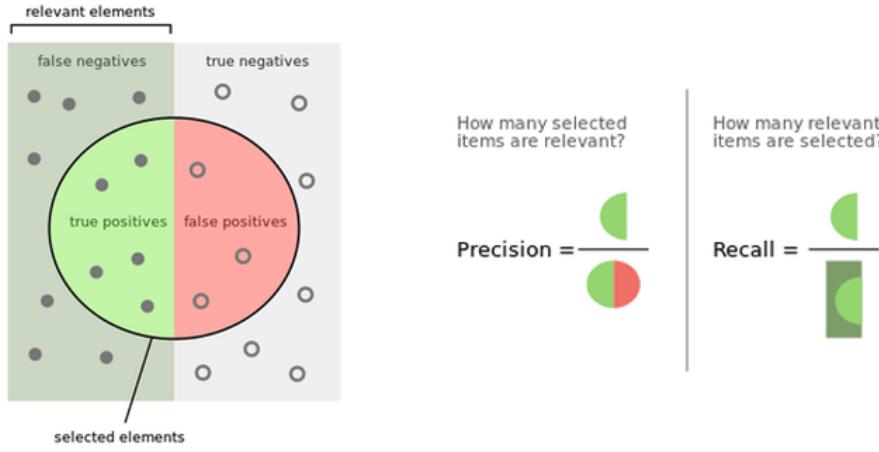


Figure 17: Precision and recall. Source: [74].

There is a trade-off between precision and recall [6, 26, 27, 72]. We can obtain the average precision (AP) by drawing the precision-recall curve (PR curve) and computing the area under the curve (AUC) [6, 72]. Finally, we get the mean average precision (mAP) by averaging the AP over all the classes [6, 26, 72]. The traditional Pascal VOC metric uses mAP@0.5, which means the IOU threshold is 0.5 [9, 58, 72]. The new MS COCO metric  $mAP_{coco} = mAP@[0.50 : 0.05 : 0.95]$  is averaged with different IOU thresholds from 0.5 to 0.95 in steps of 0.05, which rewards detectors with better localization [9, 72, 75]. Note that AP is sometimes used in the COCO metric to implicitly mean mAP, although we use mAP here consistently in this paper [75]. MS COCO also introduces mAP for different scales:  $mAP^{small}$  for small objects with area smaller than  $32^2$  pixels,  $mAP^{medium}$  for medium objects with area bigger than than  $32^2$  pixels and smaller than  $96^2$  pixels, and  $mAP^{big}$  for big objects with area bigger than  $96^2$  pixels [9, 75].

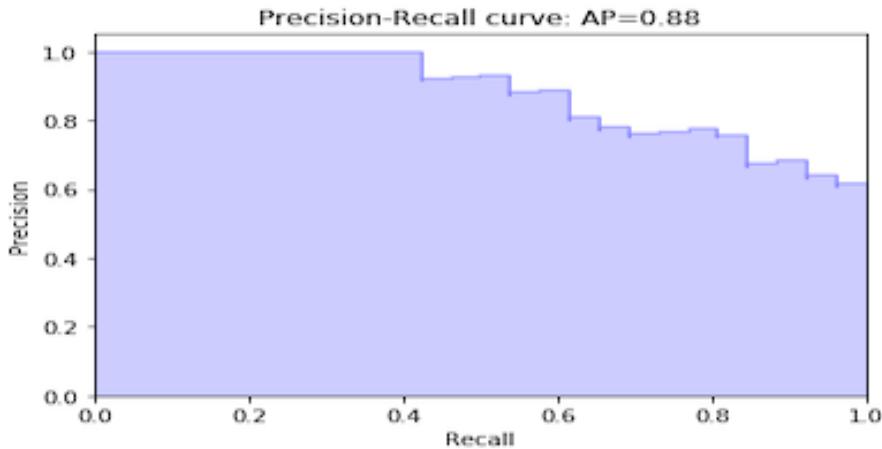


Figure 18: A PR curve with 0.88 AUC. Source: [72].

#### 1.4.2 Region-Based Convolutional Neural Networks (R-CNN)

The evolution from the original R-CNN [61] to Fast R-CNN [65] and then to Faster R-CNN [66] builds up the R-CNN family.

**R-CNN** R-CNN has four components [6, 61]:

1. Region proposal with a greedy search algorithm called selective search, which finds RoIs by combining similar pixels into boxes.
2. Feature extractor with a pretrained CNN.
3. Classification with a linear SVM.
4. Localization with a bounding-box regressor.



Figure 19: R-CNN. Source: [6].

R-CNN has the following disadvantages [6, 61, 65]:

- The FPS is very low. The selective search algorithm proposes about 2000 RoIs, which is very computationally expensive as the CNN has to process each proposal separately.
- The training is multi-stage, inelegant, expensive, and not end-to-end. It involves training three components separately: the CNN, the SVM, and the bounding-box regressor.

**Fast R-CNN** Fast R-CNN makes the following changes from R-CNN [6, 65]:

- The CNN goes before region proposal instead of after, so that the image only goes through the CNN once instead of 2000 RoIs going through the CNN separately.
- Classification is done by the softmax layer of the CNN instead of the SVM. And localization is also an output layer of the CNN.
- A RoI max pooling layer is added after region proposal to fix the input size for the fully connected layers.
- A multi-task loss function is used.

Fast R-CNN is much faster than R-CNN, although the selective search algorithm still exists as the bottleneck [6, 65, 66].

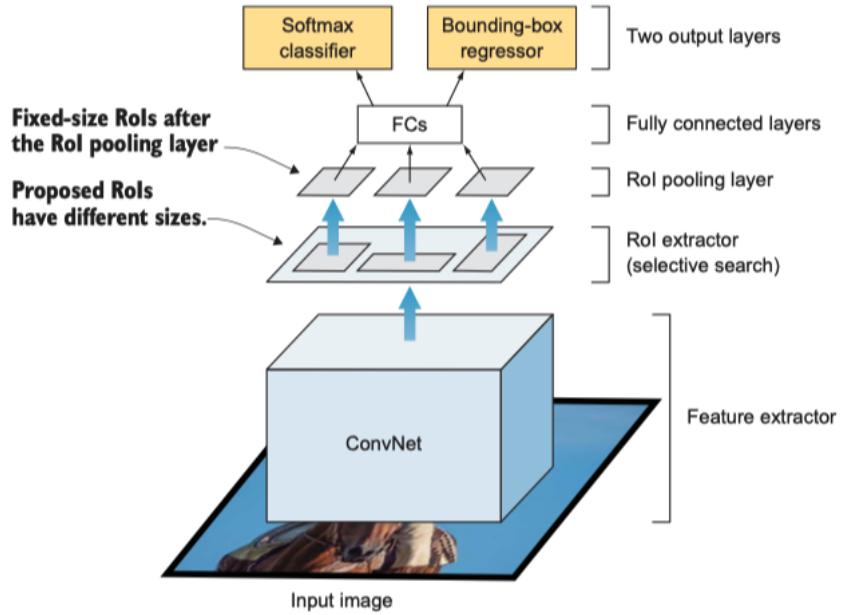


Figure 20: Fast R-CNN. Source: [6].

**Faster R-CNN** Faster R-CNN makes the following improvements from Fast R-CNN [6, 66]:

- Region Proposal Network (RPN) or attention network replaces selective search, which reduces the number of proposals, speeds up the model, and makes the model training end-to-end. RPN is a FCN that outputs objectness scores and RoIs, and it can be used as a standalone network for single-class object detection. It also shares the features with the detection network, which enables region proposal to be nearly cost-free.
- Anchors are introduced as reference boxes at different scales and aspect ratios. Thus the regression layer only needs to output the offsets of coordinates, width, and height from the anchors. The anchors are created using the sliding-window approach. By default 9 anchors (3 scales and 3 aspect ratios) centered at each sliding window are created for each window.

To summarize, the R-CNN family are two-stage detectors that separate region proposal and detection [6]. They can not achieve real-time detection (only 7 FPS), and they are too computationally intensive [6, 67, 63]. One-stage detectors like Single Shot Detector (SSD) and You Only Look Once (YOLO) skip the region proposal to achieve real-time detection speed [6]. In general, one-stage detectors sacrifices some accuracy for speed [6, 76].

#### 1.4.3 Single Shot Detector (SSD)

Single Shot Detector (SSD) makes both the objectness and class probability predictions directly in one shot [6, 67]. It has three main components [6, 67]:

- The base network, which is VGG-16 in the original paper. It also uses anchors called priors like in Faster R-CNN. But the network sends the bounding box offsets

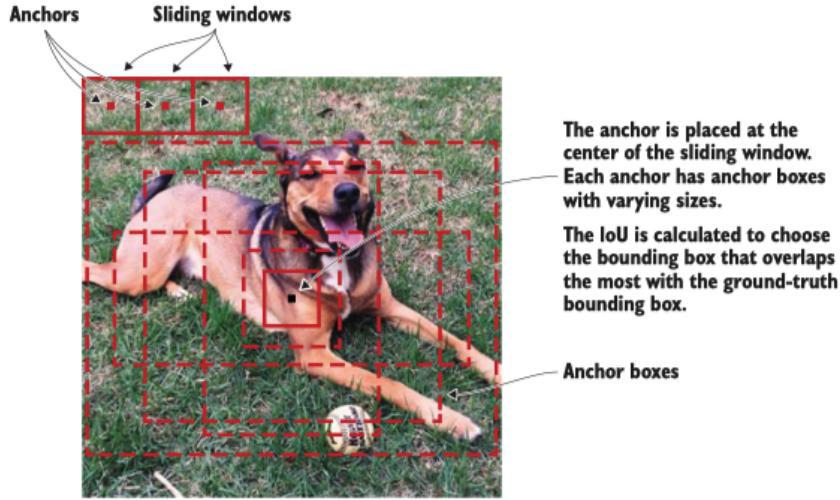


Figure 21: Anchors in Faster R-CNN. Source: [6].

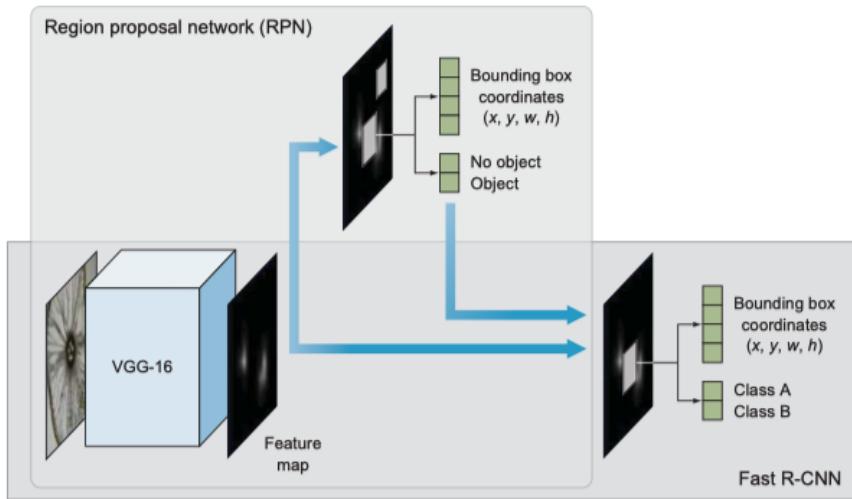


Figure 22: Faster R-CNN. Source: [6].

and the class scores to NMS directly when it finds a bounding box that contains the object features.

- Multi-scale feature layers, which are convolutional layers that decrease in size progressively to detect objects at multiple scales. The resolution of feature maps decreases as the CNN reduces the spatial dimension.
- NMS.

In short, SSD300 (300 x 300 input size) is able to achieve real-time detection with 59 FPS, while SSD512 outperforms Faster R-CNN in terms of mAP [67].

#### 1.4.4 You Only Look Once (YOLO)

Like the R-CNN family, the YOLO family has been going through a series of improvements since the original YOLO paper was published. YOLO is also a one-stage real-time

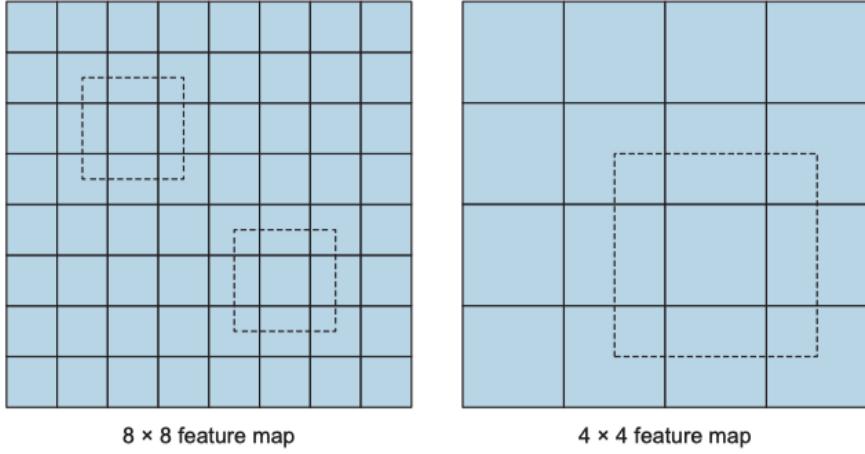


Figure 23: Multi-scale feature maps in SSD. Higher-resolution feature maps (left) detect smaller objects. Lower-resolution feature maps (right) detect bigger objects Source: [6].

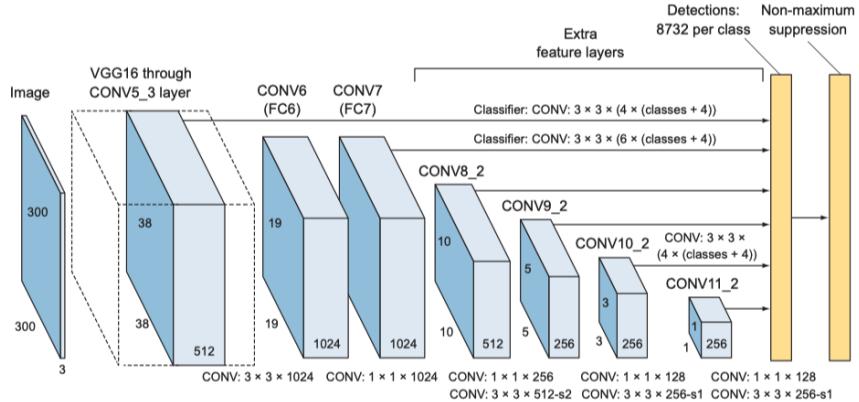


Figure 24: SSD. Source: [6].

detector similar to SSD. YOLOv1 [63] introduces the general architecture; YOLOv2 [68] adds anchors similar to Faster R-CNN and SSD; YOLOv3 [69] further refines the architecture and the training process; YOLOv4 [70] makes use of some universal object detector features called "bag of freebies" and "bag of specials"; YOLOv5 [71] is under active development and authors have yet to publish a paper.

YOLO divides the image into a grid, and a grid cell is responsible for detecting an object if the center of the object is inside the cell [6, 63]. The backbone network is called DarkNet, which is inspired by GoogLeNet [6, 63].

YOLOv4, a bleeding-edge detector introduced in 2020, utilizes numerous new features to improve the performance from YOLOv3, including DropBlock regularization [77], Mish activation [78], Self-Adversarial Training [70], etc.



Figure 25: YOLOv3 architecture. YOLO performs detections at 3 different scales. Layer 79 makes a grid of  $13 \times 13$  to detect large objects. Layer 91 makes a grid of  $26 \times 26$  to detect medium objects. And finally layer 106 makes a grid of  $52 \times 52$  to detect small objects. Source: [6].

## 2 Related Work

As we have mentioned in section 1.1.2, there is limited research on the application of deep learning for underwater archaeology and vision-based underwater object detection in general.

For fish detection, Qin et al. [17, 79], Zhang et al. [80], Villon et al. [81], Xu et al. [82], and Konovalov et al. [83] respectively used Fast R-CNN, a model similar to R-CNN, sliding window with a CNN, YOLOv3, and Xception.

For crab detection, Can et al. [84] proposed a detector called Faster MSSDLite, which is based on SSD with a MobileNetv2 backbone and Feature Pyramid Network (FPN) [85].

For planktons and corals, we have only found research for classification but not object detection [17, 23].

For amphora detection, Pasquet et al. [20, 62] used sliding window with a CNN on high-resolution orthophotos (aerial photos). And this is the only study we have found on amphora detection with deep learning.

## 3 Data and Methods

### 3.1 Data

The dataset consists of 50 images (294 objects) in the training set and 7 images (31 objects) in the validation set, which maintains the 90% : 10% ratio for the object count. Two additional images are used as the test set. All the images are obtained through various sources [86, 87, 88, 89, 90, 91, 92, 93, 94, 95] and are annotated with LabelImg [96].

### 3.2 Model

Out of the three families of obejct detection frameworks we have discussed in section 1.4, SSD is chosen due to the following reasons:

- Faster R-CNN is too computationally intensive and too slow for AUVs and UUVs, which require real-time detection.
- YOLOv5, the state-of-art model of the YOLO family, is under active development and the authors have yet to publish a paper.

The TensorFlow Object Detection API [97, 98] is used to build the model. The model name is `ssd_resnet_50_fpn_coco` in the TensorFlow Detection Model Zoo [99]. The backbone network is changed from VGG-16 in the original SSD paper to ResNet-50 (50-layer ResNet) (see section 1.2.2), as it improves the mAP significantly [45]. Similar to the approach from Can et al. [84] for crab detection, Feature Pyramid Network (FPN) is added to improve the detection at different scales [85].

### 3.3 Model Training

Transfer learning [100] is used as the model is pretrained on the COCO dataset, which means the weights and biases are restored instead of being randomly intialized and the model does not have to learn the low-level features from scratch [26]. `num_classes`, `batch_size`, and `num_examples` in `eval_config` are adjusted to 1, 8, and 7 respectively in the configuration file, while the rest of fields stay unchanged. The images are reshaped to 640 x 640 with the `fixed_shape_resizer`. The activation function is ReLU6, a modified version of ReLU that caps the maximum value at 6 and thus encourages the model to learn sparse features earlier [101]. We use  $L_2$  regularization [102] to reduce overfitting [103]. Data augmentation [26, 42] - a method to artificially enrich the dataset by randomly flipping horizontally and cropping the images - is also used as a regularization technique. We choose the momentum optimizer [104] as it converges faster than Stochastic Gradient Descent [105] by keeping accelerating to the optimum [26]. Learning rate warmup and learning rate scheduling by cosine decay are also added to speed up the convergence, so that the learning rate starts small, increases gradually, and then decreases after reaching the maximum [26, 106, 107, 108]. The model was trained on Google Colaboratory [109] with a GPU runtime, and the training took 2 hours and 40 minutes to reach the peak mAP result at step 8621.

## 4 Evaluation

The main metric  $mAP_{coco}$  (see section 1.4.1) from our model is 0.238, while the traditional  $mAP_{50}$  is 0.503. The documented  $mAP_{coco}$  in the TensorFlow Detection Model Zoo for `ssd_resnet_50_fpn_coco` is 0.35, which is measured on the COCO validation set. Our model’s performance is indeed lower than that in the model zoo. And it is somewhat difficult to perform a direct comparison with the result from Pasquet et al. [62], as they did not compute the  $mAP$  and only mentioned that they detected around 90.3 percent of amphoras. However, we can conclude that our model does not detect more than 90.3 percent based on the visual inspection of the validation images in figure 26.

Nevertheless, our model’s performance is still impressive due to the following reasons:

- Our dataset is very small. As we have mentioned before in section 1.3, the COCO dataset has 328 thousand images compared to our 57 images plus 2 test images. For Pasquet et al., they split one orthophoto (38000 x 15000 pixels) into 400 x 400 images and used 25% of them for training, which means the training set alone is around 890 images.
- Our dataset is a lot more diverse than that of Pasquet et al. Since our dataset images are obtained through numerous sources instead of from a single orthophoto, they reflect better the various shapes of amphoras (see figure 2). Plus, our dataset has both large and medium instances of amphoras that vary significantly in terms of the scale. The diversity of our dataset makes it harder to achieve a high mAP, but it also encourages the model to generalize better.
- Underwater object detection is more challenging than general object detection performed by the COCO dataset. As we have mentioned before in section 1.1.2, the same challenges also apply for amphora detection. In fact, the undetected amphoras in figure 26 are almost all either broken, or partially buried in sand, or blocked by suspended particles. We only define one class for all amphoras even if they are broken, while Pasquet et al. defined 2 separate classes for the head and the body to better detect broken instances.
- Our  $mAP_{50}$  score is in fact comparable with that from Xu et al. [82] for fish detection. They achieved a 0.5392  $mAP_{50}$  using YOLOv3, although they did not use  $mAP_{coco}$ .

We also ran the model on 2 test images shown in figure 27. To our surprise, the model managed to detect the amphora in the second image even though it is so broken that only half of it is present. As for the first image, none of the amphoras was detected as expected. The size of the first image is only 709 x 411, while it has hundreds of amphora instances. This means that they are mostly small instances defined by the COCO metric, which our training set does not include. It is a known issue that small objects are significantly harder to detect than medium and large objects, mainly due to the low resolution and thus the lack of features to learn [110, 111, 112]. Plus, the image can be described as a crowded and densely packed scene, which is also notoriously difficult for object detectors since the objects overlap with each other so strongly that it is even impossible for human experts to differentiate the instances [62, 113, 114, 115]. In fact, we tried to split the image and add parts of it to the training set. However, the inter-occlusion of the instances caused many labeling errors, and the resolution of each instance was so low that the training could not converge to a solution.

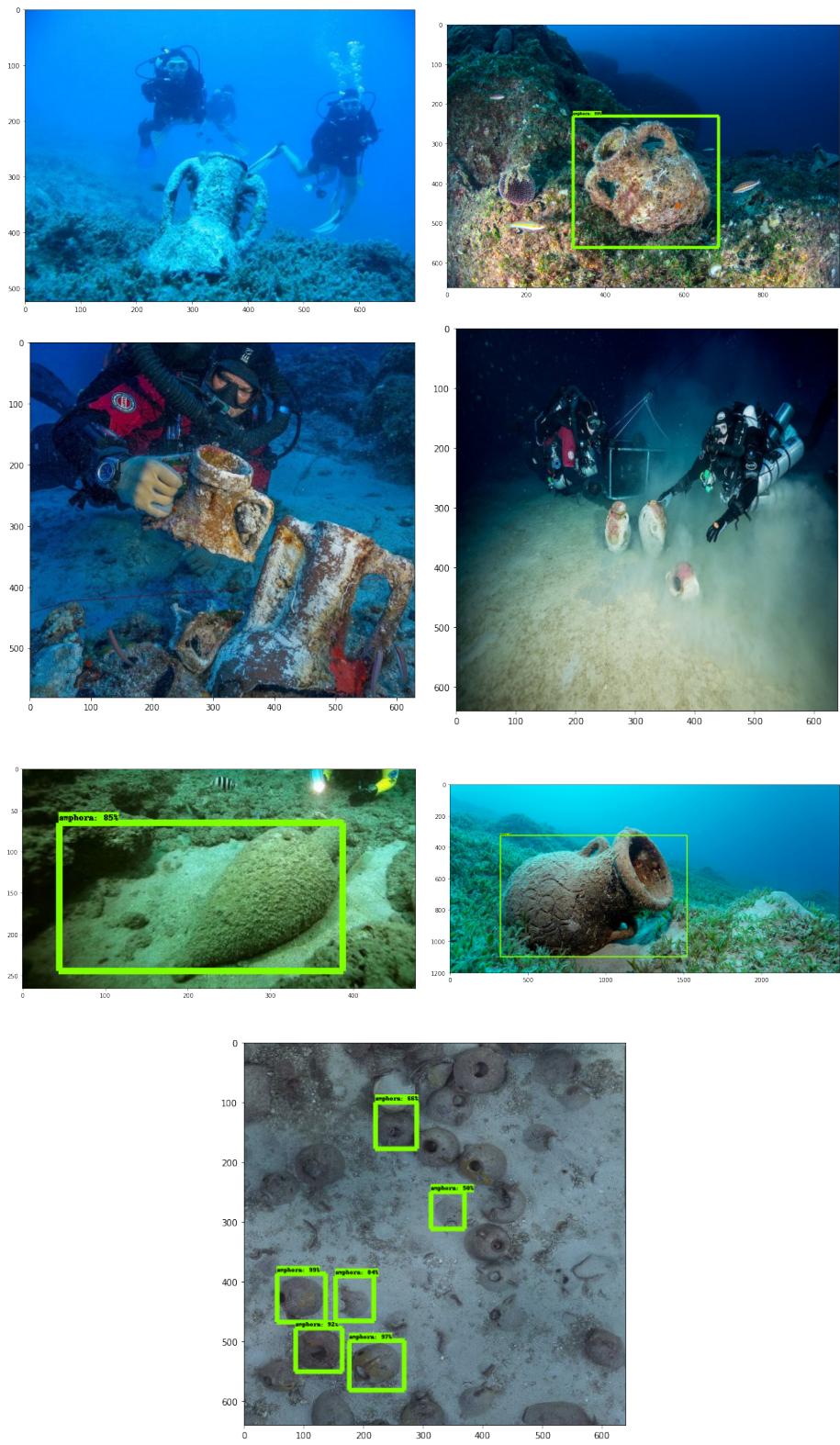


Figure 26: The validation images. Source: [87, 88, 89, 90, 91, 92, 93].

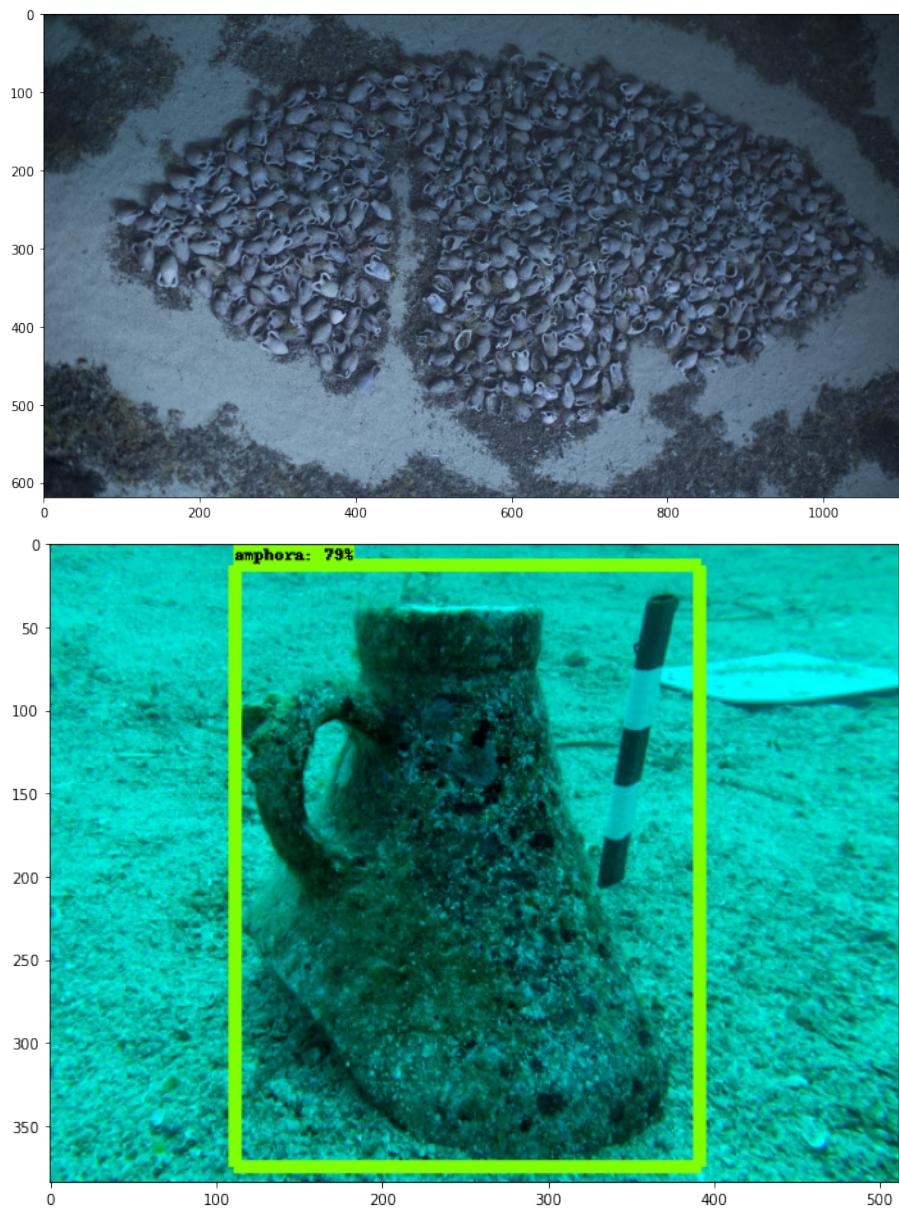


Figure 27: The test images. Source: [94, 95].

## 5 Conclusion and Future Work

In this paper, we have reviewed the relevance of amphoras, computer vision’s potential in underwater archaeology, deep learning, and three major object detector families. We have then trained an SSD model based on a very small and low-resolution dataset, and yet still managed to achieve 0.238 for  $mAP_{coco}$  and 0.5392 for  $mAP_{50}$ . Detecting underwater amphoras is a challenging task, as the object detectors have to overcome the difficulties posed by general underwater object detection (see section 1.1.2), the considerable variations of the shapes of amphoras (see figure 2), and the crowdedness of the scenes in some shipwrecks (see figure 27).

We hope this paper can serve as a proof of concept for future studies, since there are many aspects to improve upon:

- The small number and the low resolution of the images in our dataset are the bottleneck towards a higher performance. There are indeed very limited publicly available high resolution images for underwater amphoras [62]. Future studies may focus on obtaining more amphora images through AUVs and UUVs to improve the  $mAP$  in general. And higher resolution images like orthophotos can especially address the issue of detecting small objects [110]. Plus, more data augmentation techniques like randomly change to grayscale and randomly adjust brightness, contrast, and hue can be easily added in the `data_augmentation_options` from the TensorFlow Object Detection API to potentially further enrich the dataset.

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