

Homework : Answers

$$1. \quad Q = 4K + 6L$$

output capital labor
customers

$$A) \quad 200 = 4 \times 20 + 6 \times 20 = 200$$

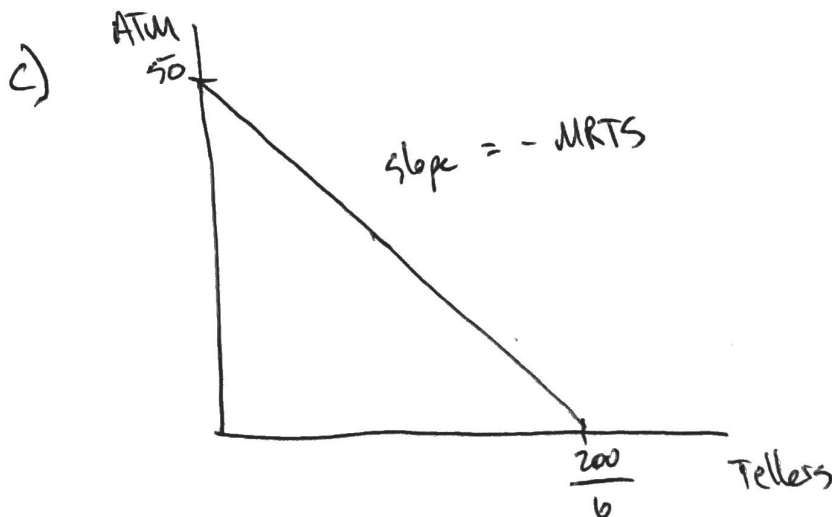
to maintain original service level (200)

$$200 = 4 \cdot 17 + 6 \times L$$

$$\boxed{L = 22}$$

Hire 2 additional tellers

B) No, the trade off between ATMs and tellers is constant : 2 tellers for every 3 ATMs to maintain the same level of service.
They are perfect substitutes



D) Production function is linear relationship
3 ATMs to 2 tellers

E) If the bank lays off 2 workers & installs 3 ATMs
the # of customers served will be unchanged.

The cost of production will change:

$$\begin{array}{ccccccc} P_{\text{ATM}} \cdot \Delta K & + & P_{\text{Teller}} \cdot \Delta L & = & \$20 \times 3 & + & 32 \cdot (-2) \\ \text{change} & & \text{change} & & & & = -4 \end{array}$$

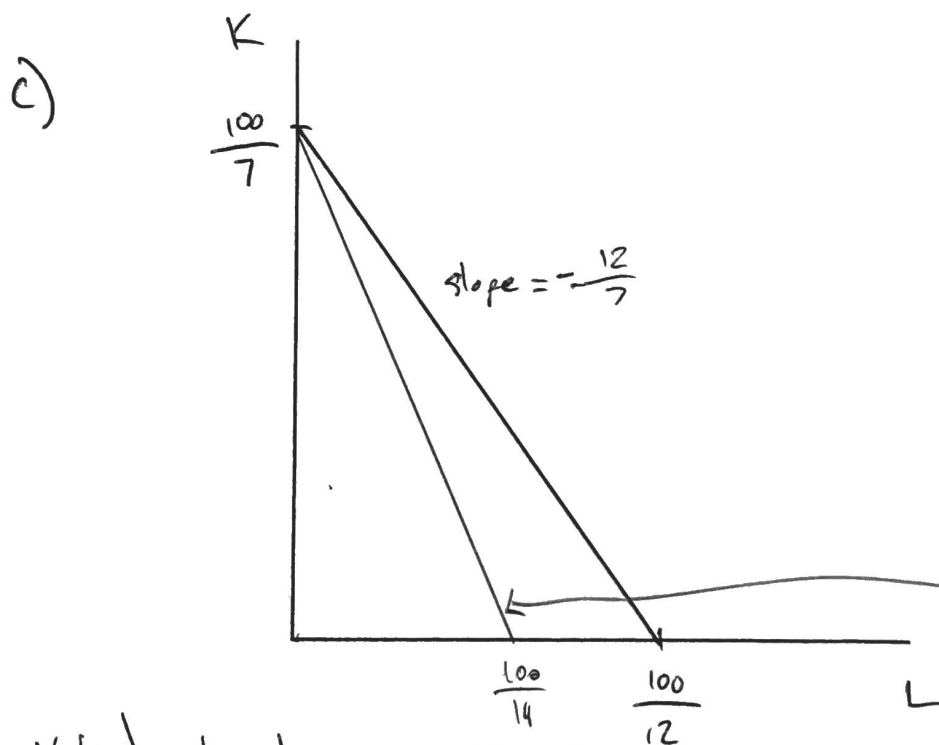
F) To minimize cost the bank should only
use ATMs

2) $w = \$12$ $r = \$7$

A) $\text{Cost} = \$12 \cdot L + \$7K$

B) $100 = \$12L + \$7K$

$$K = \frac{\$100}{\$7} - \frac{\$12}{\$7} L$$



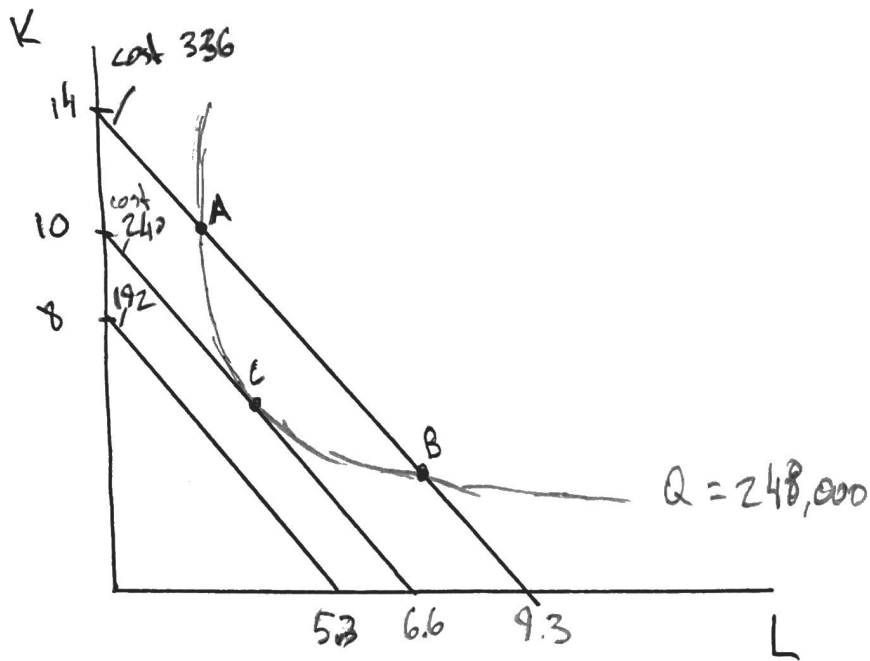
D) Vertical intercept is quantity of capital rented with \$100 and no Labor
 Horizontal intercept is quantity of Labor for \$100 with no capital (machines)

E) Slope is the (negative) ratio of the wage and rental price of capital
 $-\frac{12}{7}$

F)

$$K = \frac{100}{7} - 2L$$

3)



A) When $L = 0$, $K = \frac{\text{cost}}{r}$

$$14 = \frac{\text{cost}}{24} \Rightarrow \text{cost} = 14 \times 24 = 336$$

$$10 = \frac{\text{cost}}{24} \Rightarrow \text{cost} = 10 \times 24 = 240$$

$$8 = \frac{\text{cost}}{24} \Rightarrow \text{cost} = 8 \times 24 = 192$$

B) $K = 0 \rightarrow L = ? = \frac{\text{cost}}{w}$

$$\frac{336}{36} = 9.3$$

$$\frac{240}{36} = 6.6$$

$$\frac{192}{36} = 5.3$$

C) Yes, the firm can make 248,000 units for \$336. This would be at either points A or B.

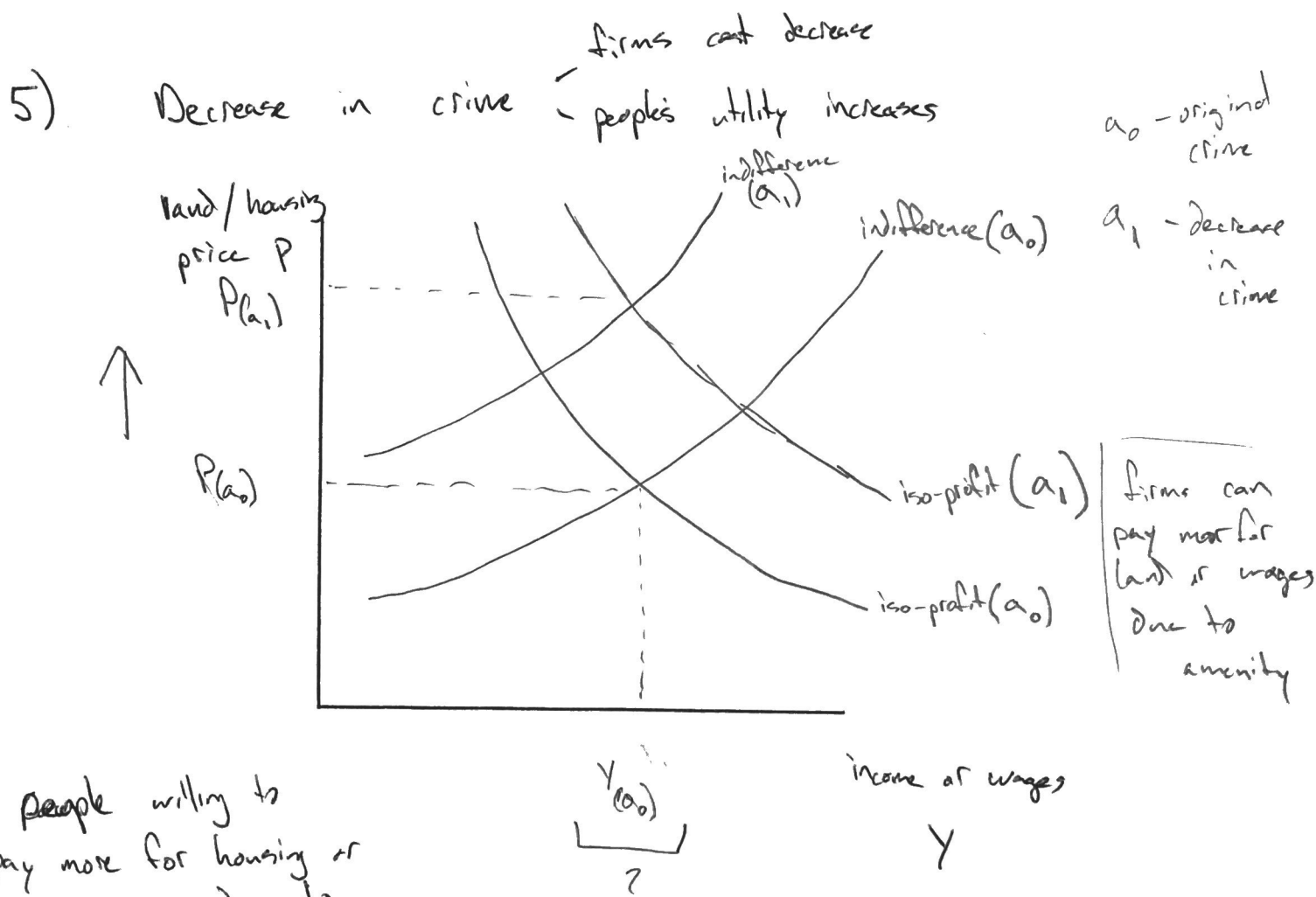
D) Minimum cost for 248,000 units is \$240 at point C.

E) Equimarginal rule

$$\frac{MP_L}{w} = \frac{MP_K}{r}$$

$$\frac{400}{36} = \frac{x}{24} \quad x = 266.\bar{6}$$

- 4) Equilibrium in the Rosen-Roback Model is that people and firms are indifferent across locations in geographic space. For people it means their utility is the same in location A : location B due to the differences in wages, housing prices and amenities.



Overall effect. income or wages depends on the size of the shifts, land prices certainly increase.