

72.5

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Part A: Hash Table Definitions (Conceptual Understanding)

Q1. Define "collision" in the context of hash tables.

A1: 不同的key 經 hash function 得到相同的 index, 造成碰撞
(hash value)

Q2. What is a "bucket" in a hash table?

A2: key $\xrightarrow{\text{hash function}}$ index 映射出 value (存放 value 的地方就是 bucket)
(hash value)

Q3. Define "load factor (α)" and explain why it affects performance.

A3: $\frac{\text{elements 的數量}}{\text{table size}}$, α 越大 element 分部的越集中, 反知亦然

Q4. What is "primary clustering," and which probing method suffers from it?

A4: linear probing
不同key 經 hash function 得到大量相同的 index, 導致 elements 大量堆積在同一處。
(hash value)

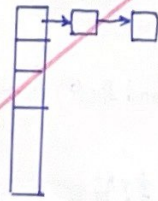
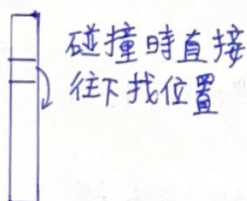
Q5. What is "secondary clustering," and how is it different from primary clustering?

A5: 不同的key 經 hash function 得到大量相同的 index, 導致 elements 大量堆積在同一處。
線性遞增
($\text{hash}(x) + c_i + c_i^2$)
hash function 的不同

Q6. Briefly explain the difference between:

- Open addressing
- Separate chaining

A6:



Part B: Hash Function Calculation (Collision & Pattern Observation)

Show your steps clearly.

Hash Function 1 — Division Method

$$h_1(k) = k \bmod 10$$

Hash Function 2 — Folding Method

Split key into two-digit chunks and sum the chunks.

$$h_2(k) = (\text{sum of 2-digit groups}) \bmod 11$$

Example:

Key = 8429 \rightarrow groups: 84 + 29 \rightarrow 113 \rightarrow 113 mod 11 = 3

Q7. (Compute using Hash Function 1)

Given keys: 27, 37, 47, 57, 67

Compute their hash values using:

$$h_1(k) = k \bmod 10$$

A7:

27, 37, 47, 57, 67
↓ ↓ ↓ ↓ ↓
hash values: 7 7 7 7 7

Q8. (Identify collision pattern)

From your results in Q1:

- What pattern do you observe?
- Explain why these keys collide.

A8: 全部的keys都有相同的hash value ④ 因為全部的keys尾數都是7, 且 mod 又取 10, 造成了所有的keys都碰撞在一起

Q9. (Compute using Hash Function 2)

Compute $h_2(k)$ for: 1234, 9217, 4519, 9902

A9: 1234 \rightarrow (12+34) mod 11 = 2

9217 \rightarrow (92+17) mod 11 = 9

4519 \rightarrow (45+19) mod 11 = 9

9902 \rightarrow (99+02) mod 11 = 2

Q10. (Compare distribution)

- Which hash function (h_1 or h_2) produced more collisions for the input set?
- Which seems to spread keys more evenly?
- Provide 1-2 sentences of explanation.

A10: ① h_1 (27, 37, 47, 57, 67) \rightarrow 碰撞

h_2 (9217, 4519) \rightarrow 碰撞

② h_2

③ ④ mod 取的數不同, 取質數分佈會較分散

② 數的拆分, 也使得keys較分散