

72.5

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Part A: Hash Table Definitions (Conceptual Understanding)

Q1. Define "collision" in the context of hash tables.

A1: 不同的 key 經 hash function 得到相同的 index，造成碰撞
 \downarrow
 (hash value)

Q2. What is a "bucket" in a hash table?

A2: key $\xrightarrow[\text{hash function}]{\downarrow}$ index 映射出 value (存放 value 的地方就是 bucket)
 \downarrow
 (hash value)

Q3. Define "load factor (α)" and explain why it affects performance.

A3: $\frac{\text{elements 的數量}}{\text{table size}}$ ， α 越大 element 分佈的越集中，反之亦然

Q4. What is "primary clustering," and which probing method suffers from it?

A4: 不同 key 經 hash function 得到大量相同的 index，導致 elements 大量堆積在
 同一處。
 \downarrow
 (hash value)

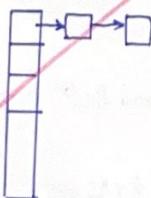
Q5. What is "secondary clustering," and how is it different from primary clustering?

A5: 不同的 key 經 hash function 得到大量相同的 index，導致 elements 大量堆積在
 同一處。
 \downarrow
 線性遞增
 $(\text{hash}(x) + ci + ci^2)$

Q6. Briefly explain the difference between:

- Open addressing
- Separate chaining

A6: 碰撞時直接
 往下找位置



透過 linked list 來解
 決碰撞

Part B: Hash Function Calculation (Collision & Pattern Observation)

Show your steps clearly.

Hash Function 1 — Division Method

$$h_1(k) = k \bmod 10$$

Hash Function 2 — Folding Method

Split key into two-digit chunks and sum the chunks.

$$h_2(k) = (\text{sum of 2-digit groups}) \bmod 11$$

Example:

Key = 8429 → groups: 84 + 29 → 113 → 113 mod 11 = 3

Q7. (Compute using Hash Function 1)

Given keys: 27, 37, 47, 57, 67

Compute their hash values using:

$$h_1(k) = k \bmod 10$$

A7:

$$\begin{array}{cccccc} 27, & 37, & 47, & 57, & 67 \\ \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ \text{hash values: } & 7 & 7 & 7 & 7 & 7 \end{array}$$

Q8. (Identify collision pattern)

From your results in Q1:

- What pattern do you observe?
- Explain why these keys collide.

A8: 全部的 keys 都有相同的 hash value ^① _②
 因為全部的 keys 尾數都是 7，且 mod 又取 10，
 造成了所有的 keys 都碰撞在一起

Q9. (Compute using Hash Function 2)

Compute $h_2(k)$ for: 1234, 9217, 4519, 9902

A9: $1234 \rightarrow (12+34) \bmod 11 = 2$

$$9217 \rightarrow (92+17) \bmod 11 = 9$$

$$4519 \rightarrow (45+19) \bmod 11 = 9$$

$$9902 \rightarrow (99+02) \bmod 11 = 2$$

Q10. (Compare distribution)

- Which hash function (h_1 or h_2) produced more collisions for the input set?
- Which seems to spread keys more evenly?
- Provide 1–2 sentences of explanation.

A10: ^① $h_1(27, 37, 47, 57, 67) \rightarrow \text{碰撞}$

$$h_2(9217, 4519) \rightarrow \text{碰撞}$$

^③ ₍₁₎ mod 取的數不同，質數分布會較分散

₍₂₎ 數的拆分，也使得 keys 較分散

②

h_2