

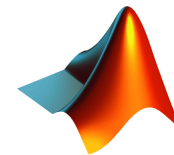
# CME 102

# MATLAB Review

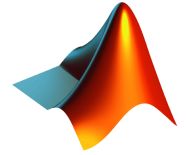
Tim Anderson



# What is your background?



- Math background
  - Math 51? Other math class at Stanford?
  - Math class outside of Stanford?
- Programming background
  - Java (CS106A)? Python? C++ (CS106B/X)? R?
- Forgot over break? Didn't really learn in CME100?
- Just a bad relationship with MATLAB?

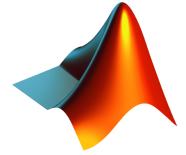


# What is MATLAB?

- Short for “matrix laboratory”
- Developed in mid-1980s
- Designed as easy environment for doing matrix computations
  - Does calculus-related stuff very well too
- Used **a lot** in education and industry
  - Jonathan Rosenberg (advisor to Larry Page): “If you want to work at Google, make sure you can use MATLAB”

# Basics

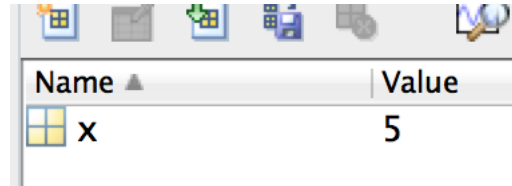
- Variables/Data types/Scope
- Mathematical operations
- **Vectors** (not exactly the same as in CME100)
  - Matrices
- Vector operations
- Plotting
- Loops
- Functions/Scripts



# Variables

- Way to store and call up a value
  - Declare variable “x” and assign value 5 as:

```
x = 5;
```

A screenshot of the MATLAB Variable Editor window. It shows a table with two columns: 'Name' and 'Value'. There is one row with the name 'x' and the value '5'.

Name	Value
x	5

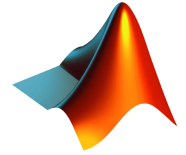
- Omit semicolon if you want to output value:

```
x = 5
```

And this outputs:

```
x =
```

5



# Variables

- Lets you call up the variable:

```
EDU>> x
```

```
x =
```

```
5
```

- And you can reassign the value as-needed:

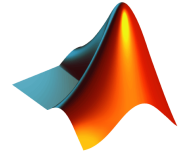
```
EDU>> x = 4
```

```
x =
```

```
4
```



# Mathematical Operations

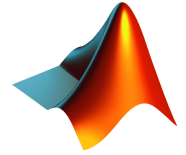


- You can perform mathematical operations on variables.  
Examples:

```
EDU>> exp(x)
ans =
    54.5982
```

```
EDU>> log(x)
ans =
    1.3863
```

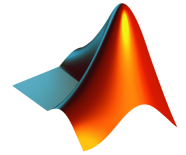
- Basically, MATLAB can work like a really good calculator



# Vectors

- **Not** the same as in CME100
  - CME100: Vector = quantity with direction and magnitude
- Matlab: linear algebra version of vector
  - Basically n-length array of numbers
  - Good for storing series of numbers such as data values





# Vectors

- Examples: Let's create a couple vectors
  - Type (if you have MATLAB open on your laptop):

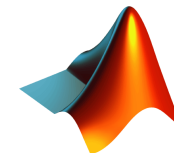
```
x = [1 4 5 8];
```

```
y = [2 13 9 4]';
```

```
z = [1; 16; 10; 3];
```

- Can index into the vector as:

```
y(4) = 4
```



# Vectors

- Output:

$x =$

1            4            5            8

← “Row vector”

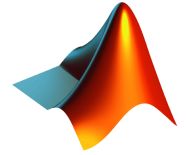
$y =$

2  
13  
9  
4

$z =$

1  
16  
10  
3

← “Column vector”



# Vectors

- Examples:

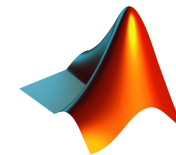
$x = [1 \quad 4 \quad 5 \quad 8];$  ← “Row vector”

$y = [2 \quad 13 \quad 9 \quad 4]';$  ← Apostrophe stands for “transpose” – flips from row to column vector or vice versa

$z = [1; 16; 10; 3];$

↖ ↗  
“Column vector”

↑  
Semicolons separate rows  
when entering data



# Matrices

- 2-D arrangement of data

— Ex:

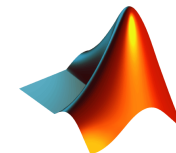
$A = [1 \quad 4 \quad 5 \quad 8; \quad 2 \quad 13 \quad 9 \quad 4; \quad 1 \quad 16 \quad 10 \quad 3];$

— Gives 3 x 4 matrix A:

$A =$

1	4	5	8
2	13	9	4
1	16	10	3

- Matrix dimensions given as rows x columns



# Matrices

- Can also be viewed as stacked row vectors:

- Ex:  $B = [x; y'; x];$

$B =$

1	4	5	8
2	13	9	4
1	4	5	8

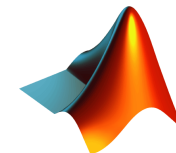
- Or side-by-side column vectors:

- Ex:  $B = [x' \ y \ x'];$

$B =$

1	2	1
4	13	4
5	9	5
8	4	8

- Putting vectors together like this is called **concatenation**



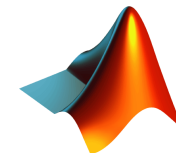
# Vector Operations

- Operators such as `log`, `exp`, etc. act on vectors **element by element**

— Ex:

```
exp(x) =  
1.0e+03 *  
    0.0027    0.0546    0.1484    2.9810
```

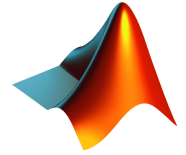
- Whatever type of vector (row or column) you put into an operator will come out of it



# Vector Operations

- **Operations between vectors must be done on vectors with the same dimension**
- Addition and subtraction are done element-by-element (just like in CME100)

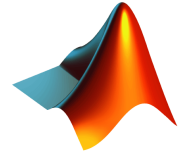
$$\begin{aligned} - \text{Ex: } \mathbf{x} + \mathbf{y}' &= \\ [3 \quad 17 \quad 14 \quad 12] \end{aligned}$$



# Vector Operations

- Multiplication/division can be a vector operation (outer/inner product) or element-by-element operation
  - Outer/inner products are from linear algebra and not needed for CME102
- To do multiplication, division, and exponentiation element-by-element, you must write `.*`, `./`, or `.^`
  - The period tells MATLAB that it's an element-by-element operation





# Vector Operations

- Examples:

$y .* z =$

2  
208  
90

12

$y(4) * z(4)$

$y ./ z =$

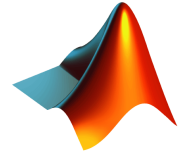
2.0000  
0.8125  
0.9000

1.3333

$y(4) / z(4)$

$y.^z =$

1.0e+17 \*  
  
0.0000  
6.6542  
0.0000  
0.0000



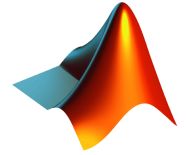
# Clearing Data

- Can clear a single variable/vector/matrix:

```
clear x
```

- Or you can clear everything:

```
clear all
```



# Plotting

- Plot two vectors of equal length as:

```
plot(x,y)
```

- If you need equally spaced data (you usually will for the x-axis variable), make it with either:

```
x = 0:0.1:10;
```

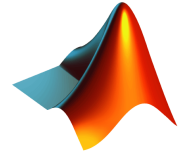
– Vector from 0 to 10 spaced by 0.1; 101 elements long

**or** `x = linspace(0,10,100);`

– 100 evenly-spaced points from 0 to 10



# Plotting

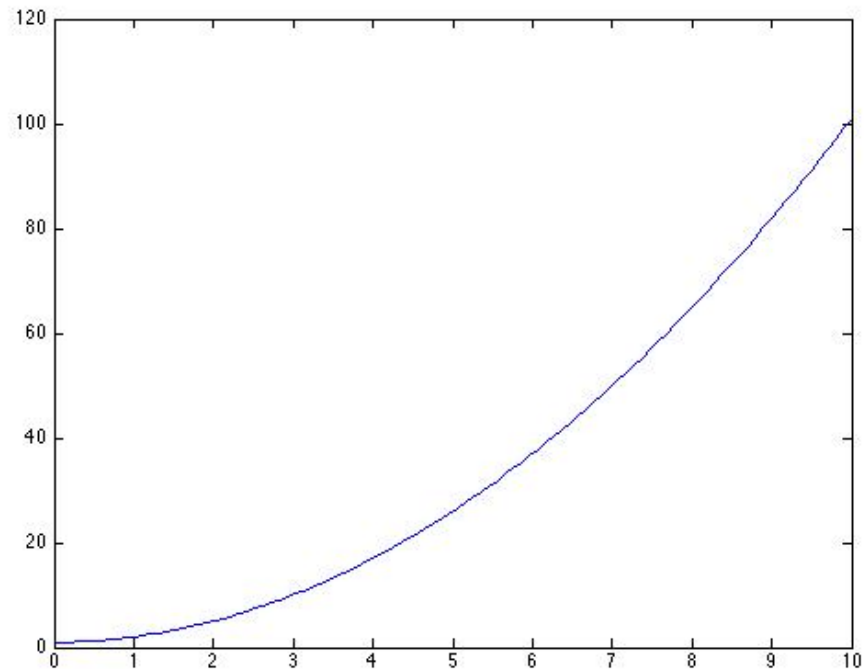


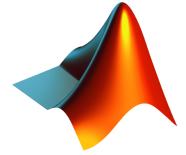
- We can generate a  $y$  variable by

$$y = x.^2 + 1;$$

- Then plot as:

`plot(x,y)`

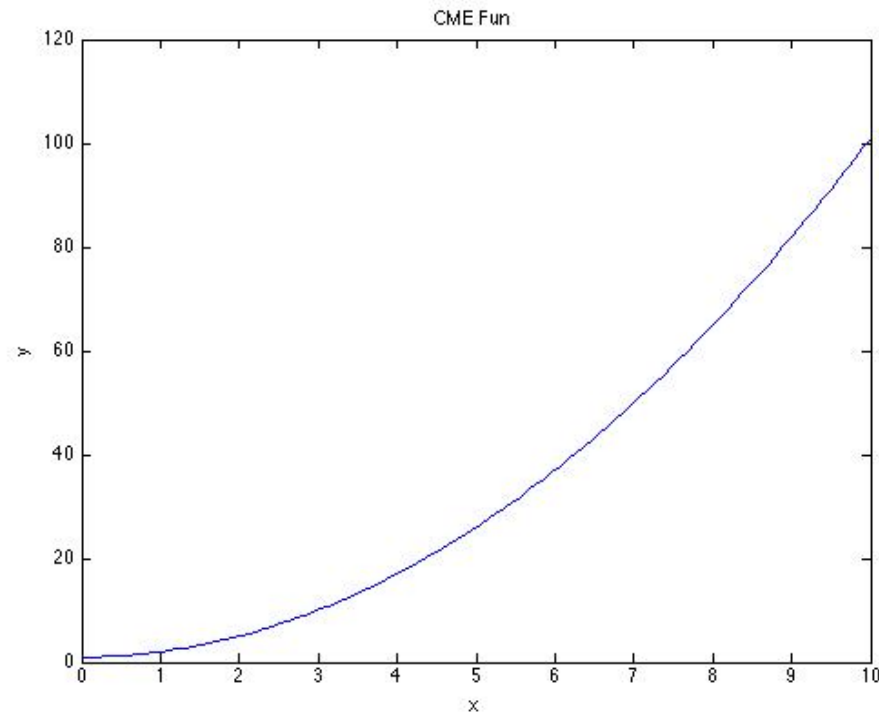


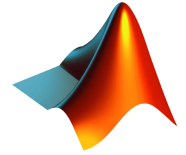


# Plotting

- Label plot using:

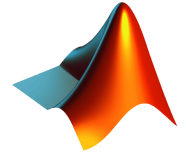
```
xlabel('x'); ylabel('y'); title('CME Fun')
```





# Plotting

- Make new plot using “figure”
- Can plot multiple things with  
    `hold on` or `hold all`
  - “on” plots everything in the same color (default = blue),  
    “all” plots each line with a different color
- Can switch between plots with  
    `figure(1)`, `figure(2)`, etc.
- Close plots with:  
    “close `all`” or “close `figure(1)`”

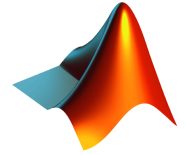


# Loops

- Loops used when you have to do something repeatedly
- E.g. running a function for a changing parameter, getting something to converge below an error, etc.
- MATLAB has `for` loops and `while` loops



# Loops



- **for loop:**

```
for i = 1:5  
    x = x + 1;  
end
```

← Loop increments counter variable on each iteration over an interval

← In MATLAB, must always terminate loops with “end”

- **while loop:**

```
x = 2;  
while x < 6  
    x = x + 1;  
end
```

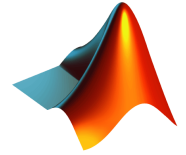
← Loop continues until condition is met—“while true” condition gives infinite loop

← Terminate loop with “end”





# Loops with Conditionals



- Can break out of loop prematurely using break statement with if statement:

```
for i = 1:5
```

```
    x = x + 1;
```

```
    if x > 5
```



Code inside if statement executes if  
and only if condition is met

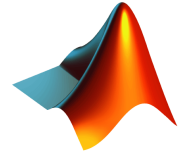
```
        break
```

```
    end
```

```
end
```

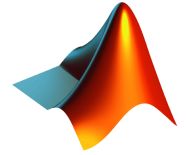


When “break” executes, it will only  
break the loop it is in, not all loops



# Functions

- MATLAB functions come in two flavors: “library/built-in functions” and “user-created functions”
  - Built-in/library functions are things like `plot()`, `exp()`, `log()`, `sum()`, etc.
- Making your own function can sometimes be useful for solving some problems
- **Numerically solving ODEs in MATLAB requires you to make your own functions**



# Functions

- You hand a functions some parameters and it will return a **value** or **vector of values**

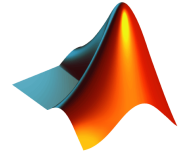
- Ex:

```
function m = sum_it_up(a,b)
    m = a + b;
end
```

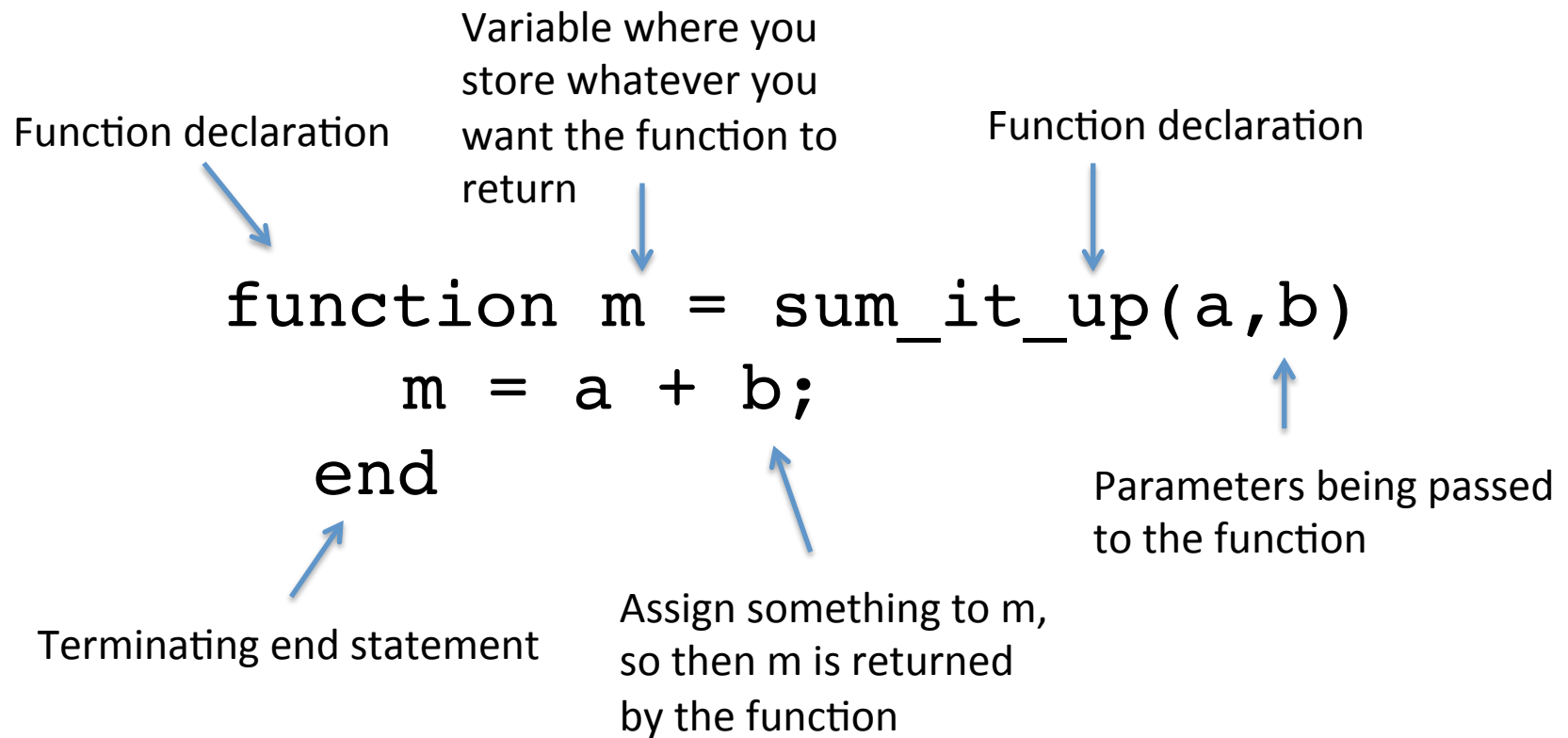
- Use function as:

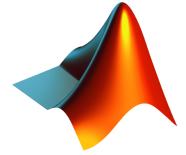
```
c = 1; d = 2;
x = sum_it_up(c,d);
```

- Output:  $x = 3$



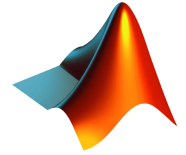
# Functions





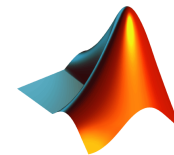
# Functions and Scope

- In MATLAB, variables are **not** global
  - Ex.: If you have variable “a” in your main script, using “a” in a function will not call up the same “a” as in the original script
  - E.g. problematic if your function evaluates a derivative of a function (something you’ll do a lot in this course) and you need to pass a parameter to the function
- There are work-arounds for this issue, but we will cover them later when needed



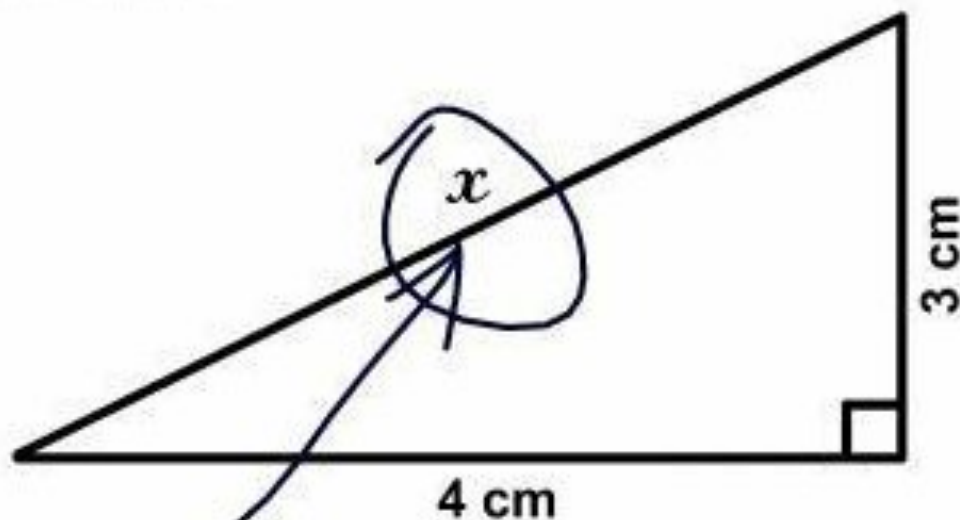
# Scripts

- Calling up other scripts within MATLAB is pretty easy (compared to doing other stuff)
- You save a MATLAB script as a .m file
- Call up a script in the command prompt or within another script by just writing the name of the script you want to call within the script you're writing
  - Can be useful for loading datasets or subroutines
- **Note: calling external scripts/datasets won't be needed much (if at all) in CME102**

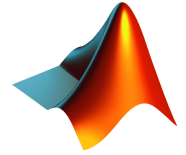


# Questions?

**3. Find  $x$ .**



*Here it is*



# Wrap-up

- This presentation owes credit to Dr. Eric Darve and Dr. Hung Lê for their development of CME102, and Dr. Vadim Khayms's CME100 MATLAB workbook
- Contact: [timmya@stanford.edu](mailto:timmya@stanford.edu)
- **If you need to learn how to do something new or troubleshoot your code, [www.mathworks.com](http://www.mathworks.com) is a tremendous resource**
- MATLAB is a great skill, learn it early and it will help a ton in your future engineering classes.



