1 A GENERALISED RANDOM ENCOUNTER MODEL FOR ESTIMATING 2 ANIMAL DENSITY WITH REMOTE SENSOR DATA

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1. Abstract

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1: Wildlife monitoring technology has advanced rapidly and the use of remote sensors such as camera traps, and acoustic detectors is becoming common in both the terrestrial and marine environments. Current capture-recapture or distance methods to estimate abundance or density require individual recognition of animals or knowing the distance of the animal from the sensor, which is often difficult. A method without these requirements, the random encounter model (REM), has been successfully applied to estimate animal densities from count data generated from camera traps. However, count data from acoustic detectors do not fit the assumptions of the REM due to the directionality of animal signals.

2: We developed a generalised REM (gREM), to estimate absolute animal density
from count data from both camera traps and acoustic detectors. We derived the
gREM for different combinations of sensor detection widths and animal signal
widths (a measure of directionality). We tested the accuracy and precision of this
model using simulations of different combinations of sensor detection widths and
animal signal widths, number of captures, and models of animal movement.

3: We find that the gREM produces accurate estimates of absolute animal density
for all combinations of sensor detection widths and animal signal widths. However, larger sensor detection and animal signal widths were found to be more precise. While the model is accurate for all capture efforts tested, the precision of the
estimate increases with the number of captures. We found no effect of different
animal movement models tested on the accuracy and precision of the gREM.

4: We conclude that the gREM provides an effective method to estimate absolute animal densities from remote sensor count data over a range of sensor and animal signal widths. The gREM is applicable for use for count data obtained in both marine and terrestrial environments, visually or acoustically (e.g., big cats, sharks, birds, bats and cetaceans). As sensors such as camera traps and acoustic detectors become more ubiquitous, the gREM will be increasingly useful for monitoring animal populations across broad spatial, temporal and taxonomic scales.

1.1. **Keywords.** Acoustic detection, Camera traps, Marine, Population monitoring, Simulations, Terrestrial

2. Introduction

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Animal population density is one of the fundamental measures needed in ecol-71 ogy and conservation. The density of a population has important implications for 72 a range of issues such as sensitivity to stochastic fluctuations (Richter-Dyn & Goel, 73 1972; Wright & Hubbell, 1983) and risk of extinction (Purvis et al., 2000). Monitor-74 ing animal population changes in response to anthropogenic pressure is becoming 75 increasingly important as humans modify habitats and change climates as never before (Everatt et al., 2014). Sensor technology, such as camera traps (Rowcliffe & 77 Carbone, 2008; Karanth, 1995) and acoustic detectors (O'Farrell & Gannon, 1999; 78 Clark, 1995; Acevedo & Villanueva-Rivera, 2006) are becoming increasingly used to monitor changes in animal populations (Rowcliffe & Carbone, 2008; Kessel et al., 2014), as they are efficient, relativity cheap and non-invasive (Cutler & Swann, 1999), allowing for surveys over large areas and long periods. However, the problem of converting sampled count data to estimates of density remains as efforts 83 must be made to account for detectability of the animals (Anderson, 2001). 84

Methods do already exist for estimating animal density if the distance between 85 the animal and the sensor can be estimated (e.g., capture-mark recapture meth-86 ods (Karanth, 1995) and distance sampling (Harris et al., 2013)). However, these 87 methods often require additional information that may not be available. For example, capture-mark-recapture methods (Karanth, 1995; Trolle & Kéry, 2003; Soisalo & Cavalcanti, 2006; Trolle et al., 2007) require recognition of individuals; distance methods require a distance estimation of how far away individuals are from the sensor barlow2005estimates, marques2011estimating. The development of the ran-92 dom encounter model (REM) (a modification of a gas model) enabled animal den-93 sities to be estimated from unmarked individuals of a known speed, and sensor detection parameters (Rowcliffe et al., 2008). The REM method has been success-95 fully applied to estimate animal densities from camera trap surveys (Manzo et al., 96 2012; Zero et al., 2013). However, extending the REM method to other types of sensors (for example acoustic detectors) is more problematic, because the original

derivation assumes a relatively narrow sensor width (up to $\pi/2$ radians) and that the animal is equally detectable irrespective of its heading (Rowcliffe *et al.*, 2008).

Whilst these restrictions are not problematic for most camera trap makes (e.g. Reconyx, Cuddeback), the REM could not be used to estimate densities from cam-era traps with a wider sensor width (e.g. canopy monitoring with fish eye lens (Brusa & Bunker, 2014)). Additionally, the REM method would not be useful in estimating densities from acoustic survey data as the acoustic detector angles are often wider than $\pi/2$ radians. Acoustic detectors are designed for a range of di-verse tasks and environments (Kessel et al., 2014), which will naturally lead to a wide range of sensor detection widths and detection distances. In addition to this, calls emitted by many animals are directional (breaking the assumption of the REM method).

There has been a sharp rise in interest around passive acoustic detectors in recent years, with a 10 fold increase in publications in the decade between 2000 and 2010 (Kessel *et al.*, 2014). Acoustic monitoring is being developed to study many aspects of ecology, including the interactions of animals and their environments (Blumstein *et al.*, 2011; Rogers *et al.*, 2013), the presence and relative abundances of species (Marcoux *et al.*, 2011), and biodiversity of an area (Depraetere *et al.*, 2012).

Acoustic data suffers from many of the problems associated with data from camera trap surveys in that individuals are often unmarked so capture-make-recapture methods cannot be used to estimate densities. In some cases the distance between the animal and the sensor is known, for example when an array of sensors and the position of the animal is estimated by triangulation (Lewis *et al.*, 2007). In these situations distance-sampling methods can be applied, a method typically used for marine mammals (Rogers *et al.*, 2013). However, in many cases distance estimation is not possible, for example when single sensors are deployed, a situation typical in the majority of terrestrial acoustic surveys (Elphick, 2008; Buckland *et al.*, 2008). In these cases, only relative measures of local abundance can be calculated, and not absolute densities. This means that comparison of populations between species and sites is problematic without assuming equal detectability (Schmidt, 2003). Equality detectability is unlikely because of differences in environmental conditions, sensor type, habitats, species biology.

In this study we create a generalised REM (gREM), as an extension to the cam-131 era trap model of (Rowcliffe et al., 2008), to estimate absolute density from count 132 data from acoustic detectors, or camera traps, where the sensor width can vary 133 from 0 to 2π radians, and the signal given off from the animal can be directional. 134 We assessed the accuracy and precision of the gREM within a simulated environ-135 ment, by varying the sensor detection widths, animal signal widths, number of 136 captures and models of animal movement. We use the simulation results to rec-137 ommend best survey practice for estimating animal densities from remote sensors. 138

3. Methods

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3.1. Analytical Model. The REM presented by (Rowcliffe et al., 2008) adapts the 140 gas model to model count data from camera trap surveys. The REM is derived as-141 suming a stationary sensor with a detection width less than $\pi/2$ radians. However, 142 in order to apply this approach more generally, and in particular to acoustic de-143 tectors, we need both to relax the constraint on sensor detection width, and allow 144 for animals with directional signals. Consequently, we derive the gREM for any 145 detection width, θ , between 0 and 2π with a detection distance r giving a circular sector within which animals can be captured (the detection zone)(Figure 1). Additionally, we model the animal as having an associated signal width α between 148 0 and 2π (Figure 1, see Appendix S1 for a list of symbols). We start deriving the 149 gREM with the simplest situation, the gas model where $\theta = 2\pi$ and $\alpha = 2\pi$. 150

3.1.1. *Gas Model.* Following Yapp (1956), we derive the gas model where sensors can capture animals in any direction and animal's signal is detectable from any direction($\theta = 2\pi$ and $\alpha = 2\pi$). We assume that animals are in a homogeneous environment, and move in straight lines of random direction with velocity v. We allow that our stationary sensor can capture animals at a detection distance r and that if an animal moves within this detection zone they are captured with a probability of one, while animals outside the zone are never captured.

In order to derive animal density, we need to consider relative velocity from the reference frame of the animals. Conceptually, this requires us to imagine that all animals are stationary and randomly distributed in space, while the sensor moves with velocity v. If we calculate the area covered by the sensor during the

survey period we can estimate the number of animals the sensor should capture.

As a circle moving across a plane, the area covered by the sensor per unit time is 2rv. The number of expected captures, z, for a survey period of t, with an animal

density of D is z = 2rvtD. To estimate the density, we rearrange to get D = z/2rvt.

3.1.2. gREM derivations for different detection and signal widths. Different combina-166 tions of θ and α would be expected to occur (e.g., sensors have different detection 167 widths and animals have different signal widths). For different combinations θ 168 and α , the area covered per unit time is no longer given by 2rv. Instead of the size 169 of the sensor detection zone having a diameter of 2r, the size changes with the 170 approach angle between the sensor and the animal. For any given signal width 171 and detector width and depending on the angle that the animal approaches the 172 sensor, the width of the area within which an animal can be detected is called the 173 profile, p. The size of the profile (averaged across all approach angles) is defined 174 as the average profile \bar{p} . However, different combinations of θ and α need different 175 equations to calculate \bar{p} . 176

We have identified the parameter space for the combinations of θ and α for which the derivation of the equations are the same (defined as sub-models in the gREM) (Figure 2). For example, the gas model becomes the simplest gREM sub-model (upper right in (Figure 2) and the REM from (Rowcliffe *et al.*, 2008) is another gREM sub-model where $\theta < \pi/2$ and $\alpha = 2\pi$. We derive one gREM sub-model SE2 as an example below (where $4\pi - 2\alpha < \theta < 2\pi$, $0 < \alpha < \pi$) (see Appendix S2 for other gREM sub-models).

3.1.3. Example derivation of SE2. In order to calculate \bar{p} , we have to integrate over the focal angle, x_1 (Figure 3a). This is the angle taken from the centre line of the sensor. Other focal angles are possible (x_2, x_3, x_4) and are used in other gREM sub-models (see Appendix S2). As the size of the profile depends on the approach angle, we present the derivation across all approach angles. When the sensor is directly approaching the animal $x_1 = \pi/2$.

Starting from $x_1 = \pi/2$ until $\theta/2 + \pi/2 - \alpha/2$, the size of the profile is $2r \sin \alpha/2$ (Figure 3b). During this first interval, the size of α limits the width of the profile.

When the animal reaches $x_1 = \theta/2 + \pi/2 - \alpha/2$ (Figure 3c), the size of the profile is

 $r \sin(\alpha/2) + r \cos(x_1 - \theta/2)$ and the size of $\theta/$ and α both limit the width of the profile (Figure 3c). Finally, at $x_1 = 5\pi/2 - \theta/2 - \alpha/2$ until $x_1 = 3\pi/2$, the width of the profile is again $2r \sin \alpha/2$ (Figure 3d) and the size of α again limits the width of the profile. The profile width p for π radians of rotation (from directly towards the sensor to directly behind the sensor) is completely characterised by the three intervals (Figure 3b–3d). Average profile width \bar{p} is calculated by integrating these profiles over their appropriate intervals of x_1 and dividing by π which gives

$$\bar{p} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}} 2r \sin\frac{\alpha}{2} dx_1 + \int_{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}} r \sin\frac{\alpha}{2} + r \cos\left(x_1 - \frac{\theta}{2}\right) dx_1 + \int_{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{3\pi}{2}} 2r \sin\frac{\alpha}{2} dx_1 \right)$$

$$= \frac{r}{\pi} \left(\theta \sin\frac{\alpha}{2} - \cos\frac{\alpha}{2} + \cos\left(\frac{\alpha}{2} + \theta\right)\right)$$
eqn 1

We then, as with the gas model, use this expression to calculate density

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$$D = z/vt\bar{p}.$$
 eqn 3

Rather than having one equation that describes \bar{p} globally, the gREM must be

split into submodels due to discontiunous changes in p as α and β change. These 203 discontinuities can occur for a number of reasons such as a profile switching be-204 tween being limited by α and θ , the difference between very small profiles and 205 profiles of size zero and the fact that the width of a sector stops increasing once 206 the central angle reaches π radians (i.e., a semi circle is just as wide as a full circle.) 207 As a visual example, if α is small, there is an interval between Fig. 3c and 3d 208 where the 'blind spot' would prevent animals being detected at all giving p = 0. 209 This would require an extra integral in our equation as simply putting our small value of α into eqn 1 would not give us this integral of p = 0. gREM submodel specifications were done by hand, and the integration was 212 done using SymPy (SymPy Development Team, 2014) in Python (Appendix S3). 213 The gREM submodels were checked by confirming that: 1) submodels adjacent 214 in parameter space were equal at the boundary between them; 2) submodels that 215 border $\alpha = 0$ had p = 0 when $\alpha = 0$; 3) average profile widths \bar{p} were between 0 and 216

2r and; 4) each integral, divided by the range of angles that it was integrated over, was between 0 and 2r. The scripts for these tests are included in Appendix S3 and the R (R Development Core Team, 2010) implementation of the gREM is given in Appendix S4.

3.2. **Simulation Model.** We tested the accuracy and precision of the gREM by de-

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veloping a spatially explicit simulation of the interaction of sensors and animals 222 using different combinations of sensor detection widths, animal signal widths, 223 number of captures, and models of animal movement. 100 simulations were run 224 where each consisted of a 7.5 km by 7.5 km square (with periodic boundaries). A 225 stationary sensor of radius r was set up in the exact centre of each simulation, cov-226 ering 7 sensor detection widths θ between 0 and $2\pi(2/9\pi, 4/9\pi, 6/9\pi, 8/9\pi, 10/9\pi,$ 227 $14/9\pi$, 2π). Each simulation was populated with a density of 70 animals km⁻². This 228 density was chosen as it is approximately the expected density of mammals animals weighing 1 g calculated form the equation in Damuth (1981). This created a 230 total of 3937 individuals per simulation which were placed randomly at the start 231 of the simulation. Individuals were assigned 9 signal detection widths α between 232 0 and π (x.x.x.x.x). 233 Each simulation lasted for N steps (xx) of duration T (15 minutes) giving a total 234 duration of 150 days. The individuals moved within each step with a distance 235 d, with an average speed, v. d, was sampled from a normal distribution with 236 mean distance, $\mu_d = vT$, and standard deviation $\sigma_d = vT/10$. An average speed, 237 $v = 40 \,\mathrm{km} \,\mathrm{days}^{-1}$, was chosen as this represents the largest day range of terrestrial 238 animals (Carbone et al., 2005), and represents the upper limit of realistic speeds. 239 At the end step, individuals were allowed to either remain stationary for a time 240 step (with a given probability, S), change direction (with a maximum angle, A) 241 between 0 and π . This resulted in 7 different movement models where: (1) simple 242 movement, where S and A = 0; (2)stop-start movement, where (i) S = 0.25, A = 0, 243 (ii) S = 0.5, A = 0, (iii) S = 0.75, A = 0; (3) random walk movement, where (i) S = 0.5244 $0, A = \pi/3$, (ii) $S = 0, A = 2\pi/3$, iii) $S = 0, A = \pi$. Individuals were counted as they 245 moved in and out of the detection zone of the sensor per simulation. 246

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We calculated the estimated animal density from the gREM by summing the number of captures per simulation and inputting these values into the correct gREM submodel. gREM accuracy was determined by comparing the density in the simulation with the estimated density. High accuracy is indicated by the mean difference between the estimated and actual values converging to zero as sample size increases. gREM precision was determined by the standard deviation of estimated densities. We constructed box plots of the error between real and estimated densities to graphically test for accuracy and precision.

We compared the accuracy and precision of all the gREM submodels. As these submodels are derived for different combinations of α and θ , we used the gREM submodel accuracy and precision to determine the impact of different values of α and θ . The impact of the number of captures and animal movement models on accuracy and precision was investigated using 4 different gREM submodels representative of the range α and θ values (submodels NW1, SW1, NE1, and SE3, Figure 2). Using these four submodels, we calculated how long the simulation needed to run to generate a range of different capture numbers (from 10 to 100 captures in 10 unit intervals), and estimated animal density. These estimated densities were compared to the real density to assess the impact on the accuracy and precision on the gREM of different simulation lengths. We also used these four submodels to compare the accuracy and precision of a simple movement model, to stop-start movement models and random walk movement models. The gREM assumes that individuals move continuously with straight-line movement (simple movement model) and we therefore assess the impact of breaking the gREM assumptions.

4. Results

4.1. **Analytical model.** The equation for \bar{p} has been newly derived for each sub-model in the gREM, except for the gas model and REM which have been calculated previously. However, many models, although derived separately, have the same expression for \bar{p} . Figure 4 shows the expression for \bar{p} in each case. The general equation for density, using the correct expression for \bar{p} is then substituted into eqn 3.

Although more thorough checks are performed in Appendix S3, it can be seen that all adjacent expressions in Figure 4 are equal when expressions for the boundaries between them are substituted in.

4.2. **Simulation model.** For each model we compared the estimated densities to the true densities in a simulation. None of the models showed any evidence of any significant differences between the estimated and true density values (Figure 5a). The precision of the models do vary however. The standard deviation of the error is strongly related to the sensor and signal width (Figure 5b), such that larger widths have greater precision. However, even the models with smaller sensor and signal widths have a relativity high level of precision.

4.2.1. *Impact of the number of captures*. The precision of the model is dependent on the number of captures during the survey. In Figure 6 we can see that the model precision gets greater as the number of captures increase. As the number of captures reaches about 100 then the coefficient of variation falls below 10% which could be considered negligible.

4.2.2. Use of the gREM when animal movement is not consistent with model assumptions. 293 Simulating start-stop instead of continuous movement had no effect the accuracy, 294 or the precision, of the estimates (Figure 7a) as long as the true overall speed of 295 the animal is known. Relaxing straight line movement to allow random or cor-296 related random walks did not effect the accuracy of the method (Figure 7b). We 297 allowed animals to change direction up to a maximum value at the end of each step, picked from a uniform distribution where the maximum angle ranged from 299 0 to π , which corresponds to straight line movement and random walk respec-300 tively. There is no significant difference in the variance for the change, this could 301 be because of the between the step length of the animal movement, 15 minutes, 302 means that immediate double counting of the same animal is unlikely. In the case 303 where large directional changes are likely to occur within short periods of time 304 leading to double counting of the same animal within a short period of time may 305 need to be adjusted because of this.

5. DISCUSSION

We have developed the gREM such that it can be used to estimate density from acoustic and optical sensors. This has entailed a generalisation of the gas model and the model in (Rowcliffe *et al.*, 2008) to be applicable to any combination of sensor width and call directionality. We have used simulations to show, as a proof of principle, that these models are accurate and precise.

The gREM is therefore available for the estimation of density of a number of taxa of importance to conservation, zoonotic diseases and ecosystem services. The models provided are suitable for certain groups for which there are currently no, or few, effective methods for density estimation. Any species that would be consistently recorded at least once when within range of a detector would be a suitable subject for the gREM, such as bats (Kunz *et al.*, 2009), songbirds (Buckland & Handel, 2006), Cetaceans (Marques *et al.*, 2009) or forest primates (Hassel-Finnegan *et al.*, 2008). Within increasing technological capabilities, this list of species is likely to increase dramatically.

Importantly the methods are noninvasive and do not require human marking or naturally identifying marks (as required for mark-recapture models). This makes them suitable for large, continuous monitoring projects with limited human resources. It also makes them suitable for species that are under pressure, species that cannot naturally be individually recognised or species that are difficult or dangerous to catch.

From our simulations we believe that this method has the potential produce accurate and precise estimates for many different species, using either camera or acoustic detectors. When choosing detectors a researcher should pick the detector with the largest radius and detection angle possible, but whilst a small capture area may reduce precision there is only a limited impact on the overall precision of the model (Figure 5b). A range of factors will affect the overall precision of the model, like size of detection zone, speed of animal, density of animals and length of survey which are reflected in the number of captures. Increasing the number of captures leads to more precise estimates, for species which more slower, or have

occur at lower densities, then the detection zone and length of survey need to be 337 increased to compensate so that at least 100 captures are collected (Figure 6). 338

Within the simulation we have assumed an equal density across the entire world, 339 however in a field environment the situation would be much more complex, with 340 additional variation coming from local changes in density between camera sites. We also assume perfect knowledge of the average speed of an animal and size of 342 the detection zone, and instant triggering of the camera. All of which may lead to 343 possible bias or decreased precision. 344

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Although we have used simulations to validate these models, much more ro-345 bust testing is needed. Although difficult, proper field test validation would be 346 required before the models could be fully trusted. Note, however, that the REM (Rowcliffe et al., 2008) has been field tested. Both Rowcliffe et al. (2008) and Zero et al. (2013) both found that the REM were effective manner of estimating animal 349 densities (Rowcliffe et al., 2008; Zero et al., 2013). There was some discrepancies 350 between the REM and the census methodologies found by Rovero and Marshall 351 which may have been down to lack of knowledge of wild animal speed, and an 352 underestimate in census results (Rovero & Marshall, 2009). In some taxa gold stan-353 dard methods of estimating animal density exist, such as capture mark recapture. 354 Where these gold standard exist, and have been proved to work, a simultaneous 355 gREM study could be completed to test the accuracy under field conditions. An 356 easier way to continue to evaluate the models is to run more extensive simulations which break the assumptions of the analytical models. The main element that 358 cannot be analytically treated is the complex movement of real animals. There-359 fore testing these methods against true animal traces, or more complex movement 360 models would be useful. 361

There are a number of positive extensions to the gREM which could be developed in the future. The original gas model was formulated for the case where both subjects, either animal and detector, or animal and animal, are moving (Hutchinson & Waser, 2007). Indeed any of the models with animals that are equally detectable in all directions ($\alpha = 2\pi$) can be trivially expanded for moving by substituting the sum of the average animal velocity and the sensor velocity for v as

used here. However, when the animal has a directional call, the extension be-368 comes much less simple. The approach would be to calculate again the mean 369 profile width. However, for each angle of approach, one would have to average 370 the profile width for an animal facing in any direction (i.e. not necessarily moving 371 towards the sensor) weighted by the relative velocity of that direction. There are 372 a number of situations where a moving detector and animal could occur and as 373 such may be advantage to have a method of estimating densities from the data 374 collected, e.g. an acoustic detector based off a boat when studying Cetacea or sea 375 birds (Yack et al., 2013). 376

Another interesting, and so far unstudied problem, is edge effects caused by trigger delays (the delay between sensing an animal and attempting to record the encounter) and time expansion acoustic detectors which repeatedly turn on an off during sampling. Both of these have potential biases as animals can move through the detection zone without being detected. The models herein are formulated assuming constant surveillance and so the error quickly becomes negligible. For example, if it takes longer for the recording device to be switched on than the length of some animal calls there could be a systematic underestimation of density.

6. ACKNOWLEDGMENTS

386 REFERENCES

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Acevedo, M.A. & Villanueva-Rivera, L.J. (2006) Using automated digital recording systems as effective tools for the monitoring of birds and amphibians. *Wildlife Society Bulletin*, **34**, 211–214.

Anderson, D.R. (2001) The need to get the basics right in wildlife field studies.

Wildlife Society Bulletin, pp. 1294–1297.

Blumstein, D.T., Mennill, D.J., Clemins, P., Girod, L., Yao, K., Patricelli, G., Deppe, J.L., Krakauer, A.H., Clark, C., Cortopassi, K.A. *et al.* (2011) Acoustic monitoring in terrestrial environments using microphone arrays: applications, technological considerations and prospectus. *Journal of Applied Ecology*, **48**, 758–767.

Brusa, A. & Bunker, D.E. (2014) Increasing the precision of canopy closure estimates from hemispherical photography: Blue channel analysis and underexposure. *Agricultural and Forest Meteorology*, **195**, 102–107.

- Buckland, S.T. & Handel, C. (2006) Point-transect surveys for songbirds: robust
- methodologies. *The Auk*, **123**, 345–357.
- 401 Buckland, S.T., Marsden, S.J. & Green, R.E. (2008) Estimating bird abundance:
- making methods work. *Bird Conservation International*, **18**, S91–S108.
- 403 Carbone, C., Cowlishaw, G., Isaac, N.J. & Rowcliffe, J.M. (2005) How far do ani-
- mals go? Determinants of day range in mammals. The American Naturalist, 165,
- 405 290–297.
- 406 Clark, C.W. (1995) Application of US Navy underwater hydrophone arrays for
- scientific research on whales. Reports of the International Whaling Commission, 45,
- 408 210-212.
- 409 Cutler, T.L. & Swann, D.E. (1999) Using remote photography in wildlife ecology:
- a review. *Wildlife Society Bulletin*, pp. 571–581.
- Damuth, J. (1981) Population density and body size in mammals. Nature, 290,
- 412 699-700.
- Depraetere, M., Pavoine, S., Jiguet, F., Gasc, A., Duvail, S. & Sueur, J. (2012) Mon-
- 414 itoring animal diversity using acoustic indices: implementation in a temperate
- woodland. *Ecological Indicators*, **13**, 46–54.
- Elphick, C.S. (2008) How you count counts: the importance of methods research
- in applied ecology. *Journal of Applied Ecology*, **45**, 1313–1320.
- 418 Everatt, K.T., Andresen, L. & Somers, M.J. (2014) Trophic scaling and occupancy
- analysis reveals a lion population limited by top-down anthropogenic pressure
- in the limpopo national park, mozambique. *PloS one*, **9**, e99389.
- 421 Harris, D., Matias, L., Thomas, L., Harwood, J. & Geissler, W.H. (2013) Applying
- distance sampling to fin whale calls recorded by single seismic instruments in
- the northeast atlantic. The Journal of the Acoustical Society of America, 134, 3522-
- 424 3535.
- Hassel-Finnegan, H.M., Borries, C., Larney, E., Umponjan, M. & Koenig, A. (2008)
- How reliable are density estimates for diurnal primates? International Journal of
- *Primatology*, **29**, 1175–1187.
- Hutchinson, J.M.C. & Waser, P.M. (2007) Use, misuse and extensions of "ideal gas"
- models of animal encounter. Biological Reviews of the Cambridge Philosophical So-
- 430 *ciety*, **82**, 335–359.

- Karanth, K. (1995) Estimating tiger (Panthera tigris) populations from camera-trap
- data using capture–recapture models. *Biological Conservation*, **71**, 333–338.
- 433 Kessel, S., Cooke, S., Heupel, M., Hussey, N., Simpfendorfer, C., Vagle, S. & Fisk, A.
- 434 (2014) A review of detection range testing in aquatic passive acoustic telemetry
- studies. Reviews in Fish Biology and Fisheries, 24, 199–218.
- 436 Kunz, T.H., Betke, M., Hristov, N.I. & Vonhof, M. (2009) Methods for assessing
- colony size, population size, and relative abundance of bats. Ecological and be-
- havioral methods for the study of bats (TH Kunz and S Parsons, eds) 2nd ed Johns
- Hopkins University Press, Baltimore, Maryland, pp. 133–157.
- Lewis, T., Gillespie, D., Lacey, C., Matthews, J., Danbolt, M., Leaper, R.,
- McLanaghan, R. & Moscrop, A. (2007) Sperm whale abundance estimates from
- acoustic surveys of the ionian sea and straits of sicily in 2003. Journal of the Ma-
- rine Biological Association of the United Kingdom, 87, 353–357.
- 444 Manzo, E., Bartolommei, P., Rowcliffe, J.M. & Cozzolino, R. (2012) Estimation of
- population density of european pine marten in central italy using camera trap-
- ping. *Acta Theriologica*, **57**, 165–172.
- 447 Marcoux, M., Auger-Méthé, M., Chmelnitsky, E.G., Ferguson, S.H. & Humphries,
- 448 M.M. (2011) Local passive acoustic monitoring of narwhal presence in the cana-
- dian arctic: a pilot project. Arctic, pp. 307–316.
- 450 Marques, T.A., Thomas, L., Ward, J., DiMarzio, N. & Tyack, P.L. (2009) Estimating
- cetacean population density using fixed passive acoustic sensors: An example
- with Blainville's beaked whales. The Journal of the Acoustical Society of America,
- **125**, 1982–1994.
- 454 O'Farrell, M.J. & Gannon, W.L. (1999) A comparison of acoustic versus capture
- techniques for the inventory of bats. *Journal of Mammalogy*, pp. 24–30.
- Purvis, A., Gittleman, J.L., Cowlishaw, G. & Mace, G.M. (2000) Predicting extinc-
- tion risk in declining species. *Proceedings of the Royal Society of London Series B:*
- 458 Biological Sciences, **267**, 1947–1952.
- R Development Core Team (2010) R: A Language And Environment For Statistical
- 460 Computing. R Foundation For Statistical Computing, Vienna, Austria. ISBN 3-
- 900051-07-0.

- Richter-Dyn, N. & Goel, N.S. (1972) On the extinction of a colonizing species. The-
- oretical Population Biology, **3**, 406–433.
- Rogers, T.L., Ciaglia, M.B., Klinck, H. & Southwell, C. (2013) Density can be mis-
- leading for low-density species: benefits of passive acoustic monitoring. Public
- Library of Science One, 8, e52542.
- ⁴⁶⁷ Rovero, F. & Marshall, A.R. (2009) Camera trapping photographic rate as an index
- of density in forest ungulates. *Journal of Applied Ecology*, **46**, 1011–1017.
- Rowcliffe, J.M. & Carbone, C. (2008) Surveys using camera traps: are we looking
- to a brighter future? *Animal Conservation*, **11**, 185–186.
- Rowcliffe, J., Field, J., Turvey, S. & Carbone, C. (2008) Estimating animal density
- using camera traps without the need for individual recognition. Journal of Ap-
- 473 plied Ecology, **45**, 1228–1236.
- Schmidt, B.R. (2003) Count data, detection probabilities, and the demography, dy-
- namics, distribution, and decline of amphibians. Comptes Rendus Biologies, 326,
- 476 119–124.
- 477 Soisalo, M.K. & Cavalcanti, S. (2006) Estimating the density of a jaguar population
- in the Brazilian Pantanal using camera-traps and capture-recapture sampling in
- combination with GPS radio-telemetry. *Biological Conservation*, **129**, 487–496.
- 480 SymPy Development Team (2014) SymPy: Python library for symbolic mathematics.
- 481 Trolle, M. & Kéry, M. (2003) Estimation of ocelot density in the Pantanal using
- capture-recapture analysis of camera-trapping data. Journal of mammalogy, 84,
- 483 607–614.
- Trolle, M., Noss, A.J., Lima, E.D.S. & Dalponte, J.C. (2007) Camera-trap studies of
- maned wolf density in the Cerrado and the Pantanal of Brazil. Biodiversity and
- 486 *Conservation*, **16**, 1197–1204.
- 487 Wright, S.J. & Hubbell, S.P. (1983) Stochastic extinction and reserve size: a focal
- species approach. Oikos, pp. 466–476.
- Yack, T.M., Barlow, J., Calambokidis, J., Southall, B. & Coates, S. (2013) Passive
- 490 acoustic monitoring using a towed hydrophone array results in identification of
- a previously unknown beaked whale habitat. The Journal of the Acoustical Society
- of America, **134**, 2589–2595.
- 493 Yapp, W. (1956) The theory of line transects. *Bird study*, **3**, 93–104.

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- ⁴⁹⁴ Zero, V.H., Sundaresan, S.R., O'Brien, T.G. & Kinnaird, M.F. (2013) Monitoring
- an endangered savannah ungulate, Grevy's zebra (Equus grevyi): choosing a
- method for estimating population densities. *Oryx*, **47**, 410–419.

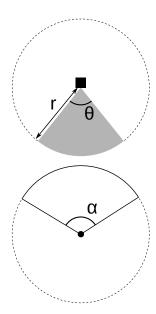


FIGURE 1. Representation of sensor detection width and animal signal width. The filled square and circle represent a sensor and an animal, respectively; θ , sensor detection width (radians); r, sensor detection distance; dark grey shaded area, sensor detection zone; α , animal signal width (radians). Dashed lines around the filled square and circle represents the maximum extent of θ and α , respectively.

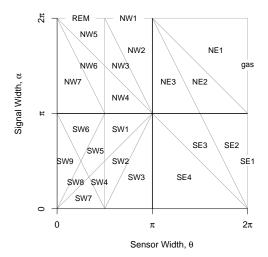


FIGURE 2. Locations where derivation of the average profile \bar{p} is the same for different combinations of sensor detection width and animal signal width. Symbols within each polygon refer to each gREM submodel named after their compass point, except for Gas and REM which highlight the position of these previously derived models within the gREM. Symbols on the edge of the plot are for submodels with $\alpha, \theta = 2\pi$

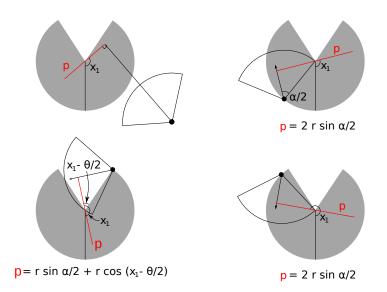


FIGURE 3. An overview of the derivation of SE2. The filled circles represent animals, with the animal signal shown as a unfilled sector and the direction of movement shown as an arrow. The detection zone of the sensors are shown as filled grey sectors with a detection distance of r. The SYMBOL shows the direction the sensor is facing; θ , sensor detection width; α , animal signal width. The profile p (the line an animal must pass through in order to be captured) is shown in red and x_1 is the focal angle, where (a) shows the location of x_1 . The derivation of p changes as the animal approaches the sensor from different directions where (b) is the derivation of p when x_1 is in the interval $\left[\frac{\pi}{2}, \frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}\right]$, (c) p when x_1 is in the interval $\left[\frac{\pi}{2}, \frac{\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}, \frac{3\pi}{2}\right]$. The resultant equation for p is shown beneath each figure.

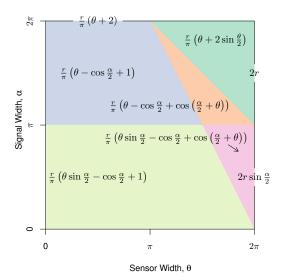
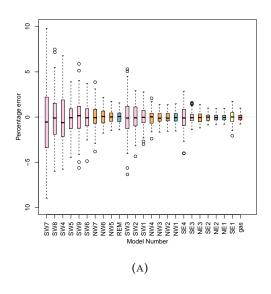


FIGURE 4. Expressions for the average profile wide, \bar{p} , given sensor and signal widths. Despite independent derivation within each block, many models result in the same expression. These are collected together and presented as one block of colour. Expressions on the edge of the plot are for submodels with α , $\theta = 2\pi$.



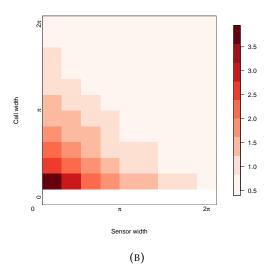


FIGURE 5. The precision of the gREM given a range of detection and call angles. The standard deviation of the percentage error for sensor, and call angles between 0 and 2π where: $r=100\,\mathrm{m}$; $T=150\,\mathrm{days}$; $v=40\,\mathrm{km\,days^{-1}}$; $D=70\,\mathrm{animals\,km^{-2}}$; and with detection angles varying between models. Where red indicates a high standard deviation and blue represents a low standard deviation.

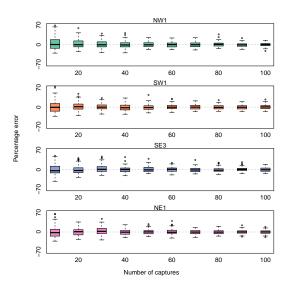


FIGURE 6. Accuracy of the gREM reminds unchanged, whilst precision increases, with captures. Box plots of four test models when given different numbers of captures where: $r=100\,\mathrm{m}$; $T=150\,\mathrm{days}$; $v=40\,\mathrm{km\,days^{-1}}$; $D=70\,\mathrm{animals\,km^{-2}}$; and with angles varying between models. Where the model names refer to Figure 1 in Appendix S2.

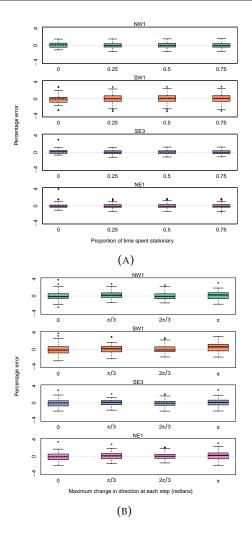


FIGURE 7. Accuracy and the precision of the gREM given changes in the amount of time an animal spends stationary on average. Distribution of model error when simulated animals spend increasing proportion of time stationary where: $r=100\,\mathrm{m};\ T=150\,\mathrm{days};\ v=40\,\mathrm{km}\,\mathrm{days^{-1}};\ D=70\,\mathrm{animals}\,\mathrm{km^{-2}};$ and with detection angles varying between models. Where the model names refer to Figure 1 in Appendix S2. Accuracy and the precision of the gREM given different types of correlated walks. Distribution of model error when simulated animals move with different types of correlated walk where: $r=10\,\mathrm{m};\ T=352\,\mathrm{days};\ v=40\,\mathrm{km}\,\mathrm{days^{-1}};\ D=70\,\mathrm{animals}\,\mathrm{km^{-2}};$ and with angles varying between models. Where the model names refer to Figure 1 in Appendix S2.