1 A GENERALISED RANDOM ENCOUNTER MODEL FOR ESTIMATING 2 ANIMAL DENSITY WITH REMOTE SENSOR DATA

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- 5 Authors:
- ${\small \small \textbf{1} Im C.D. Lucas}^{1,2,3}\dagger, Elizabeth \ A. \ Moorcroft^{1,4,5}\dagger, \ Robin \ Freeman^{5}, Marcus \ J. \ Rowcliffe^{5}, \\ \\ {\small \small \small } \\$
- 7 Kate E. Jones^{2,5}
- 8 Addresses:
- 9 1 CoMPLEX, University College London, Physics Building, Gower Street, Lon-
- 10 don, WC1E 6BT, UK
- 11 2 Centre for Biodiversity and Environment Research, Department of Genetics,
- 12 Evolution and Environment, University College London, Gower Street, London,
- 13 WC1E 6BT, UK
- 3 Department of Statistical Science, University College London, Gower Street,
- 15 London, WC1E 6BT, UK
- ¹⁶ 4 Department of Computer Science, University College London, Gower Street,
- 17 London, WC1E 6BT, UK
- 5 Institute of Zoology, Zoological Society of London, Regents Park, London, NW1
- 19 4RY, UK
- ²⁰ † First authorship shared.
- 21 Corresponding authors:
- 22 Kate E. Jones,
- 23 Centre for Biodiversity and Environment Research,
- 24 Department of Genetics, Evolution and Environment,
- 25 University College London,
- 26 Gower Street,
- 27 London,
- 28 WC1E 6BT,

Lucas et al. A generalised random encounter model for animals

- 29 UK
- 30 kate.e.jones@ucl.ac.uk

- 32 Marcus J. Rowcliffe,
- 33 Institute of Zoology,
- ³⁴ Zoological Society of London,
- 35 Regents Park,
- 36 London,
- 37 NW1 4RY,
- 38 UK
- marcus.rowcliffe@ioz.ac.uk

40 ABSTRACT

1: Wildlife monitoring technology is advancing rapidly and the use of remote sensors such as camera traps and acoustic detectors is becoming common in both the
terrestrial and marine environments. Current methods to estimate abundance or
density require individual recognition of animals or knowing the distance of the
animal from the sensor, which is often difficult. A method without these requirements, the random encounter model (REM), has been successfully applied to estimate animal densities from count data generated from camera traps. However,
count data from acoustic detectors do not fit the assumptions of the REM due to
the directionality of animal signals.

2: We developed a generalised REM (gREM), to estimate absolute animal density from count data from both camera traps and acoustic detectors. We derived the gREM for different combinations of sensor detection widths and animal signal widths (a measure of directionality). We tested the accuracy and precision of this model using simulations of different combinations of sensor detection widths and animal signal widths, number of captures, and models of animal movement.

3: We find that the gREM produces accurate estimates of absolute animal density for all combinations of sensor detection widths and animal signal widths. However, larger sensor detection and animal signal widths were found to be more precise. While the model is accurate for all capture efforts tested, the precision of the estimate increases with the number of captures. We found no effect of different animal movement models on the accuracy and precision of the gREM.

4: We conclude that the gREM provides an effective method to estimate absolute animal densities from remote sensor count data over a range of sensor and animal signal widths. The gREM is applicable for count data obtained in both marine and terrestrial environments, visually or acoustically (e.g., big cats, sharks, birds, echolocating bats and cetaceans). As sensors such as camera traps and acoustic detectors become more ubiquitous, the gREM will be increasingly useful for monitoring unmarked animal populations across broad spatial, temporal and taxonomic scales.

Keywords. Acoustic detection, camera traps, marine, population monitoring, sim ulations, terrestrial

Introduction

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The density of animal populations is one of the fundamental measures in ecol-73 ogy and conservation and has important implications for a range of issues, such 74 as sensitivity to stochastic fluctuations (Wright & Hubbell, 1983) and extinction 75 risk (Purvis et al., 2000). Monitoring animal population changes in response to 76 anthropogenic pressure is becoming increasingly important as humans rapidly 77 modify habitats and change climates (Everatt et al., 2014). Sensor technology, such 78 as camera traps (Karanth, 1995; Rowcliffe & Carbone, 2008) and acoustic detectors (Acevedo & Villanueva-Rivera, 2006; Walters et al., 2012) are widely used to monitor changes in animal populations as they are efficient, relativity cheap and 81 non-invasive, allowing for surveys over large areas and long periods (Rowcliffe & Carbone, 2008; Kessel et al., 2014; Walters et al., 2013). However, converting sam-83 pled count data into estimates of density is problematic as detectability of animals 84 needs to be accounted for (Anderson, 2001). 85

Existing methods for estimating animal density often require additional infor-86 mation that is often unavailable. For example, capture-mark-recapture methods 87 (Karanth, 1995; Borchers et al., 2014) require recognition of individuals, and dis-88 tance methods (Harris et al., 2013) require estimates of how far away individuals are from the sensor (Barlow & Taylor, 2005; Marques et al., 2011). When individuals cannot be told apart, an extension of occupancy modelling can be used to estimate absolute abundance (Royle & Nichols, 2003). However, as the model is 92 originally formulated to estimate occupancy, count information is simplified to 93 presence-absence data. Assumptions about the distribution of individuals (e.g. a 94 poisson distribution) must also be made (Royle & Nichols, 2003) which may be a 95 poor assumption for nonrandomly distributed species. Furthermore repeat, inde-96 pendent surveys must be performed and the definition of a site can be difficult, 97 especially for wide-ranging species (MacKenzie & Royle, 2005).

More recently, the development of the random encounter model (REM), a mod-99 ification of an ideal gas model (Yapp, 1956; Hutchinson & Waser, 2007), has en-100 abled animal densities to be estimated from unmarked individuals of a known 101 speed, and with known sensor detection parameters (Rowcliffe et al., 2008). The 102 REM method has been successfully applied to estimate animal densities from cam-103 era trap surveys (Zero et al., 2013). However, extending the REM method to other 104 types of sensors (e.g., acoustic detectors) is more problematic, because the original 105 derivation assumes a relatively narrow sensor width (up to $\pi/2$ radians) and that 106 the animal is equally detectable irrespective of its heading (Rowcliffe et al., 2008). 107 Whilst these restrictions are not problematic for most camera trap makes (e.g., 108 Reconyx, Cuddeback), the REM cannot be used to estimate densities from camera traps with a wider sensor width (e.g. canopy monitoring with fish eye lenses, Brusa & Bunker (2014)). Additionally, the REM method is not useful in estimating 111 densities from acoustic survey data as acoustic detector angles are often wider 112 than $\pi/2$ radians. Acoustic detectors are designed for a range of diverse tasks 113 and environments (Kessel et al., 2014), which naturally leads to a wide range of 114

There has been a sharp rise in interest around passive acoustic detectors in recent years, with a 10 fold increase in publications in the decade between 2000 and 2010 (Kessel *et al.*, 2014). Acoustic monitoring is being developed to study many aspects of ecology, including the interactions of animals and their environments (Blumstein *et al.*, 2011; Rogers *et al.*, 2013), the presence and relative abundances of species (Marcoux *et al.*, 2011), biodiversity of an area (Depraetere *et al.*, 2012), and monitoring population trends (Walters *et al.*, 2013).

sensor detection widths and detection distances. In addition to this, calls emitted

by many animals are directional (Blumstein et al., 2011), breaking the assumption

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of the REM method.

Acoustic data suffers from many of the problems associated with data from camera trap surveys in that individuals are often unmarked, making capture-mark-recapture methods more difficult to use (Marques *et al.*, 2013). In some cases the distance between the animal and the sensor is known, for example when an array of sensors is deployed and the position of the animal is estimated by triangulation (Lewis *et al.*, 2007). In these situations distance-sampling methods can be

applied, a method typically used for marine mammals (Rogers et al., 2013). How-131 ever, in many cases distance estimation is not possible, for example when single 132 sensors are deployed, a situation typical in the majority of terrestrial acoustic sur-133 veys (Buckland et al., 2008). In these cases, only relative measures of local abun-134 dance can be calculated, and not absolute densities. This means that comparison 135 of populations between species and sites is problematic without assuming equal 136 detectability (Schmidt, 2003; Walters et al., 2013). Equal detectability is unlikely be-137 cause of differences in environmental conditions, sensor type, habitat, and species 138 biology. 139

In this study, we create a generalised REM (gREM) as an extension to the camera trap model of Rowcliffe *et al.* (2008), to estimate absolute density from count data from acoustic detectors, or camera traps, where the sensor width can vary from 0 to 2π radians, and the signal given from the animal can be directional. We assessed the accuracy and precision of the gREM within a simulated environment, by varying the sensor detection widths, animal signal widths, number of captures and models of animal movement. We use the simulation results to recommend best survey practice for estimating animal densities from remote sensors.

148 METHODS

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Analytical Model. The REM presented by Rowcliffe et al. (2008) adapts the gas 149 model to count data collected from camera trap surveys. The REM is derived 150 assuming a stationary sensor with a detection width less than $\pi/2$ radians. How-151 ever, in order to apply this approach more generally, and in particular to stationary acoustic detectors, we need both to relax the constraint on sensor detection width, 153 and allow for animals with directional signals. Consequently, we derive the gREM 154 for any detection width, θ , between 0 and 2π with a detection distance r giving a 155 circular sector within which animals can be captured (the detection zone) (Fig-156 ure 1). Additionally, we model the animal as having an associated signal width 157 α between 0 and 2π (Figure 1, see Appendix S1 for a list of symbols). We start 158 deriving the gREM with the simplest situation, the gas model where $\theta = 2\pi$ and 159 $\alpha = 2\pi$. 160

Gas Model. Following Yapp (1956), we derive the gas model where sensors can capture animals in any direction and animal signals are detectable from any direction ($\theta = 2\pi$ and $\alpha = 2\pi$). We assume that animals are in a homogeneous environment, and move in straight lines of random direction with velocity v. We allow that our stationary sensor can capture animals at a detection distance r and that if an animal moves within this detection zone they are captured with a probability of one; while outside this zone, animals are never captured.

In order to derive animal density, we need to consider relative velocity from the 168 reference frame of the animals. Conceptually, this requires us to imagine that all 169 animals are stationary and randomly distributed in space, while the sensor moves 170 with velocity v. If we calculate the area covered by the sensor during the survey 171 period, we can estimate the number of animals the sensor should capture. As a 172 circle moving across a plane, the area covered by the sensor per unit time is 2rv. 173 The expected number of captures, z, for a survey period of t, with an animal den-174 sity of D is z = 2rvtD. To estimate the density we rearrange to get D = z/2rvt. Note 175 that as z is the number of encounters, not individuals, the possibility of repeated 176 detections of the same individual is accounted for (Hutchinson & Waser, 2007). 177

gREM derivations for different detection and signal widths. Different combinations of 178 θ and α would be expected to occur (e.g., sensors have different detection widths 179 and animals have different signal widths). For different combinations θ and α , the 180 area covered per unit time is no longer given by 2rv. Instead of the size of the 181 sensor detection zone having a diameter of 2r, the size changes with the approach angle between the sensor and the animal. The width of the area within which an 183 animal can be detected is called the profile, p. The size of p depends on the signal 184 width, detector width and the angle that the animal approaches the sensor. The 185 size of the profile (averaged across all approach angles) is defined as the average 186 profile \bar{p} . However, different combinations of θ and α need different equations to 187 calculate \bar{p} . 188

We have identified the parameter space for the combinations of θ and α for which the derivation of the equations are the same (defined as sub-models in the

gREM) (Figure 2). For example, the gas model becomes the simplest gREM sub-191 model (upper right in Figure 2) and the REM from Rowcliffe et al. (2008) is another 192 gREM sub-model where $\theta < \pi/2$ and $\alpha = 2\pi$. We derive one gREM sub-model 193 SE2 as an example below, where $2\pi - \alpha/2 < \theta < 2\pi$, $0 < \alpha < \pi$ (see Appendix 194 S2 for derivations of all gREM sub-models). Any estimate of density would re-195 quire prior knowledge of animal velocity, v and animal signal width, α taken from 196 other sources, for example existing literature (Brinkløv et al., 2011; Carbone et al., 197 2005). Sensor width, θ , and detection distance, r would also need to be measured 198 or obtained from manufacturer specifications (Holderied & Von Helversen, 2003; 199 Adams et al., 2012). 200

focal angle, x_1 (Figure 3a). This is the angle taken from the centre line of the sensor. 202 Other focal angles are possible (x_2, x_3, x_4) and are used in other gREM sub-models 203 (see Appendix S2). As the size of the profile depends on the approach angle, we 204 present the derivation across all approach angles. When the sensor is directly 205 approaching the animal $x_1 = \pi/2$. 206 Starting from $x_1 = \pi/2$ until $\theta/2 + \pi/2 - \alpha/2$, the size of the profile is $2r \sin \alpha/2$ 207 (Figure 3b). During this first interval, the size of α limits the width of the profile. 208 When the animal reaches $x_1 = \theta/2 + \pi/2 - \alpha/2$ (Figure 3c), the size of the profile is 209 $r\sin(\alpha/2) + r\cos(x_1 - \theta/2)$ and the size of θ and α both limit the width of the profile 210 (Figure 3c). Finally, at $x_1 = 5\pi/2 - \theta/2 - \alpha/2$ until $x_1 = 3\pi/2$, the width of the profile 211 is again $2r \sin \alpha/2$ (Figure 3d) and the size of α again limits the width of the profile. 212 The profile width p for π radians of rotation (from directly towards the sensor 213 to directly behind the sensor) is completely characterised by the three intervals 214 (Figure 3b-d). Average profile width \bar{p} is calculated by integrating these profiles 215 over their appropriate intervals of x_1 and dividing by π which gives 216

Example derivation of SE2. In order to calculate \bar{p} , we have to integrate over the

$$\bar{p} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{\alpha}{2} + \frac{\theta}{2} - \frac{\alpha}{2}} 2r \sin \frac{\alpha}{2} dx_1 + \int_{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}} r \sin \frac{\alpha}{2} + r \cos \left(x_1 - \frac{\theta}{2} \right) dx_1 + \int_{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{3\pi}{2}} 2r \sin \frac{\alpha}{2} dx_1 \right)$$

$$= \frac{r}{\pi} \left(\theta \sin \frac{\alpha}{2} - \cos \frac{\alpha}{2} + \cos \left(\frac{\alpha}{2} + \theta \right) \right)$$

$$= qn \ 2$$

We then use this expression to calculate density

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$$D = z/vt\bar{p}.$$
 eqn 3

Rather than having one equation that describes \bar{p} globally, the gREM must be split into submodels due to discontinuous changes in p as α and β change. These 220 discontinuities can occur for a number of reasons such as a profile switching be-22 tween being limited by α and θ , the difference between very small profiles and 222 profiles of size zero, and the fact that the width of a sector stops increasing once 223 the central angle reaches π radians (i.e., a semi-circle is just as wide as a full circle). As an example, if α is small, there is an interval between Figure 3c and 3d where the 'blind spot' would prevent animals being detected giving p = 0. This would 226 require an extra integral in our equation, as simply putting our small value of α 227 into eqn 1 would not give us this integral of p = 0. 228 gREM submodel specifications were done by hand, and the integration was 229 done using SymPy (SymPy Development Team, 2014) in Python (Appendix S3). 230 The gREM submodels were checked by confirming that: (1) submodels adjacent 231 in parameter space were equal at the boundary between them; (2) submodels that 232 border $\alpha = 0$ had p = 0 when $\alpha = 0$; (3) average profile widths \bar{p} were between 0 233 and 2r and; (4) each integral, divided by the range of angles that it was integrated over, was between 0 and 2r. The scripts for these tests are included in Appendix 235 S3 and the R (Team, 2014) implementation of the gREM is given in Appendix S4. 236

Simulation Model. We tested the accuracy and precision of the gREM by devel-237 oping a spatially explicit simulation of the interaction of sensors and animals using 238 different combinations of sensor detection widths, animal signal widths, number 239 of captures, and models of animal movement. One hundred simulations were run 240

where each consisted of a 7.5 km by 7.5 km square with periodic boundaries. A stationary sensor of radius r, 10 m, was set up in the exact centre of each simulated 242 study area, covering seven sensor detection widths θ , between 0 and 2π (2/9 π , 243 $4/9\pi$, $6/9\pi$, $8/9\pi$, $10/9\pi$, $14/9\pi$, and 2π). Each sensor was set to record continuously 244 and to capture animal signals instantaneously from emission. Each simulation 245 was populated with a density of 70 animals km⁻², calculated from the equation in 246 Damuth (1981) as the expected density of mammals weighing 1 g. This density 247 therefore represents a reasonable estimate of density of individuals, given that the 248 smallest mammal is around 2 g (Jones et al., 2009). A total of 3937 individuals per 249 simulation were created which were placed randomly at the start of the simula-250 tion. 11 signal widths α between 0 and π were used $(1/11\pi, 2/11\pi, 3/11\pi, 4/11\pi,$ 251 $5/11\pi$, $6/11\pi$, $7/11\pi$, $8/11\pi$, $9/11\pi$, $10/11\pi$, π). 252 Each simulation lasted for N steps (14400) of duration T (15 minutes) giving a 253 total duration of 150 days. The individuals moved within each step with a dis-254 tance d, with an average speed, v. The distance, d, was sampled from a normal 255 distribution with mean distance, $\mu_d = vT$, and standard deviation, $\sigma_d = vT/10$, 256 where the standard deviation was chosen to scale with the average distance trav-257 elled. An average speed, $v = 40 \,\mathrm{km} \,\mathrm{day}^{-1}$, was chosen based on the largest day 258 range of terrestrial animals (Carbone et al., 2005), and represents the upper limit of 259 realistic speeds. At the end of each step, individuals were allowed to either remain 260 stationary for a time step (with a given probability, S), or change direction where 261 the change in direction has a uniform distribution in the interval [-A, A]. This re-262 sulted in seven different movement models where: (1) simple movement, where S 263 and A = 0; (2) stop-start movement, where (i) S = 0.25, A = 0, (ii) S = 0.5, A = 0, (iii) 264 S = 0.75, A = 0; (3) correlated random walk movement, where (i) S = 0, $A = \pi/3$, (ii) 265 $S=0, A=2\pi/3$, iii) $S=0, A=\pi$. Individuals were counted as they moved into the 266 detection zone of the sensor per simulation. 267 We calculated the estimated animal density from the gREM by summing the 268 number of captures per simulation and inputting these values into the correct 269 gREM submodel. The accuracy of the gREM was determined by comparing the 270 true simulation density with the estimated density. Precision of the gREM was determined by the standard deviation of estimated densities. We used this method to compare the accuracy and precision of all the gREM submodels. As these submodels are derived for different combinations of α and θ , the accuracy and precision of the submodels was used to determine the impact of different values of α and θ .

The influence of the number of captures and animal movement models on accuracy and precision was investigated using four different gREM submodels representative of the range α and θ values (submodels NW1, SW1, NE1, and SE3, Figure 2). From a random starting point we ran the simulation until a range of different capture numbers were recorded (from 10 to 100 captures), recorded the length of time this took, and estimated the animal density for each of the four submodels. These estimated densities were compared to the true density to assess the impact on the accuracy and precision of the gREM. We calculated the coefficient of variation in order to compare the precision of the density estimates from simulations with different expected numbers of captures. The gREM also assumes that individuals move continuously with straight-line movement (simple movement model) and we therefore assessed the impact of breaking the gREM assumptions. We used the four submodels to compare the accuracy and precision of a simple movement model, stop-start movement models (using different average amounts of time spent stationary), and random walk movement models. Finally, as the parameters $(\alpha, \beta, r \text{ and } v)$ are likely to be measured with error, we compared true simulation densities to densities estimated with parameters with errors of 0%, ±5% and ±10%, for all gREM submodels.

294 RESULTS

Analytical model. The equation for \bar{p} has been newly derived for each submodel 295 in the gREM, except for the gas model and REM which have been calculated pre-296 viously. However, many models, although derived separately, have the same ex-297 pression for \bar{p} . Figure 4 shows the expression for \bar{p} in each case. The general 298 equation for density, eqn 3, is used with the correct value of \bar{p} substituted. Al-299 though more thorough checks are performed in Appendix S3, it can be seen that 300 all adjacent expressions in Figure 4 are equal when expressions for the boundaries 301 between them are substituted in. 302

Simulation model.

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gREM submodels. All gREM submodels showed a high accuracy, i.e., the median difference between the estimated and true values was less than 2% across all mod-305 els (Figure 5). However, the precision of the submodels do vary, where the gas 306 model is the most precise and the SW7 sub model the least precise, having the 307 smallest and the largest interquartile range, respectively (Figure 5). The standard 308 deviation of the error between the estimated and true densities is strongly related 309 to both the sensor and signal widths (Appendix S5), such that larger widths have 310 lower standard deviations (greater precision) due to the increased capture rate of 311 these models. 312 Number of captures. Within the four gREM submodels tested (NW1, SW1, SE3, 313 NE1), the accuracy was not strongly affected by the number of captures. The me-314 dian difference between the estimated and true values was less than 15% across 315 all capture rates (Figure 6). However, the precision was dependent on the num-316 ber of captures across all four of the gREM submodels, where precision increases 317 as number of captures increases, as would be expected for any statistical estimate (Figure 6). For all gREM submodels, the the coefficient of variation falls to 10% at 100 captures. 320 Movement models. Within the four gREM submodels tested (NW1, SW1, SE3, NE1), 321 neither the accuracy or precision was affected by the average amount of time spent 322 stationary. The median difference between the estimated and true values was less 323 than 2% for each category of stationary time (0, 0.25, 0.5 and 0.75) (Figure 7a). 324 Altering the maximum change in direction in each step $(0, \pi/3, 2\pi/3, \text{ and } \pi)$ did 325 not affect the accuracy or precision of the four gREM submodels (Figure 7b). 326 Impact of parameter error. The percentage error in the density estimates across all 327 parameters and gREM submodels shows a similar response for under and over 328 estimated parameters, suggesting the accuracy is reasonable with respect to pa-329 rameter error (Appendix S6). The impact of parameter error on the precision of the 330 density estimate varies across gREM submodels and parameters, where α shows 331 the largest variation including the largest values. However, in all cases the per-332 centage error in the density estimate is not more than 5% greater than the error in 333 the parameter estimate (Appendix S6).

DISCUSSION 335

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Analytical model. We have developed the gREM such that it can be used to esti-336 mate density from acoustic sensors and camera traps. This has entailed a gener-337 alisation of the gas model and the REM in Rowcliffe et al. (2008) to be applicable 338 to any combination of sensor width θ and signal directionality α . We emphasise 339 that the approach is robust to multiple detections of the same individual. We have 340 used simulations to show, as a proof of principle, that these models are accurate and precise. 342

There are a number of possible extensions to the gREM which could be developed in the future. The original gas model was formulated for the case where both animals and sensor are moving (Hutchinson & Waser, 2007). Indeed any of the models which have animals that are equally detectable in all directions ($\alpha = 2\pi$) can be trivially expanded by replacing animal speed v with $v + v_s$ where v_s is the speed of the sensor. However, when the animal has a directional call the extension becomes less simple. The approach would be to calculate again the mean profile width. However, for each angle of approach, one would have to average the profile width for an animal facing in any direction (i.e., not necessarily moving towards the sensor) weighted by the relative velocity of that direction. There are a number of situations where a moving detector and animal could occur, e.g. an acoustic detector towed from a boat when studying porpoises (Kimura et al., 2014) or surveying echolocating bats from a moving car (Jones et al., 2013).

Interesting but unstudied problems impacting the gREM are firstly, edge effects caused by sensor trigger delays (the delay between sensing an animal and attempting to record the encounter) (Rovero et al., 2013), and secondly, sensors which repeatedly turn on an off during sampling (Jones et al., 2013). The second problem is particularly relevant to acoustic detectors which record ultrasound by time expansion. Here ultrasound is recorded for a set time period and then slowed down and played back, rendering the sensor 'deaf' periodically during sampling. Both of these problems may cause biases in the gREM, as animals can move through the detection zone without being detected. As the gREM assumes constant surveillance, the error created by switching the sensor on and off quickly will become more important if the sensor is only on for short periods of time. We recommend that the gREM is applied to constantly sampled data, and the impacts of breaking these assumptions on the gREM should be further explored.

Accuracy, Precision and Recommendations for Best Practice. Based on our sim-369 ulations, we believe that the gREM has the potential to produce accurate estimates for many different species, using either camera traps or acoustic detectors. How-371 ever, the precision of the gREM differed between submodels. For example, when 372 the sensor and signal width were small, the precision of the model was reduced. 373 Therefore when choosing a sensor for use in a gREM study, the sensor detection 374 width should be maximised. If the study species has a narrow signal direction-375 ality, other aspects of the study protocol, such as length of the survey, should be 376 used to compensate. 377

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The precision of the gREM is greatly affected by the number of captures. The coefficient of variation falls dramatically between 10 and 60 captures and then after this continues to slowly reduce. At 100 captures the submodels reach 10% coefficient of variation, considered to be a very good level of precision and better than many previous studies (Thomas & Marques, 2012; O'Brien *et al.*, 2003; Foster & Harmsen, 2012). The length of surveys in the field will need to be adjusted so that enough data can be collected to reach this precision level. Populations of fast moving animals or populations with high densities will require less survey effort than those species that are slow moving or have populations with low densities.

We found that the sensitivity of the gREM to inaccurate parameter estimates 387 was both predictable and reasonable (Appendix S6), although this varies between different parameters and gREM submodels. Whilst care should be taken in pa-389 rameter estimation when analysing both acoustic and camera trap data, acoustic 390 data poses particular problems. For acoustic surveys, estimates of r (detection 391 distance) can be measured directly or calculated using sound attenuation models 392 (Holderied & Von Helversen, 2003), while the sensor angle is often easily mea-393 sured (Adams et al., 2012) or found in the manufacturer's specifications. When 394 estimating animal movement speed v, only the speed of movement during the 395 survey period should be used. The signal width is the most sensitive parameter 396

to inaccurate estimates (Appendix S6) and is also the most difficult to measure. While this parameter will typically be assumed to be 2π for camera trap surveys, fewer estimates exist for acoustic signal widths. Although signal width has been measured for echolocating bats using arrays of microphones (Brinkløv *et al.*, 2011), more work should be done on obtaining estimates for a range of acoustically surveyed species.

Limitations. Although the REM has been found to be effective in field tests (Row-403 cliffe et al., 2008; Zero et al., 2013), the gREM requires further validation by both 404 field tests and simulations. For example, capture-mark-recapture methods could 405 be used alongside the gREM to test the accuracy under field conditions (Rowcliffe 406 et al., 2008). While we found no effect of the movement model on the accuracy 407 or precision of the gREM, the models we have used in our simulations to vali-408 date the gREM are still simple representations of true animal movement. Animal movement may be highly nonlinear and often dependent on multiple factors such as behavioural state and existence of home ranges (Smouse et al., 2010). Therefore testing the gREM against real animal data, or further simulations with more 412 complex movement models, would be beneficial. 413

The assumptions of our simulations may require further consideration, for ex-414 ample we have assumed an equal density across the study area. However, in 415 a field environment the situation may be more complex, with additional varia-416 tion coming from local changes in density between sensor sites. Athough unequal 417 densities should theoretically not affect accuracy (Hutchinson & Waser, 2007), it 418 will affect precision and further simulations should be used to quantify this effect. Additionally, we allowed the sensor to be stationary and continuously detecting, 420 negating the triggering, and non-continuous recording issues that could exist with 421 some sensors and reduce precision or accuracy. Finally, in the simulation animals 422 moved at the equivalent of the largest day range of terrestrial animals (Carbone 423 et al., 2005). Slower speed values should not alter the accuracy of the gREM, but 424 precision would be affected since slower speeds produce fewer records. The gREM 425 was both accurate and precise for all the movement models we tested (stop-start 426 movement and correlated random walks). 427

A feature of the gREM is that it does not fit a statistical model to estimate detection probability as occupancy models and distance sampling do (Royle & Nichols, 2003; Barlow & Taylor, 2005; Marques *et al.*, 2011). Instead it explicitly models the process, with animals only being detected if they approach the sensor from a suitable direction. Other processes that affect detection probability could be included in the model to improve realism.

Implications for ecology and conservation. The gREM is applicable for count 434 data obtained either visually or acoustically in both marine and terrestrial environments, and is suitable for taxa including echolocating bats (Walters et al., 2012), songbirds (Buckland & Handel, 2006), whales (Marques et al., 2011) and forest pri-437 mates (Hassel-Finnegan et al., 2008). Many of these taxa contain critically endan-438 gered species and monitoring their populations is of conservation interest. For ex-439 ample, current methods of density estimation for the threatened Franciscana dol-440 phin (Pontoporia blainvillei) may result in underestimation of their numbers (Cre-441 spo et al., 2010). In addition, using gREM may be easier than other methods for 442 measuring the density of animals which may be useful in quantifying ecosystem 443 services, such as songbirds with a known positive influence on pest control (Jirinec et al., 2011).

The gREM will aid researchers to study species with non-invasive methods 446 such as remote sensors, which allows for large, continuous monitoring projects 447 with limited human resources (Kelly et al., 2012). The gREM is also suitable for 448 species that are sensitive to human contact or are difficult or dangerous to catch 449 (Thomas & Marques, 2012). As sensors such as camera traps and acoustic detec-450 tors become more ubiquitous, the gREM will be increasingly useful for monitor-451 ing unmarked animal populations across broad spatial, temporal and taxonomic 452 scales. 453

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- Acevedo, M.A. & Villanueva-Rivera, L.J. (2006) Using automated digital recording

REFERENCES

- systems as effective tools for the monitoring of birds and amphibians. Wildlife
- Society Bulletin, **34**, 211–214.

- Adams, A., Jantzen, M., Hamilton, R. & Fenton, M. (2012) Do you hear what I
- hear? Implications of detector selection for acoustic monitoring of bats. Methods
- in Ecology and Evolution.
- 468 Anderson, D.R. (2001) The need to get the basics right in wildlife field studies.
- 469 Wildlife Society Bulletin, **29**, 1294–1297.
- Barlow, J. & Taylor, B. (2005) Estimates of sperm whale abundance in the north-
- eastern temperate pacific from a combined acoustic and visual survey. Marine
- 472 *Mammal Science*, **21**, 429–445.
- Blumstein, D.T., Mennill, D.J., Clemins, P., Girod, L., Yao, K., Patricelli, G., Deppe,
- J.L., Krakauer, A.H., Clark, C., Cortopassi, K.A. et al. (2011) Acoustic monitoring
- in terrestrial environments using microphone arrays: applications, technologi-
- cal considerations and prospectus. *Journal of Applied Ecology*, **48**, 758–767.
- Borchers, D., Distiller, G., Foster, R., Harmsen, B. & Milazzo, L. (2014) Continuous-
- time spatially explicit capture–recapture models, with an application to a jaguar
- camera-trap survey. *Methods in Ecology and Evolution*, **5**, 656–665.
- 480 Brinkløv, S., Jakobsen, L., Ratcliffe, J., Kalko, E. & Surlykke, A. (2011) Echoloca-
- tion call intensity and directionality in flying short-tailed fruit bats, Carollia per-
- spicillata (phyllostomidae). The Journal of the Acoustical Society of America, 129,
- 483 427–435.
- Brusa, A. & Bunker, D.E. (2014) Increasing the precision of canopy closure es-
- timates from hemispherical photography: Blue channel analysis and under-
- exposure. *Agricultural and Forest Meteorology*, **195**, 102–107.
- Buckland, S.T. & Handel, C. (2006) Point-transect surveys for songbirds: robust
- methodologies. *The Auk*, **123**, 345–357.

- Buckland, S.T., Marsden, S.J. & Green, R.E. (2008) Estimating bird abundance:
- making methods work. Bird Conservation International, 18, S91–S108.
- 491 Carbone, C., Cowlishaw, G., Isaac, N.J. & Rowcliffe, J.M. (2005) How far do ani-
- mals go? Determinants of day range in mammals. The American Naturalist, 165,
- 493 290-297.
- 494 Crespo, E.A., Pedraza, S.N., Grandi, M.F., Dans, S.L. & Garaffo, G.V. (2010) Abun-
- dance and distribution of endangered Franciscana dolphins in Argentine waters
- and conservation implications. *Marine Mammal Science*, **26**, 17–35.
- Damuth, J. (1981) Population density and body size in mammals. Nature, 290,
- 498 699–700.
- Depraetere, M., Pavoine, S., Jiguet, F., Gasc, A., Duvail, S. & Sueur, J. (2012) Mon-
- itoring animal diversity using acoustic indices: implementation in a temperate
- woodland. Ecological Indicators, 13, 46–54.
- 502 Everatt, K.T., Andresen, L. & Somers, M.J. (2014) Trophic scaling and occupancy
- analysis reveals a lion population limited by top-down anthropogenic pressure
- in the Limpopo National Park, Mozambique. *PloS one*, **9**, e99389.
- Foster, R.J. & Harmsen, B.J. (2012) A critique of density estimation from camera-
- trap data. The Journal of Wildlife Management, 76, 224–236.
- 507 Harris, D., Matias, L., Thomas, L., Harwood, J. & Geissler, W.H. (2013) Applying
- distance sampling to fin whale calls recorded by single seismic instruments in
- the northeast Atlantic. The Journal of the Acoustical Society of America, 134, 3522–
- 510 3535.
- Hassel-Finnegan, H.M., Borries, C., Larney, E., Umponjan, M. & Koenig, A. (2008)
- How reliable are density estimates for diurnal primates? *International Journal of*
- 513 *Primatology*, **29**, 1175–1187.
- Holderied, M. & Von Helversen, O. (2003) Echolocation range and wingbeat pe-
- riod match in aerial-hawking bats. *Proc R Soc B*, **270**, 2293–2299.
- Hutchinson, J.M.C. & Waser, P.M. (2007) Use, misuse and extensions of "ideal gas"
- models of animal encounter. Biological Reviews of the Cambridge Philosophical So-
- 518 *ciety*, **82**, 335–359.
- 519 Jirinec, V., Campos, B.R. & Johnson, M.D. (2011) Roosting behaviour of a migratory
- songbird on Jamaican coffee farms: landscape composition may affect delivery

- of an ecosystem service. *Bird Conservation International*, **21**, 353–361.
- Jones, K.E., Bielby, J., Cardillo, M., Fritz, S.A., O'Dell, J., Orme, C.D.L., Safi, K.,
- 523 Sechrest, W., Boakes, E.H., Carbone, C., Connolly, C., Cutts, M.J., Foster, J.K.,
- Grenyer, R., Habib, M., Plaster, C.A., Price, S.A., Rigby, E.A., Rist, J., Teacher,
- A., Bininda-Emonds, O.R.P., Gittleman, J.L., Mace, G.M., Purvis, A. & Michener,
- W.K. (2009) PanTHERIA: a species-level database of life history, ecology, and
- geography of extant and recently extinct mammals. *Ecology*, **90**, 2648.
- Jones, K.E., Russ, J.A., Bashta, A.T., Bilhari, Z., Catto, C., Csősz, I., Gorbachev,
- 529 A., Győrfi, P., Hughes, A., Ivashkiv, I., Koryagina, N., Kurali, A., Langton, S.,
- Collen, A., Margiean, G., Pandourski, I., Parsons, S., Prokofev, I., Szodoray-
- Paradi, A., Szodoray-Paradi, F., Tilova, E., Walters, C.L., Weatherill, A. &
- Zavarzin, O. (2013) Indicator bats program: A system for the global acoustic
- monitoring of bats. B. Collen, N. Pettorelli, J.E.M. Baillie & S.M. Durant, eds.,
- Biodiversity Monitoring and Conservation, pp. 211–247. Wiley-Blackwell.
- Karanth, K. (1995) Estimating tiger (Panthera tigris) populations from camera-trap
- data using capture–recapture models. *Biological Conservation*, **71**, 333–338.
- Kelly, M.J., Betsch, J., Wultsch, C., Mesa, B. & Mills, L.S. (2012) Noninvasive sam-
- pling for carnivores. L. Boitani & R. Powell, eds., Carnivore ecology and conserva-
- tion: a handbook of techniques, pp. 47–69. Oxford University Press, New York.
- Kessel, S., Cooke, S., Heupel, M., Hussey, N., Simpfendorfer, C., Vagle, S. & Fisk, A.
- 541 (2014) A review of detection range testing in aquatic passive acoustic telemetry
- studies. *Reviews in Fish Biology and Fisheries*, **24**, 199–218.
- Kimura, S., Akamatsu, T., Dong, L., Wang, K., Wang, D., Shibata, Y. & Arai, N.
- (2014) Acoustic capture-recapture method for towed acoustic surveys of echolo-
- cating porpoises. *The Journal of the Acoustical Society of America*, **135**, 3364–3370.
- Lewis, T., Gillespie, D., Lacey, C., Matthews, J., Danbolt, M., Leaper, R.,
- McLanaghan, R. & Moscrop, A. (2007) Sperm whale abundance estimates from
- acoustic surveys of the Ionian Sea and Straits of Sicily in 2003. Journal of the
- Marine Biological Association of the United Kingdom, 87, 353–357.
- MacKenzie, D.I. & Royle, J.A. (2005) Designing occupancy studies: general advice
- and allocating survey effort. *Journal of Applied Ecology*, **42**, 1105–1114.

- Marcoux, M., Auger-Méthé, M., Chmelnitsky, E.G., Ferguson, S.H. & Humphries,
- 553 M.M. (2011) Local passive acoustic monitoring of narwhal presence in the Cana-
- dian Arctic: a pilot project. Arctic, 64, 307–316.
- Marques, T.A., Munger, L., Thomas, L., Wiggins, S. & Hildebrand, J.A. (2011) Es-
- timating North Pacific right whale (Eubalaena japonica) density using passive
- acoustic cue counting. *Endangered Species Research*, **13**, 163–172.
- Marques, T.A., Thomas, L., Martin, S.W., Mellinger, D.K., Ward, J.A., Moretti, D.J.,
- Harris, D. & Tyack, P.L. (2013) Estimating animal population density using pas-
- sive acoustics. *Biological Reviews*, **88**, 287–309.
- O'Brien, T.G., Kinnaird, M.F. & Wibisono, H.T. (2003) Crouching tigers, hidden
- prey: Sumatran tiger and prey populations in a tropical forest landscape. *Animal*
- 563 *Conservation*, **6**, 131–139.
- Purvis, A., Gittleman, J.L., Cowlishaw, G. & Mace, G.M. (2000) Predicting extinc-
- tion risk in declining species. Proceedings of the Royal Society of London Series B:
- 566 Biological Sciences, **267**, 1947–1952.
- Rogers, T.L., Ciaglia, M.B., Klinck, H. & Southwell, C. (2013) Density can be mis-
- leading for low-density species: benefits of passive acoustic monitoring. Public
- Library of Science One, 8, e52542.
- Rovero, F., Zimmermann, F., Berzi, D. & Meek, P. (2013) "Which camera trap type
- and how many do I need?" a review of camera features and study designs for a
- range of wildlife research applications. *Hystrix*, **24**, 148–156.
- Rowcliffe, J.M. & Carbone, C. (2008) Surveys using camera traps: are we looking
- to a brighter future? *Animal Conservation*, **11**, 185–186.
- Rowcliffe, J., Field, J., Turvey, S. & Carbone, C. (2008) Estimating animal density
- using camera traps without the need for individual recognition. Journal of Ap-
- plied Ecology, **45**, 1228–1236.
- Royle, J.A. & Nichols, J.D. (2003) Estimating abundance from repeated presence-
- absence data or point counts. *Ecology*, **84**, 777–790.
- 580 Schmidt, B.R. (2003) Count data, detection probabilities, and the demography, dy-
- namics, distribution, and decline of amphibians. Comptes Rendus Biologies, 326,
- 582 119–124.

- 583 Smouse, P.E., Focardi, S., Moorcroft, P.R., Kie, J.G., Forester, J.D. & Morales, J.M.
- (2010) Stochastic modelling of animal movement. Philosophical Transactions of the
- Royal Society B: Biological Sciences, **365**, 2201–2211.
- 586 SymPy Development Team (2014) SymPy: Python library for symbolic mathematics.
- Team, R.C. (2014) R: A Language and Environment for Statistical Computing. R Foun-
- dation for Statistical Computing, Vienna, Austria.
- Thomas, L. & Marques, T.A. (2012) Passive acoustic monitoring for estimating an-
- imal density. *Acoustics Today*, **8**, 35–44.
- ⁵⁹¹ Walters, C.L., Collen, A., Lucas, T., Mroz, K., Sayer, C.A. & Jones, K.E. (2013) Chal-
- lenges of using bioacoustics to globally monitor bats. R.A. Adams & S.C. Ped-
- ersen, eds., Bat Evolution, Ecology, and Conservation, pp. 479–499. Springer.
- Walters, C.L., Freeman, R., Collen, A., Dietz, C., Brock Fenton, M., Jones, G., Obrist,
- 595 M.K., Puechmaille, S.J., Sattler, T., Siemers, B.M. et al. (2012) A continental-scale
- tool for acoustic identification of European bats. Journal of Applied Ecology, 49,
- 597 1064–1074.
- 598 Wright, S.J. & Hubbell, S.P. (1983) Stochastic extinction and reserve size: a focal
- species approach. Oikos, pp. 466–476.
- Yapp, W. (1956) The theory of line transects. Bird Study, 3, 93–104.
- ⁶⁰¹ Zero, V.H., Sundaresan, S.R., O'Brien, T.G. & Kinnaird, M.F. (2013) Monitoring
- an endangered savannah ungulate, Grevy's zebra (Equus grevyi): choosing a
- method for estimating population densities. *Oryx*, **47**, 410–419.

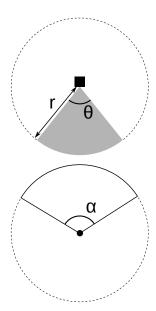


Figure 1. Representation of sensor detection width and animal signal width. The filled square and circle represent a sensor and an animal, respectively; θ , sensor detection width (radians); r, sensor detection distance; dark grey shaded area, sensor detection zone; α , animal signal width (radians). Dashed lines around the filled square and circle represents the maximum extent of θ and α , respectively.

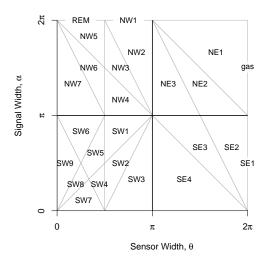


Figure 2. Locations where derivation of the average profile \bar{p} is the same for different combinations of sensor detection and animal signal widths. Symbols within each polygon refer to each gREM submodel named after their compass point, except for Gas and REM which highlight the position of these previously derived models within the gREM. Symbols on the edge of the plot are for submodels where $\alpha, \theta = 2\pi$

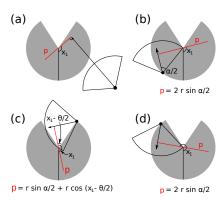


Figure 3. An overview of the derivation of the average profile \bar{p} for the gREM submodel SE2, where (a) shows the location of the profile *p* (the line an animal must pass through in order to be captured) in red and the focal angle, x_1 , for an animal (filled circle), its signal (unfilled sector), and direction of movement (shown as an arrow). The detection zone of the sensor is shown as a filled grey sector with a detection distance of r. The vertical black line within the circle shows the direction the sensor is facing. The derivation of p changes as the animal approaches the sensor from different directions (shown in b-d), where (b) is the derivation of p when x_1 is in the interval $\left[\frac{\pi}{2}, \frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}\right]$, (c) p when x_1 is in the interval $\left[\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}, \frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}\right]$ and (d) p when x_1 is in the interval $\left[\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}, \frac{3\pi}{2}\right]$, where θ , sensor detection width; α , animal signal width. The resultant equation for p is shown beneath bd. The average profile \bar{p} is the size of the profile averaged across all approach angles.

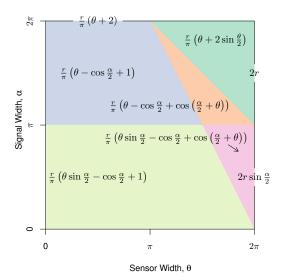


Figure 4. Expressions for the average profile width, \bar{p} , given a range of sensor and signal widths. Despite independent derivation within each block, many models result in the same expression. These are collected together and presented as one block of colour. Expressions on the edge of the plot are for submodels with α , $\theta = 2\pi$.

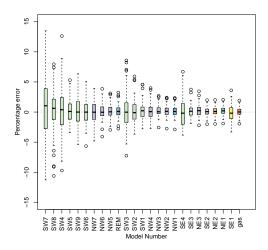


Figure 5. Simulation model results of the accuracy and precision for gREM submodels. The percentage error between estimated and true density for each gREM sub model is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Box colours correspond to the expressions for average profile width \bar{p} given in Figure 4.

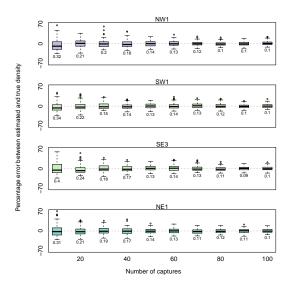


Figure 6. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different numbers of captures. The percentage error between estimated and true density within each gREM sub model for capture rate is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Sensor and signal widths vary between submodels. The numbers beneath each plot represent the coefficient of variation. The colour of each box plot corresponds to the expressions for average profile width \bar{p} given in Figure 4.

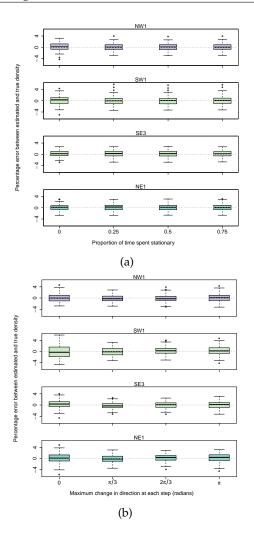


Figure 7. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different movement models where (a) average amount of time spent stationary (stop-start movement) and (b) maximum change in direction at each step (correlated random walk model). The percentage error between estimated and true density within each gREM sub model for the different movement models is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. The simple model is represented where time and maximum change in direction equals 0. The colour of each box plot corresponds to the expressions for average profile width \bar{p} given in Figure 4.