1 A GENERALISED RANDOM ENCOUNTER MODEL FOR ESTIMATING 2 ANIMAL DENSITY WITH REMOTE SENSOR DATA

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40 ABSTRACT

1: Wildlife monitoring technology is advancing rapidly and the use of remote sensors such as camera traps and acoustic detectors is becoming common in both the
terrestrial and marine environments. Current methods to estimate abundance or
density require individual recognition of animals or knowing the distance of the
animal from the sensor, which is often difficult. A method without these requirements, the random encounter model (REM), has been successfully applied to estimate animal densities from count data generated from camera traps. However,
count data from acoustic detectors do not fit the assumptions of the REM due to
the directionality of animal signals.

2: We developed a generalised REM (gREM), to estimate absolute animal density from count data from both camera traps and acoustic detectors. We derived the gREM for different combinations of sensor detection widths and animal signal widths (a measure of directionality). We tested the accuracy and precision of this model using simulations of different combinations of sensor detection widths and animal signal widths, number of captures, and models of animal movement.

3: We find that the gREM produces accurate estimates of absolute animal density for all combinations of sensor detection widths and animal signal widths. However, larger sensor detection and animal signal widths were found to be more precise. While the model is accurate for all capture efforts tested, the precision of the estimate increases with the number of captures. We found no effect of different animal movement models on the accuracy and precision of the gREM.

4: We conclude that the gREM provides an effective method to estimate absolute animal densities from remote sensor count data over a range of sensor and animal signal widths. The gREM is applicable for count data obtained in both marine and terrestrial environments, visually or acoustically (e.g., big cats, sharks, birds, echolocating bats and cetaceans). As sensors such as camera traps and acoustic detectors become more ubiquitous, the gREM will be increasingly useful for monitoring unmarked animal populations across broad spatial, temporal and taxonomic scales.

Keywords. Acoustic detection, camera traps, marine, population monitoring, simulations, terrestrial

INTRODUCTION

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Animal population density is one of the fundamental measures in ecology and 73 conservation. The density of a population has important implications for a range of issues such as sensitivity to stochastic fluctuations (Richter-Dyn & Goel, 1972; 75 Wright & Hubbell, 1983) and risk of extinction (Purvis et al., 2000). Monitoring 76 animal population changes in response to anthropogenic pressure is becoming 77 increasingly important as humans rapidly modify habitats and change climates (Everatt et al., 2014). Sensor technology, such as camera traps (Karanth, 1995; Row-79 cliffe & Carbone, 2008) and acoustic detectors (Clark, 1995; Acevedo & Villanueva-80 Rivera, 2006; Walters et al., 2012) are becoming widely used to monitor changes in animal populations (Rowcliffe & Carbone, 2008; Kessel et al., 2014; Walters et al., 2013), as they are efficient, relativity cheap and non-invasive (Cutler & Swann, 1999), allowing for surveys over large areas and long periods. However, converting sampled count data into estimates of density is problematic as detectability of 85 animals needs to be accounted for (Anderson, 2001). 86

Existing methods for estimating animal density often require additional infor-87 mation that is often unavailable. For example, capture-mark-recapture methods 88 (Karanth, 1995; Trolle et al., 2007; Borchers et al., 2014) require recognition of indi-89 viduals, and distance methods (Harris et al., 2013) require an estimation of how far away individuals are from the sensor (Barlow & Taylor, 2005; Marques et al., 2011). More recently, the development of the random encounter model (REM) (a modification of a gas model) has enabled animal densities to be estimated from 93 unmarked individuals of a known speed, and with known sensor detection parameters (Rowcliffe et al., 2008). The REM method has been successfully applied 95 to estimate animal densities from camera trap surveys (Manzo et al., 2012; Zero 96 et al., 2013). However, extending the REM method to other types of sensors (e.g., 97 acoustic detectors) is more problematic, because the original derivation assumes a 98 relatively narrow sensor width (up to $\pi/2$ radians) and that the animal is equally detectable irrespective of its heading (Rowcliffe et al., 2008).

Whilst these restrictions are not problematic for most camera trap makes (e.g., 101 Reconyx, Cuddeback), the REM cannot be used to estimate densities from camera 102 traps with a wider sensor width (e.g. canopy monitoring with fish eye lenses, 103 Brusa & Bunker (2014)). Additionally, the REM method is not useful in estimating 104 densities from acoustic survey data as acoustic detector angles are often wider 105 than $\pi/2$ radians. Acoustic detectors are designed for a range of diverse tasks 106 and environments (Kessel et al., 2014), which naturally leads to a wide range of 107 sensor detection widths and detection distances. In addition to this, calls emitted 108 by many animals are directional (Blumstein et al., 2011), breaking the assumption 109 of the REM method. 110

There has been a sharp rise in interest around passive acoustic detectors in recent years, with a 10 fold increase in publications in the decade between 2000 and 2010 (Kessel *et al.*, 2014). Acoustic monitoring is being developed to study many aspects of ecology, including the interactions of animals and their environments (Blumstein *et al.*, 2011; Rogers *et al.*, 2013), the presence and relative abundances of species (Marcoux *et al.*, 2011), biodiversity of an area (Depraetere *et al.*, 2012), and monitoring population trends (Walters *et al.*, 2013).

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Acoustic data suffers from many of the problems associated with data from 118 camera trap surveys in that individuals are often unmarked, so capture-mark-119 recapture methods cannot be used to estimate densities. In some cases the dis-120 tance between the animal and the sensor is known, for example when an array of 121 sensors is deployed and the position of the animal is estimated by triangulation 122 (Lewis et al., 2007). In these situations distance-sampling methods can be applied, 123 a method typically used for marine mammals (Rogers et al., 2013). However, in 124 many cases distance estimation is not possible, for example when single sensors 125 are deployed, a situation typical in the majority of terrestrial acoustic surveys (El-126 phick, 2008; Buckland et al., 2008). In these cases, only relative measures of local 127 abundance can be calculated, and not absolute densities. This means that compar-128 ison of populations between species and sites is problematic without assuming 129 equal detectability (Hayes, 2000; Schmidt, 2003; Walters et al., 2013). Equal de-130 tectability is unlikely because of differences in environmental conditions, sensor 131 type, habitat, and species biology.

In this study, we create a generalised REM (gREM) as an extension to the cam-133 era trap model of Rowcliffe et al. (2008), to estimate absolute density from count 134 data from acoustic detectors, or camera traps, where the sensor width can vary 135 from 0 to 2π radians, and the signal given from the animal can be directional. We 136 assessed the accuracy and precision of the gREM within a simulated environment, 137 by varying the sensor detection widths, animal signal widths, number of captures 138 and models of animal movement. We use the simulation results to recommend 139 best survey practice for estimating animal densities from remote sensors. 140

141 METHODS

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Analytical Model. The REM presented by Rowcliffe et al. (2008) adapts the gas 142 model to count data collected from camera trap surveys. The REM is derived 143 assuming a stationary sensor with a detection width less than $\pi/2$ radians. How-144 ever, in order to apply this approach more generally, and in particular to stationary 145 acoustic detectors, we need both to relax the constraint on sensor detection width, 146 and allow for animals with directional signals. Consequently, we derive the gREM 147 for any detection width, θ , between 0 and 2π with a detection distance r giving a circular sector within which animals can be captured (the detection zone) (Figure 1). Additionally, we model the animal as having an associated signal width 150 α between 0 and 2π (Figure 1, see Appendix S1 for a list of symbols). We start 151 deriving the gREM with the simplest situation, the gas model where $\theta = 2\pi$ and 152 $\alpha = 2\pi$. 153

Gas Model. Following Yapp (1956), we derive the gas model where sensors can capture animals in any direction and animal signals are detectable from any direction ($\theta = 2\pi$ and $\alpha = 2\pi$). We assume that animals are in a homogeneous environment, and move in straight lines of random direction with velocity v. We allow that our stationary sensor can capture animals at a detection distance r and that if an animal moves within this detection zone they are captured with a probability of one, while animals outside the zone are never captured.

In order to derive animal density, we need to consider relative velocity from the reference frame of the animals. Conceptually, this requires us to imagine that all animals are stationary and randomly distributed in space, while the sensor moves with velocity v. If we calculate the area covered by the sensor during the survey period, we can estimate the number of animals the sensor should capture. As a circle moving across a plane, the area covered by the sensor per unit time is 2rv. The number of expected captures, z, for a survey period of t, with an animal density of D is z = 2rvtD. To estimate the density, we rearrange to get D = z/2rvt.

gREM derivations for different detection and signal widths. Different combinations of 169 θ and α would be expected to occur (e.g., sensors have different detection widths 170 and animals have different signal widths). For different combinations θ and α , the 171 area covered per unit time is no longer given by 2rv. Instead of the size of the 172 sensor detection zone having a diameter of 2r, the size changes with the approach 173 angle between the sensor and the animal. For any given signal width and detec-174 tor width and depending on the angle that the animal approaches the sensor, the 175 width of the area within which an animal can be detected is called the profile, p. 176 The size of the profile (averaged across all approach angles) is defined as the average profile \bar{p} . However, different combinations of θ and α need different equations 178 to calculate \bar{p} . 179

We have identified the parameter space for the combinations of θ and α for which the derivation of the equations are the same (defined as sub-models in the gREM) (Figure 2). For example, the gas model becomes the simplest gREM sub-model (upper right in Figure 2) and the REM from Rowcliffe *et al.* (2008) is another gREM sub-model where $\theta < \pi/2$ and $\alpha = 2\pi$. We derive one gREM sub-model SE2 as an example below, where $2\pi - \alpha/2 < \theta < 2\pi$, $0 < \alpha < \pi$ (see Appendix S2 for derivations of all gREM sub-models).

Example derivation of SE2. In order to calculate \bar{p} , we have to integrate over the focal angle, x_1 (Figure 3a). This is the angle taken from the centre line of the sensor. Other focal angles are possible (x_2 , x_3 , x_4) and are used in other gREM sub-models (see Appendix S2). As the size of the profile depends on the approach angle, we present the derivation across all approach angles. When the sensor is directly approaching the animal $x_1 = \pi/2$.

Starting from $x_1 = \pi/2$ until $\theta/2 + \pi/2 - \alpha/2$, the size of the profile is $2r \sin \alpha/2$ (Figure 3b). During this first interval, the size of α limits the width of the profile.

When the animal reaches $x_1 = \theta/2 + \pi/2 - \alpha/2$ (Figure 3c), the size of the profile is $r \sin(\alpha/2) + r \cos(x_1 - \theta/2)$ and the size of θ and α both limit the width of the profile (Figure 3c). Finally, at $x_1 = 5\pi/2 - \theta/2 - \alpha/2$ until $x_1 = 3\pi/2$, the width of the profile is again $2r \sin \alpha/2$ (Figure 3d) and the size of α again limits the width of the profile. The profile width p for π radians of rotation (from directly towards the sensor to directly behind the sensor) is completely characterised by the three intervals (Figure 3b–d). Average profile width \bar{p} is calculated by integrating these profiles over their appropriate intervals of x_1 and dividing by π which gives

$$\bar{p} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}} 2r \sin \frac{\alpha}{2} dx_1 + \int_{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}} r \sin \frac{\alpha}{2} + r \cos \left(x_1 - \frac{\theta}{2} \right) dx_1 + \int_{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{3\pi}{2}} 2r \sin \frac{\alpha}{2} dx_1 \right)$$

$$= \frac{r}{\pi} \left(\theta \sin \frac{\alpha}{2} - \cos \frac{\alpha}{2} + \cos \left(\frac{\alpha}{2} + \theta \right) \right)$$

$$= qn \ 2$$

We then use this expression to calculate density

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$$D = z/vt\bar{p}.$$
 eqn 3

Rather than having one equation that describes \bar{p} globally, the gREM must be 205 split into submodels due to discontinuous changes in p as α and β change. These 206 discontinuities can occur for a number of reasons such as a profile switching be-207 tween being limited by α and θ , the difference between very small profiles and 208 profiles of size zero, and the fact that the width of a sector stops increasing once 209 the central angle reaches π radians (i.e., a semi-circle is just as wide as a full circle.) 210 As an example, if α is small, there is an interval between Figure 3c and 3d where the 'blind spot' would prevent animals being detected giving p = 0. This would require an extra integral in our equation, as simply putting our small value of α 213 into eqn 1 would not give us this integral of p = 0. 214 gREM submodel specifications were done by hand, and the integration was 215 done using SymPy (SymPy Development Team, 2014) in Python (Appendix S3). 216 The gREM submodels were checked by confirming that: (1) submodels adjacent 217 in parameter space were equal at the boundary between them; (2) submodels that 218

border $\alpha = 0$ had p = 0 when $\alpha = 0$; (3) average profile widths \bar{p} were between 0 and 2r and; (4) each integral, divided by the range of angles that it was integrated 220 over, was between 0 and 2r. The scripts for these tests are included in Appendix 221 S3 and the R (Team, 2014) implementation of the gREM is given in Appendix S4. 222

Simulation Model. We tested the accuracy and precision of the gREM by devel-

oping a spatially explicit simulation of the interaction of sensors and animals using 224 different combinations of sensor detection widths, animal signal widths, number 225 of captures, and models of animal movement. 100 simulations were run where 226 each consisted of a 7.5 km by 7.5 km square with periodic boundaries. A station-227 ary sensor of radius r was set up in the exact centre of each simulation, covering 228 seven sensor detection widths θ , between 0 and 2π (2/9 π , 4/9 π , 6/9 π , 8/9 π , 10/9 π , 229 $14/9\pi$, and 2π). Each sensor was set to record continuously and to capture ani-230 mal signals instantaneously from emission. Each simulation was populated with 231 a density of 70 animals km⁻², calculated from the equation in Damuth (1981) as the expected density of mammals weighing 1 g. This density therefore represents 233 a reasonable estimate of density of individuals, given that the smallest mammal is 234 around 2 g (Jones et al., 2009). A total of 3937 individuals per simulation were cre-235 ated which were placed randomly at the start of the simulation. Individuals were 236 assigned 11 signal widths α between 0 and π (1/11 π , 2/11 π , 3/11 π , 4/11 π , 5/11 π , 237 $6/11\pi$, $7/11\pi$, $8/11\pi$, $9/11\pi$, $10/11\pi$, π). 238 Each simulation lasted for N steps (14400) of duration T (15 minutes) giving a 239 total duration of 150 days. The individuals moved within each step with a dis-240 tance d, with an average speed, v. d, was sampled from a normal distribution with mean distance, $\mu_d = vT$, and standard deviation $\sigma_d = vT/10$. An average 242 speed, $v = 40 \,\mathrm{km} \,\mathrm{day}^{-1}$, was chosen as this is the largest day range of terrestrial an-243 imals (Carbone et al., 2005), and represents the upper limit of realistic speeds. At 244 the end step, individuals were allowed to either remain stationary for a time step 245 (with a given probability, S), or change direction (in a uniform distribution with a 246 maximum angle, A) between 0 and π . This resulted in seven different movement 247 models where: (1) simple movement, where S and A = 0; (2) stop-start movement, 248 where (i) S = 0.25, A = 0, (ii) S = 0.5, A = 0, (iii) S = 0.75, A = 0; (3) random walk movement, where (i) S = 0, $A = \pi/3$, (ii) S = 0, $A = 2\pi/3$, iii) S = 0, $A = \pi$. Individuals were counted as they moved in and out of the detection zone of the sensor per simulation.

We calculated the estimated animal density from the gREM by assuming the 253 number of captures per simulation and inputting these values into the correct 254 gREM submodel. gREM accuracy was determined by comparing the density in 255 the simulation with the estimated density. High accuracy is indicated by the mean 256 difference between the estimated and actual values not being significantly differ-257 ent from zero (Wilcoxon signed-rank test). gREM precision was determined by 258 the standard deviation of estimated densities. We used this method to compare 250 the accuracy and precision of all the gREM submodels. As these submodels are derived for different combinations of α and θ , the accuracy and precision of the submodels was used to determine the impact of different values of α and θ . 262

The influence of the number of captures and animal movement models on ac-263 curacy and precision was investigated using four different gREM submodels rep-264 resentative of the range α and θ values (submodels NW1, SW1, NE1, and SE3, 265 Figure 2). Using these four submodels, we calculated how long the simulation 266 needed to run to generate a range of different capture numbers (from 10 to 100 cap-267 tures in 10 unit intervals), and estimated animal density. These estimated densities 268 were compared to the real density to assess the impact on the accuracy and preci-269 sion of the gREM. We calculated the coefficient of variation in order the compare 270 the precision between capture numbers. The gREM also assumes that individuals move continuously with straight-line movement (simple movement model) and 272 we therefore assessed the impact of breaking the gREM assumptions. We used 273 the four submodels to compare the accuracy and precision of a simple movement 274 model, stop-start movement models (using different amounts of time spent sta-275 tionary), and random walk movement models. 276

277 RESULTS

Analytical model. The equation for \bar{p} has been newly derived for each submodel in the gREM, except for the gas model and REM which have been calculated previously. However, many models, although derived separately, have the same expression for \bar{p} . Figure 4 shows the expression for \bar{p} in each case. The general equation for density, using the correct expression for \bar{p} is then substituted into eqn 3. Although more thorough checks are performed in Appendix S3, it can be seen that all adjacent expressions in Figure 4 are equal when expressions for the boundaries between them are substituted in.

286 Simulation model.

gREM submodels. All gREM submodels showed a high accuracy, i.e., the mean dif-287 ference between the estimated and actual values was not significantly different 288 from zero across all models, at p <0.05, corrected for multiple tests (all gREM sub models Wilcoxon signed-rank test) (Figure 5). However, the precision of the sub-290 models do vary, where the gas model is the most precise and the SW7 sub model 291 the least precise, having the smallest and the largest interquartile range, respec-292 tively (Figure 5). The standard deviation of the error between the estimated and 293 true densities is strongly related to both the sensor and signal widths (Appendix 294 S5), such that larger widths have lower standard deviations (greater precision). 295

Number of captures. Within the four gREM submodels tested (NW1, SW1, SE3, 296 NE1), the accuracy was not affected by the number of captures. The mean differ-297 ence between the estimated and actual values was not significantly different from 298 zero across all capture rates, at p <0.05, corrected for multiple tests (Wilcoxon 299 signed-rank test) (Figure 6). However, the precision was dependent on the num-300 ber of captures across all four of the gREM submodels, where precision increases 301 as number of captures increases (Figure 6). For all gREM submodels, the the coef-302 ficient of variation falls to 10% at 100 captures. 303

Movement models. Within the four gREM submodels tested (NW1, SW1, SE3, NE1), neither the accuracy or precision was affected by the amount of time spent station-305 ary. The mean difference between the estimated and actual values was not signifi-306 cantly different from zero for each category of stationary time (0, 0.25, 0.5 and 0.75), 307 at p <0.05, corrected for multiple tests (all gREM sub models Wilcoxon signed-308 rank test) (Figure 7a). Altering the maximum change in direction in each step (0, 309 pi/3, 2pi/3, and pi) did not affect the accuracy or precision of the four gREM sub-310 models tested, at p <0.05, corrected for multiple testing (Wilcoxon signed-rank 311 test) (Figure 7b). 312

313 DISCUSSION

We have developed the gREM such that it can be used to estimate density from acoustic sensors and camera traps. This has entailed a generalisation of the gas model and the REM in Rowcliffe *et al.* (2008) to be applicable to any combination of sensor width and signal directionality. We have used simulations to show, as a proof of principle, that these models are accurate and precise. The precision of the gREM was found to be dependent on the width of the sensor and the signal, and the number of captures.

Analytical model. The gREM was derived for different combinations of α and θ 321 resulting in 25 different submodels, the expression for \bar{p} are equal for many of 322 these submodels resulting in eight different equations including the previously 323 derived gas model and REM. These submodels were tested for consistency with 324 adjacent expressions being equal at their boundaries. These new submodels will 325 allow researchers to evaluate the absolute density of animals that have previously been difficult to study, such as echolocating bats (Clement & Castleberry, 2013), 327 with non-invasive methods such as remote sensors. The gREM also allows the data from acoustic detectors to be used where an animal has a directional calls, 329 this could be used for a range of animals including songbirds (Blumstein et al., 330 2011), dolphins (Lammers & Au, 2003), as well as echolocating bats (Walters et al., 331 2013). 332

There are a number of possible extensions to the gREM which could be developed in the future. The original gas model was formulated for the case where both

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subjects, either animal and detector, or animal and animal, are moving (Hutchin-335 son & Waser, 2007). Indeed any of the models with animals that are equally de-336 tectable in all directions ($\alpha = 2\pi$) can be trivially expanded for moving by substi-337 tuting the sum of the average animal velocity and the sensor velocity for v as used 338 here. However, when the animal has a directional call, as seen in both terrestrial 339 and aquatic environments (Lammers & Au, 2003; Blumstein et al., 2011), the ex-340 tension becomes less simple. The approach would be to calculate again the mean 341 profile width. However, for each angle of approach, one would have to average 342 the profile width for an animal facing in any direction (i.e., not necessarily moving 343 towards the sensor) weighted by the relative velocity of that direction. There are 344 a number of situations where a moving detector and animal could occur, e.g. an acoustic detector towed from a boat when studying porpoises (Kimura et al., 2014) or surveying echolocating bats from a moving car (Ahlen & Baagøe, 1999; Jones 347 et al., 2013). 348

Interesting but unstudied problems impacting the gREM are firstly, edge effects 349 caused by sensor trigger delays (the delay between sensing an animal and attempt-350 ing to record the encounter) (Rovero et al., 2013), and secondly, sensors which re-351 peatedly turn on an off during sampling (Jones et al., 2013). The second problem is 352 particualrly relevant to acoustic detectors which record ultrasound by time expan-353 sion. Here ultrasound is recorded for a set time period and then slowed down and 354 played back, rendering the sensor 'deaf' periodically during sampling. Both of these problems may cause biases in the gREM, as animals can move through the 356 detection zone without being detected. As the gREM assumes constant surveil-357 lance, the error created by switching the sensor on and off quickly will become 358 more important if the sensor is only on for short periods of time. For example, if 359 it takes longer for the recording device to be switched on than the length of some 360 animal calls, then there could be a systematic underestimation of density. We rec-361 ommend that the gREM is applied to constantly sampled data, and the impacts of 362 breaking these assumptions on the gREM should be further explored. 363

Accuracy, Precision and Recommodations for Best Practice. Based on our simulations, we believe that the gREM has the potential to produce accurate estimates

for many different species, using either camera traps or acoustic detectors. However, the precision of the gREM differed between submodels. For example, when
the sensor and signal width were small, the precision of the model was reduced.
Therefore when choosing a sensor for use in a gREM study, the sensor detection
width should be maximised. If the study species has a narrow signal directionality, other aspects of the study protocol, such as length of the survey, should be
used to compensate.

The precision of the gREM is greatly affected by the number of captures. The 373 coefficient of variation falls dramatically between 10 and 60 captures and then 374 after this continues to slowly reduce. At 100 captures the submodels reach 10% 375 coefficient of variation, considered to a very good level of precision (Thomas & 376 Marques, 2012). Many current studies do not reach this level of precision, with most studies reporting coefficient of variations greater than the 10% level (O'Brien 378 et al., 2003; Proctor et al., 2010; Foster & Harmsen, 2012). The length of surveys 379 in the field will need to be adjusted so that enough data can be collected to reach 380 this precision level. Populations of fast moving animals or populations with high 381 densities will require less survey effort than those species that are slow moving or 382 have populations with low densities. 383

The gREM was both accurate and precise for all the movement models we 384 tested (stop-start movement and correlated random walks). However, these move-385 ment models are still simple representations of true animal movement which are 386 dependent on multiple factors such as behavioural state and existence of home 387 ranges (Smouse et al., 2010). The accuracy of the gREM may be affected by the 388 interaction between the movement model and the size of the detection radius. 389 We have studied a relatively long step length compared to the size of the detec-390 tion radius, and therefore the chance of catching the same animal multiple times 391 within a short space of time was reduced and there is little effect on the precision 392 of the model (Figure 7b). However, if the ratio of step length to detection radius 393 was smaller, then this may decrease the precision of the model (but should not 394 decrease its accuracy). 395

Limitations. Although we have used simulations to validate the gREM submodels, much more robust testing is needed. Although difficult, proper field test val-397 idation would be required before the models could be fully trusted. The REM 398 (Rowcliffe et al., 2008) has already been field tested, and both Rowcliffe et al. (2008) 399 and Zero et al. (2013) both found that the REM was an effective manner of esti-400 mating animal densities (Rowcliffe et al., 2008; Zero et al., 2013). In some taxa gold 401 standard methods of estimating animal density exist, such as capture mark recap-402 ture (Sollmann et al., 2013). Where these gold standard exist or true numbers are 403 known, a simultaneous gREM study could be completed to test the accuracy un-404 der field conditions, similar to the tests in Rowcliffe et al. (2008). An easier way to 405 continue to evaluate the models is to run more extensive simulations which break the assumptions of the analytical models. The main element that cannot be ana-407 lytically treated is the complex movement of real animals. Therefore testing these 408 methods against true animal traces, or more complex movement models would be 409 required. 410 Within the simulation we have assumed an equal density across the entire world, 411 however in a field environment the situation would be much more complex, with 412 additional variation coming from local changes in density between sensor sites. 413 We allowed the sensor to be stationary and continuously detecting, negating the 414 triggering, and non-continuous recording issues that could exist with some sen-415 sors. In the simulation, the distance travelled of animal was assumed to be 40 km day⁻¹, the largest day range of terrestrial animals (Carbone et al., 2005). Other speed values should not alter the accuracy of the gREM, however, precision would be af-418 fected, all else being equal, since slower speeds produce fewer records. We also 419 assume perfect knowledge of the average speed of an animal and size of the de-420

Implications for ecology and conservation. The gREM can estimate densities of a number of taxa where no, or few, accurate methods currently exist to measure absolute animal density and trends in absolute abundances (Thomas & Marques,

tection zone. All of which may lead to possible bias or a decrease in precision.

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2012). Many of these species are critically endangered and monitoring their pop-425 ulations is of conservation interest. For example, current methods of density esti-426 mation for the threatened Francisana dolphin (Pontoporia blainvillei) may result in 427 underestimation of their numbers (Crespo et al., 2010). Our method may also be 428 important for understanding zoonotic diseases, for example estimating popula-429 tion sizes of echolocating bats, which are important reservoir of infectious disease 430 that affect humans, livestock and wildlife (Calisher et al., 2006). In addition, the 431 gREM will make it possible to measure the density of animals which may be use-432 ful in quantifying ecosystem services, such as studying the levels of songbirds 433 which are known to have a positive influence on pest control in coffee production 434 (Jirinec et al., 2011). The gREM is suitable for any species that would be consis-435 tently recorded within range of a detector, such as echolocating bats (Kunz et al., 2009), songbirds (Buckland & Handel, 2006), whales (Marques et al., 2009) or forest 437 primates (Hassel-Finnegan et al., 2008). With increasing technological capabilities, 438 this list of species is likely to increase dramatically. Finally, the passive sensor 439 methods that the gREM use are noninvasive and do not require individual mark-440 ing (Jewell, 2013) or naturally identifying marks (as required for mark-recapture 441 models). This makes them suitable for large, continuous monitoring projects with 442 limited human resources (Kelly et al., 2012). It also makes them suitable for species 443 that are under pressure, species that cannot naturally be individually recognised 444 or species that are difficult or dangerous to catch (Thomas & Marques, 2012).

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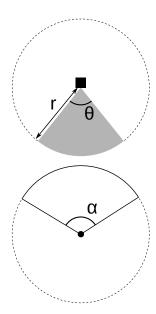


Figure 1. Representation of sensor detection width and animal signal width. The filled square and circle represent a sensor and an animal, respectively; θ , sensor detection width (radians); r, sensor detection distance; dark grey shaded area, sensor detection zone; α , animal signal width (radians). Dashed lines around the filled square and circle represents the maximum extent of θ and α , respectively.

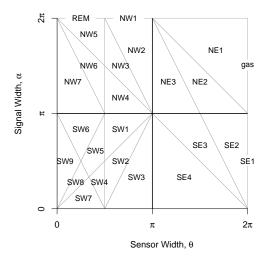


Figure 2. Locations where derivation of the average profile \bar{p} is the same for different combinations of sensor detection and animal signal widths. Symbols within each polygon refer to each gREM submodel named after their compass point, except for Gas and REM which highlight the position of these previously derived models within the gREM. Symbols on the edge of the plot are for submodels where $\alpha, \theta = 2\pi$

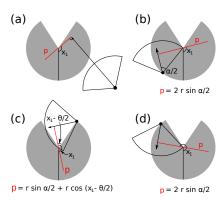


Figure 3. An overview of the derivation of the average profile \bar{p} for the gREM submodel SE2, where (a) shows the location of the profile *p* (the line an animal must pass through in order to be captured) in red and the focal angle, x_1 , for an animal (filled circle), its signal (unfilled sector), and direction of movement (shown as an arrow). The detection zone of the sensor is shown as a filled grey sector with a detection distance of r. The vertical black line within the circle shows the direction the sensor is facing. The derivation of p changes as the animal approaches the sensor from different directions (shown in b-d), where (b) is the derivation of p when x_1 is in the interval $\left[\frac{\pi}{2}, \frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}\right]$, (c) p when x_1 is in the interval $\left[\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}, \frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}\right]$ and (d) p when x_1 is in the interval $\left[\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}, \frac{3\pi}{2}\right]$, where θ , sensor detection width; α , animal signal width. The resultant equation for p is shown beneath bd. The average profile \bar{p} is the size of the profile averaged across all approach angles.

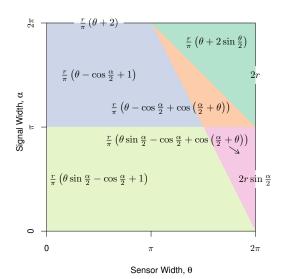


Figure 4. Expressions for the average profile width, \bar{p} , given a range of sensor and signal widths. Despite independent derivation within each block, many models result in the same expression. These are collected together and presented as one block of colour. Expressions on the edge of the plot are for submodels with α , $\theta = 2\pi$.

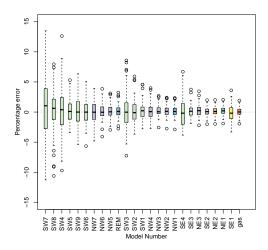


Figure 5. Simulation model results of the accuracy and precision for gREM submodels. The percentage error between estimated and true density for each gREM sub model is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Box colours correspond to the expressions for average profile width \bar{p} given in Figure 4.

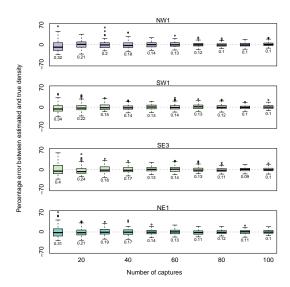


Figure 6. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different numbers of captures. The percentage error between estimated and true density within each gREM sub model for capture rate is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Sensor and signal widths vary between submodels. The numbers beneath each plot represent the coefficient of variation. The colour of each box plot corresponds to the expressions for average profile width \bar{p} given in Figure 4.

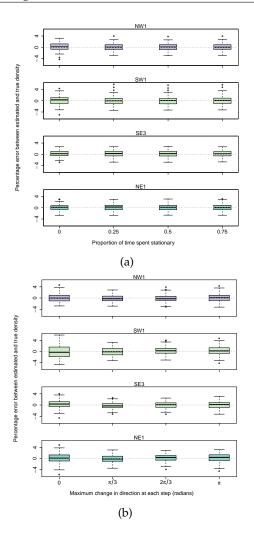


Figure 7. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different movement models where (a) amount of time spent stationary (stop-start movement) and (b) maximum change in direction at each step (correlated random walk model). The percentage error between estimated and true density within each gREM sub model for the different movement models is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. The simple model is represented where time and maximum change in direction equals 0. The colour of each box plot corresponds to the expressions for average profile width \bar{p} given in Figure 4.