1 A GENERALISED RANDOM ENCOUNTER MODEL FOR ESTIMATING 2 ANIMAL DENSITY WITH REMOTE SENSOR DATA

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40 ABSTRACT

1: Wildlife monitoring technology is advancing rapidly and the use of remote sensors such as camera traps and acoustic detectors is becoming common in both the
terrestrial and marine environments. Current methods to estimate abundance or
density require individual recognition of animals or knowing the distance of the
animal from the sensor, which is often difficult. A method without these requirements, the random encounter model (REM), has been successfully applied to estimate animal densities from count data generated from camera traps. However,
count data from acoustic detectors do not fit the assumptions of the REM due to
the directionality of animal signals.

2: We developed a generalised REM (gREM), to estimate absolute animal density from count data from both camera traps and acoustic detectors. We derived the gREM for different combinations of sensor detection widths and animal signal widths (a measure of directionality). We tested the accuracy and precision of this model using simulations of different combinations of sensor detection widths and animal signal widths, number of captures, and models of animal movement.

3: We find that the gREM produces accurate estimates of absolute animal density for all combinations of sensor detection widths and animal signal widths. However, larger sensor detection and animal signal widths were found to be more precise. While the model is accurate for all capture efforts tested, the precision of the estimate increases with the number of captures. We found no effect of different animal movement models on the accuracy and precision of the gREM.

4: We conclude that the gREM provides an effective method to estimate absolute animal densities from remote sensor count data over a range of sensor and animal signal widths. The gREM is applicable for count data obtained in both marine and terrestrial environments, visually or acoustically (e.g., big cats, sharks, birds, echolocating bats and cetaceans). As sensors such as camera traps and acoustic detectors become more ubiquitous, the gREM will be increasingly useful for monitoring unmarked animal populations across broad spatial, temporal and taxonomic scales.

Keywords. Acoustic detection, camera traps, marine, population monitoring, simulations, terrestrial

INTRODUCTION

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Animal population density is one of the fundamental measures in ecology and conservation. The density of a population has important implications for a range of issues such as sensitivity to stochastic fluctuations (Richter-Dyn & Goel, 1972; 75 Wright & Hubbell, 1983) and risk of extinction (Purvis et al., 2000). Monitoring 76 animal population changes in response to anthropogenic pressure is becoming in-77 creasingly important as humans rapidly modify habitats and change climates (Ev-78 eratt et al., 2014). Sensor technology, such as camera traps (Karanth, 1995; Row-79 cliffe & Carbone, 2008) and acoustic detectors (Clark, 1995; O'Farrell & Gannon, 1999; Acevedo & Villanueva-Rivera, 2006; Walters et al., 2012) are becoming widely used to monitor changes in animal populations (Rowcliffe & Carbone, 2008; Kessel et al., 2014; Walters et al., 2013), as they are efficient, relativity cheap and non-83 invasive (Cutler & Swann, 1999), allowing for surveys over large areas and long periods. However, converting sampled count data into estimates of density is 85 problematic as detectability of animals needs to be accounted for (Anderson, 2001). 86 Existing methods for estimating animal density often require additional infor-87 mation that is often unavailable. For example, capture-mark-recapture methods 88 (Karanth, 1995; Trolle & Kéry, 2003; Soisalo & Cavalcanti, 2006; Trolle et al., 2007; Borchers et al., 2014) require recognition of individuals, and distance methods (Harris et al., 2013) require an estimation of how far away individuals are from the sensor (Barlow & Taylor, 2005; Marques et al., 2011). More recently, the development of the random encounter model (REM) (a modification of a gas model) has 93 enabled animal densities to be estimated from unmarked individuals of a known speed, and with known sensor detection parameters (Rowcliffe et al., 2008). The 95 REM method has been successfully applied to estimate animal densities from cam-96 era trap surveys (Manzo et al., 2012; Zero et al., 2013). However, extending the 97 REM method to other types of sensors (e.g., acoustic detectors) is more problematic, because the original derivation assumes a relatively narrow sensor width (up to $\pi/2$ radians) and that the animal is equally detectable irrespective of its heading (Rowcliffe *et al.*, 2008).

102 Whilst these restrictions are not problematic for most camera trap makes (e.g., Reconyx, Cuddeback), the REM cannot be used to estimate densities from camera 103 traps with a wider sensor width (e.g. canopy monitoring with fish eye lenses, 104 Brusa & Bunker (2014)). Additionally, the REM method is not useful in estimating 105 densities from acoustic survey data as acoustic detector angles are often wider 106 than $\pi/2$ radians. Acoustic detectors are designed for a range of diverse tasks 107 and environments (Kessel et al., 2014), which naturally leads to a wide range of 108 sensor detection widths and detection distances. In addition to this, calls emitted 109 by many animals are directional (Blumstein et al., 2011), breaking the assumption 110 of the REM method.

There has been a sharp rise in interest around passive acoustic detectors in recent years, with a 10 fold increase in publications in the decade between 2000 and 2010 (Kessel *et al.*, 2014). Acoustic monitoring is being developed to study many aspects of ecology, including the interactions of animals and their environments (Blumstein *et al.*, 2011; Rogers *et al.*, 2013), the presence and relative abundances of species (Marcoux *et al.*, 2011), biodiversity of an area (Depraetere *et al.*, 2012), and monitoring population trends (Walters *et al.*, 2013).

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Acoustic data suffers from many of the problems associated with data from 119 camera trap surveys in that individuals are often unmarked, so capture-mark-120 recapture methods cannot be used to estimate densities. In some cases the dis-121 tance between the animal and the sensor is known, for example when an array of 122 sensors is deployed and the position of the animal is estimated by triangulation 123 (Lewis et al., 2007). In these situations distance-sampling methods can be applied, 124 a method typically used for marine mammals (Rogers et al., 2013). However, in 125 many cases distance estimation is not possible, for example when single sensors 126 are deployed, a situation typical in the majority of terrestrial acoustic surveys (El-127 phick, 2008; Buckland et al., 2008). In these cases, only relative measures of local 128 abundance can be calculated, and not absolute densities. This means that comparison of populations between species and sites is problematic without assuming equal detectability (Hayes, 2000; Schmidt, 2003; Walters *et al.*, 2013). Equal detectability is unlikely because of differences in environmental conditions, sensor type, habitat, and species biology.

In this study, we create a generalised REM (gREM) as an extension to the camera trap model of Rowcliffe *et al.* (2008), to estimate absolute density from count data from acoustic detectors, or camera traps, where the sensor width can vary from 0 to 2π radians, and the signal given from the animal can be directional. We assessed the accuracy and precision of the gREM within a simulated environment, by varying the sensor detection widths, animal signal widths, number of captures and models of animal movement. We use the simulation results to recommend best survey practice for estimating animal densities from remote sensors.

142 METHODS

Analytical Model. The REM presented by Rowcliffe et al. (2008) adapts the gas 143 model to count data collected from camera trap surveys. The REM is derived 144 assuming a stationary sensor with a detection width less than $\pi/2$ radians. How-145 ever, in order to apply this approach more generally, and in particular to stationary acoustic detectors, we need both to relax the constraint on sensor detection width, and allow for animals with directional signals. Consequently, we derive the gREM 148 for any detection width, θ , between 0 and 2π with a detection distance r giving a 149 circular sector within which animals can be captured (the detection zone) (Fig-150 ure 1). Additionally, we model the animal as having an associated signal width 151 α between 0 and 2π (Figure 1, see Appendix S1 for a list of symbols). We start 152 deriving the gREM with the simplest situation, the gas model where $\theta = 2\pi$ and 153 $\alpha = 2\pi$. 154

Gas Model. Following Yapp (1956), we derive the gas model where sensors can capture animals in any direction and animal signals are detectable from any direction ($\theta = 2\pi$ and $\alpha = 2\pi$). We assume that animals are in a homogeneous environment, and move in straight lines of random direction with velocity v. We allow that our stationary sensor can capture animals at a detection distance r and that if an animal moves within this detection zone they are captured with a probability of one, while animals outside the zone are never captured.

In order to derive animal density, we need to consider relative velocity from 162 the reference frame of the animals. Conceptually, this requires us to imagine that 163 all animals are stationary and randomly distributed in space, while the sensor 164 moves with velocity v. If we calculate the area covered by the sensor during the 165 survey period, we can estimate the number of animals the sensor should capture. 166 As a circle moving across a plane, the area covered by the sensor per unit time is 167 2rv. The number of expected captures, z, for a survey period of t, with an animal 168 density of *D* is z = 2rvtD. To estimate the density, we rearrange to get D = z/2rvt. 169

gREM derivations for different detection and signal widths. Different combinations of 170 θ and α would be expected to occur (e.g., sensors have different detection widths 171 and animals have different signal widths). For different combinations θ and α , the 172 area covered per unit time is no longer given by 2rv. Instead of the size of the 173 sensor detection zone having a diameter of 2r, the size changes with the approach 174 angle between the sensor and the animal. For any given signal width and detec-175 tor width and depending on the angle that the animal approaches the sensor, the 176 width of the area within which an animal can be detected is called the profile, p. The size of the profile (averaged across all approach angles) is defined as the average profile \bar{p} . However, different combinations of θ and α need different equations 179 to calculate \bar{p} . 180

We have identified the parameter space for the combinations of θ and α for which the derivation of the equations are the same (defined as sub-models in the gREM) (Figure 2). For example, the gas model becomes the simplest gREM sub-model (upper right in Figure 2) and the REM from Rowcliffe *et al.* (2008) is another gREM sub-model where $\theta < \pi/2$ and $\alpha = 2\pi$. We derive one gREM sub-model SE2 as an example below, where $2\pi - \alpha/2 < \theta < 2\pi$, $0 < \alpha < \pi$ (see Appendix S2 for derivations of all gREM sub-models).

Example derivation of SE2. In order to calculate \bar{p} , we have to integrate over the focal angle, x_1 (Figure 3a). This is the angle taken from the centre line of the sensor.

Other focal angles are possible (x_2 , x_3 , x_4) and are used in other gREM sub-models (see Appendix S2). As the size of the profile depends on the approach angle, we

present the derivation across all approach angles. When the sensor is directly

approaching the animal $x_1 = \pi/2$. 193 Starting from $x_1 = \pi/2$ until $\theta/2 + \pi/2 - \alpha/2$, the size of the profile is $2r \sin \alpha/2$ 194 (Figure 3b). During this first interval, the size of α limits the width of the profile. 195 When the animal reaches $x_1 = \theta/2 + \pi/2 - \alpha/2$ (Figure 3c), the size of the profile is

 $r\sin(\alpha/2) + r\cos(x_1 - \theta/2)$ and the size of θ and α both limit the width of the profile 197 (Figure 3c). Finally, at $x_1 = 5\pi/2 - \theta/2 - \alpha/2$ until $x_1 = 3\pi/2$, the width of the profile 198

is again $2r \sin \alpha/2$ (Figure 3d) and the size of α again limits the width of the profile. 199 The profile width p for π radians of rotation (from directly towards the sensor 200 to directly behind the sensor) is completely characterised by the three intervals 201 (Figure 3b–d). Average profile width \bar{p} is calculated by integrating these profiles over their appropriate intervals of x_1 and dividing by π which gives

$$\bar{p} = \frac{1}{\pi} \left(\int_{\frac{\pi}{2}}^{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}} 2r \sin \frac{\alpha}{2} dx_1 + \int_{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}} r \sin \frac{\alpha}{2} + r \cos \left(x_1 - \frac{\theta}{2} \right) dx_1 + \int_{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{3\pi}{2}} 2r \sin \frac{\alpha}{2} dx_1 \right)$$

$$= \frac{r}{\pi} \left(\theta \sin \frac{\alpha}{2} - \cos \frac{\alpha}{2} + \cos \left(\frac{\alpha}{2} + \theta \right) \right)$$

$$= qn \ 2$$

We then use this expression to calculate density

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$$D = z/vt\bar{p}.$$
 eqn 3

Rather than having one equation that describes \bar{p} globally, the gREM must be 206 split into submodels due to discontinuous changes in p as α and β change. These 207 discontinuities can occur for a number of reasons such as a profile switching be-208 tween being limited by α and θ , the difference between very small profiles and 209 profiles of size zero, and the fact that the width of a sector stops increasing once 210 the central angle reaches π radians (i.e., a semi-circle is just as wide as a full circle.) 211 As an example, if α is small, there is an interval between Figure 3c and 3d where 212 the 'blind spot' would prevent animals being detected giving p = 0. This would 213 require an extra integral in our equation, as simply putting our small value of α 214 into eqn 1 would not give us this integral of p = 0. 215

gREM submodel specifications were done by hand, and the integration was 216 done using SymPy (SymPy Development Team, 2014) in Python (Appendix S3). 217 The gREM submodels were checked by confirming that: (1) submodels adjacent 218 in parameter space were equal at the boundary between them; (2) submodels that 219 border $\alpha = 0$ had p = 0 when $\alpha = 0$; (3) average profile widths \bar{p} were between 0 220 and 2r and; (4) each integral, divided by the range of angles that it was integrated 221 over, was between 0 and 2r. The scripts for these tests are included in Appendix 222 S3 and the R (Team, 2014) implementation of the gREM is given in Appendix S4. 223

Simulation Model. We tested the accuracy and precision of the gREM by devel-224 oping a spatially explicit simulation of the interaction of sensors and animals using 225 different combinations of sensor detection widths, animal signal widths, number 226 of captures, and models of animal movement. 100 simulations were run where 227 each consisted of a 7.5 km by 7.5 km square with periodic boundaries. A station-228 ary sensor of radius r was set up in the exact centre of each simulation, covering 229 seven sensor detection widths θ , between 0 and 2π (2/9 π , 4/9 π , 6/9 π , 8/9 π , 10/9 π , 230 $14/9\pi$, and 2π). Each sensor was set to record continuously and to capture ani-231 mal signals instantaneously from emission. Each simulation was populated with 232 a density of 70 animals km⁻², calculated from the equation in Damuth (1981) as 233 the expected density of mammals weighing 1 g. This density therefore represents 234 a reasonable estimate of density of individuals, given that the smallest mammal is 235 around 2 g (Jones et al., 2009). A total of 3937 individuals per simulation were cre-236 ated which were placed randomly at the start of the simulation. Individuals were 237 assigned 11 signal widths α between 0 and π (1/11 π , 2/11 π , 3/11 π , 4/11 π , 5/11 π , $6/11\pi$, $7/11\pi$, $8/11\pi$, $9/11\pi$, $10/11\pi$, π). 239 Each simulation lasted for N steps (14400) of duration T (15 minutes) giving a 240

Each simulation lasted for N steps (14400) of duration T (15 minutes) giving a total duration of 150 days. The individuals moved within each step with a distance d, with an average speed, v. d, was sampled from a normal distribution with mean distance, $\mu_d = vT$, and standard deviation $\sigma_d = vT/10$. An average speed, $v = 40 \,\mathrm{km}\,\mathrm{day}^{-1}$, was chosen as this is the largest day range of terrestrial animals (Carbone $et\ al.$, 2005), and represents the upper limit of realistic speeds. At the end step, individuals were allowed to either remain stationary for a time step

(with a given probability, S), or change direction (in a uniform distribution with a maximum angle, A) between 0 and π . This resulted in seven different movement models where: (1) simple movement, where S and A=0; (2) stop-start movement, where (i) S=0.25, A=0, (ii) S=0.5, A=0, (iii) S=0.75, A=0; (3) random walk movement, where (i) S=0, $A=\pi/3$, (ii) S=0, $A=2\pi/3$, iii) S=0, $A=\pi$. Individuals were counted as they moved in and out of the detection zone of the sensor per simulation.

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We calculated the estimated animal density from the gREM by assuming the number of captures per simulation and inputting these values into the correct gREM submodel. gREM accuracy was determined by comparing the density in the simulation with the estimated density. High accuracy is indicated by the mean difference between the estimated and actual values not being significantly different from zero (Wilcoxon signed-rank test). gREM precision was determined by the standard deviation of estimated densities. We used this method to compare the accuracy and precision of all the gREM submodels. As these submodels are derived for different combinations of α and θ , the accuracy and precision of the submodels was used to determine the impact of different values of α and θ .

The influence of the number of captures and animal movement models on ac-264 curacy and precision was investigated using four different gREM submodels rep-265 resentative of the range α and θ values (submodels NW1, SW1, NE1, and SE3, 266 Figure 2). Using these four submodels, we calculated how long the simulation 267 needed to run to generate a range of different capture numbers (from 10 to 100 cap-268 tures in 10 unit intervals), and estimated animal density. These estimated densities 269 were compared to the real density to assess the impact on the accuracy and preci-270 sion of the gREM. We calculated the coefficient of variation in order the compare 271 the precision between capture numbers. The gREM also assumes that individuals 272 move continuously with straight-line movement (simple movement model) and 273 we therefore assessed the impact of breaking the gREM assumptions. We used 274 the four submodels to compare the accuracy and precision of a simple movement 275 model, stop-start movement models (using different amounts of time spent stationary), and random walk movement models.

278 RESULTS

Analytical model. The equation for \bar{p} has been newly derived for each submodel in the gREM, except for the gas model and REM which have been calculated previously. However, many models, although derived separately, have the same expression for \bar{p} . Figure 4 shows the expression for \bar{p} in each case. The general equation for density, using the correct expression for \bar{p} is then substituted into eqn 3. Although more thorough checks are performed in Appendix S3, it can be seen that all adjacent expressions in Figure 4 are equal when expressions for the boundaries between them are substituted in.

287 Simulation model.

gREM submodels. All gREM submodels showed a high accuracy, i.e., the mean dif-288 ference between the estimated and actual values was not significantly different 289 from zero across all models, at p <0.05, corrected for multiple tests (all gREM sub models Wilcoxon signed-rank test) (Figure 5). However, the precision of the sub-291 models do vary, where the gas model is the most precise and the SW7 sub model 292 the least precise, having the smallest and the largest interquartile range, respec-293 tively (Figure 5). The standard deviation of the error between the estimated and 294 true densities is strongly related to both the sensor and signal widths (Appendix 295 S5), such that larger widths have lower standard deviations (greater precision). 296

Number of captures. Within the four gREM submodels tested (NW1, SW1, SE3, 297 NE1), the accuracy was not affected by the number of captures. The mean differ-298 ence between the estimated and actual values was not significantly different from 299 zero across all capture rates, at p <0.05, corrected for multiple tests (Wilcoxon 300 signed-rank test) (Figure 6). However, the precision was dependent on the num-301 ber of captures across all four of the gREM submodels, where precision increases 302 as number of captures increases (Figure 6). For all gREM submodels, the the coef-303 ficient of variation falls to 10% at 100 captures. 304

Movement models. Within the four gREM submodels tested (NW1, SW1, SE3, NE1), neither the accuracy or precision was affected by the amount of time spent station-306 ary. The mean difference between the estimated and actual values was not signifi-307 cantly different from zero for each category of stationary time (0, 0.25, 0.5 and 0.75), 308 at p <0.05, corrected for multiple tests (all gREM sub models Wilcoxon signed-309 rank test) (Figure 7a). Altering the maximum change in direction in each step (0, 310 pi/3, 2pi/3, and pi) did not affect the accuracy or precision of the four gREM sub-311 models tested, at p <0.05, corrected for multiple testing (Wilcoxon signed-rank 312 test) (Figure 7b). 313

314 DISCUSSION

We have developed the gREM such that it can be used to estimate density from acoustic sensors and camera traps. This has entailed a generalisation of the gas model and the REM in Rowcliffe *et al.* (2008) to be applicable to any combination of sensor width and signal directionality. We have used simulations to show, as a proof of principle, that these models are accurate and precise. The precision of the gREM was found to be dependent on the width of the sensor and the signal, and the number of captures.

Analytical model. The gREM was derived for different combinations of α and θ 322 resulting in 25 different submodels, the expression for \bar{p} are equal for many of 323 these submodels resulting in eight different equations including the previously 324 derived gas model and REM. These submodels were tested for consistency with 325 adjacent expressions being equal at their boundaries. These new submodels will 326 allow researchers to evaluate the absolute density of animals that have previously been difficult to study, such as echolocating bats (Clement & Castleberry, 2013), 328 with non-invasive methods such as remote sensors. The gREM also allows the data from acoustic detectors to be used where an animal has a directional calls, 330 this could be used for a range of animals including songbirds (Blumstein et al., 331 2011), dolphins (Lammers & Au, 2003), as well as echolocating bats (Walters et al., 332 2013). 333

There are a number of possible extensions to the gREM which could be developed in the future. The original gas model was formulated for the case where both

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subjects, either animal and detector, or animal and animal, are moving (Hutchinson & Waser, 2007). Indeed any of the models with animals that are equally de-337 tectable in all directions ($\alpha = 2\pi$) can be trivially expanded for moving by substi-338 tuting the sum of the average animal velocity and the sensor velocity for v as used 339 here. However, when the animal has a directional call, as seen in both terrestrial 340 and aquatic environments (Lammers & Au, 2003; Blumstein et al., 2011), the ex-341 tension becomes less simple. The approach would be to calculate again the mean 342 profile width. However, for each angle of approach, one would have to average 343 the profile width for an animal facing in any direction (i.e., not necessarily moving 344 towards the sensor) weighted by the relative velocity of that direction. There are 345 a number of situations where a moving detector and animal could occur, e.g. an acoustic detector towed from a boat when studying porpoises (Kimura et al., 2014) or surveying echolocating bats from a moving car (Ahlen & Baagøe, 1999; Jones 348 et al., 2013). 349

Interesting but unstudied problems impacting the gREM are firstly, edge effects 350 caused by sensor trigger delays (the delay between sensing an animal and attempt-351 ing to record the encounter) (Rovero et al., 2013), and secondly, sensors which re-352 peatedly turn on an off during sampling (Jones et al., 2013). The second problem is 353 particualrly relevant to acoustic detectors which record ultrasound by time expan-354 sion. Here ultrasound is recorded for a set time period and then slowed down and 355 played back, rendering the sensor 'deaf' periodically during sampling. Both of these problems may cause biases in the gREM, as animals can move through the 357 detection zone without being detected. As the gREM assumes constant surveil-358 lance, the error created by switching the sensor on and off quickly will become 359 more important if the sensor is only on for short periods of time. For example, if 360 it takes longer for the recording device to be switched on than the length of some 361 animal calls, then there could be a systematic underestimation of density. We rec-362 ommend that the gREM is applied to constantly sampled data, and the impacts of 363 breaking these assumptions on the gREM should be further explored. 364

Accuracy, Precision and Recommodations for Best Practice. Based on our simulations, we believe that the gREM has the potential to produce accurate estimates

for many different species, using either camera traps or acoustic detectors. However, the precision of the gREM differed between submodels. For example, when
the sensor and signal width were small, the precision of the model was reduced.
Therefore when choosing a sensor for use in a gREM study, the sensor detection
width should be maximised. If the study species has a narrow signal directionality, other aspects of the study protocol, such as length of the survey, should be
used to compensate.

The precision of the gREM is greatly affected by the number of captures. The 374 coefficient of variation falls dramatically between 10 and 60 captures and then 375 after this continues to slowly reduce. At 100 captures the submodels reach 10% 376 coefficient of variation, considered to a very good level of precision (Thomas & 377 Marques, 2012). Many current studies do not reach this level of precision, with most studies reporting coefficient of variations greater than the 10% level (O'Brien 379 et al., 2003; Proctor et al., 2010; Foster & Harmsen, 2012). The length of surveys 380 in the field will need to be adjusted so that enough data can be collected to reach 381 this precision level. Populations of fast moving animals or populations with high 382 densities will require less survey effort than those species that are slow moving or 383 have populations with low densities. 384

The gREM was both accurate and precise for all the movement models we 385 tested (stop-start movement and correlated random walks). However, these move-386 ment models are still simple representations of true animal movement which are 387 dependent on multiple factors such as behavioural state and existence of home 388 ranges (Smouse et al., 2010). The accuracy of the gREM may be affected by the 389 interaction between the movement model and the size of the detection radius. 390 We have studied a relatively long step length compared to the size of the detec-391 tion radius, and therefore the chance of catching the same animal multiple times 392 within a short space of time was reduced and there is little effect on the precision 393 of the model (Figure 7b). However, if the ratio of step length to detection radius 394 was smaller, then this may decrease the precision of the model (but should not 395 decrease its accuracy). 396

Limitations. Although we have used simulations to validate the gREM submod-397 els, much more robust testing is needed. Although difficult, proper field test val-398 idation would be required before the models could be fully trusted. The REM 399 (Rowcliffe et al., 2008) has already been field tested, and both Rowcliffe et al. (2008) 400 and Zero et al. (2013) both found that the REM was an effective manner of esti-401 mating animal densities (Rowcliffe et al., 2008; Zero et al., 2013). In some taxa gold 402 standard methods of estimating animal density exist, such as capture mark recap-403 ture (Sollmann et al., 2013). Where these gold standard exist or true numbers are 404 known, a simultaneous gREM study could be completed to test the accuracy un-405 der field conditions, similar to the tests in Rowcliffe et al. (2008). An easier way to 406 continue to evaluate the models is to run more extensive simulations which break the assumptions of the analytical models. The main element that cannot be analytically treated is the complex movement of real animals. Therefore testing these 409 methods against true animal traces, or more complex movement models would be 410 required. 411 Within the simulation we have assumed an equal density across the entire world, 412 however in a field environment the situation would be much more complex, with 413 additional variation coming from local changes in density between sensor sites. 414 We allowed the sensor to be stationary and continuously detecting, negating the 415 triggering, and non-continuous recording issues that could exist with some sen-416 sors. In the simulation, the distance travelled of animal was assumed to be 40 km day⁻¹, the largest day range of terrestrial animals (Carbone et al., 2005). Other speed values should not alter the accuracy of the gREM, however, precision would be af-419 fected, all else being equal, since slower speeds produce fewer records. We also 420 assume perfect knowledge of the average speed of an animal and size of the de-421 tection zone. All of which may lead to possible bias or a decrease in precision.

Implications for ecology and conservation. The gREM can estimate densities of 423 a number of taxa where no, or few, accurate methods currently exist to measure 424 absolute animal density and trends in absolute abundances (Thomas & Marques, 425

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2012). Many of these species are critically endangered and monitoring their pop-426 ulations is of conservation interest. For example, current methods of density esti-427 mation for the threatened Francisana dolphin (Pontoporia blainvillei) may result in 428 underestimation of their numbers (Crespo et al., 2010). Our method may also be 429 important for understanding zoonotic diseases, for example estimating popula-430 tion sizes of echolocating bats, which are important reservoir of infectious disease 431 that affect humans, livestock and wildlife (Calisher et al., 2006). In addition, the 432 gREM will make it possible to measure the density of animals which may be use-433 ful in quantifying ecosystem services, such as studying the levels of songbirds 434 which are known to have a positive influence on pest control in coffee production 435 (Jirinec et al., 2011). The gREM is suitable for any species that would be consistently recorded within range of a detector, such as echolocating bats (Kunz et al., 437 2009), songbirds (Buckland & Handel, 2006), whales (Marques et al., 2009) or forest 438 primates (Hassel-Finnegan et al., 2008). With increasing technological capabilities, 439 this list of species is likely to increase dramatically. Finally, the passive sensor 440 methods that the gREM use are noninvasive and do not require individual mark-441 ing (Jewell, 2013) or naturally identifying marks (as required for mark-recapture 442 models). This makes them suitable for large, continuous monitoring projects with 443 limited human resources (Kelly et al., 2012). It also makes them suitable for species that are under pressure, species that cannot naturally be individually recognised 445 or species that are difficult or dangerous to catch (Thomas & Marques, 2012).

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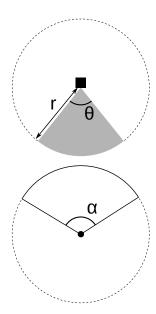


Figure 1. Representation of sensor detection width and animal signal width. The filled square and circle represent a sensor and an animal, respectively; θ , sensor detection width (radians); r, sensor detection distance; dark grey shaded area, sensor detection zone; α , animal signal width (radians). Dashed lines around the filled square and circle represents the maximum extent of θ and α , respectively.

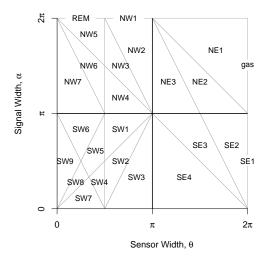


Figure 2. Locations where derivation of the average profile \bar{p} is the same for different combinations of sensor detection and animal signal widths. Symbols within each polygon refer to each gREM submodel named after their compass point, except for Gas and REM which highlight the position of these previously derived models within the gREM. Symbols on the edge of the plot are for submodels where $\alpha, \theta = 2\pi$

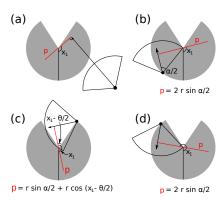


Figure 3. An overview of the derivation of the average profile \bar{p} for the gREM submodel SE2, where (a) shows the location of the profile *p* (the line an animal must pass through in order to be captured) in red and the focal angle, x_1 , for an animal (filled circle), its signal (unfilled sector), and direction of movement (shown as an arrow). The detection zone of the sensor is shown as a filled grey sector with a detection distance of r. The vertical black line within the circle shows the direction the sensor is facing. The derivation of p changes as the animal approaches the sensor from different directions (shown in b-d), where (b) is the derivation of p when x_1 is in the interval $\left[\frac{\pi}{2}, \frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}\right]$, (c) p when x_1 is in the interval $\left[\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}, \frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}\right]$ and (d) p when x_1 is in the interval $\left[\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}, \frac{3\pi}{2}\right]$, where θ , sensor detection width; α , animal signal width. The resultant equation for p is shown beneath bd. The average profile \bar{p} is the size of the profile averaged across all approach angles.

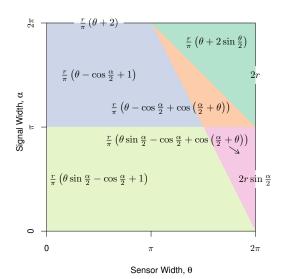


Figure 4. Expressions for the average profile width, \bar{p} , given a range of sensor and signal widths. Despite independent derivation within each block, many models result in the same expression. These are collected together and presented as one block of colour. Expressions on the edge of the plot are for submodels with α , $\theta = 2\pi$.

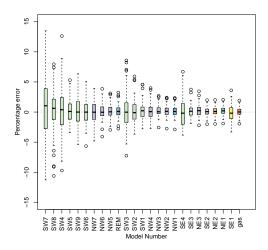


Figure 5. Simulation model results of the accuracy and precision for gREM submodels. The percentage error between estimated and true density for each gREM sub model is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Box colours correspond to the expressions for average profile width \bar{p} given in Figure 4.

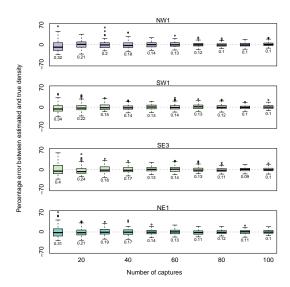


Figure 6. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different numbers of captures. The percentage error between estimated and true density within each gREM sub model for capture rate is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Sensor and signal widths vary between submodels. The numbers beneath each plot represent the coefficient of variation. The colour of each box plot corresponds to the expressions for average profile width \bar{p} given in Figure 4.

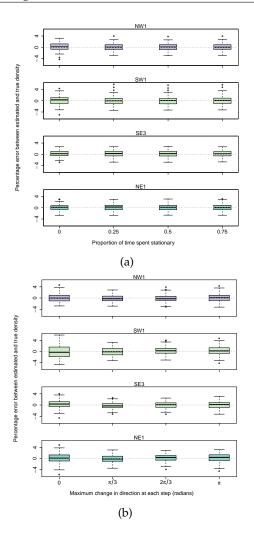


Figure 7. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different movement models where (a) amount of time spent stationary (stop-start movement) and (b) maximum change in direction at each step (correlated random walk model). The percentage error between estimated and true density within each gREM sub model for the different movement models is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. The simple model is represented where time and maximum change in direction equals 0. The colour of each box plot corresponds to the expressions for average profile width \bar{p} given in Figure 4.