## A GENERALISED RANDOM ENCOUNTER MODEL FOR ESTIMATING ANIMAL DENSITY WITH REMOTE SENSOR

2 ESTIMATING ANIMAL DENSITY WITH REMOTE S
3 DATA

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Abstract

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1: Wildlife monitoring technology is advancing rapidly and the use of remote sensors such as camera traps and acoustic detectors is becoming common in both the terrestrial and marine environments. Current methods to estimate abundance or density require individual recognition of animals or knowing the distance of the animal from the sensor, which is often difficult. A method without these requirements, the random encounter model (REM), has been successfully applied to estimate animal densities from count data generated from camera traps. However, count data from acoustic detectors do not fit the assumptions of the REM due to the directionality of animal signals.

2: We developed a generalised REM (gREM), to estimate absolute animal density from count data from both camera traps and acoustic detectors. We derived the gREM for different combinations of sensor detection widths and animal signal widths (a measure of directionality). We tested the accuracy and precision of this model using simulations of different combinations of sensor detection widths and animal signal widths, number of captures, and models of animal movement.

3: We find that the gREM produces accurate estimates of absolute animal density
for all combinations of sensor detection widths and animal signal widths. However,
larger sensor detection and animal signal widths were found to be more precise.
While the model is accurate for all capture efforts tested, the precision of the
estimate increases with the number of captures. We found no effect of different
animal movement models on the accuracy and precision of the gREM.

4: We conclude that the gREM provides an effective method to estimate absolute animal densities from remote sensor count data over a range of sensor and animal signal widths. The gREM is applicable for count data obtained in both marine and terrestrial environments, visually or acoustically (e.g., big cats, sharks, birds, echolocating bats and cetaceans). As sensors such as camera traps and acoustic detectors become more ubiquitous, the gREM will be increasingly useful for monitoring unmarked animal populations across broad spatial, temporal and taxonomic scales.

71 **Keywords.** Acoustic detection, camera traps, marine, population monitoring, sim-72 ulations, terrestrial

Introduction

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The density of animal populations is one of the fundamental measures in ecology and conservation and has important implications for a range of issues, such 75 as sensitivity to stochastic fluctuations (Wright & Hubbell, 1983) and extinction 76 risk (Purvis et al., 2000). Monitoring animal population changes in response to an-77 thropogenic pressure is becoming increasingly important as humans rapidly mod-78 ify habitats and change climates (Everatt et al., 2014). Sensor technology, such 79 as camera traps (Karanth, 1995; Rowcliffe & Carbone, 2008) and acoustic detec-80 tors (Acevedo & Villanueva-Rivera, 2006; Walters et al., 2012) are widely used to 81 monitor changes in animal populations as they are efficient, relativity cheap and non-invasive, allowing for surveys over large areas and long periods (Rowcliffe & Carbone, 2008; Kessel et al., 2014; Walters et al., 2013). However, converting sampled count data into estimates of density is problematic as detectability of animals needs to be accounted for (Anderson, 2001). 86 Existing methods for estimating animal density often require additional infor-87 mation that is often unavailable. For example, capture-mark-recapture methods

88 (Karanth, 1995; Borchers et al., 2014) require recognition of individuals, and dis-89 tance methods (Harris et al., 2013) require estimates of how far away individuals 90 are from the sensor (Barlow & Taylor, 2005; Marques et al., 2011). When individuals cannot be told apart, an extension of occupancy modelling can be used to estimate absolute abundance (Royle & Nichols, 2003). However, as the model is originally formulated to estimate occupancy, count information is simplified to presence-absence data. Assumptions about the distribution of individuals (e.g. a 95 poisson distribution) must also be made (Royle & Nichols, 2003) which may be a poor assumption for nonrandomly distributed species. Furthermore repeat, inde-97 pendent surveys must be performed and the definition of a site can be difficult, 98 especially for wide-ranging species (MacKenzie & Royle, 2005). gg

More recently, the development of the random encounter model (REM), a modification of an ideal gas model (Yapp, 1956; Hutchinson & Waser, 2007), has enabled

animal densities to be estimated from unmarked individuals of a known speed, and 102 with known sensor detection parameters (Rowcliffe et al., 2008). The REM method 103 has been successfully applied to estimate animal densities from camera trap surveys 104 (Zero et al., 2013). However, extending the REM method to other types of sensors 105 (e.g., acoustic detectors) is more problematic, because the original derivation as-106 sumes a relatively narrow sensor width (up to  $\pi/2$  radians) and that the animal is 107 equally detectable irrespective of its heading (Rowcliffe et al., 2008). 108 Whilst these restrictions are not problematic for most camera trap makes (e.g., 109

Reconyx, Cuddeback), the REM cannot be used to estimate densities from camera 110 traps with a wider sensor width (e.g. canopy monitoring with fish eye lenses, Brusa 111 & Bunker (2014)). Additionally, the REM method is not useful in estimating 112 densities from acoustic survey data as acoustic detector angles are often wider than  $\pi/2$  radians. Acoustic detectors are designed for a range of diverse tasks 114 and environments (Kessel et al., 2014), which naturally leads to a wide range of 115 sensor detection widths and detection distances. In addition to this, calls emitted 116 by many animals are directional (Blumstein et al., 2011), breaking the assumption 117 of the REM method. 118

There has been a sharp rise in interest around passive acoustic detectors in recent years, with a 10 fold increase in publications in the decade between 2000 and 2010 (Kessel et al., 2014). Acoustic monitoring is being developed to study many aspects of ecology, including the interactions of animals and their environments (Blumstein et al., 2011; Rogers et al., 2013), the presence and relative abundances of species (Marcoux et al., 2011), biodiversity of an area (Depraetere et al., 2012), and monitoring population trends (Walters et al., 2013).

Acoustic data suffers from many of the problems associated with data from camera trap surveys in that individuals are often unmarked, making capture-mark-recapture methods more difficult to use (Marques et al., 2013). In some cases the distance between the animal and the sensor is known, for example when an array of sensors is deployed and the position of the animal is estimated by triangulation (Lewis et al., 2007). In these situations distance-sampling methods can be applied (Buckland et al., 2008). However, in many cases distance estimation is not possible, for example when single sensors are deployed, a situation typical in the majority

of terrestrial acoustic surveys (Buckland et al., 2008). In these cases, only relative measures of local abundance can be calculated, and not absolute densities. This 135 means that comparison of populations between species and sites is problematic 136 without assuming equal detectability (Schmidt, 2003; Walters et al., 2013). Equal 137 detectability is unlikely because of differences in environmental conditions, sensor 138 type, habitat, and species biology. 139 In this study, we create a generalised REM (gREM) as an extension to the camera 140 trap model of Rowcliffe et al. (2008), to estimate absolute density from count data 141 from acoustic detectors, or camera traps, where the sensor width can vary from 142 0 to  $2\pi$  radians, and the signal given from the animal can be directional. We assessed the accuracy and precision of the gREM within a simulated environment, by varying the sensor detection widths, animal signal widths, number of captures 145 and models of animal movement. We use the simulation results to recommend best 146 survey practice for estimating animal densities from remote sensors. 147

148 METHODS

Analytical Model. The REM presented by Rowcliffe et al. (2008) adapts the 149 gas model to count data collected from camera trap surveys. The REM is derived 150 assuming a stationary sensor with a detection width less than  $\pi/2$  radians. How-151 ever, in order to apply this approach more generally, and in particular to stationary 152 acoustic detectors, we need both to relax the constraint on sensor detection width, 153 and allow for animals with directional signals. Consequently, we derive the gREM 154 for any detection width,  $\theta$ , between 0 and  $2\pi$  with a detection distance r giving 155 a circular sector within which animals can be captured (the detection zone) (Fig-156 ure 1). Additionally, we model the animal as having an associated signal width 157  $\alpha$  between 0 and  $2\pi$  (Figure 1, see Appendix S1 for a list of symbols). We start 158 deriving the gREM with the simplest situation, the gas model where  $\theta = 2\pi$  and 159  $\alpha = 2\pi$ . 160

Gas Model. Following Yapp (1956), we derive the gas model where sensors can capture animals in any direction and animal signals are detectable from any direction ( $\theta = 2\pi$  and  $\alpha = 2\pi$ ). We assume that animals are in a homogeneous environment, and move in straight lines of random direction with velocity v. We allow that our

stationary sensor can capture animals at a detection distance r and that if an animal moves within this detection zone they are captured with a probability of one; while outside this zone, animals are never captured.

In order to derive animal density, we need to consider relative velocity from the 168 reference frame of the animals. Conceptually, this requires us to imagine that all 169 animals are stationary and randomly distributed in space, while the sensor moves 170 with velocity v. If we calculate the area covered by the sensor during the survey 171 period, we can estimate the number of animals the sensor should capture. As a 172 circle moving across a plane, the area covered by the sensor per unit time is 2rv. 173 The expected number of captures, z, for a survey period of t, with an animal density 174 of D is z = 2rvtD. To estimate the density we rearrange to get D = z/2rvt. Note 175 that as z is the number of encounters, not individuals, the possibility of repeated 176 detections of the same individual is accounted for (Hutchinson & Waser, 2007). 177

gREM derivations for different detection and signal widths. Different combinations 178 of  $\theta$  and  $\alpha$  would be expected to occur (e.g., sensors have different detection widths 179 and animals have different signal widths). For different combinations  $\theta$  and  $\alpha$ , the 180 area covered per unit time is no longer given by 2rv. Instead of the size of the 181 sensor detection zone having a diameter of 2r, the size changes with the approach 182 angle between the sensor and the animal. The width of the area within which an 183 animal can be detected is called the profile, p. The size of p depends on the signal 184 width, detector width and the angle that the animal approaches the sensor. The 185 size of the profile (averaged across all approach angles) is defined as the average 186 profile  $\bar{p}$ . However, different combinations of  $\theta$  and  $\alpha$  need different equations to 187 calculate  $\bar{p}$ . 188

We have identified the parameter space for the combinations of  $\theta$  and  $\alpha$  for which the derivation of the equations are the same (defined as sub-models in the gREM) (Figure 2). For example, the gas model becomes the simplest gREM sub-model (upper right in Figure 2) and the REM from Rowcliffe *et al.* (2008) is another gREM sub-model where  $\theta < \pi/2$  and  $\alpha = 2\pi$ . We derive one gREM sub-model SE2 as an example below, where  $2\pi - \alpha/2 < \theta < 2\pi$ ,  $0 < \alpha < \pi$  (see Appendix S2 for derivations of all gREM sub-models). Any estimate of density would require prior

knowledge of animal velocity, v and animal signal width,  $\alpha$  taken from other sources, for example existing literature (Brinkløv et al., 2011; Carbone et al., 2005). Sensor width,  $\theta$ , and detection distance, r would also need to be measured or obtained from manufacturer specifications (Holderied & Von Helversen, 2003; Adams et al., 200 2012).

Example derivation of SE2. In order to calculate  $\bar{p}$ , we have to integrate over the

focal angle,  $x_1$  (Figure 3a). This is the angle taken from the centre line of the 202 sensor. Other focal angles are possible  $(x_2, x_3, x_4)$  and are used in other gREM sub-models (see Appendix S2). As the size of the profile depends on the approach 204 angle, we present the derivation across all approach angles. When the sensor is 205 directly approaching the animal  $x_1 = \pi/2$ . 206 Starting from  $x_1 = \pi/2$  until  $\theta/2 + \pi/2 - \alpha/2$ , the size of the profile is  $2r \sin \alpha/2$ 207 (Figure 3b). During this first interval, the size of  $\alpha$  limits the width of the profile. 208 When the animal reaches  $x_1 = \theta/2 + \pi/2 - \alpha/2$  (Figure 3c), the size of the profile 209 is  $r\sin(\alpha/2) + r\cos(x_1 - \theta/2)$  and the size of  $\theta$  and  $\alpha$  both limit the width of the 210 profile (Figure 3c). Finally, at  $x_1 = 5\pi/2 - \theta/2 - \alpha/2$  until  $x_1 = 3\pi/2$ , the width of 211 the profile is again  $2r \sin \alpha/2$  (Figure 3d) and the size of  $\alpha$  again limits the width 212 of the profile. The profile width p for  $\pi$  radians of rotation (from directly towards the sensor to directly behind the sensor) is completely characterised by the three intervals 215 (Figure 3b-d). Average profile width  $\bar{p}$  is calculated by integrating these profiles 216 over their appropriate intervals of  $x_1$  and dividing by  $\pi$  which gives 217

$$\bar{p} = \frac{1}{\pi} \left( \int_{\frac{\pi}{2}}^{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}} 2r \sin\frac{\alpha}{2} dx_1 + \int_{\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}} r \sin\frac{\alpha}{2} + r \cos\left(x_1 - \frac{\theta}{2}\right) dx_1 + \int_{\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}}^{\frac{3\pi}{2}} 2r \sin\frac{\alpha}{2} dx_1 \right)$$

$$= \frac{r}{\pi} \left(\theta \sin\frac{\alpha}{2} - \cos\frac{\alpha}{2} + \cos\left(\frac{\alpha}{2} + \theta\right)\right)$$

$$= qn \ 1$$

$$= qn \ 2$$

218 We then use this expression to calculate density

$$D = z/vt\bar{p}.$$
 eqn 3

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Rather than having one equation that describes  $\bar{p}$  globally, the gREM must be 220 split into submodels due to discontinuous changes in p as  $\alpha$  and  $\beta$  change. These 221 discontinuities can occur for a number of reasons such as a profile switching between 222 being limited by  $\alpha$  and  $\theta$ , the difference between very small profiles and profiles of 223 size zero, and the fact that the width of a sector stops increasing once the central 224 angle reaches  $\pi$  radians (i.e., a semi-circle is just as wide as a full circle). As an 225 example, if  $\alpha$  is small, there is an interval between Figure 3c and 3d where the 226 'blind spot' would prevent animals being detected giving p=0. This would require 227 an extra integral in our equation, as simply putting our small value of  $\alpha$  into eqn 1 228 would not give us this integral of p = 0. gREM submodel specifications were done by hand, and the integration was done 230 using SymPy (SymPy Development Team, 2014) in Python (Appendix S3). The gREM submodels were checked by confirming that: (1) submodels adjacent in 232 parameter space were equal at the boundary between them; (2) submodels that 233 border  $\alpha = 0$  had p = 0 when  $\alpha = 0$ ; (3) average profile widths  $\bar{p}$  were between 0 234 and 2r and; (4) each integral, divided by the range of angles that it was integrated 235 over, was between 0 and 2r. The scripts for these tests are included in Appendix 236 S3 and the R (Team, 2014) implementation of the gREM is given in Appendix S4. 237

Simulation Model. We tested the accuracy and precision of the gREM by devel-238 oping a spatially explicit simulation of the interaction of sensors and animals using 239 different combinations of sensor detection widths, animal signal widths, number 240 of captures, and models of animal movement. One hundred simulations were run where each consisted of a 7.5 km by 7.5 km square with periodic boundaries. A 242 stationary sensor of radius r, 10 m, was set up in the exact centre of each simulated 243 study area, covering seven sensor detection widths  $\theta$ , between 0 and  $2\pi$  (2/9 $\pi$ , 4/9 $\pi$ , 244  $6/9\pi$ ,  $8/9\pi$ ,  $10/9\pi$ ,  $14/9\pi$ , and  $2\pi$ ). Each sensor was set to record continuously and 245 to capture animal signals instantaneously from emission. Each simulation was pop-246 ulated with a density of 70 animals km<sup>-2</sup>, calculated from the equation in Damuth 247 (1981) as the expected density of mammals weighing 1 g. This density therefore 248 represents a reasonable estimate of density of individuals, given that the smallest

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mammal is around 2 g (Jones et al., 2009). A total of 3937 individuals per simu-
         lation were created which were placed randomly at the start of the simulation. 11
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         signal widths \alpha between 0 and \pi were used (1/11\pi, 2/11\pi, 3/11\pi, 4/11\pi, 5/11\pi, 5/
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         6/11\pi, 7/11\pi, 8/11\pi, 9/11\pi, 10/11\pi, \pi).
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              Each simulation lasted for N steps (14400) of duration T (15 minutes) giving a
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         total duration of 150 days. The individuals moved within each step with a distance
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         d, with an average speed, v. The distance, d, was sampled from a normal distri-
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         bution with mean distance, \mu_d = vT, and standard deviation, \sigma_d = vT/10, where
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         the standard deviation was chosen to scale with the average distance travelled. An
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         average speed, v = 40 \,\mathrm{km}\,\mathrm{day}^{-1}, was chosen based on the largest day range of ter-
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         restrial animals (Carbone et al., 2005), and represents the upper limit of realistic
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         speeds. At the end of each step, individuals were allowed to either remain sta-
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         tionary for a time step (with a given probability, S), or change direction where the
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         change in direction has a uniform distribution in the interval [-A, A]. This resulted
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         in seven different movement models where: (1) simple movement, where S and A
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         = 0; (2) stop-start movement, where (i) S = 0.25, A = 0, (ii) S = 0.5, A = 0, (iii)
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         S=0.75,\,A=0;\, (3) correlated random walk movement, where (i) S=0,\,A=\pi/3,
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         (ii) S=0, A=2\pi/3, iii) S=0, A=\pi. Individuals were counted as they moved
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         into the detection zone of the sensor per simulation.
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              We calculated the estimated animal density from the gREM by summing the
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         number of captures per simulation and inputting these values into the correct gREM
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         submodel. The accuracy of the gREM was determined by comparing the true sim-
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         ulation density with the estimated density. Precision of the gREM was determined
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         by the standard deviation of estimated densities. We used this method to compare
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         the accuracy and precision of all the gREM submodels. As these submodels are
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         derived for different combinations of \alpha and \theta, the accuracy and precision of the
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         submodels was used to determine the impact of different values of \alpha and \theta.
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              The influence of the number of captures and animal movement models on ac-
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         curacy and precision was investigated using four different gREM submodels rep-
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         resentative of the range \alpha and \theta values (submodels NW1, SW1, NE1, and SE3,
         Figure 2). From a random starting point we ran the simulation until a range of
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         different capture numbers were recorded (from 10 to 100 captures), recorded the
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length of time this took, and estimated the animal density for each of the four sub-models. These estimated densities were compared to the true density to assess 283 the impact on the accuracy and precision of the gREM. We calculated the coeffi-284 cient of variation in order to compare the precision of the density estimates from 285 simulations with different expected numbers of captures. The gREM also assumes 286 that individuals move continuously with straight-line movement (simple movement 287 model) and we therefore assessed the impact of breaking the gREM assumptions. 288 We used the four submodels to compare the accuracy and precision of a simple 280 movement model, stop-start movement models (using different average amounts of 290 time spent stationary), and random walk movement models. Finally, as the pa-29 rameters  $(\alpha, \beta, r \text{ and } v)$  are likely to be measured with error, we compared true simulation densities to densities estimated with parameters with errors of 0%,  $\pm 5\%$ and  $\pm 10\%$ , for all gREM submodels. 294

295 RESULTS

Analytical model. The equation for  $\bar{p}$  has been newly derived for each submodel in the gREM, except for the gas model and REM which have been calculated previously. However, many models, although derived separately, have the same expression for  $\bar{p}$ . Figure 4 shows the expression for  $\bar{p}$  in each case. The general equation for density, eqn 3, is used with the correct value of  $\bar{p}$  substituted. Although more thorough checks are performed in Appendix S3, it can be seen that all adjacent expressions in Figure 4 are equal when expressions for the boundaries between them are substituted in.

## 304 Simulation model.

gREM submodels. All gREM submodels showed a high accuracy, i.e., the median difference between the estimated and true values was less than 2% across all models (Figure 5). However, the precision of the submodels do vary, where the gas model is the most precise and the SW7 sub model the least precise, having the smallest and the largest interquartile range, respectively (Figure 5). The standard deviation of the error between the estimated and true densities is strongly related to both the sensor and signal widths (Appendix S5), such that larger widths have lower

standard deviations (greater precision) due to the increased capture rate of these models.

Number of captures. Within the four gREM submodels tested (NW1, SW1, SE3, 314 NE1), the accuracy was not strongly affected by the number of captures. The 315 median difference between the estimated and true values was less than 15% across 316 all capture rates (Figure 6). However, the precision was dependent on the number 317 of captures across all four of the gREM submodels, where precision increases as 318 number of captures increases, as would be expected for any statistical estimate 319 (Figure 6). For all gREM submodels, the the coefficient of variation falls to 10% at 320 100 captures. 321

Movement models. Within the four gREM submodels tested (NW1, SW1, SE3, NE1), neither the accuracy or precision was affected by the average amount of time spent stationary. The median difference between the estimated and true values was less than 2% for each category of stationary time (0, 0.25, 0.5 and 0.75) (Figure 7a). Altering the maximum change in direction in each step  $(0, \pi/3, 2\pi/3, \text{ and } \pi)$  did not affect the accuracy or precision of the four gREM submodels (Figure 7b).

Impact of parameter error. The percentage error in the density estimates across all parameters and gREM submodels shows a similar response for under and over estimated parameters, suggesting the accuracy is reasonable with respect to parameter error (Appendix S6). The impact of parameter error on the precision of the density estimate varies across gREM submodels and parameters, where  $\alpha$  shows the largest variation including the largest values. However, in all cases the percentage error in the density estimate is not more than 5% greater than the error in the parameter estimate (Appendix S6).

336 DISCUSSION

Analytical model. We have developed the gREM such that it can be used to estimate density from acoustic sensors and camera traps. This has entailed a generalisation of the gas model and the REM in Rowcliffe *et al.* (2008) to be applicable to any combination of sensor width  $\theta$  and signal directionality  $\alpha$ . We emphasise that the approach is robust to multiple detections of the same individual. We have

used simulations to show, as a proof of principle, that these models are accurate and precise.

There are a number of possible extensions to the gREM which could be developed 344 in the future. The original gas model was formulated for the case where both 345 animals and sensor are moving (Hutchinson & Waser, 2007). Indeed any of the 346 models which have animals that are equally detectable in all directions ( $\alpha = 2\pi$ ) can 347 be trivially expanded by replacing animal speed v with  $v+v_s$  where  $v_s$  is the speed of 348 the sensor. However, when the animal has a directional call the extension becomes 349 less simple. The approach would be to calculate again the mean profile width. 350 However, for each angle of approach, one would have to average the profile width 351 for an animal facing in any direction (i.e., not necessarily moving towards the sensor) weighted by the relative velocity of that direction. There are a number of situations where a moving detector and animal could occur, e.g. an acoustic detector towed 354 from a boat when studying porpoises (Kimura et al., 2014) or surveying echolocating 355 bats from a moving car (Jones et al., 2013). 356

Interesting but unstudied problems impacting the gREM are firstly, edge effects 357 caused by sensor trigger delays (the delay between sensing an animal and attempt-358 ing to record the encounter) (Rovero et al., 2013), and secondly, sensors which 359 repeatedly turn on an off during sampling (Jones et al., 2013). The second prob-360 lem is particularly relevant to acoustic detectors which record ultrasound by time 36 expansion. Here ultrasound is recorded for a set time period and then slowed down 362 and played back, rendering the sensor 'deaf' periodically during sampling. Both 363 of these problems may cause biases in the gREM, as animals can move through 364 the detection zone without being detected. As the gREM assumes constant surveil-365 lance, the error created by switching the sensor on and off quickly will become more 366 important if the sensor is only on for short periods of time. We recommend that 367 the gREM is applied to constantly sampled data, and the impacts of breaking these 368 assumptions on the gREM should be further explored. 369

Accuracy, Precision and Recommendations for Best Practice. Based on our simulations, we believe that the gREM has the potential to produce accurate estimates for many different species, using either camera traps or acoustic detectors.

However, the precision of the gREM differed between submodels. For example, when the sensor and signal width were small, the precision of the model was reduced. 374 Therefore when choosing a sensor for use in a gREM study, the sensor detection 375 width should be maximised. If the study species has a narrow signal directionality, 376 other aspects of the study protocol, such as length of the survey, should be used to 377 compensate. 378

The precision of the gREM is greatly affected by the number of captures. The 379 coefficient of variation falls dramatically between 10 and 60 captures and then 380 after this continues to slowly reduce. At 100 captures the submodels reach 10% coefficient of variation, considered to be a very good level of precision and better 382 than many previous studies (Thomas & Marques, 2012; O'Brien et al., 2003; Foster & Harmsen, 2012). The length of surveys in the field will need to be adjusted so that enough data can be collected to reach this precision level. Populations of fast 385 moving animals or populations with high densities will require less survey effort 386 than those species that are slow moving or have populations with low densities. 387

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We found that the sensitivity of the gREM to inaccurate parameter estimates 388 was both predictable and reasonable (Appendix S6), although this varies between 380 different parameters and gREM submodels. Whilst care should be taken in param-390 eter estimation when analysing both acoustic and camera trap data, acoustic data 391 poses particular problems. For acoustic surveys, estimates of r (detection distance) 392 can be measured directly or calculated using sound attenuation models (Holderied 393 & Von Helversen, 2003), while the sensor angle is often easily measured (Adams 394 et al., 2012) or found in the manufacturer's specifications. When estimating animal 395 movement speed v, only the speed of movement during the survey period should 396 be used. The signal width is the most sensitive parameter to inaccurate estimates 397 (Appendix S6) and is also the most difficult to measure. While this parameter will 398 typically be assumed to be  $2\pi$  for camera trap surveys, fewer estimates exist for 399 acoustic signal widths. Although signal width has been measured for echolocating 400 bats using arrays of microphones (Brinkløv et al., 2011), more work should be done 401 on obtaining estimates for a range of acoustically surveyed species. 402

**Limitations.** Although the REM has been found to be effective in field tests (Rowcliffe et al., 2008; Zero et al., 2013), the gREM requires further validation by both 404 field tests and simulations. For example, capture-mark-recapture methods could 405 be used alongside the gREM to test the accuracy under field conditions (Rowcliffe 406 et al., 2008). While we found no effect of the movement model on the accuracy 407 or precision of the gREM, the models we have used in our simulations to vali-408 date the gREM are still simple representations of true animal movement. Animal 409 movement may be highly nonlinear and often dependent on multiple factors such 410 as behavioural state and existence of home ranges (Smouse et al., 2010). There-411 fore testing the gREM against real animal data, or further simulations with more 412 complex movement models, would be beneficial. 413 The assumptions of our simulations may require further consideration, for example we have assumed an equal density across the study area. However, in a field 415 environment the situation may be more complex, with additional variation com-416 ing from local changes in density between sensor sites. Athough unequal densities 417 should theoretically not affect accuracy (Hutchinson & Waser, 2007), it will affect 418 precision and further simulations should be used to quantify this effect. Addition-419 ally, we allowed the sensor to be stationary and continuously detecting, negating 420 the triggering, and non-continuous recording issues that could exist with some sen-421 sors and reduce precision or accuracy. Finally, in the simulation animals moved at 422 the equivalent of the largest day range of terrestrial animals (Carbone et al., 2005). 423 Slower speed values should not alter the accuracy of the gREM, but precision would 424 be affected since slower speeds produce fewer records. The gREM was both accu-425 rate and precise for all the movement models we tested (stop-start movement and 426 correlated random walks). 427 A feature of the gREM is that it does not fit a statistical model to estimate 428 detection probability as occupancy models and distance sampling do (Royle & 429 Nichols, 2003; Barlow & Taylor, 2005; Marques et al., 2011). Instead it explicitly 430 models the process, with animals only being detected if they approach the sensor 431 from a suitable direction. Other processes that affect detection probability could 432

be included in the model to improve realism.

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Implications for ecology and conservation. The gREM is applicable for count data obtained either visually or acoustically in both marine and terrestrial environ-435 ments, and is suitable for taxa including echolocating bats (Walters et al., 2012), 436 songbirds (Buckland & Handel, 2006), whales (Marques et al., 2011) and forest 437 primates (Hassel-Finnegan et al., 2008). Many of these taxa contain critically en-438 dangered species and monitoring their populations is of conservation interest. For 439 example, current methods of density estimation for the threatened Franciscana 440 dolphin (Pontoporia blainvillei) may result in underestimation of their numbers 441 (Crespo et al., 2010). In addition, using gREM may be easier than other methods 442 for measuring the density of animals which may be useful in quantifying ecosystem services, such as songbirds with a known positive influence on pest control (Jirinec et al., 2011). The gREM will aid researchers to study species with non-invasive methods such 446 as remote sensors, which allows for large, continuous monitoring projects with lim-447 ited human resources (Kelly et al., 2012). The gREM is also suitable for species 448 that are sensitive to human contact or are difficult or dangerous to catch (Thomas 449 & Marques, 2012). As sensors such as camera traps and acoustic detectors become 450 more ubiquitous, the gREM will be increasingly useful for monitoring unmarked 451 animal populations across broad spatial, temporal and taxonomic scales. 452

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460

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## Data Accessibility

The code used in this paper is available on Github at https://github.com/
timcdlucas/lucasMoorcroftManuscript/tree/postPeerReview.

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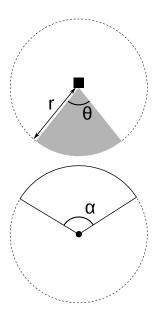


Figure 1. Representation of sensor detection width and animal signal width. The filled square and circle represent a sensor and an animal, respectively;  $\theta$ , sensor detection width (radians); r, sensor detection distance; dark grey shaded area, sensor detection zone;  $\alpha$ , animal signal width (radians). Dashed lines around the filled square and circle represents the maximum extent of  $\theta$  and  $\alpha$ , respectively.

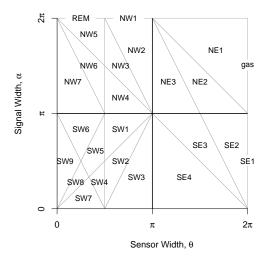


Figure 2. Locations where derivation of the average profile  $\bar{p}$  is the same for different combinations of sensor detection and animal signal widths. Symbols within each polygon refer to each gREM submodel named after their compass point, except for Gas and REM which highlight the position of these previously derived models within the gREM. Symbols on the edge of the plot are for submodels where  $\alpha, \theta = 2\pi$ 

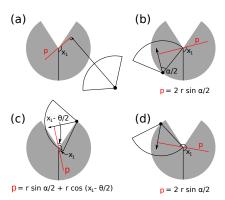


Figure 3. An overview of the derivation of the average profile  $\bar{p}$  for the gREM submodel SE2, where (a) shows the location of the profile p (the line an animal must pass through in order to be captured) in red and the focal angle,  $x_1$ , for an animal (filled circle), its signal (unfilled sector), and direction of movement (shown as an arrow). The detection zone of the sensor is shown as a filled grey sector with a detection distance of r. The vertical black line within the circle shows the direction the sensor is facing. The derivation of p changes as the animal approaches the sensor from different directions (shown in b-d), where (b) is the derivation of p when  $x_1$  is in the interval  $\left[\frac{\pi}{2}, \frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}\right]$ , (c) p when  $x_1$  is in the interval  $\left[\frac{\pi}{2} + \frac{\theta}{2} - \frac{\alpha}{2}, \frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}\right]$  and (d) p when  $x_1$  is in the interval  $\left[\frac{5\pi}{2} - \frac{\theta}{2} - \frac{\alpha}{2}, \frac{3\pi}{2}\right]$ , where  $\theta$ , sensor detection width;  $\alpha$ , animal signal width. The resultant equation for p is shown beneath b-d. The average profile  $\bar{p}$  is the size of the profile averaged across all approach angles.

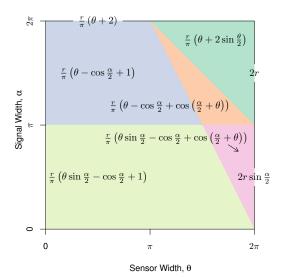


Figure 4. Expressions for the average profile width,  $\bar{p}$ , given a range of sensor and signal widths. Despite independent derivation within each block, many models result in the same expression. These are collected together and presented as one block of colour. Expressions on the edge of the plot are for submodels with  $\alpha, \theta = 2\pi$ .

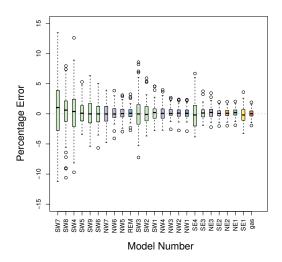


Figure 5. Simulation model results of the accuracy and precision for gREM submodels. The percentage error between estimated and true density for each gREM sub model is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Box colours correspond to the expressions for average profile width  $\bar{p}$  given in Figure 4.

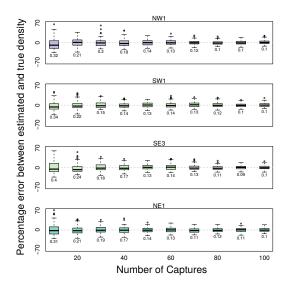


Figure 6. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different numbers of captures. The percentage error between estimated and true density within each gREM sub model for capture rate is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50% of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. Sensor and signal widths vary between submodels. The numbers beneath each plot represent the coefficient of variation. The colour of each box plot corresponds to the expressions for average profile width  $\bar{p}$  given in Figure 4.

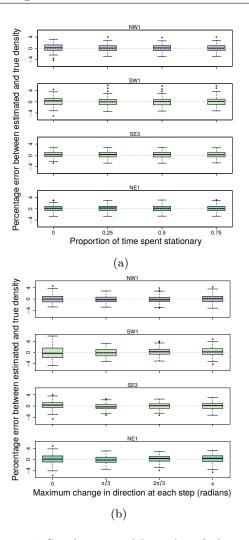


Figure 7. Simulation model results of the accuracy and precision of four gREM submodels (NW1, SW1, SE3 and NE1) given different movement models where (a) average amount of time spent stationary (stop-start movement) and (b) maximum change in direction at each step (correlated random walk model). The percentage error between estimated and true density within each gREM sub model for the different movement models is shown within each box plot, where the black line represents the median percentage error across all simulations, boxes represent the middle 50%of the data, whiskers represent variability outside the upper and lower quartiles with outliers plotted as individual points. The simple model is represented where time and maximum change in direction equals 0. The colour of each box plot corresponds to the expressions for average profile width  $\bar{p}$  given in Figure 4.