

Matrix variance as defined in Matrix Bernstein is the same as regular variance.

$$E((A+B)^2) - E((A+B)^2) = E(A^2 + B^2 + AB + BA) - E(A^2) - E(AB + BA) - E(B^2) = Var(A) + Var(B) \quad (1)$$