```
In[1]:= Clear[t, m, n, o, p]
    lösche
    f[a_{,} b_{,} c_{,} d_{,} e_{,} x_{,}] = e + dx + cx^{2} + bx^{3} + ax^{4}
    df[a_{,} b_{,} c_{,} d_{,} e_{,} x_{]} = D[f[a, b, c, d, e, x], \{x, 1\}]
                                     leite ab
    energyAtAPoint[a_, b_, c_, d_, e_, x_] = (ddf[a, b, c, d, e, x])^2
    energy[a_, b_, c_, d_, e_, t_] =
     Integrate[energyAtAPoint[a, b, c, d, e, x], \{x, 0, t\}]
     lintegriere
    constraints = {
        f[a, b, c, d, e, 0] == m,
        df[a, b, c, d, e, 0] == n,
       f[a, b, c, d, e, t] == o,
       df[a, b, c, d, e, t] == p
      };
    Print["constraintsSolutions:"]
    gebe aus
    constraintsSolutions = Solve[constraints, {b, c, d, e}]
                               löse
    Print["Constraints with solutions:"]
    gebe aus
    constraintsSimplified = constraints /. constraintsSolutions[[1]]
    energyWithSolutions[a_, t_] =
     Evaluate[energy[a, b, c, d, e, t] /. constraintsSolutions[[1]]]
     werte aus
    Print["Energy function:"]
    gebe aus
    energySimplified[a_, t_] = Simplify[energyWithSolutions[a, t]]
                                   vereinfache
    Print["solution: (a, b, c, d, e)"]
    gebe aus
    (*without loss of generality: t is always 1*)
    amin = ArgMin[{energySimplified[a, 1]}, a]
            Argument des Minimums
    bmin = First[Evaluate[b /. constraintsSolutions /. \{t \rightarrow 1, a \rightarrow amin\}]
            erstes… werte aus
    cmin =
     First[Evaluate[c /. constraintsSolutions /. \{t \rightarrow 1, a \rightarrow amin, b \rightarrow bmin\}]
     Lerstes... werte aus
    dmin = First[Evaluate[
            erstes... werte aus
        d /. constraintsSolutions /. \{t \rightarrow 1, a \rightarrow amin, b \rightarrow bmin, c \rightarrow cmin\}]
    emin = First[Evaluate[e /. constraintsSolutions /.
            erstes... werte aus
         \{t \rightarrow 1, a \rightarrow amin, b \rightarrow bmin, c \rightarrow cmin, d \rightarrow dmin\}]
    Print["Check:"]
    Simplify[constraints \ /. \ \{t \to 1, \ a \to amin, \ b \to bmin, \ c \to cmin, \ d \to dmin, \ e \to emin\}]
    vereinfache
    Print["Target function:"]
    f [amin, bmin, cmin, dmin, emin, x]
```

2 | axisRotationPlanning.nb
Out(2)=
$$e + dx + cx^2 + bx^3 + ax^4$$
Out(5)= $d + 2cx + 3bx^2 + 4ax^3$
Out(5)= $d + 2cx + 3bx^2 + 4ax^3$
Out(5)= $d + 2cx + 12ax^2$
Out(6)= $d + 2cx + 12ax^2$
Out(6)= $d + 2cx + 12bc^2 + 12b^2t^3 + 16act^3 + 36abt^4 + \frac{144a^2t^5}{5}$
constraintsSolutions:
Out(6)= $d + 2cx + 12bc^2 + 12b^2t^3 + 16act^3 + 36abt^4 + \frac{144a^2t^5}{5}$
Constraints With solutions:
Out(1)= $d + 2cx + 2cx + 12bc^2 + 12b^2t^3 + 16act^3 + 36abt^4 + \frac{144a^2t^5}{5}$
Constraints with solutions:
Out(1)= $d + 2cx +$

$$\text{Out[14]= } \frac{4 \, \left(15 \, \text{m}^2 + 15 \, \text{o}^2 - 15 \, \text{o} \, \left(n + p\right) \, \, \text{t} + 15 \, \text{m} \, \left(-2 \, \text{o} + \, \left(n + p\right) \, \, \text{t}\right) \, + \, \text{t}^2 \, \left(5 \, n^2 + 5 \, n \, p + 5 \, p^2 + a^2 \, \, \text{t}^6\right)\right)}{5 \, \text{t}^3}$$

solution: (a, b, c, d, e)

Out[16]= 0

$$\text{Out[17]=} \ 2\ m\ +\ n\ -\ 2\ o\ +\ p$$

Out[18]=
$$-3 m - 2 n + 3 o - p$$

Out[19]= n

Out[20]= **m**

Check:

Out[22]= {True, True, True, True}

Target function:

$${\hbox{Out}} \hbox{${\scriptstyle [24]=}} \ m+n\ x+\ \left(-\ 3\ m-\ 2\ n+\ 3\ o-\ p\right)\ x^2+\ \left(\ 2\ m+n-\ 2\ o+\ p\right)\ x^3$$

In[419]:=

bestWay = Evaluate[ArgMin[{energySimplified[a, 5], constraintsSimplified}, {a}]] Lwerte aus LArgument des Minimums

Out[419]= $\{0\}$

$$\begin{array}{ll} & \text{In} [335] := & \textbf{ArgMin} \Big[\Big\{ \textbf{Function} \big[\big\{ \textbf{a'} \,, \, \, \textbf{5'} \big\} \,, \\ & \big\lfloor \text{Argument} \cdot \cdot \big\lfloor \text{Funktion} \big\rfloor \end{array} \Big]$$

energy[a, b, c, d, e, 5] /. constraintsSolutions[1]], {True, True,

$$\begin{split} m + n \, t + a \, t^4 + t^3 \, \left(-2 \, a \, t - \frac{-2 \, m + 2 \, o - n \, t - p \, t}{t^3} \right) + t^2 \, \left(a \, t^2 - \frac{3 \, m - 3 \, o + 2 \, n \, t + p \, t}{t^2} \right) &= o, \\ n + 4 \, a \, t^3 + 3 \, t^2 \, \left(-2 \, a \, t - \frac{-2 \, m + 2 \, o - n \, t - p \, t}{t^3} \right) + \\ 2 \, t \, \left(a \, t^2 - \frac{3 \, m - 3 \, o + 2 \, n \, t + p \, t}{t^2} \right) &= p \Big\} \Big\}, \, \{a\} \Big] \end{split}$$

{True, True, at⁴ + t³ $\left(-\frac{20}{t^3} - 2 \text{ at}\right) + t^2 \left(\frac{30}{t^2} + \text{ at}^2\right) = 10$, $4 a t^3 + 3 t^2 \left(-\frac{20}{t^3} - 2 a t \right) + 2 t \left(\frac{30}{t^2} + a t^2 \right) = 0 \right) \right\}, \{a\}$

In[32]:= Quit[]

$$m := -1.4$$

$$n := -0.5$$

targetF[x_] = f[amin, bmin, cmin, dmin, emin, x] Plot[targetF[x], {x, 0, 2}]

graphische Funktionsdarstellung

Out[30]=
$$\left\{-1.4 - 0.5 x + 8.5 x^2 - 5.3 x^3\right\}$$

