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# An Integrated Circuit Design for Silicon-Nanowire

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# Abstract



# 中 文 摘 要

關鍵詞：



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Abstract

中文摘要

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# Chapter 1

## Introduction

### 1.1 Motivation

Poly-silicon nanowire(SiNW) is a well-studied and promising one-dimensional nanostructures. As reported by [4], there have been a lot of valuable research on fabrication and electrical properties. It was first introduced to the biosensor field in 2001[3] and has become a promising candidate for various features such as high surface-to-volume ratio, ultra sensitivity, label-free electrical detection and real-time measurement.

Although there have been substantial advances on nanowire structure design [6], the work of systems-level engineering is still insufficient. Systems designed for a specific purpose can help the device to meet practical needs such as noise reduction, real-time measurement, and analog-to-digital conversion. Moreover, there are still several challenges that may be overcome through a better signal acquisition system [6].

One of the challenges is that the mass production of robust nanowire elements is still improbable. Element disparity may be the main reason among others. This problem also happens to the measurement of our nanowire (Fig. 3.11). The nanowire we use is made by Professor Yang's team (National Chiao Tung University). And according to them, the nanowire use thick gate dielectric and have non-regular cross-sectional shape, which results in uncertainties of fabrication [8].

## 1.2 Introduction

In this project, we design a nanowire read-out circuit with two modes. In DC mode, one can use the circuit to perform a DC sweep of drain current ( $I_D$ ) to show how the gate voltage ( $V_G$ ) changes, or gives nanowire a constant  $I_D$  and measures the  $V_G$  response to different solution concentration. In AC mode, the circuit detects and amplifies the current variance of the nanowire with constant bias voltages applied ( $V_D$ ,  $V_G$ ,  $V_S$ ). We also combine two modes to implement a proposed method that may mitigate the disparity problem.

### Dealing with the disparity problem

The proposed method base on two assumptions:

1. The nanowire transconductance ( $g_m = \frac{\partial I_D}{\partial V_{GS}}$ ) depends on  $I_D$  and independent on  $V_{GS}$ .
2. The changing of the concentration of biomolecule can be viewed as a voltage signal input to the gate end of a transistor.

The first assumption implies one can control the nanowire transconductance by its  $I_D$ . The second assumption means that as long as different nanowire elements have a same transconductance, the output current induced by a concentration difference should be same.

The method works as follows:

**Initial stage:** At the beginning of each measurement event, we perform a DC sweep with the circuit in DC mode. By handling the sweep results with numerical method, we keep all nanowire elements under a selected transconductance by controlling their  $I_D$  and corresponded  $V_G$ .

**Measurement stage:** We put the circuit in AC mode at this stage. Since the transconductance of all elements is same, they should behave uniformly based on assumption 2. At the end of the stage, we return to DC mode to reset  $I_D$  of the elements. The circuit adjusts their  $V_G$  to do so.

At the beginning of each measurement stage, an element always has a same  $I_D$  but different  $V_G$ . Based on assumption 1, its transconductance is kept constant.

The minutiae are reviewed in chapter 5. Currently, most operations are manual. We hope to make them automatic in the future, which may require digital circuit assistance.

## 1.3 Design Flow and Chapter Layout

In this thesis, there are six chapters sorted according to the design flow.

Chapter 2 reviews the basic theories and the literature that are related to our work. Most of those are the drain current of nanowire sweeping along the gate voltage ( $I_d$ - $V_g$  curves). We present some of the raw data and the analysis results in this part.

Chapter 3 gives a brief description of nanowire structure. It is then followed by two sections about some measurement and data analysis. The data of the first one is from the biological experiments while the second one is from the electrical measurement. We use the analysis results to design the read-out circuit.

Chapter 4 is an “accessory”. This chapter contains the discrete circuit which was designed for ion-sensitive field-effect transistor (ISFET) [10]. We construct it and perform some electrical measurement. The purpose of this process is to practice the constant current method. The outcomes are deficient, and it is its reference value which we spotlight.

Chapter 5 talks about the schematic, design process and the simulation results of the read-out circuit.

Chapter 6 presents the measurement results of our integrated circuit and the conclusion of this project.

# Chapter 2

## Literature Review & Theory Description

As previously mentioned in the introduction section, the read-out circuit we proposed has two operation mode (DC and AC). The DC mode control the drain current ( $I_D$ ) of nanowire while the AC mode is for current variance measurement. Each of them references different sources. In section 2.1, we first talk about the reason why we perform  $I_D$ - $V_G$  sweep. Then we review the reference of our DC mode circuit design. The references of AC mode circuit design is in section 2.2. In the last section, we discuss the two assumptions mentioned in section 1.2.

### 2.1 DC Sweep: $I_D$ - $V_G$ Curves

In this section, we review the knowledge and an article that is related to our design of large signal mode (DC).

#### 2.1.1 $I_D$ - $V_G$ and Transconductance

A common method for examining nanowire electrical properties is to perform DC sweep. Among all kinds of sweep method, we choose the  $I_D$ - $V_G$  in respect of the physical characteristic. In the n-type transistor, the binding of negatively charged biomolecules induces surface-near silicon ions discharged and thus lower the threshold voltage. It is straightforward to think of these binding molecules as a voltage

signal input to the gate with its value depends on the concentration. And this voltage signal effect nanowire in the same way  $V_G$  does. So by plotting  $I_D$ - $V_G$  curves, we can have a thumbnail of how concentration affects the  $I_D$ .

### 2.1.2 Source Follower

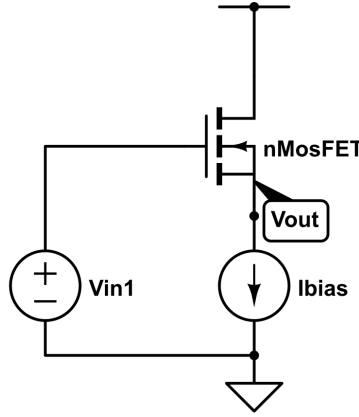


Figure 2.1: Source Follower

As one of the basic single stage amplifier, source follower (common drain) are employed to transfer voltage signal from gate to source while keeping drain current constant. The transfer function can be derived as:

$$\frac{V_{out}}{V_{in}} = \frac{r_{ds}g_m}{1 + r_{ds}g_m} \quad (2.1)$$

$$\approx 1 \quad \text{for} \quad r_{ds}g_m \gg 1 \quad (2.2)$$

$g_m$  is the transconductance ( $\frac{\partial I_d}{\partial V_{gs}}$ ) and  $r_{ds}$  is the drain-to-source resistance. Although we haven't seen the structure be applied to nanowire, there have been several applications in the read-out circuits of ISFET (Ion-sensitive Field-effect Transistor)[10, 12] for a long time.

The read-out circuit in [10] applied ISFET as a biological transducer that converts detected bio-signal into the electrical signal, which resembles our nanowire biosensor. Its adopt source follower structure as its analog front-end. The bio-signal induced voltage difference at the ISFET gate-end is converted to the source-end. This structure requires a biasing current source which may have to be stable, noiseless or wide-range on demand. Since the bias current is usually under micro-scale

even nano-scale, it is impractical to use an external current source merely. The article used two resistors and an op-amp to design a current scale down circuit. Bias current decreases in proportional to the resistance ratio ( $N$ ) of one resistor to another. Moreover, by keeping  $V_{ds}$  at a constant value (0.5v), the circuit also removes the short channel effect. Below show the schematic where two op-amp based unit gain buffer are added to force the voltage at drain-end follows the source-end.

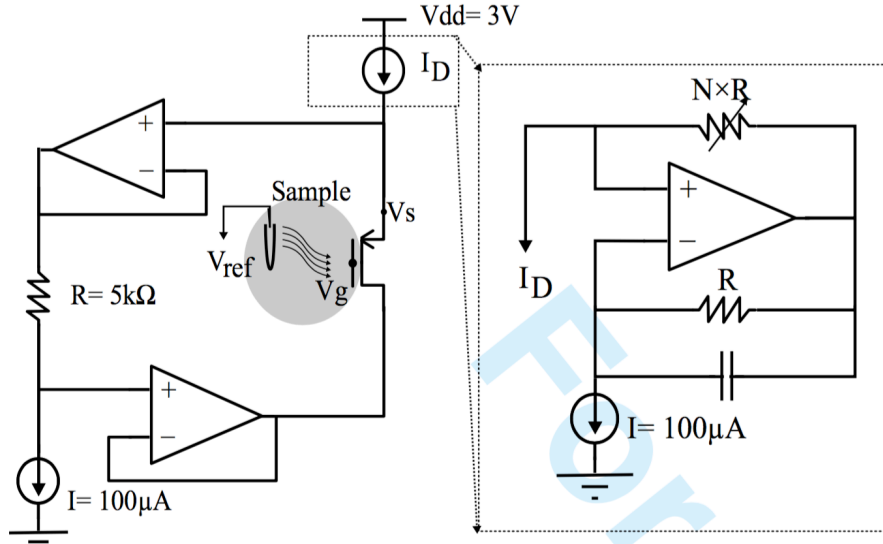


Figure 2.2: ISFET readout circuit in [10]

An issue needed to be aware is the impedance matching between the element and the current source circuit. The output impedance of current source should be much larger than the input impedance of the biasing element. The equation for the output impedance of source follower is:

$$\frac{r_{ds}}{1 + g_m r_{ds}} \quad (2.3)$$

This equation can be simplified as:

$$\frac{1}{g_m} \quad \text{for} \quad g_m r_{ds} \gg 1 \quad (2.4)$$

The output impedance of the current source circuit is:

$$N \times R_s \quad (2.5)$$

$R_s$  is the impedance of the right-bottom current source in Fig.2.2. In the integrated circuit,  $R_s$  is not ideal but usually close to the  $r_{ds}$  of a single MOSFET.

As mentioned, Eq.2.5 should be far larger than Eq.2.4. However,  $g_m$  is proportional to  $I_d$ , which means Eq.2.4 is inversely proportional to  $N$ . When the bias current decreases, the output impedance decreases while the input impedance at the ISFET source-end increases. Therefore, there is a lower boundary of the bias current. We observed this boundary when we construct this circuit with discrete elements. These will be presented and discussed in chapter 4.

The source follower structure provides a direct signal transition method. It is a good candidate for the read-out circuit with the aim of detecting transconductance or threshold voltage variance. Nevertheless, post-processing such as amplification and filtering are necessary. The experiment results in the article are untreated. Strong signal attenuation exists, which are mainly caused by low-frequency noise and ISFET drift [9]. The drift problem is dealt with through signal processing techniques while noise problems are left untreated.

## 2.2 Small Signal (AC) Measurement Method Review

In the previous section, the source follower we mentioned exhibited compelling advantages as a signal processing structure of nano-device. However, the structure overcomes obstacles when being applied to the small signal detection. Parasitic capacitors and resistors can severely influence the results.

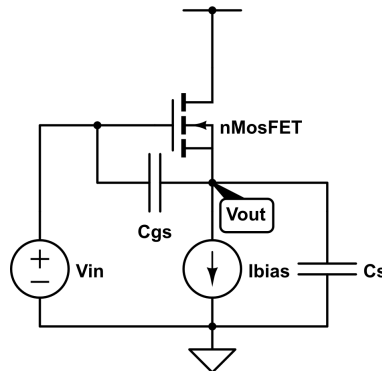


Figure 2.3: Source Follower with parasitic capacitance

As in figure 2.3 where the parasitic elements are included, we modified the transfer function Eq.2.2 as:

$$\frac{V_{out}}{V_{in}} = \frac{r_{ds}(sC_{gs} + gm)}{1 + r_{ds}(gm + s(C_{gs} + C_s))} \quad (2.6)$$

The equation can be similar to Eq.2.2 which roughly equals to 1 as long as  $C_s$  is far more smaller than  $C_{gs}$ . Unfortunately,  $C_s$  can be large for the output end of source follower usually connects to a next stage input or a pad. In that case, the parasitic capacitors may attenuate the signal.

We want to build another circuit structure that can not only performs AC signal measurement but also immunes from parasitic capacitance. We started by reviewing those works that try to measure the parasitic capacitance. Below, the works from two teams aim to measure drain-to-source resistance ( $R_{NW}$ ) and drain-to-source capacitance ( $C_{NW}$ ). The focus of the review is on the function and design theory of their read-out circuit.

### 2.2.1 RC Time Delay Measuring

The measurement system for ZnO-nanowire based sensor array from [1] applies the Time-over-Threshold techniques to its read-out circuit (Fig.2.4). The circuit alternatively charges an on-chip capacitor ( $C_{int}$ ) with a constant current and discharges it through the nano-material resistance (nanowire). An inverter with its output switches from on to off when the capacitor is charged to its input threshold voltage, and vice versa. This behavior converts information of nanowire such as capacitance and resistance into time information. Both  $C_{int}$  and  $C_{NW}$  effect charging time and together with the  $R_{NW}$  effect the discharging time.

The work presented in [1] doesn't have enough explanation about how do they interpret the capacitance and resistance information. It merely mentioned that a microcontroller is responsible for the calculation. Besides, the work lacks simulation and experiment of using complex elements as measured target. Most of the results are the measurement of using a concrete resistor as the substitute for nanowire and regard the  $C_{NW}$  as 0p. The only nanowire experiment given at last doesn't have good performance. It seems that the design may only be applied to a pure resistance



or pure capacitance type element.

The recent publican [2] by the team is more elaborate and contains the measurement of complex elements (An element composed of a discrete resistor and a discrete capacitor).

In Fig.2.5, nanowire append between point A and B. The charging current can be applied from Mp1 or Mp2, which is determined by the “sel” signal with the aid from the MUXs. We simply assume  $\text{sel} = 1$  and point B is virtually ground. (When the  $\text{sel} = 0$ , the circuit measures the element with a reversed biasing current.) Now, we can see that the circuit design concept is same with [1]. The current charge both  $C_{int}$  and  $C_{NW}$ . When the voltage at A exceed the threshold voltage, the output switches to off and feedback to turn off the Mp1. (To be noted that a Schmitt trigger replaces the inverter at the output stage in [1].) Then the capacitor discharges through nanowire ( $r_{ds}$ ).

The right-bottom plot in Fig.2.5 defines  $T_0$  as the charging time and  $T_1$  as the discharging time. The calculation of the  $R_{NW}$  and  $C_{NW}$  can be simplified as:

$$C_{NW} = T_0 - C_{base} \quad (2.7)$$

$$R_{NW} = \frac{T_1 R_{par}}{(C_{NW} + C_{base}) R_{par} - T_1} \quad (2.8)$$

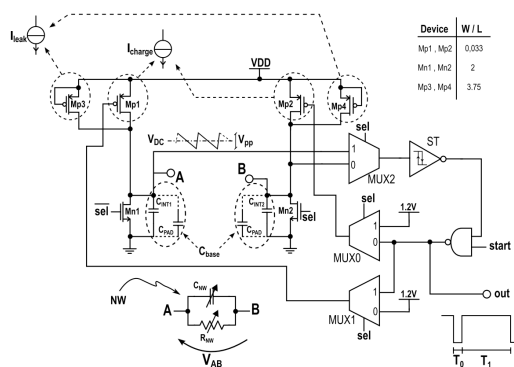
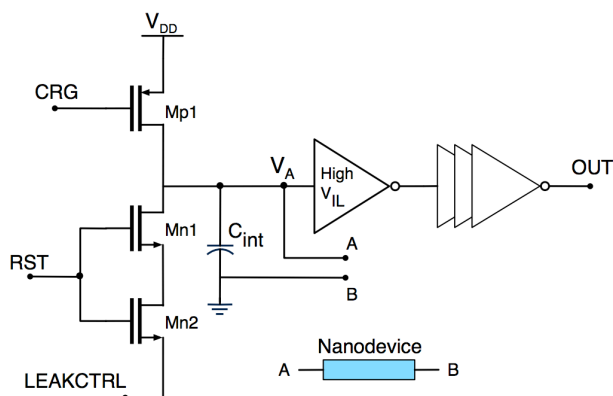
$$\text{where } R_{NW} || R_{par} = \frac{T_1}{C_{NW} + C_{base}} \quad (2.9)$$

$C_{base}$  are the  $C_{int}$  plus parasitic capacitance and  $R_{par}$  the parasitic resistance. These parasitic elements come from the transistor in the integrated circuit block such as MUX and Mp. It must be noticed that we don't concern the hysteresis of the Schmitt trigger here owing to simplicity.

### 2.2.2 Complex Impedance Solving

The nanowire-based hydrogen sensor measurement system from [13] adopts another method. It treat It use a lock-in amplifier to realize both resistive and capacitive impedance measurement.

As the previous method, it treats nanowire as a complexed one-dimensional element. The nanowire is modeled as a parallel aligned resistor and a capacitor. The

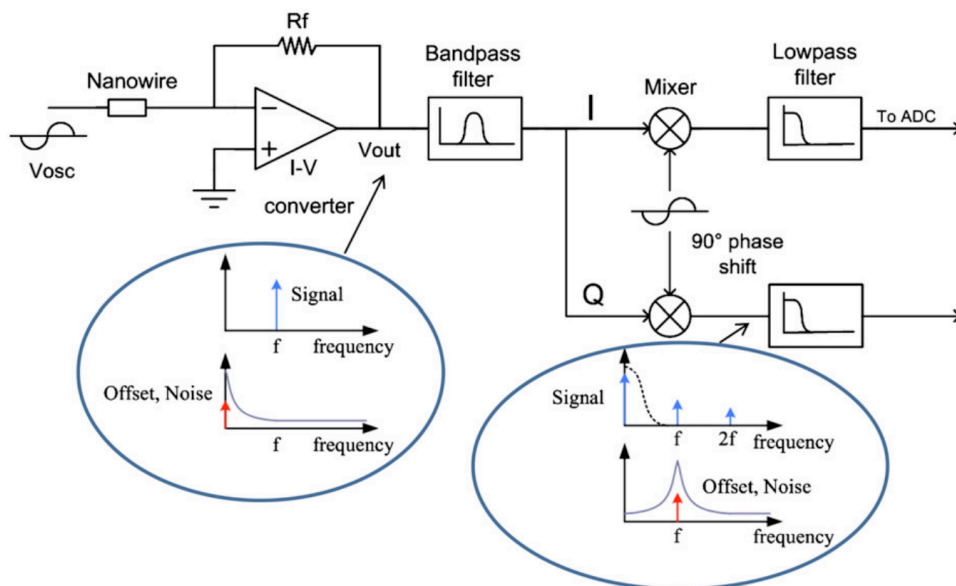


**Figure 2.4:** (a) Schematic of [1]

**Figure 2.5:** (b) Schematic of [2]

None

**Figure 2.6:** Draw mos with (Cgd + Cd) and rds is modeled by Rnw and Cnw



**Figure 2.7:** Block diagram of the lock-in amplifier in [13]

system supplies a sinusoidal voltage signal to one end of the element. Another end of the element is grounded virtually by a transimpedance amplifier (TIA). The TIA then converts the current variance into voltage output which contains complex impedance information. The resistance is in the real part while the capacitance is in the virtual part.

$$V_{out} = I_{NW} R_{TIA} \quad (2.10)$$

$$I_{NW} = V_{in} \left( \frac{1}{R_{NW}} + j2\pi f C_{NW} \right) \quad (2.11)$$

$f$  is the frequency of input signal.

The output of TIA is followed by a controllable bandpass filter (BP). The BP removes high-order harmonic interferences. Then the signal is demodulated. The resistive and capacitive impedance values are resolved through two channels: I and Q with their phase different by 90 degrees. A mixer which is a linear multiplier performs the demodulation. With a radio frequency (RF) input and the input local oscillator (LO) input, it produce an output signal that consists of signals with frequencies  $f_{RF} + f_{LO}$  and  $f_{RF} - f_{LO}$ . Incidentally, the signal is immune from the perturbation of low-frequency noise which is a common problem for the biosensor.

### 2.2.3 Comparison and Conclusion

We compare Method 1 (Sec.2.2.1) and Method 2 (Sec.2.2.2) here. Both of them focus on detecting the  $R_{NW}$  difference. According to the comparison table below (2.1), we can see the resistor measurement range of Method 1 is different from Method 2 by a large extent. This may because the minimum bias current of nanowire provided by the circuits are different. The minimum current in Method 1 is limited by the pmos(I charge) and the leakage current. In Method 2, it is limited by the TIA. Our method adopts this TIA block and will discuss this problem in chapter 5.

Method 2 perform well when it comes to noise suppression. In fact, the circuit in Method 1 doesn't provide noise reduction ability. The particular structure it uses (The article [1] mentioned it as M4N approach) is the one responsible for that.

Method 1 has a lower power consumption. However, it doesn't include the power of microcontroller and may underestimate.

	[2]	[13]
R meas range	1M - 1G	10 - 40k
R meas error	< 2.5%	< 2%
C meas range	100fF - 1uF	0.5 - 1.8nF
C meas error	< 3%	< 3%
SNR	> 45dB	-
Input refered noise	-	190 nV/sqrt(Hz) @ 5 kHz
CMOS Technology	0.13um	0.18um
Power consumption	14.82uW	2mW

**Table 2.1:** Specification Summary

In our project, capacitance measurement is not our object. But we still need to consider the parasitic capacitor effect in our circuit design. Method 1 converts the resistance information into time (frequency) information. If one want to avoid the effect of the parasitic capacitor, he should apply a  $C_{int}$  that is much larger than  $C_{NW}$ . However, it is not practical in integrated design because the chip size is limited.

Method 2 uses a TIA to measure resistance and capacitance together first and then resolve the complex value. We can write the complex impedance value as:

$$\frac{1}{1/R_{NW} + i2\pi f C_{NW}} \quad (2.12)$$

In Eq.2.12,  $i$  is imaginary unit and  $f$  is the signal frequency. We notice that the capacitance value is much larger than the resistance value. This difference may be revised downward in our silicon nanowire case. The resistance can be more than 100M and the  $1/g_m$  is roughly 1M.

Another reason that makes Method 2 more attractive is that it is more flexible. One can add other analog blocks such as noise filter or amplifier to it.

Overall, Method 1 has the advantage in detecting range and accuracy while Method 2 has better noise suppression and flexibility.

## 2.3 Two assumption for Dealing with Disparity Problem

In chapter 1, to deal with disparity problem, we assume that:

1. The nanowire transconductance ( $g_m = \frac{\partial I_D}{\partial V_{GS}}$ ) depends on  $I_D$  and independent on  $V_{GS}$ .
2. The changing of the concentration of biomolecule can be viewed as a voltage signal input to the gate end of a transistor.

We discuss them in this section.

### 2.3.1 Transconductance and $I_D$

With the MOSFET model of weak and strong inversion, we have the  $I_D$  equations of MOSFET:

weak inversion:  $I_D = I_0 e^{\kappa V_{GS}/\phi_t} (1 - e^{-V_{DS}/\phi_t})$  (2.13)

$= I_0 e^{\kappa V_{GS}/\phi_t}$  where  $V_{DS} > 4\phi_t$  (2.14)

strong inversion:  $I_D = \mu C_{ox} \frac{W}{L} ((V_{GS} - V_{th})V_{DS} - \frac{V_{DS}^2}{2})$  (2.15)

$= \mu C_{ox} \frac{W}{L} (V_{GS} - V_{th})^2$  where  $V_{DS} > V_{GS} - V_{th}$  (2.16)

$C_{ox}$  is the oxide capacitance and  $\mu$  is the electron mobility. Both of them depends on doping concentration.  $W$  and  $L$  are the width and length of the transistor.  $\phi_t$  is the thermal voltage depending on temperature. The  $\kappa$  is the gate coupling coefficient. It will be discuss in the next paragraph. To be noted that we ignore the short channel effect, which doesn't effect our discussion since we always keep  $V_{DS}$  constant.

We then derive  $g_m$ :

$$\text{weak inversion: } g_m = \frac{\kappa I_D}{\phi_t} \quad (2.17)$$

$$\text{strong inversion: } g_m = \sqrt{2\mu C_{ox} \left(\frac{W}{L}\right) I_D} \quad (2.18)$$

$$(2.19)$$

For the strong inversion, the Eq.2.19 shows that the assumption 1 is correct. However, the assumption is not completely right for transistor in weak inversion. According to the Eq.2.18, the  $g_m$  is effect not only by  $I_D$  but also by the  $\kappa$ . It is a non-linear parameter effected by  $V_G$  and other factors. Its value is range from 0.4 to 0.9. In our circuit, this problem is currently left unsolved. We present its effect in chapter 6.

### 2.3.2 A Simple Model for Concentration Affect

In [5], the team plot the  $I_D$ - $V_G$  curves and study how the curve changes with the concentration of biomolecules. We observe that in the plot (Fig.2.8) with a log scale for the y-axis, curves with different concentration exhibit a same rising trend when  $I_D$  is low ( $< 100\text{nA}$ ). Each curve seems to be different with the other by a constant fold. By applying the weak inversion current equation of MOSFET, we found that the assumption can explain this concentration effect.

$$I_{D1} = I_0 e^{\kappa(V_{GS}-V_{th})/\phi_t} \quad (2.20)$$

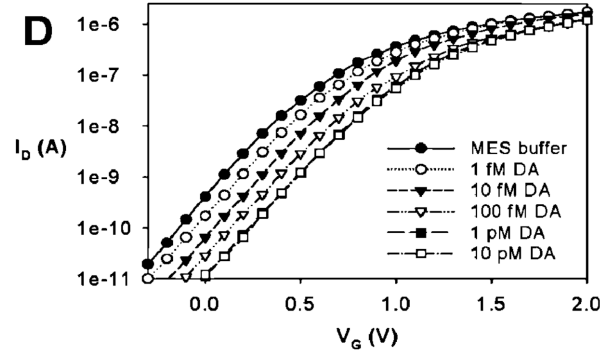
$$I_{D2} = I_0 e^{\kappa(V_{GS}-(V_{th}-v_c))/\phi_t} \quad (2.21)$$

$$\rightarrow I_{D2} = f(v_c) \times I_{D1} \quad \text{where} \quad f(\Delta v_g) = e^{v_c/\phi_t} \quad (2.22)$$

The  $I_{D1}$  and  $I_{D2}$  are the current of two nanowire elements placed in solutions of different concentration. The  $(v_c)$  is a concentration related variable we create. The Eq.2.22 implies that when nanowire is in weak inversion region, its log  $I_D$  difference is independent of  $V_g$ .

$$\log I_{D2} - \log I_{D1} = \log \frac{I_{D2}}{I_{D1}} = \log f(v_c) = v_c/\phi_t \quad (2.23)$$

As for strong inversion region which refer to the large current section in Fig.2.8, the difference of the curves diminish as  $V_G$  increasing. The strong inversion equation (Eq.2.16) shows that if  $V_{GS}$  is far larger then  $v_c$ , the concentration effect can be ignored.



**Figure 2.8:** Concentration-dependent electric response( $I_D - V_G$ ) of biotin-modified poly-Si NWFET following biotin-streptavidin interaction.[5]

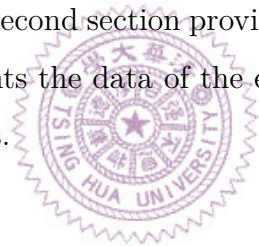
We will further prove the two assumptions by the data of biology experiment in section.3.2.2.



## Chapter 3

# Nanowire Structure and Measurement

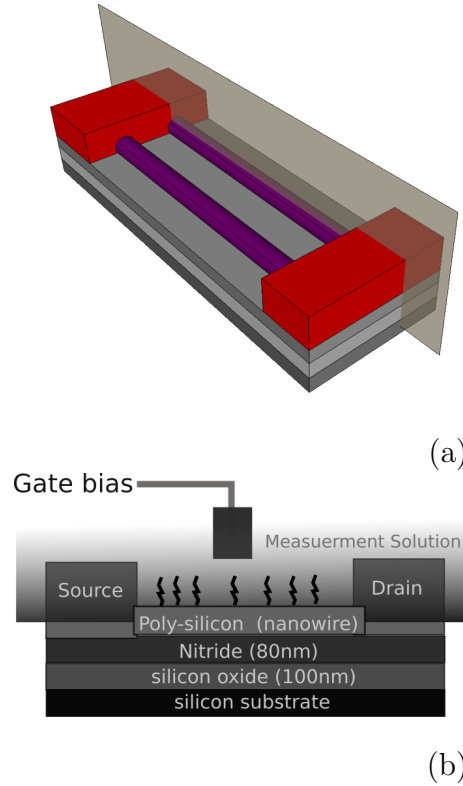
In this chapter, we present the experiment data and some analysis which are the foundation of our circuit design. The first section gives a brief description of our silicon nanowire element. The second section provides the data of the biology experiments. The last section presents the data of the electrical measurement, on which our circuit design spec depends.



### 3.1 Brief Description of Nanowire Structure

The nanowire we use is made by Prof. Yang's team (National Chiao Tung University)[7]. Fig.3.1 is the sectional view of the nanowire structure. The fabrication process is based on the poly silicon sidewall spacer technique. The n-Type doped poly-SiNW FET has two to ten poly silicon channels. Each channel is 80nm in width and 2 $\mu$ m in length. A Large portion of the channel surface is exposed to environment. The exposed region, through several post-process, capture the DNA probe and serve as the sensing site for DNA molecules.[7, 8]



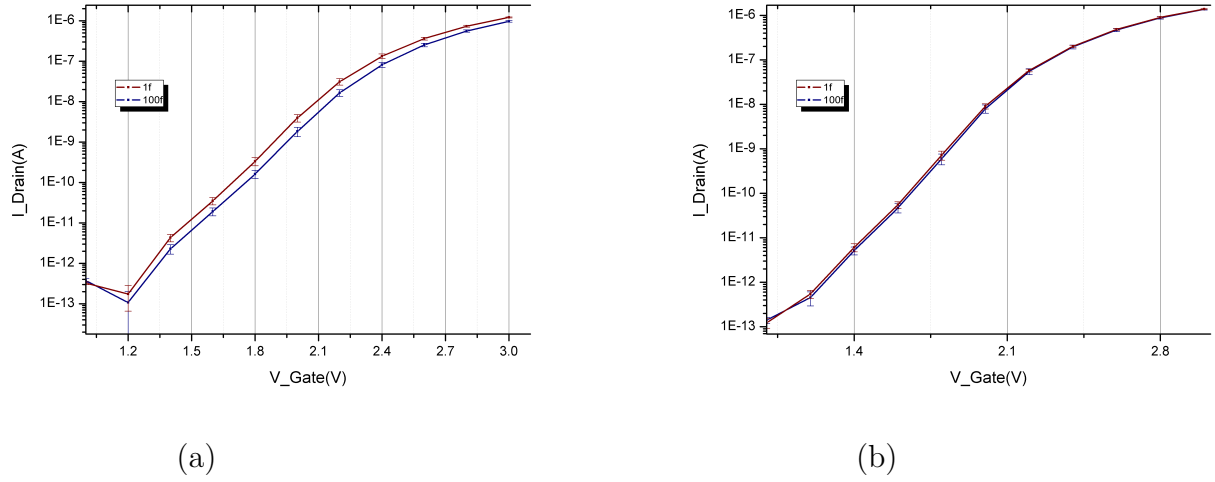


**Figure 3.1:** Nanowire Structure. (a) A nanowire element with two poly silicon channels. (b) is the sectional view of the cutting plane in (a).

## 3.2 Biology Experiment

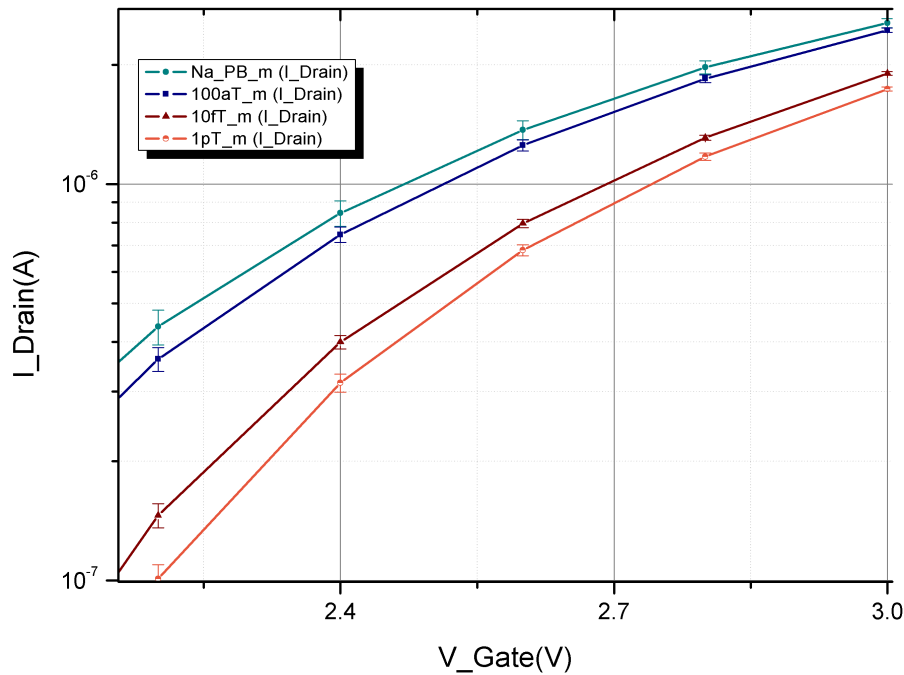
The biology experiment data are provided by Prof. Yang's team. These data are the Id-V<sub>g</sub> measurement of the same biomolecule placed under different circumstances or with different nanowire elements. With each measurement repeated three times, we find the mean and standard deviation (SD) of them and consider the SD value as the intrinsic noise of nanowire. We want to ensure that such noise should not be greater than the signal. To be more specific, we examine whether the Id-V<sub>g</sub> curves of different concentration overlap with each other or not. We present an example below:

The Fig.3.2 are concentration-dependent measurements (1 femto mole(fM) and 100fM biomolecule solution) obtained with two elements ((a) and (b)). The two curves in the (a) are distinguishable from the other after gate voltage of 1.4v They are not distinguishable in the (b) since they overlap each other. We thus assert that the element of (b) can't detect the concentration difference between 1fM and 100fM.



**Figure 3.2:** Concentration-dependent  $I_D$ - $V_G$  curves of two equivalent nanowire elements. In (a), the measurement result of 1fM and 100fM biomolecule solution is distinguishable. There is no overlap between two curves. This is not true in (b).

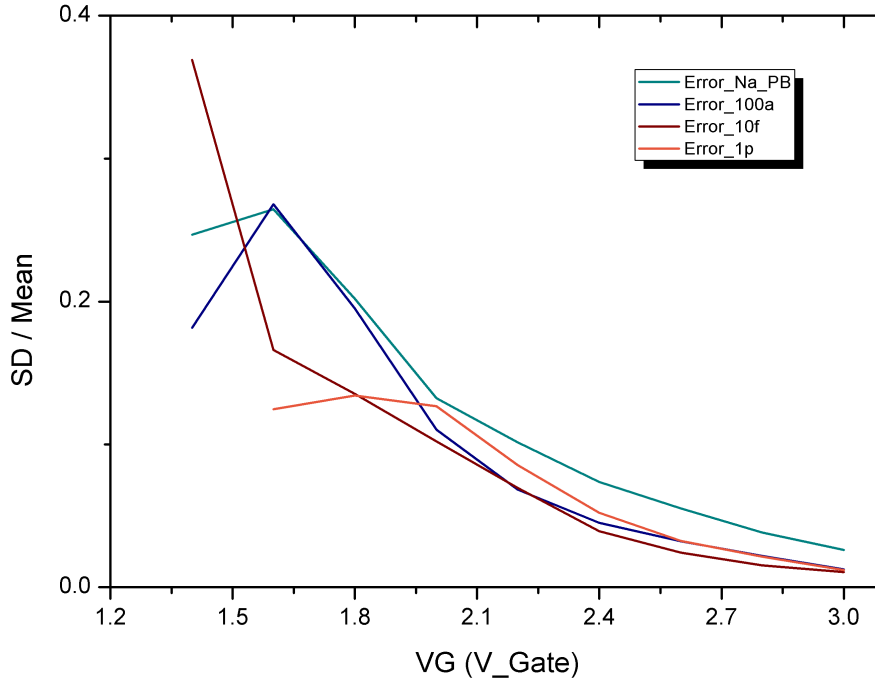
The noise is stronger than the signal (The signal means the  $I_D$  difference caused by the concentration difference). The element of (a) can do so if it is biased at gate voltage larger than 1.4v or drain current larger than  $10^{-11}$ .



**Figure 3.3:** Concentration-dependent  $I_D$ - $V_G$  curves. Since the biomolecule is negative-charged, the lower the concentration is, the higher the curve is. To be noticed, the 10fM curve is closer to the curve of 1pM than 100aM.

In Fig.3.3,  $I_D$  increase with the biomolecule concentration. One can find that there is only a few “space” between PBS buffer and solution containing biomolecule with the concentration of 100aM. Hence the 100aM should be the limit of detection.

It is worth noting that there is more space between 100aM and 10fM than the space between 10fM and 1pM. And the noise rate:  $SD/Mean$  is independent of concentration (Fig.3.4). Hence we say that the “resolution” for detecting concentration ranging from 100aM to 10fM may be better than the that ranging from 10fM to 1pM.



**Figure 3.4:** The noise rate of Fig.3.3. The noise rate is obtained by dividing SD by Mean.

### 3.2.1 Appropriate operation region

In [8], the team found that “the induced change of current ( $I_D$ ) following biomolecule was dependent on the applied gate voltage (VG)” (Fig.). In other words, a “biomolecule concentration resolution” seems to depend on  $V_G$ . The team tried to find a bias gate voltage range which can induce more current response. In our opinion, the induced change of current ( $I_D$ ) following biomolecule is not directly dependent on  $V_G$ . Based

on the our assumption 2 (section1.2), it depends on the transconductance. The phenomenon is found by  $I_D$ - $V_G$  curves, which means the  $V_G$  also affect the  $I_D$  which cause different transconductance.

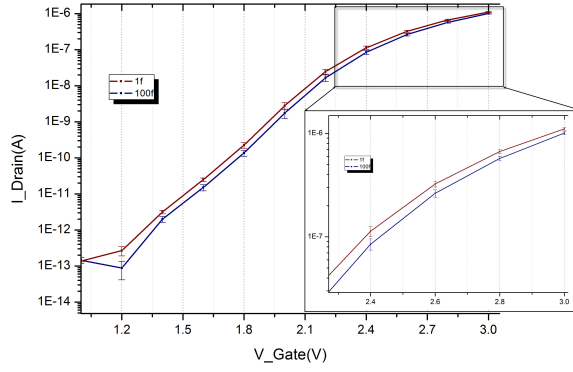
Furthermore, we think the noise effect should be taken into consideration. Some kinds of noise have positive correlations with transconductance.

Still, we want find an appropriate operation region of nanowire that has the largest concentration resolution. We proposed a comprehensive method that one should choose the operation region with more “noise tolerance”. The noise tolerance is defined as:

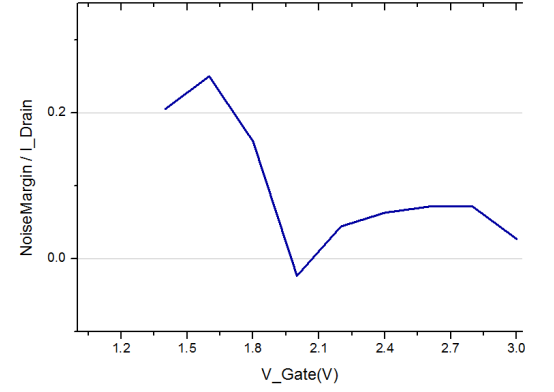
$$\text{noise tolerance} = \frac{I_{D1} - SD1 - (I_{D2} + SD2)}{I_{D2}} \quad (3.1)$$

$I_D$  and  $SD$  are the mean and standard deviation of a curve. The larger the noise tolerance implies there is more space between two curves. And more space implies the less chance of overlapping between to concentration curves may happens.

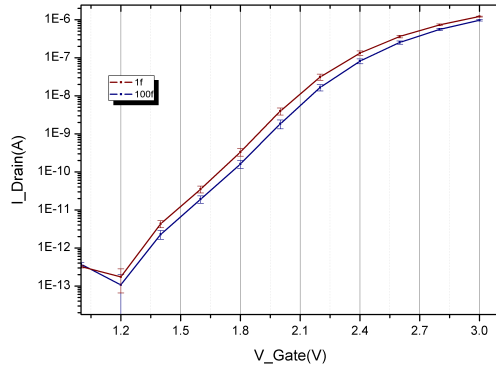
We present analysis results from three nanowire elements. The Fig.3.5(a), (c), (e) are the  $I_D$ - $V_G$  curves of three elements and the Fig.3.5(b), (d), (f) are the noise tolerance respectively. One can observe in (b) and (d) that there is first a rising trend then followed by a drop as gate voltage decrease. The drop doesn't exist in (f) may because the weak inversion is too narrow. The transistor enters into the reverse region before the drop appears. The highest points of (b) and (d) locate in the weak inversion region and is close to the transition region (The region between strong inversion and weak inversion region). We therefore suggest that in this section nanowire should has the largest concentration resolution.



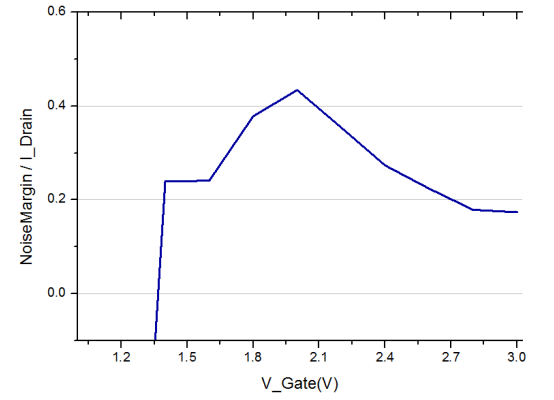
(a)



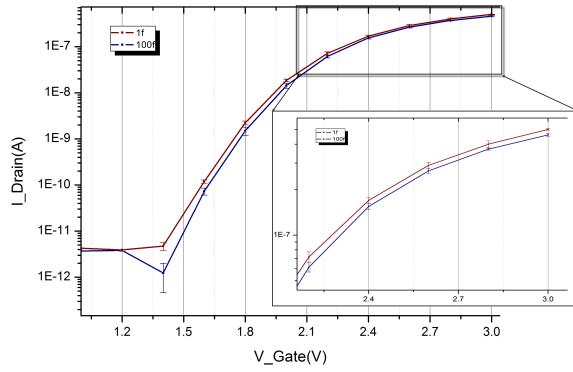
(b)



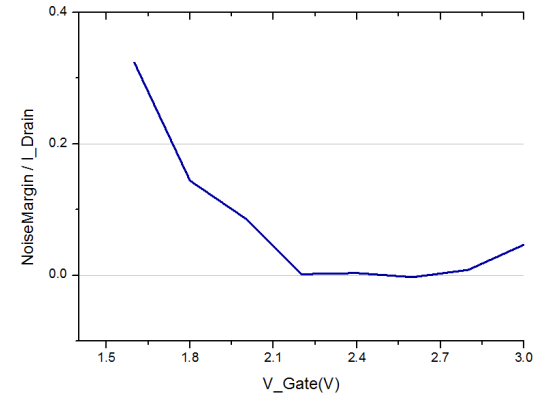
(c)



(d)



(e)

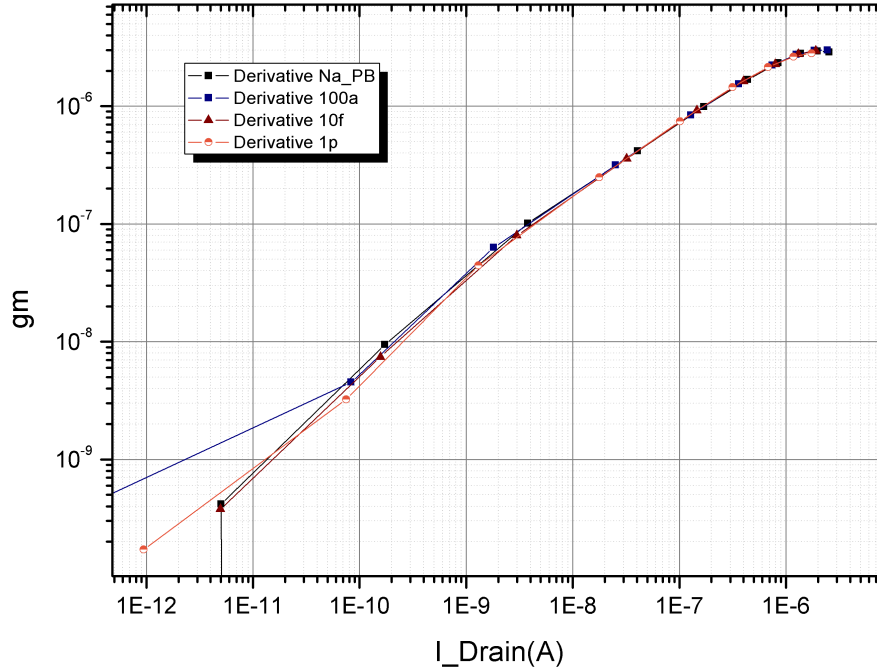


(f)

Figure 3.5

### 3.2.2 $g_m$ - $I_D$ Plot

We plot the  $g_m$ - $I_D$  curve with the data in Fig.3.3. It clearly proves our two assumptions for dealing the disparity problem, which we have discussed in section.2.3.



**Figure 3.6:** The  $g_m$ - $I_D$  curve obtained by the  $I_D$ - $V_G$  curve in Fig.3.3. The curves start splitting after  $I_D > 1\mu\text{A}$  where the element may enter into strong inversion region.

In Fig.3.6, when  $I_D$  is from  $0.1\text{nA}$  to  $1\mu\text{A}$ , we can observe that the  $g_m$  of nanowire is almost independent of concentration and merely depends on  $I_D$ . In fact, the curves start splitting after  $I_D > 1\mu\text{A}$ . It means the element is no longer in weak inversion region but enters into strong inversion region. And we should not operate our nanowire elements in that region.

### 3.3 Electrical Measurements

This section presents the data analysis results. The data are obtained from our measurements with the source meter (Keithley 2602). To exclude the ion effect, we placed nanowire elements in dd-water instead of biomolecule solution. And there is no DNA probe on the poly-Si channel surfaces.

### 3.3.1 Front Gate and Back Gate

Our nanowire has two gates available: floating gate (liquid gate) and back-gate. We choose floating gate as the operation gate mainly because the floating gate can induce larger drain-current. In other words, it has higher transconductance (Fig.3.7). In our circuit design, nanowire is placed in a feedback loop where its transconductance is proportional to the loop gain (chapter 5).

There are some advantages of back-gate. One of them is the ability to lower the  $1/f$  noise [14, 11]. However, this only happens in a very high gate voltage, which is not practical in the integrated circuit design.

### 3.3.2 Transconductance

The most crucial parameter for our circuit design is the transconductance ( $g_m$ ). We acquire it by finding the partial derivative of  $I_D$  of  $V_G$ . Since in section.2.3.1 we proved that  $g_m$  is related to  $I_D$ , we plot the  $g_m$ - $I_D$  curve to reveal their relation (Fig.3.8(b)).

The  $g_m$ - $I_D$  plot indicates that there is a “linear region” where  $g_m$  is proportional to  $I_D$ . This corresponds to our induction (Eq.2.18). We can recognize that our nanowire element is operated in weak inversion region when  $I_D$  is less than  $10\mu\text{A}$ . Therefore, by the section.3.2.1, we decide our the  $I_D$  of our nanowire should be operated below  $10\mu\text{A}$ .

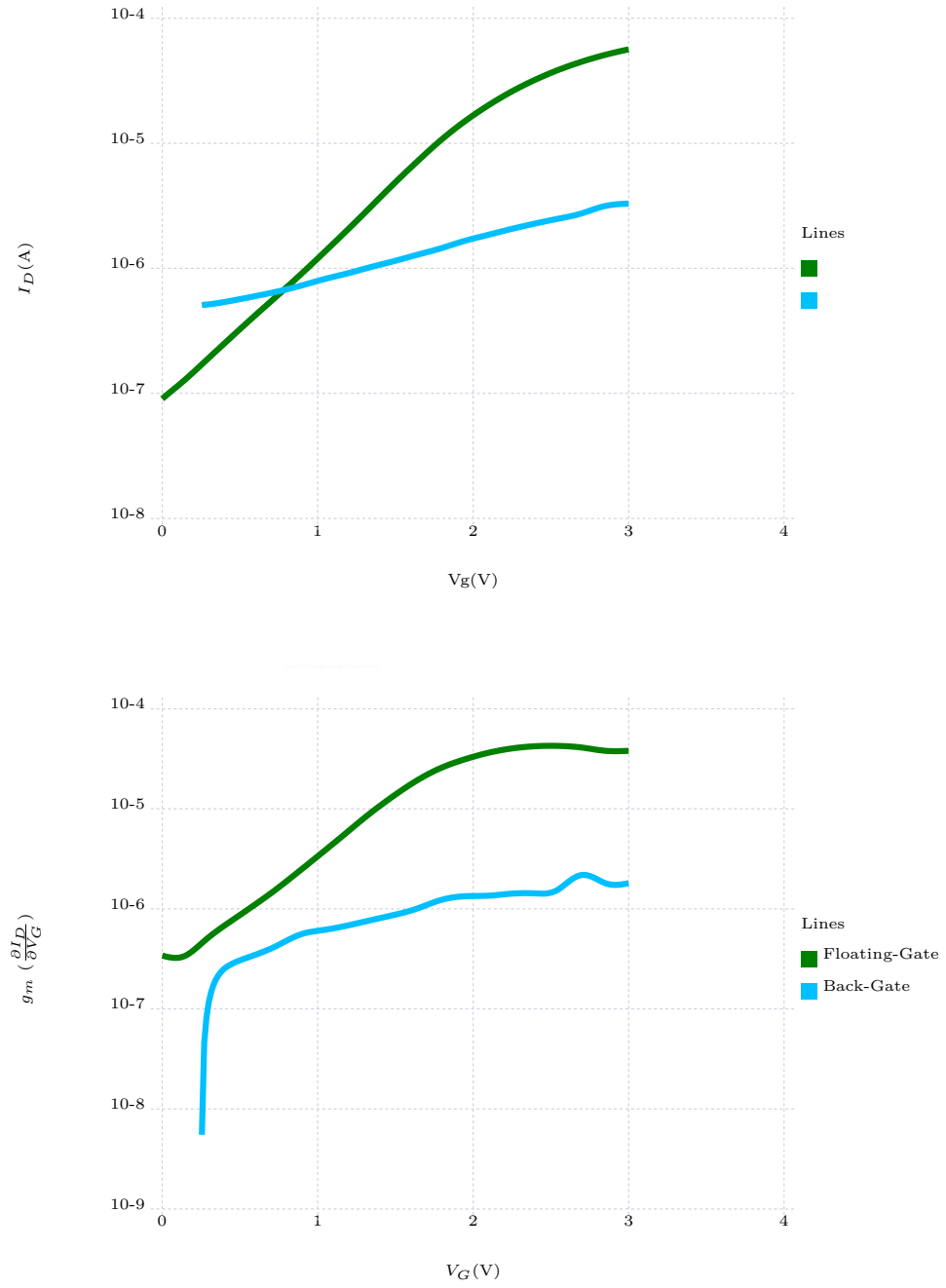
We also proved that the transconductance under this region is unaffected by the  $V_{DS}$ .

### 3.3.3 Drain-to-source impedance ( $r_{ds}$ )

In our circuit design, we keep  $V_{DS}$  constant. By the measurement in last section, 0.7 is enough to keep nanowire in saturation region for  $V_G$  range from 0v to 3v. However, due to the fabrication variance, the value varies from 0.75v to 1v.

We concern about how the  $I_D$  effect  $r_{ds}$ . The way we obtained  $r_{ds}$  is as follows:

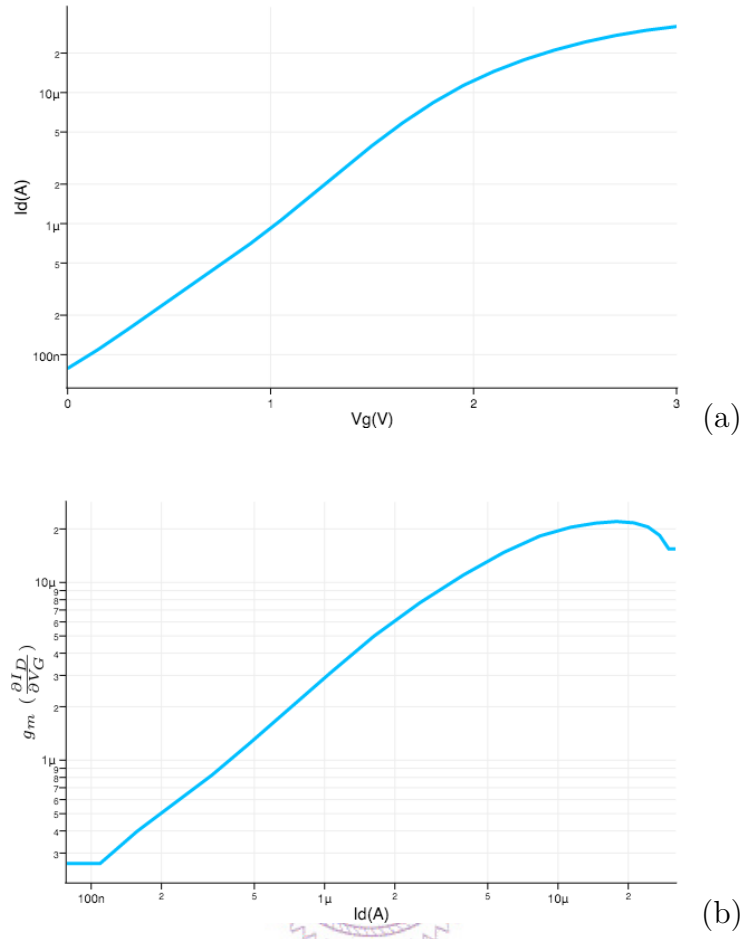
1. Perform  $I_D$ - $V_G$  sweep with two different  $V_D$ .



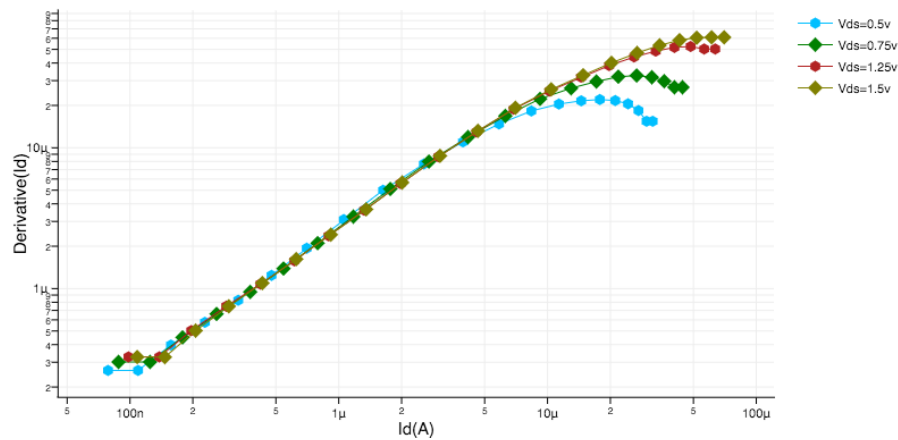
**Figure 3.7:** Comparison between the DC sweep of voltage on the floating gate and back gate. (a)  $I_D$  (b) Transconductance ( $g_m$ ): the derivative of  $I_D$

. The transconductance of the floating gate is larger than the back gate.





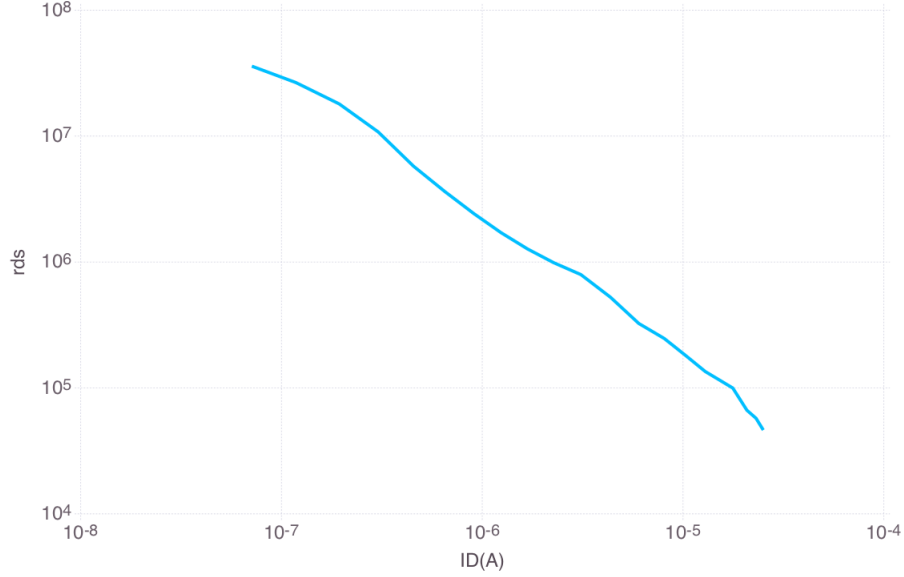
**Figure 3.8:** Electrical response of a nanowire element. (a) Sweep  $V_G$  and measure the  $I_D$  changes. And by finding the transconductance ( $g_m$ ): the derivative of  $I_D$  of  $V_G$ , we plot (b) the  $g_m$ - $I_D$  curve



**Figure 3.9:** Id-transconductance with  $V_{ds}$  variance

2. Find the difference of  $I_D$  at each  $V_G$  sweep point and divide it by the difference of  $V_D$ .

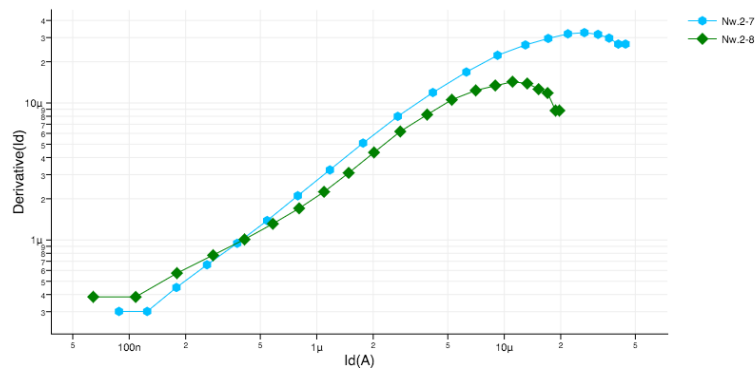
The result is as Fig.3.10



**Figure 3.10:** Id-transconductance with Vds variance

### 3.4 Disparity Problem exists

We measured two nanowire elements which lie on the same wafer and are immersed with the same testing PBS solution. Below, the  $g_m$ - $I_D$  plot (Fig.3.11) shows that even the environment is same, two elements exhibit different electrical response.



**Figure 3.11:** Disparity problem casue nanowire elements with same environment can exhibit different electrical responses.

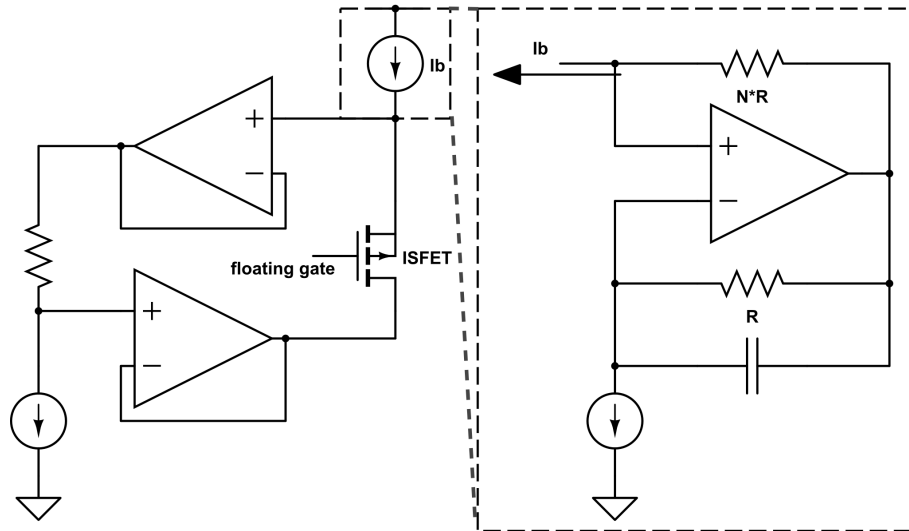
# Chapter 4

## Discrete Circuitry Design

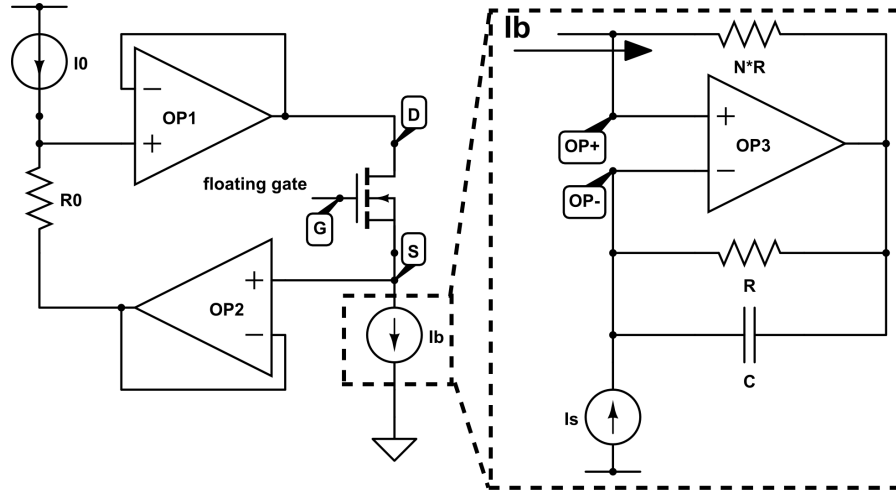
This chapter contains the discrete circuit which has been briefly reviewed in section 2.1.2. We build this circuit to practice the constant current method.

### 4.1 Transforming the design from p-type measuring into n-type measuring

In [10], the circuit is for p-type ISFET element (Fig.4.1). Our nanowire element is n-type. Hence we transform the circuit as Fig.4.2.



**Figure 4.1:** The schematic of read-out circuit from [10]. The ISFET is a p-type element. It is controlled by the current source  $I_b$  whose sub-circuit is shown at right.



**Figure 4.2:** The our circuit schematic transformed from Fig.???. The center transistor is a n-type element. It is controlled by the current source  $I_b$  whose sub-circuit is shown at right.

## 4.2 Circuit Description

The circuit is divided into two sections: the circuit body and the biasing current source ( $I_b$ ).

### Circuit Body

The circuit body section is a source follower structure. The input of the circuit is at the floating gate ( $G$ ) of the center transistor, where the output is at its source ( $S$ ).

The  $I_D$  of the transistor is controlled by the  $I_b$ . The leakage current flowing into the negative input of OP2 is less than 0.1nA. Thus the  $I_D$  of the transistor should always be same as bias current  $I_b$ .

The  $V_{DS}$  is always equal to the potential difference ( $I_0 \times R_0$ ) across the resistor  $R_0$ . This is achieved by two OP-based unity gain buffer. They connected serially with  $R_b$  and cause the voltage at drain end  $D$  follows the voltage at  $S$ .

### biasing current source ( $I_b$ )

The  $I_b$  is in fact a current scale down circuit. By concerning the OP as ideal, the node  $OP+$  has the same voltage with  $OP-$ . This equalize the potential difference across two resistors whose resistance are different by  $N$ -fold. As the result, the current of  $I_b$  and  $I_s$  are also different by  $N$ -fold.  $I_b = I_s/N$ .

The capacitor is for filtering. It filter the high frequency noise out to create a stable output current.

### 4.3 Discrete Element

We use tlc2264 made by Texas Instrument (TI) as our OP. This OP element has working voltage of  $\pm 5v$  and can perform rail-to-rail output operation. Its gain (Large-signal differential voltage amplification rate) is 170 for the output load greater than 50k.

For the current source  $I_s$  and  $I_0$ , we use lm334 made by National Semiconductor. It is a 3-terminal adjustable current sources with wide dynamic voltage range of 1v to 40v and current accuracy of  $\pm 3\%$ . In our experiment, the current  $I_s$  is fixed at  $1\mu A$  where its output impedance is  $1.2G\Omega$ .

### 4.4 Circuit Performance and Conclusion

We examined the performance of our circuit by plotting its  $I_D-V_G$  curve. The  $I_0$ ,  $R_0$  and  $V_G$  were kept constant. We swept the  $I_D$  by changing the  $N$  value with a variable resistor. The  $N$  ranges from 1 to 1000. And the Ib circuit should produces bias current  $I_b$  from  $1\mu A$  to  $1nA$ .

We measured the output voltage at  $S$  and subtracted this value from  $V_G$  to get the respective  $V_{GS}$ . These two value gave result to the  $I_D-V_G$  curve in Fig.4.3.

The measurement result shows that when  $I_D$  is larger than  $10nA$ , the circuit is functional. The  $I_D-V_G$  curve obtained by the circuit is same as the one obtained by directly sweeping  $V_G$  and measuring  $I_D$  with Source Meter (Keithley 2602).

The circuit fails when  $I_D$  is smaller than  $10nA$ . This is caused by the unmatched impedance, which we have discussed in section.2.1.2.

The output impedance of Ib circuit is:

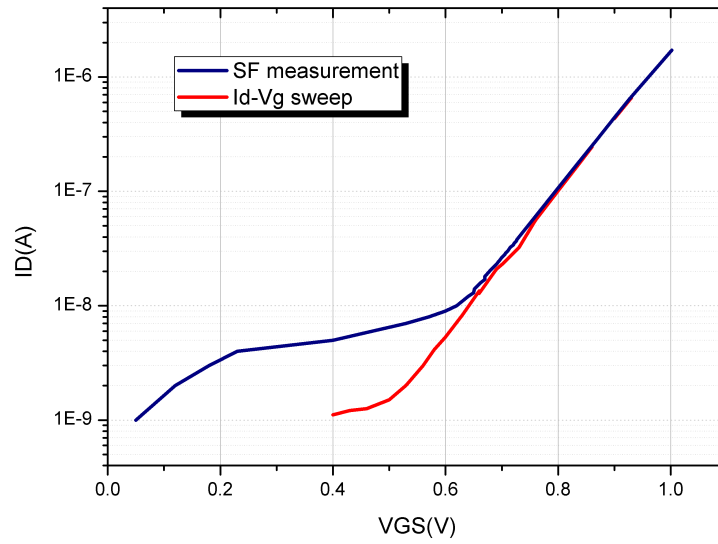
$$N \times R_s \tag{4.1}$$

$R_s$  is the output impedance of current source  $I_s$  which equals to  $1.2G\Omega$ . And the

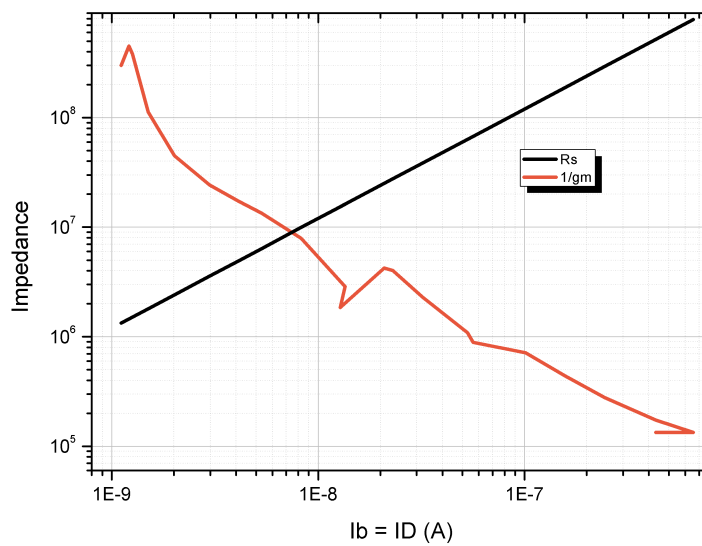
input impedance of transistor is:

$$\frac{1}{g_m} \quad (4.2)$$

We plot the  $I_D$ -Impedance plot in Fig.4.4.



**Figure 4.3:** The measurement result (“SF\_measurement”) compares with the direct  $I_D$ - $V_G$  sweep (“Id-Vg sweep”).



**Figure 4.4:** Input impedance of transistor (“1/gm”) and output impedance of Ib circuit (“Rs”). The former is found by the derivative of  $I_D$  of  $V_{G_s}$ . The latter is obtained by Eq.4.1.

Fig.4.4 proves that the  $R_s$  is close to the input impedance of transistor around  $I_D = 10nA$ . The result is that we overestimate the  $I_b$ .

Overall, the constant current method is feasible. What one needs to noticed when applying the constant current method is the impedance matching. In source follower structure, its current input impedance varies with the bias current. The varying range effect the dynamic range and need more design concern.



# Chapter 5

## Integrated Circuitry Design

This chapter presents the design of the read-out circuit and the simulation results.

### 5.1 Main

The review of source follower in section.2.1.2 suggests the constant current method for the circuit of DC measurement. The data analysis from chapter 3 supports it by the linear relation between  $I_D$  and  $g_m$ . However, the section.2.2 shows that source follower is not suitable for AC measurement. It alternatively recommends the circuit in Fig.2.7 which measures ac current signal and converts it into voltage output. This circuit is appealing because of its noise suppression, simplicity and flexibility.



# Chapter 6

## Discussion and Conclusions



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# Acknowledgement

