

Statistical Inference Part II Homework

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I produced the material below with no assistance

Exercises 6 through 10 on pages 86 and 87 of *Reasoning with Data: An Introduction to Traditional and Bayesian Statistics Using R*

6. The PlantGrowth data set contains three different groups, with each representing various plant food diets (you may need to type `data(PlantGrowth)` to activate it). The group labeled “ctrl” is the control group, while “trt1” and “trt2” are different types of experimental treatment. As a reminder, this subsetting statement accesses the weight data for the control group: `PlantGrowth$weight[PlantGrowth$group=="ctrl"]` and this subsetting statement accesses the weight data for treatment group 1: `PlantGrowth$weight[PlantGrowth$group=="trt1"]`. Run a t-test to compare the means of the control group (“ctrl”) and treatment group 1 (“trt1”) in the PlantGrowth data. Report the observed value of t, the degrees of freedom, and the p-value associated with the observed value. Assuming an alpha threshold of .05, decide whether you should reject the null hypothesis or fail to reject the null hypothesis. In addition, report the upper and lower bound of the confidence interval.

```
data("PlantGrowth")
head(PlantGrowth)
```

```
##   weight group
## 1   4.17  ctrl
## 2   5.58  ctrl
## 3   5.18  ctrl
## 4   6.11  ctrl
## 5   4.50  ctrl
## 6   4.61  ctrl
```

```
ctrl <- PlantGrowth[PlantGrowth$group == 'ctrl',]
trt1 <- PlantGrowth[PlantGrowth$group == 'trt1',]
trt2 <- PlantGrowth[PlantGrowth$group == 'trt2',]
```

```
t.test(ctrl$weight, trt1$weight)
```

```
##
## Welch Two Sample t-test
##
## data: ctrl$weight and trt1$weight
## t = 1.1913, df = 16.524, p-value = 0.2504
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
```

```
## -0.2875162  1.0295162
## sample estimates:
## mean of x mean of y
##      5.032      4.661
```

Answer: The *t* value for the T-test comparing the ctrl group and the trt1 group is **1.1913**. The degrees of freedom value is **16.524**. The p-value is **0.2504**. The upper bound of the confidence interval is **1.0295162** and lower bound of the confidence interval is **-0.2875162**. Given the *alpha* of **0.05**, and the p-value being **0.2504** (greater than the alpha), we fail to reject the null hypothesis.

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7. Install and library() the BEST package. Note that you may need to install a program called JAGS onto your computer before you try to install the BEST package inside of R. Use BESTmcmc() to compare the PlantGrowth control group ("ctrl") to treatment group 1 ("trt1"). Plot the result and document the boundary values that BESTmcmc() calculated for the HDI. Write a brief definition of the meaning of the HDI and interpret the results from this comparison.

```
#install.packages("BEST")
library(BEST)
```

```
## Loading required package: HDInterval
```

```
BESTmcmc(ctrl$weight, trt1$weight)
```

```
## Waiting for parallel processing to complete...
```

```
## done.
```

```
## MCMC fit results for BEST analysis:
```

```
## 100002 simulations saved.
```

```
##      mean      sd  median HDIlo HDIup  Rhat n.eff
## mu1      5.0268  0.2248  5.0266 4.5775  5.470 1.000 54896
## mu2      4.6417  0.3065  4.6389 4.0309  5.251 1.000 53891
## nu      34.3770 29.6486 25.8153 1.1628 92.988 1.000 20920
## sigma1   0.6628  0.2059  0.6237 0.3360  1.068 1.000 25834
## sigma2   0.8959  0.2811  0.8436 0.4585  1.458 1.002 23514
##
```

```
## 'HDIlo' and 'HDIup' are the limits of a 95% HDI credible interval.
```

```
## 'Rhat' is the potential scale reduction factor (at convergence, Rhat=1).
```

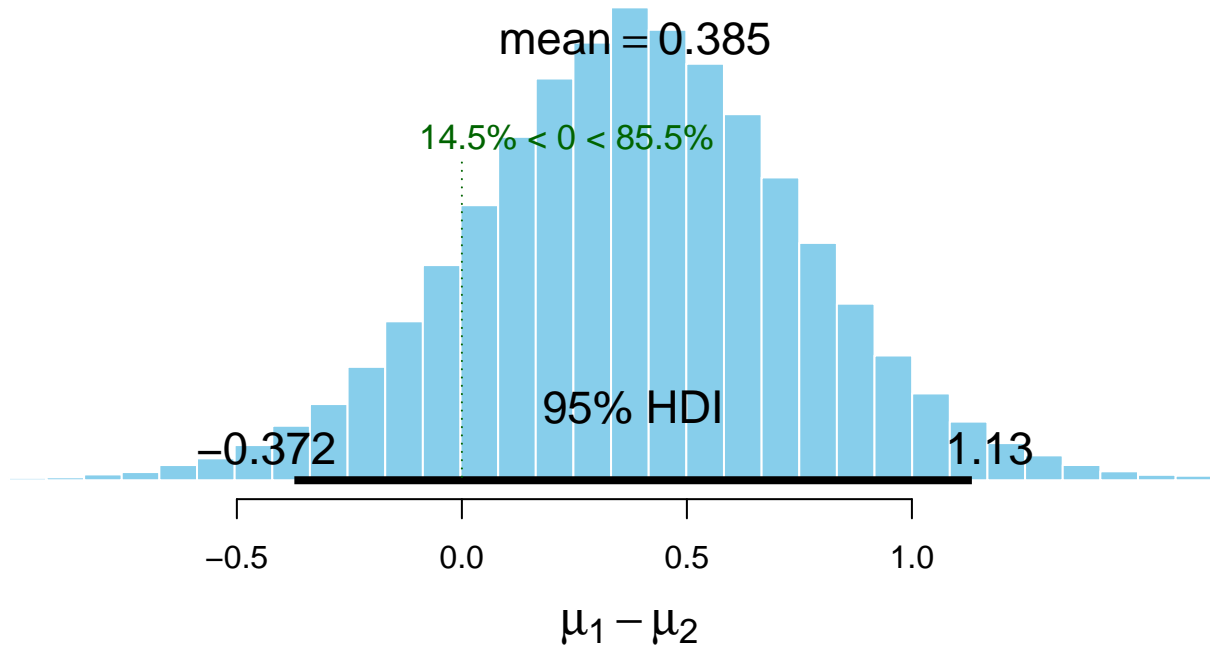
```
## 'n.eff' is a crude measure of effective sample size.
```

```
plants <- BESTmcmc(ctrl$weight, trt1$weight)
```

```
## Waiting for parallel processing to complete...done.
```

```
plot(plants)
```

Difference of Means



Answer: The difference in the two population means is **0.386**. This is a result of subtracting the population mean of the first group from the population mean of the second group. It also means that the difference between these two averages is *not* zero. **14.4%** of the mean differences in the distribution were negative while **85.6%** of the mean differences in the distribution were positive, as shown by the inequality in green. The highest density interval, or HDI, is between **-0.345** and **1.15**. This means that there is a *95%* probability that the population mean difference between the ctrl group and the trt1 group falls within the range of **-0.345** and **1.15**.

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8. Compare and contrast the results of Exercise 6 and Exercise 7. You have three types of evidence: the results of the null hypothesis test, the confidence interval, and the HDI from the BESTmcmc() procedure. Each one adds something, in turn, to the understanding of the difference between groups. Explain what information each test provides about the comparison of the control group (“ctrl”) and the treatment group 1 (“trt1”).

Answer: Given the *alpha* of **0.05**, and the p-value being **0.2504** (greater than the alpha), we fail to reject the null hypothesis. The upper bound of the confidence interval is **1.0295162** and lower bound of the confidence interval is **-0.2875162**. This means that if the study were run 100 times, then 95 times out of 100 the the confidence interval would contain the population mean within it’s range. According to the HDI between **-0.345** and **1.15**, there is a *95%* probability that the population mean difference between the ctrl group and the trt1 group falls within the range of **-0.345** and **1.15**.

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9. Using the same PlantGrowth data set, compare the “ctrl” group to the “trt2” group. Use all of the methods described earlier (t-test, confidence interval, and Bayesian method) and explain all of the results.

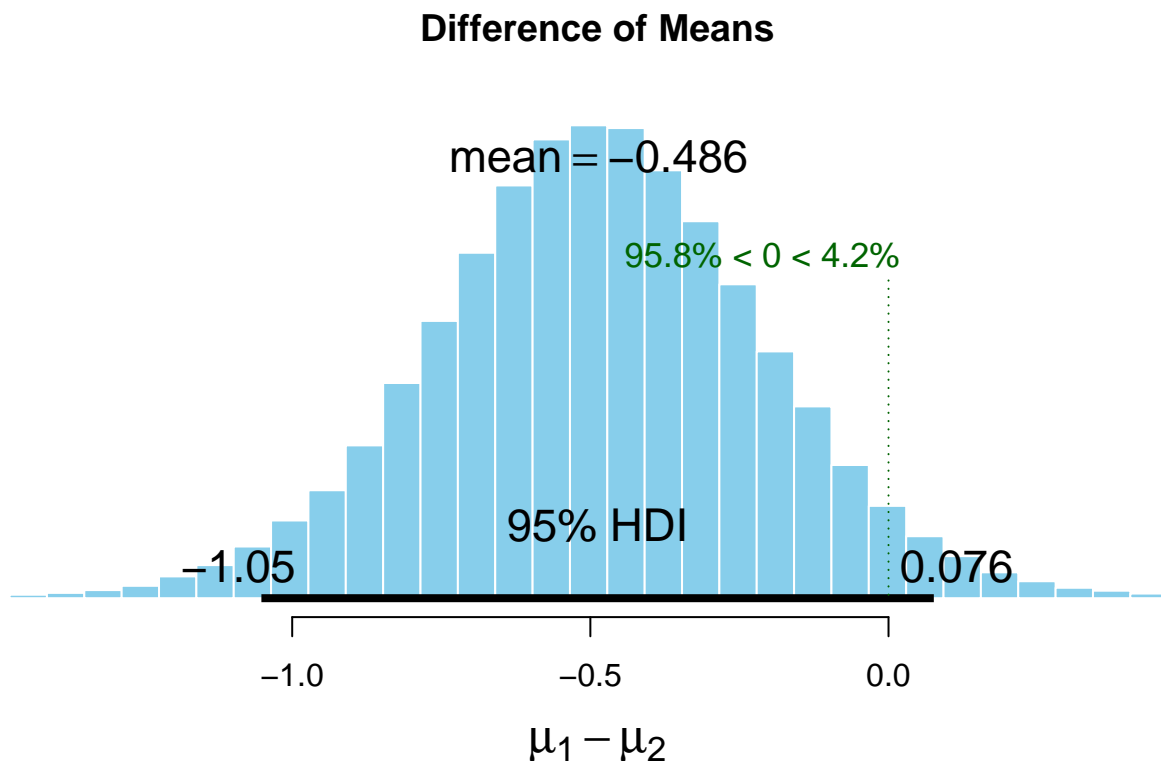
```
t.test(ctrl$weight, trt2$weight)
```

```
##
## Welch Two Sample t-test
##
## data: ctrl$weight and trt2$weight
## t = -2.134, df = 16.786, p-value = 0.0479
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.98287213 -0.00512787
## sample estimates:
## mean of x mean of y
## 5.032 5.526
```

```
plants2 <- BESTmcmc(ctrl$weight, trt2$weight)
```

```
## Waiting for parallel processing to complete...done.
```

```
plot(plants2)
```



Answer: The t value for the T-test comparing the ctrl group and the trt2 group is **-2.134**. The degrees of freedom value is **16.786**. The p-value is **0.0479**. The upper bound of the confidence interval is **-0.00512787** and lower bound of the confidence interval is **-0.98287213**. Given the α of **0.05**, and the p-value being **0.0479** (less than the alpha), we reject the null hypothesis. The difference in the two population means is **-0.488**. This is a result of subtracting the population mean of the first group from the population mean of the second group. It also means that the difference between these two averages is *not* zero. **95.8%** of the mean differences in the distribution were negative while **4.2%** of the mean differences in the distribution

were positive, as shown by the inequality in green. The HDI is between **-1.06** and **0.0645**. This means that there is a *95%* probability that the population mean difference between the ctrl group and the trt2 group falls within the range of **-1.06** and **0.0645**.

10. Consider this t-test, which compares two groups of $n = 100,000$ observations each: `t.test(rnorm(100000,mean=17.1,sd=3.8),rnorm(100000,mean=17.2,sd=3.8))`. For each of the groups, the `rnorm()` command was used to generate a random normal distribution of observations similar to those for the automatic transmission group in the `mtcars` database (compare the programmed standard deviation for the random normal data to the actual `mtcars` data). The only difference between the two groups is that in the first `rnorm()` call, the mean is set to 17.1 mpg and in the second it is set to 17.2 mpg. I think you would agree that this is a negligible difference, if we are discussing fuel economy. Run this line of code and comment on the results of the t-test. What are the implications in terms of using the NHST on very large data sets?

```
t.test(rnorm(100000,mean=17.1,sd=3.8),rnorm(100000,mean=17.2,sd=3.8))

##
##  Welch Two Sample t-test
##
## data:  rnorm(1e+05, mean = 17.1, sd = 3.8) and rnorm(1e+05, mean = 17.2, sd = 3.8)
## t = -4.6659, df = 199992, p-value = 3.075e-06
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##  -0.11263108 -0.04599696
## sample estimates:
## mean of x mean of y
##  17.12388  17.20320
```

Answer: If we begin by asserting a null hypothesis that there is no mean difference between the means of two groups and choose an “alpha level” probability of 0.05, then we see that the p-value is **0.00000001692**. This means that the p-value is less than the alpha, therefore we reject the null hypothesis (this can be considered evidence in favor of some unspecified alternative hypothesis). We can also see in the output that the *mean of x* is **17.09229** and *mean of y* is **17.18805**, resulting in a negligible difference of **0.09576**.