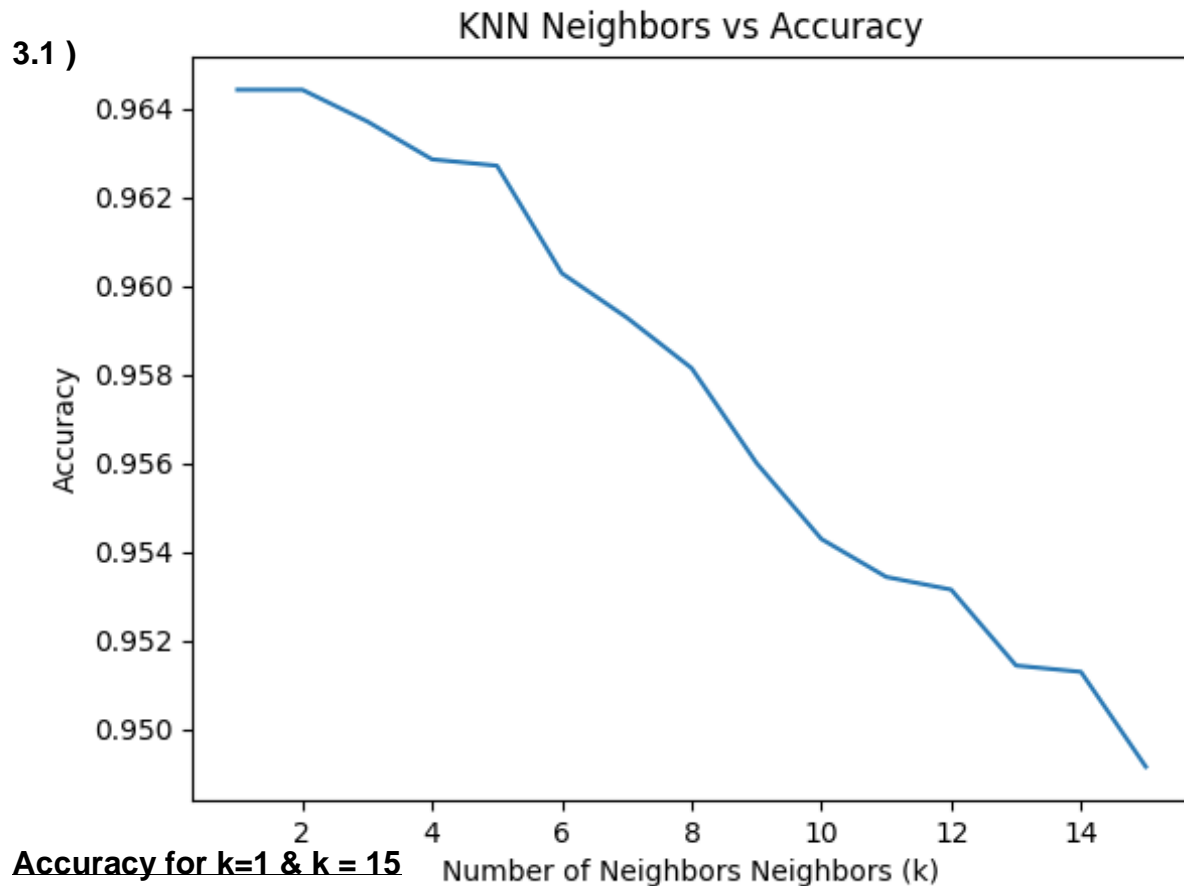
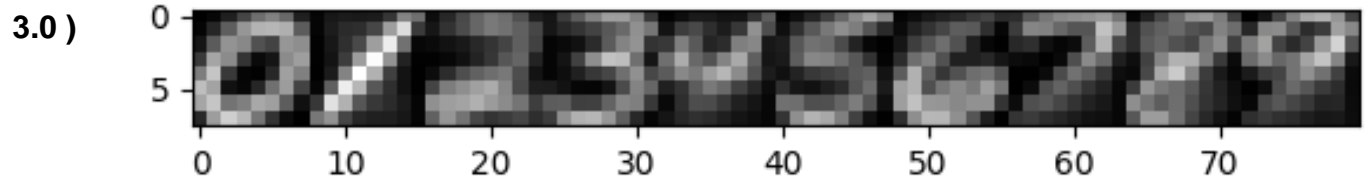


K Nearest Neighbors



As shown in the above graph:

The accuracy for $k = 1$ neighbors was among the best at $0.96875 \sim 0.97$.

The accuracy for $k = 15$ neighbors was also quite high at $0.958 \sim 0.96$.

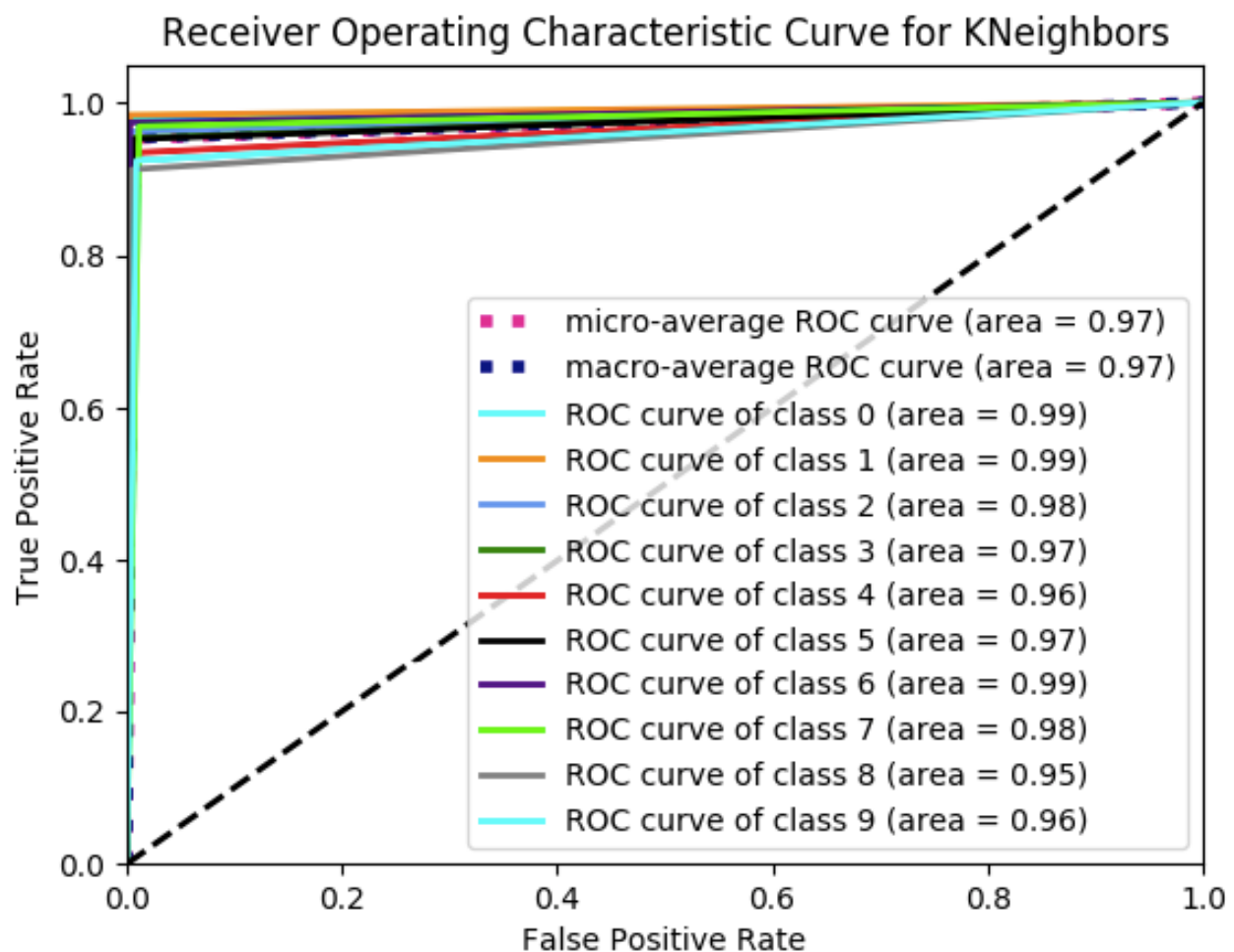
However, after $k=2$, you could see from the above graph that the model began to overfit, and subsequently decreased in accuracy. However, the decrease in accuracy is negligible, at least in the context of this data set.

Breaking Ties for $k > 1$:

To break ties, I decided to choose the digit with that was most common in the dataset. I chose this method because it was easy to implement, and would be easy to explain to others. This goes well with a KNN classifier because one of its best attributes is ease of explainability. On a more technical side, I found that without breaking ties, my optimal k was $k=3$, and I had a lower average accuracy. Thus, I conclude that the strategy of choosing the most common label improved my models performance. This could be because

Optimal k :

I had two optimal k values: $k=1$. The accuracy of both was: 0.9644285714285715



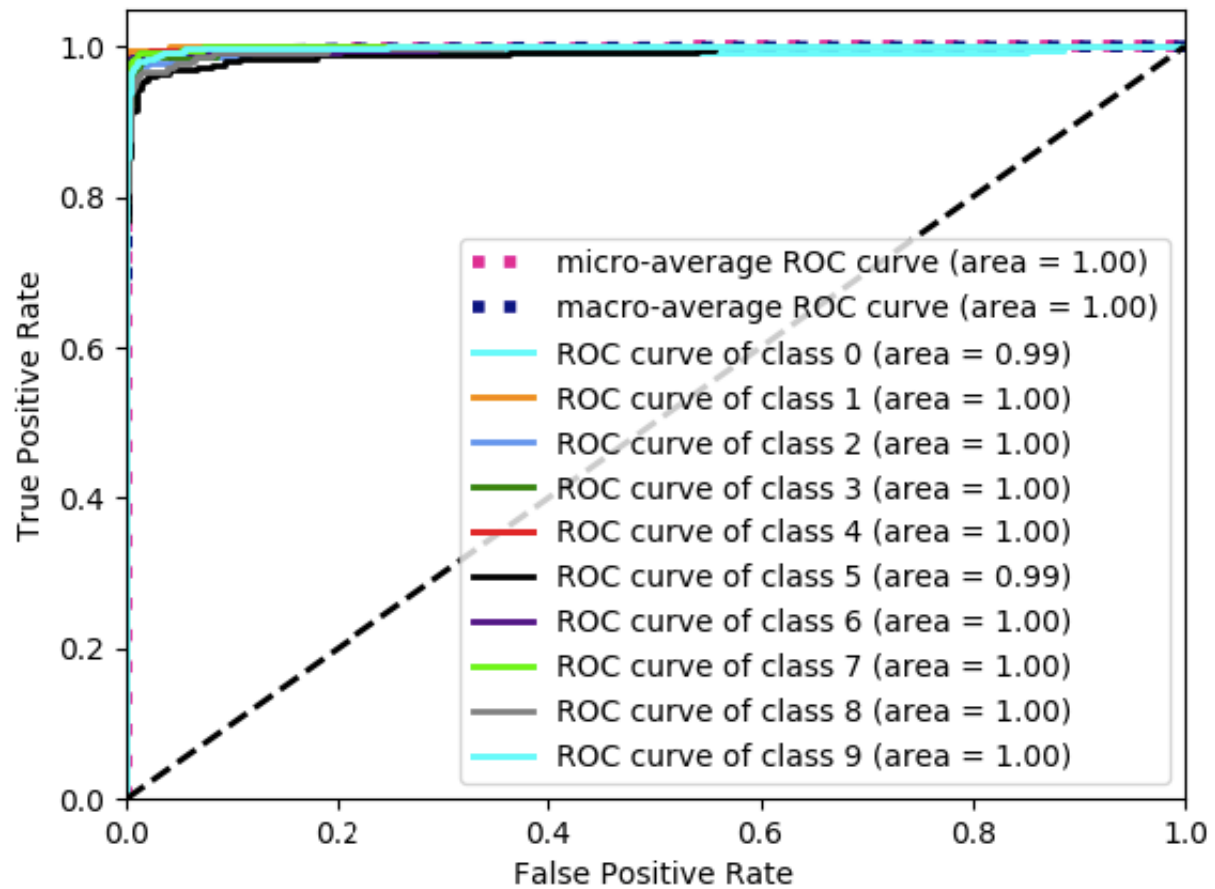
Digit	precision	recall	f1-score	support
0.0	0.98	0.99	0.99	400
1.0	0.98	1.00	0.99	400
2.0	0.98	0.97	0.97	400
3.0	0.95	0.95	0.95	400
4.0	0.97	0.96	0.97	400
5.0	0.95	0.95	0.95	400
6.0	0.98	0.98	0.98	400
7.0	0.97	0.97	0.97	400
8.0	0.99	0.94	0.96	400
9.0	0.93	0.97	0.95	400
accuracy			0.97	4000
macro avg	0.97	0.97	0.97	4000
weighted avg	0.97	0.97	0.97	4000

```
[[398  0  0  0  0  0  1  1  0  0]
 [  0 399  1  0  0  0  0  0  0  0]
 [  4  0 389  3  1  0  0  1  1  1]
 [  0  1  4 379  0 11  1  2  1  1]
 [  0  0  0  0 386  0  2  2  0 10]
 [  1  0  0 12  0 381  3  1  2  0]
 [  0  4  2  0  0  0 393  0  1  0]
 [  0  1  1  0  3  0  0 387  0  8]
 [  2  2  1  2  1  7  0  2 374  9]
 [  0  0  0  1  7  0  0  3  0 389]]
```

Best Parameters are: {'n_neighbors': 1}

MLP Neural Network

Receiver Operating Characteristic Curve for MLP Neural Network

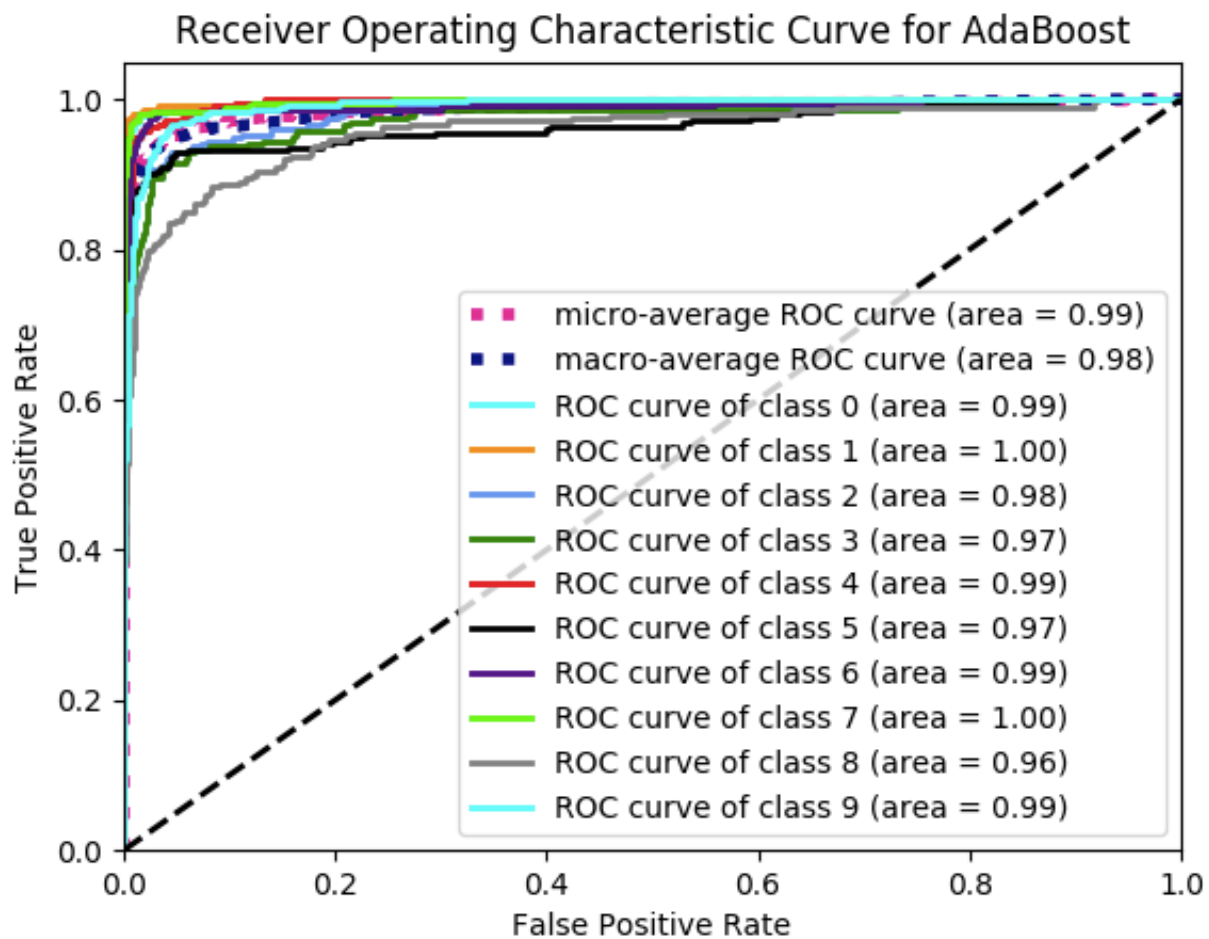


Digit	precision	recall	f1-score	support
0.0	0.98	0.99	0.98	400
1.0	0.99	1.00	1.00	400
2.0	0.96	0.95	0.96	400
3.0	0.96	0.93	0.95	400
4.0	0.98	0.99	0.99	400
5.0	0.96	0.96	0.96	400
6.0	0.97	0.98	0.97	400
7.0	0.98	0.97	0.98	400
8.0	0.96	0.97	0.96	400
9.0	0.97	0.96	0.97	400
accuracy			0.97	4000
macro avg	0.97	0.97	0.97	4000
weighted avg	0.97	0.97	0.97	4000

```
[[395  1  0  0  1  0  2  0  1  0]
 [ 0 399  0  0  1  0  0  0  0  0]
 [ 1  0 381  3  0  1  8  2  3  1]
 [ 0  0  7 372  0  9  0  1  9  2]
 [ 0  0  1  0 397  0  2  0  0  0]
 [ 4  0  0  5  0 386  0  0  4  1]
 [ 2  1  3  0  2  1 391  0  0  0]
 [ 0  0  2  0  1  0  0 390  0  7]
 [ 1  0  1  5  0  3  1  1 388  0]
 [ 1  1  0  2  4  2  1  2  1 386]]
```

Best Parameters are: {'hidden_layer_sizes': (100,), 'max_iter': 1000, 'random_state': 3, 'solver': 'adam'}

Adaboost



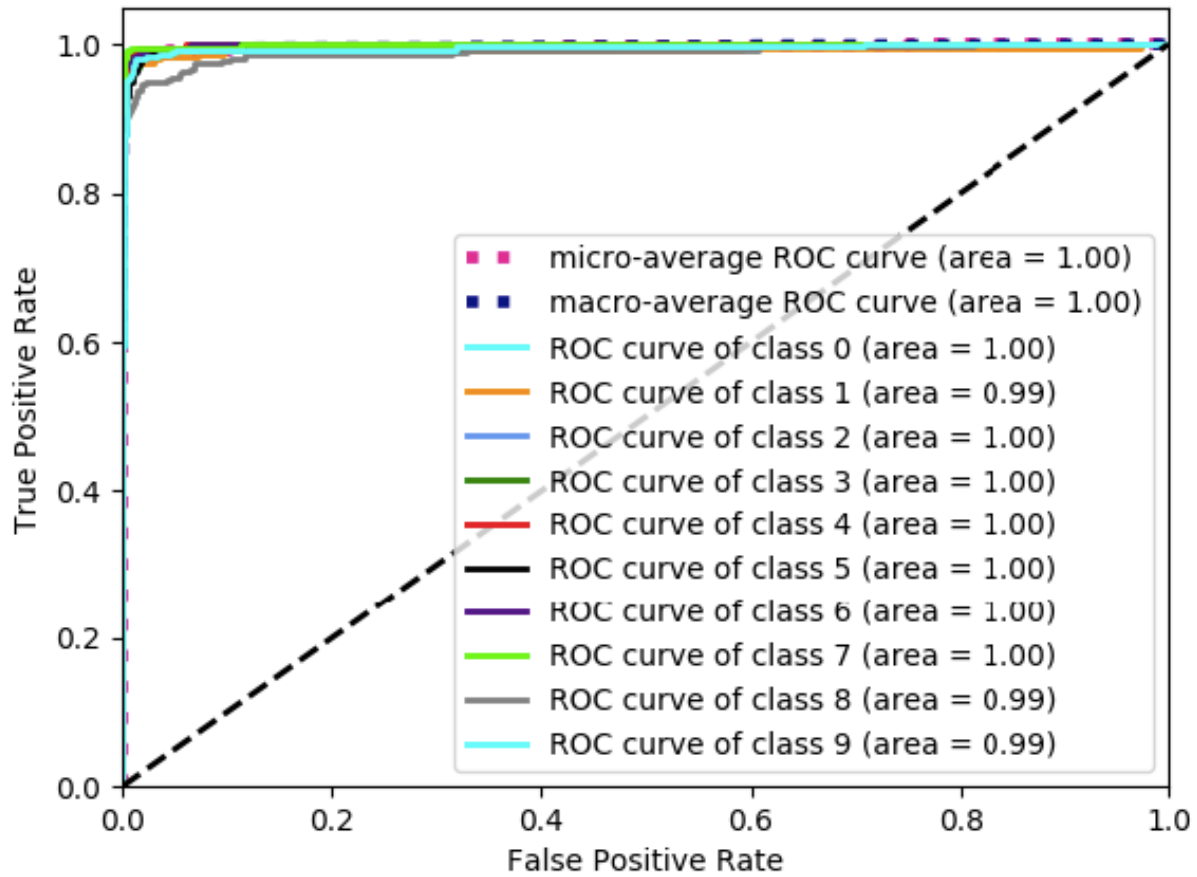
Digit	precision	recall	f1-score	support
0.0	0.68	0.82	0.74	400
1.0	0.94	0.86	0.90	400
2.0	0.72	0.70	0.71	400
3.0	0.75	0.80	0.77	400
4.0	0.81	0.80	0.80	400
5.0	0.73	0.80	0.76	400
6.0	0.84	0.56	0.67	400
7.0	0.88	0.74	0.80	400
8.0	0.70	0.80	0.75	400
9.0	0.73	0.81	0.76	400
accuracy			0.77	4000
macro avg	0.78	0.77	0.77	4000
weighted avg	0.78	0.77	0.77	4000

```
[[328  2 12 10  0 16  2  0 30  0]
 [  0 344 13  7 20  5  0  0 11  0]
 [ 18  2 282 16  8 22 19  0 32  1]
 [  1  0 28 320  0 29  0  0 19  3]
 [  2  6  1  0 319  0 18  5  7 42]
 [  3  4  6 41  8 319  4  1 13  1]
 [115  1 18  0  8 27 226  0  5  0]
 [  0  4  5 18  4  1  0 297  6 65]
 [ 12  3 23 10  4 18  1  0 319 10]
 [  2  1  2  5 22  0  0 35 11 322]]
```

Best Parameters are: {'learning_rate': 1, 'n_estimators': 45, 'random_state': 3}

Support Vector Machine

Receiver Operating Characteristic Curve for Support Vector Machine



```
[[396  0  0  1  0  0  2  0  1  0]
 [  0 395  1  0  0  0  1  0  3  0]
 [  0  0 390  2  1  1  0  0  6  0]
 [  0  1  4 377  0  5  0  1 12  0]
 [  0  0  0  0 398  0  2  0  0  0]
 [  1  0  1  7  0 386  2  0  2  1]
 [  0  0  1  0  1  0 396  0  2  0]
 [  0  0  1  0  3  0  0 388  1  7]
 [  1  0  1  4  0  4  0  0 388  2]
 [  0  1  0  3  3  0  0  6  1 386]]
```


	precision	recall	f1-score	support
0.0	0.99	0.99	0.99	398
1.0	0.99	0.99	0.99	397
2.0	0.97	0.98	0.98	399
3.0	0.94	0.96	0.95	394
4.0	0.99	0.98	0.99	406
5.0	0.96	0.97	0.97	396
6.0	0.99	0.98	0.99	403
7.0	0.97	0.98	0.98	395
8.0	0.97	0.93	0.95	416
9.0	0.96	0.97	0.97	396
accuracy			0.97	4000
macro avg	0.97	0.98	0.98	4000
weighted avg	0.98	0.97	0.97	4000

Best Parameters are: {'SVM__C': 0.1, 'SVM__gamma': 0.1}