

<sup>1</sup> An investigation of factors affecting inferences from and  
<sup>2</sup> reliability of state-space age-structured assessment  
models

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<sup>23</sup> patterns

<sup>24</sup> **Abstract**

<sup>25</sup> State-space models have been promoted as the next-generation of fisheries stock assessment  
<sup>26</sup> and evaluation of their reliability is needed. We simulated operating models that varied fish-  
<sup>27</sup> ing pressure, magnitude of observation error, and sources of process error. For each operating  
<sup>28</sup> model, we fit a range of estimating models with correct and incorrect configurations. We  
<sup>29</sup> measured reliability of estimating models by convergence rate, accuracy of AIC-based model  
<sup>30</sup> selection, estimation bias, and magnitude of retrospective patterns. All reliability measures  
<sup>31</sup> were generally better with lower observation error, contrast in fishing pressure over time,  
<sup>32</sup> and when median natural mortality rate is known. The magnitude of the log-likelihood  
<sup>33</sup> gradients was not a reliable indicator of convergence. AIC can generally distinguish process  
<sup>34</sup> error source with lower observation error and higher true process error variability. Disting-  
<sup>35</sup> uishing the stock recruit relationship with AIC required large contrast in spawning biomass  
<sup>36</sup> and low recruitment variation, but bias in stock-recruit parameter estimation was prevalent.  
<sup>37</sup> Retrospective patterns were not large for mis-specified models. These findings improve our  
<sup>38</sup> understanding of when results from state space models will be reliable.

<sup>39</sup> **Introduction**

<sup>40</sup> Application of state-space models in fisheries stock assessment and management has ex-  
<sup>41</sup> panded dramatically within the International Council for the Exploration of the Sea (ICES),  
<sup>42</sup> Canada, and the Northeast US (Nielsen and Berg 2014; Cadigan 2016; Pedersen and Berg  
<sup>43</sup> 2017; Stock and Miller 2021). State-space models treat latent population characteristics  
<sup>44</sup> as statistical time series with periodic observations that also may have error due to sam-  
<sup>45</sup> pling or other measurement properties. Traditional assessment models may use state-space  
<sup>46</sup> approaches to account for temporal variability in population characteristics (Legault and  
<sup>47</sup> Restrepo 1999; Methot and Wetzel 2013), but these models treat the annual parameters as  
<sup>48</sup> penalized fixed effect parameters where the variance parameters controlling the penalties are  
<sup>49</sup> assumed known (Thorson and Minto 2015). Modern state-space models can estimate the  
<sup>50</sup> annually varying parameters as random effects with variance parameters estimated using  
<sup>51</sup> maximum marginal likelihood or corresponding Bayesian approaches. These random-effects  
<sup>52</sup> approaches are considered best practice and are recommended for the next generation of  
<sup>53</sup> stock assessment models (Hoyle et al. 2022; Punt 2023).

<sup>54</sup> State-space stock assessment models, with nonlinear functions of latent parameters and  
<sup>55</sup> multiple types of observations with varying distributional assumptions, are one of the most  
<sup>56</sup> complex examples of this analytical approach. Statistical aspects of state-space models and  
<sup>57</sup> their application within fisheries have been studied extensively, but previous work has focused  
<sup>58</sup> primarily on linear and Gaussian state-space models (Aeberhard et al. 2018; Auger-Méthé  
<sup>59</sup> et al. 2021). Therefore, current understanding of the reliability of state-space models does  
<sup>60</sup> not extend to usage for stock assessment.

<sup>61</sup> As state-space models provide greater flexibility by allowing multiple processes to vary as  
<sup>62</sup> random effects (Nielsen and Berg 2014; Aeberhard et al. 2018; Stock et al. 2021), one of the  
<sup>63</sup> most immediate questions regards the implications of mis-specification among alternative  
<sup>64</sup> sources of process error. Incorrect treatment of population attributes as temporally varying

65 (Trijoulet et al. 2020; Liljestrand et al. 2024) could lead to misidentification of stock  
66 status and biased population estimates, ultimately impacting fisheries management decisions  
67 (Legault and Palmer 2016; Szuwalski et al. 2018; Cronin-Fine and Punt 2021). Furthermore,  
68 biological, fishery, and observational processes are often confounded in catch-at-age data,  
69 which may adversely affect the ability to distinguish between true process variability and  
70 observational error (Punt et al. 2014; Stewart and Monnahan 2017; Cronin-Fine and Punt  
71 2021; Fisch et al. 2023; Li et al. 2025a).

72 Li et al. (2024) conducted a full-factorial simulation-estimation study to assess model reli-  
73 ability when confounding random-effects processes (numbers-at-age, fishery selectivity, and  
74 natural mortality) were included. Their results suggest that while state-space models can  
75 generally identify sources of process error, overly complex models, even when misspecified  
76 (i.e., incorporating process error that did not exist in reality), often performed similarly to  
77 correctly specified models, with little to no bias in key management quantities. Similarly,  
78 Liljestrand et al. (2024) found little downside in assuming process error in recruitment or  
79 selectivity, even when it was absent.

80 Despite increasing research on state space assessment models, several uncertainties in state  
81 space assessment modeling remain. First, confounding processes that can be treated as ran-  
82 dom effects in the model have not been thoroughly examined or tested within a simulation-  
83 estimation framework. Second, previous studies relied on operating models conditioned on  
84 specific fisheries, limiting their generalizability (Liljestrand et al. 2024; Li et al. 2025a).  
85 In particular, the effects of observation error and underlying fishing history have not been  
86 fully isolated in simulation study designs, making it challenging to disentangle the interplay  
87 between process and observation error magnitudes, as demonstrated in Fisch et al. (2023).  
88 Third, explicitly modeling stock-recruit relationships (SRRs) as mechanistic drivers of pop-  
89 ulation dynamics is promising (Fleischman et al. 2013; Pontavice et al. 2022), but reliability  
90 of inferences within integrated state-space age-structured models has not been evaluated.  
91 Evidence from other studies suggests that when both process and observation errors are un-

known, estimating density dependence parameters becomes highly uncertain (Knape 2008; Polansky et al. 2009). In particular, Knape (2008) demonstrated that stronger density dependence becomes increasingly difficult to estimate in the presence of observation error. Therefore, it is crucial to assess whether density-dependent mechanisms can be estimated with sufficient precision for use in fisheries management (Auger-Méthé et al. 2016). Finally, although the importance of autocorrelation in process errors is recognized, investigations of the ability to distinguish state-space assessment models with and without autocorrelation and whether such misspecification is detrimental to estimation of important population metrics are lacking (Johnson et al. 2016; Xu et al. 2019).

In the present study, we conduct a simulation study with operating models (OMs) varying by degree of observation error, source and variability of process error, and fishing history. The simulations from these OMs are fitted with estimation models (EMs) that make alternative assumptions for sources of process error, whether an SRR was estimated, and whether natural mortality is estimated. Given the confounding nature of process errors, developing diagnostic tools to detect model misspecification is of great scientific interest and could aid the next generation of stock assessments (Auger-Méthé et al. 2021). We evaluate whether OM and EM attributes affect rates of convergence and the ability of Akaike Information Criterion (AIC) to correctly determine the source of process error or the existence of an SRR. We also evaluate effects of OM and EM attributes on magnitude of retrospective patterns and bias in estimation of parameters and other model outputs important for management.

## Methods

We used the Woods Hole Assessment Model (WHAM) to configure OMs and EMs in our simulation study (Stock and Miller 2021; Miller et al. 2025). WHAM is an R package freely available via a Github repository and is built on the Template Model Builder package (Kristensen et al. 2016). For this study we used version 1.0.6.9000, commit 77bbd94.

117 WHAM has also been used to configure OMs and EMs for closed loop simulations evaluating  
118 index-based assessment methods (Legault et al. 2023) and is currently used or accepted for  
119 use in management of numerous Northeast United States (NEUS) fish stocks (e.g., NEFSC  
120 2022a, 2022b; NEFSC 2024).

121 We completed a simulation study with a number of OMs that can be categorized based on  
122 where process error random effects were assumed. R OMs assume process error for recruit-  
123 ment only. Other OM categories assume recruitment process errors along with process errors  
124 for apparent survival (R+S), natural mortality (R+M), fleet selectivity (R+Sel), or index  
125 catchability (R+q). We refer to the R+S OMs as modeling apparent survival because on  
126 log-scale the random effects are additive to the total mortality (fishing and natural mortal-  
127 ity) between numbers at age, thus they modify the survival term. For each OM, assumptions  
128 about the magnitude of the variance of process errors and observations are required and the  
129 values we used were based on a review of the range of estimates from NEUS assessments  
130 using WHAM.

131 In total, we configured 72 OMs with alternative assumptions about the source and magni-  
132 tude of process errors, magnitude of observation error in indices and age composition data,  
133 and contrast in fishing pressure over time. For each OM, we simulated 100 time series of  
134 abundance at age with process errors, and for each realized time series, we simulated obser-  
135 vation data sets. For each data set, we fitted a number of EMs that differed in assumptions  
136 about the source of process errors, whether natural mortality (or the median for models with  
137 process error in natural mortality) was estimated, and whether a Beverton-Holt SRR was  
138 estimated within the EM. Details of each of the OMs and EMs are described below. We did  
139 not use the log-normal bias-correction feature for process errors or observations described  
140 by Stock and Miller (2021) for OMs and EMs to simplify interpretation of the study results  
141 (Li et al. 2025b). All code we used to perform the simulation study and summarize results  
142 can be found at [https://github.com/timjmiller/SSRTWG/tree/main/Project\\_0/code](https://github.com/timjmiller/SSRTWG/tree/main/Project_0/code).

<sup>143</sup> **Operating models**

<sup>144</sup> **Population**

<sup>145</sup> We intended the population demographics and observation types to represent a general  
<sup>146</sup> NEUS groundfish stock. The population consists of 10 age classes, ages 1 to 10+, with the  
<sup>147</sup> last being a plus group that accumulates ages 10 and older. The maturity at age was a  
<sup>148</sup> logistic curve with  $a_{50} = 2.89$  and slope = 0.88 (Figure S1, top left). Weight at age ( $W_a$ )  
<sup>149</sup> was generated with a von Bertalanffy growth function defining length at age:

$$L_a = L_\infty \left(1 - e^{-k(a-t_0)}\right),$$

<sup>150</sup> where  $t_0 = 0$ ,  $L_\infty = 85$ , and  $k = 0.3$ , and a length-weight relationship such that

$$W_a = \theta_1 L_a^{\theta_2},$$

<sup>151</sup> where  $\theta_1 = e^{-12.1}$  and  $\theta_2 = 3.2$  (Figure S1, top right).

<sup>152</sup> We assumed a Beverton-Holt SRR with constant pre-recruit mortality parameters for all  
<sup>153</sup> OMs. We assume spawning occurs annually 0.25 of each year and recruitment at age 1  
<sup>154</sup> ( $N_{1,y}$ ). All biological inputs to calculations of spawning stock biomass (SSB) per recruit  
<sup>155</sup> (i.e., weight, maturity, and natural mortality at age) are constant in the R+S, R+Sel, and  
<sup>156</sup> R+q process error OMs. Therefore, steepness and unfished recruitment are also constant  
<sup>157</sup> over the time period for those OMs (Miller and Brooks 2021). We assumed a value of 0.2 for  
<sup>158</sup> the natural mortality rate in OMs without process errors on natural mortality. We specified  
<sup>159</sup> unfished recruitment equal to  $e^{10}$  and  $F_{MSY} = F_{40\%} = 0.348$ , which equates to a steepness of  
<sup>160</sup> 0.69 and  $a = 0.60$  and  $b = 2.4 \times 10^{-5}$  for the Beverton-Holt parameterization

$$N_{1,y} = \frac{aSSB_{y-1}}{1 + bSSB_{y-1}}$$

161 (Figure S1, bottom right). For OMs with time-varying random effects for natural mortality,  
162 steepness is not constant. However, we used the same  $a$  and  $b$  parameters as other OMs,  
163 which equates to a steepness and  $R_0$  at the median of the time series process for natural mor-  
164 tality. Similarly, for OMs with time-varying random effects for fishery selectivity,  $F_{MSY}$  also  
165 varies temporally, so equilibrium conditions for these OMs are defined for mean selectivity  
166 parameters.

167 We used two fishing scenarios for OMs. In the first scenario, the stock experiences over-  
168 fishing at  $2.5F_{MSY}$  for the first 20 years followed by fishing at  $F_{MSY}$  for the last 20 years  
169 (denoted  $2.5F_{MSY} \rightarrow F_{MSY}$ ). In the second scenario, the stock is fished at  $F_{MSY}$  for the  
170 entire time period (40 years). The magnitude of the overfishing assumptions is based on  
171 average estimates of overfishing for NEUS groundfish stocks from Wiedenmann et al. (2019)  
172 and similar to the approach in Legault et al. (2023). The second scenario represents the  
173 ideal situation where the stock is fished at an optimal level, but provides less contrast in  
174 stock sizes over time. We specified initial population abundance at age at the equilibrium  
175 distribution that corresponds to fishing at either  $F = 2.5F_{MSY}$  or  $F = F_{MSY}$ . This implies  
176 that, for a deterministic model, the abundance at age would not change from year to year  
177 at the beginning of the time series.

## 178 Fleets

179 We assumed a single fleet operating year round for catch observations with logistic selectivity  
180 ( $a_{50} = 5$  and slope = 1; Figure S1, bottom left). This selectivity was used to define  $F_{MSY}$  for  
181 the Beverton-Holt SRR parameters above. We assumed a logistic-normal distribution with  
182 no correlation on the multivariate normal scale for the corresponding annual age-composition  
183 observations.

<sup>184</sup> **Indices**

<sup>185</sup> Two time series of fishery-independent surveys measured in numbers are generated for the  
<sup>186</sup> entire 40 year period with one occurring in the spring (0.25 of each year) and one in the  
<sup>187</sup> fall (0.75 of each year), representing current bottom trawl surveys conducted in the NEUS.  
<sup>188</sup> Catchability of both surveys are assumed to be 0.1. Like the fishing fleet, we assumed logistic  
<sup>189</sup> selectivity for both indices ( $a_{50} = 5$  and slope = 1) and a logistic-normal distribution with  
<sup>190</sup> no correlation on the multivariate normal scale for the annual age-composition observations.

<sup>191</sup> **Observation Uncertainty**

<sup>192</sup> The standard deviation for log-aggregate catch was 0.1 for all OMs, a common assumption  
<sup>193</sup> for commercial removals in NEUS stock assessments. Two levels of observation error variance  
<sup>194</sup> (high and low) were specified for indices and all age composition observations (both indices  
<sup>195</sup> and catch). The low uncertainty specification assumed a standard deviation of 0.1 for both  
<sup>196</sup> series of log-aggregate index observations, and the standard deviation of the logistic-normal  
<sup>197</sup> for age composition observations was 0.3. In the high uncertainty specification, the standard  
<sup>198</sup> deviation for log-aggregate indices was 0.4 and that for the age composition observations  
<sup>199</sup> was 1.5. The low standard deviation for index observations is typical for fish stocks that  
<sup>200</sup> are consistently sampled across survey stations whereas the high value is typical for more  
<sup>201</sup> sporadically sampled stocks. The standard deviations for the age composition observations  
<sup>202</sup> were determined from the range of values estimated from WHAM fits to NEUS stocks that  
<sup>203</sup> assumed the logistic-normal model. For all EMs, the standard deviation for log-aggregate  
<sup>204</sup> observations was assumed known whereas that for the logistic-normal age composition ob-  
<sup>205</sup> servations was estimated.

206 **Operating models with random effects on numbers at age**

207 For operating models with random effects on recruitment only and also on apparent survival  
208 ( $R$ ,  $R+S$ ), we assumed marginal standard deviations for recruitment of  $\sigma_R \in \{0.5, 1.5\}$ . The  
209 marginal standard deviations for apparent survival random effects at older age classes were  
210  $\sigma_{2+} \in \{0, 0.25, 0.5\}$ . The full factorial combination of these process error assumptions ( $2 \times 3$   
211 levels) and scenarios for fishing history (2 levels) and observation error (2 levels) scenarios  
212 described above results in 24 different  $R$  ( $\sigma_{2+} = 0$ ) and  $R+S$  operating models (Table S1).

213 **Operating models with random effects on natural mortality**

214 All  $R+M$  OMs treat natural mortality as constant across age, but with annually varying  
215 random effects. WHAM treats natural mortality as a log-transformed parameter

$$\log M_{y,a} = \mu_M + \epsilon_{M,y}$$

216 that is a linear combination of a mean log-natural mortality parameter that is constant  
217 across ages ( $\mu_M = \log(0.2)$ ) and any annual random effects are marginally distributed as  
218  $\epsilon_{M,y} \sim N(0, \sigma_M^2)$ . The marginal standard deviations we assumed for log natural mortality  
219 random effects were  $\sigma_M \in \{0.1, 0.5\}$  and the random effects were either uncorrelated or first-  
220 order autoregressive (AR1,  $\rho_M \in \{0, 0.9\}$ ). Uncorrelated random effects were also included  
221 on recruitment with  $\sigma_R = 0.5$  (hence, we denote these OMs as  $R+M$ ). The full factorial  
222 combination of these process error assumptions and fishing history (2 levels) and observation  
223 error (2 levels) scenarios described above results in 16 different  $R+M$  OMs (Table S2).

224 **Operating models with random effects on fleet selectivity**

225 WHAM treats each selectivity parameter  $s$  as a logit-transformed parameter

$$\log \left( \frac{p_{s,y} - l_s}{u_s - p_{s,y}} \right) = \mu_s + \epsilon_{s,y}$$

226 that is a linear combination of a mean  $\mu_s$  and any annual random effects marginally dis-  
227 tributed as  $\epsilon_{s,y} \sim N(0, \sigma_s^2)$ , where the lower and upper bounds of the parameter ( $l_s$  and  
228  $u_s$ ) can be specified by the user. All selectivity parameters ( $a_{50}$  and slope parameters) were  
229 bounded by  $s_l = 0$  and  $s_u = 10$  for all OMs and EMs. The marginal standard deviations  
230 we assumed for logit scale random effects were  $\sigma_s \in \{0.1, 0.5\}$  and AR1 autocorrelation pa-  
231 rameters of  $\rho_s \in \{0, 0.9\}$ . Like R+M OMs, the full factorial combination of these process  
232 error assumptions (2x2 levels) and scenarios described above for fishing history (2 levels)  
233 and observation error (2 levels) results in 16 different R+Sel OMs (Table S3).

234 **Operating models with random effects on index catchability**

235 Like selectivity parameters, WHAM treats catchability for an index  $i$  as a logit-transformed  
236 parameter

$$\log \left( \frac{q_{i,y} - l_i}{u_i - q_{i,y}} \right) = \mu_i + \epsilon_{i,y}$$

237 that is a linear combination of a mean  $\mu_i$  and any annual random effects marginally dis-  
238 tributed as  $\epsilon_{i,y} \sim N(0, \sigma_i^2)$  where the lower and upper bounds of the catchability ( $l_i$  and  $u_i$ )  
239 can be specified by the user. We assumed bounds of 0 and 1000 for all OMs and EMs. For  
240 all OMs and EMs with process errors on catchability, the temporal variation only applies  
241 to the first index, which could be interpreted as capturing some unmeasured seasonal pro-  
242 cess that affects availability to the survey. The marginal standard deviations we assumed  
243 for logit scale random effects were  $\sigma_i \in \{0.1, 0.5\}$  and AR1 autocorrelation parameters of  
244  $\rho_i \in \{0, 0.9\}$ . Like R+M and R+Sel OMs, the full factorial combination of these process

<sup>245</sup> error assumptions and fishing history (2 levels) and observation error (2 levels) scenarios  
<sup>246</sup> described above results in 16 different R+q OM<sub>s</sub> (Table S4).

## <sup>247</sup> Estimation models

<sup>248</sup> For each of the data sets simulated from an OM, 20 EM<sub>s</sub> were fit. A total of 32 different  
<sup>249</sup> EM<sub>s</sub> were fit across OM<sub>s</sub> where the subset of 20 depended on the source of process error  
<sup>250</sup> in the OM (Table S5). The EM<sub>s</sub> have different assumptions about the source of process  
<sup>251</sup> error (R+S, R+M, R+Sel, R+q) and whether or not 1) there is temporal autocorrelation,  
<sup>252</sup> 2) a Beverton-Holt SRR is estimated, and 3) the natural mortality rate ( $\mu_M$ , the constant  
<sup>253</sup> or mean on log scale for R+M EM<sub>s</sub>) is estimated. For simplicity we refer to the derived  
<sup>254</sup> estimate  $e^{\mu_M}$  as the median natural mortality rate regardless of whether natural mortality  
<sup>255</sup> random effects are estimated in the EM.

<sup>256</sup> Subsets of 20 EM<sub>s</sub> in Table S5 were fit to simulated data sets from each of the OM process  
<sup>257</sup> error sources. For R and R+S OM<sub>s</sub>, fitted EM<sub>s</sub> had matching process error assumptions  
<sup>258</sup> as well as R+Sel, R+M, and R+q assumptions without autocorrelation. For other OM  
<sup>259</sup> process error sources, we fit EM<sub>s</sub> with correct process error assumptions, the correct process  
<sup>260</sup> error source but incorrect correlation assumption, and the incorrect process error source  
<sup>261</sup> without autocorrelation. As such, EM<sub>s</sub> were configured correctly for the OM, or they had  
<sup>262</sup> mis-specification in assumptions of process error autocorrelation, the source of process error,  
<sup>263</sup> and(or) the SRR (Beverton-Holt or none).

<sup>264</sup> The maturity at age, weight at age for catch and SSB, and observation error standard devi-  
<sup>265</sup> ations for aggregate catch and indices were all assumed known at the true values. However,  
<sup>266</sup> the variance parameters for the logistic-normal distributions for age composition observations  
<sup>267</sup> were estimated in the EM<sub>s</sub>.

268 **Measures of reliability**

269 **Convergence**

270 The first measure of reliability we investigated was frequency of convergence when fitting  
271 each EM to the simulated data sets. There are various ways to assess convergence of the  
272 fit (e.g., Carvalho et al. 2021; Kapur et al. 2025), but given the importance of estimates  
273 of uncertainty when using assessment models in management, we estimated probability of  
274 convergence as measured by occurrence of a positive-definite Hessian matrix at the optimized  
275 negative log-likelihood that could be inverted (i.e., providing Hessian-based standard error  
276 estimates). We also provide results in the Supplementary Materials for convergence defined  
277 by the maximum absolute gradient  $< 1^{-6}$  and the maximum of the absolute gradient values  
278 for all fits of a given EM to all simulated data sets from a given OM that produced Hessian-  
279 based standard errors for all estimated fixed effects. This provides an indication of how  
280 poor the calculated gradients can be, but still presumably converged adequately enough for  
281 parameter inferences.

282 **AIC for model selection**

283 We investigated the reliability of AIC-based model selection for two purposes. First, we  
284 analyzed selection of each process error model source (R, R+S, R+M, R+Sel, R+q) using  
285 marginal AIC. For a given OM simulated data set, we compared AIC for EMs with different  
286 process error assumption conditional on whether median natural mortality rate and the  
287 Beverton-Holt SRR were estimated. Second, we analyzed AIC-based selection between EMs  
288 with and without the Beverton-Holt SRR assumed. Contrast in fishing pressure and time  
289 series with recruitment at low stock size have been shown to improve estimation of SRR  
290 parameters (Magnusson and Hilborn 2007; Conn et al. 2010). Our preliminary inspections  
291 indicated generally poor performance of AIC in determining the Beverton-Holt SRR model  
292 for a given set of OM factors (including contrast in fishing pressure), even when the EM

293 was configured with the correct process error source. Therefore, we conditioned on the EMs  
294 having the correct process error assumption and also considered the effect of the log-standard  
295 deviation of the true log(SSB) ( $\log \text{SD}_{\text{SSB}}$ ; similar to the log of the coefficient of variation  
296 for SSB) on model selection since simulations with realized SSB producing low and high  
297 recruitment would have larger variation in realized SSB.

298 All model selection results condition only on completion of the optimization process without  
299 failure for all of the compared EMs. We did not condition on convergence as defined above  
300 because optimization could correctly determine an inappropriate process error assumption  
301 by estimating variance parameters at the lower bound of zero. Such an optimization could  
302 indicate poor convergence but the likelihood would be equivalent to that without the mis-  
303 specified random effects and the AIC would be appropriately higher because more (variance)  
304 parameters were estimated. All other measures of reliability described below (bias and  
305 Mohn's  $\rho$ ) use these same criteria for inclusion of EM fits in the summarized results.

306 **Bias**

307 We also investigated bias in estimation of various model attributes as a measure of reliability.  
308 For a given model attribute we calculated the relative error

$$\text{RE}(\theta_j) = \frac{\hat{\theta}_j - \theta_j}{\theta_j} \quad (1)$$

309 from fitting a given EM to simulated data set  $j$  configured for a given OM where  $\hat{\theta}_j$  and  
310  $\theta_j$  are the estimated and true values for simulation  $j$ . We analyzed simulation results for  
311 estimates of terminal year SSB and recruitment, Beverton-Holt SRR parameters ( $a$  and  $b$ ),  
312 and median natural mortality rate.

313 **Mohn's  $\rho$**

314 Finally, we investigated presence of retrospective patterns in fitted models as a measure of  
315 reliability. We calculated Mohn's  $\rho$  for SSB, fishing mortality (averaged over all age classes),  
316 and recruitment for each EM fit to each OM simulated data set (Mohn 1999). We fit  $P = 7$   
317 peels to each simulated data set and calculated Mohn's  $\rho$  for a given attribute  $\theta$  as

$$\rho(\theta) = \frac{1}{P} \sum_{p=1}^P \frac{\hat{\theta}_{Y-p,Y-p} - \hat{\theta}_{Y-p,Y}}{\hat{\theta}_{Y-p,Y}} \quad (2)$$

318 where  $Y$  is last year of the full set of observations and  $\hat{\theta}_{y,y'}$  is the estimate for attribute  $\theta$  in  
319 year  $y$  from a model fit using data up to year  $y' \geq y$ . Thus,  $\theta$  terms where  $y' = Y$  refer to  
320 estimates from the fit to all years of data.

321 **Summarizing results across OM and EM attributes**

322 Because the OM and EM attributes that we investigated are numerous, we used two methods  
323 to summarize the most important factors for differences in results within a given OM process  
324 error source. The first method was fitting regression models with the response being each  
325 of the measures of reliability described above and predictor variables were defined based on  
326 OM and EM characteristics (e.g., MacKinnon et al. 1995; Wang et al. 2017; Harwell et  
327 al. 2018). For the binary indicators of convergence and AIC-based selection of an SRR, we  
328 performed logistic regressions. For indicators of AIC-based selection of EM process error  
329 source (multiple categories) we performed multinomial regressions. For other measures of  
330 reliability we fit linear regression models to transformed responses. Because relative errors  
331 (Eq. 1) and Mohn's  $\rho$  for the various parameters are bounded below at -1, we used a  
332 transformation of these values

$$y_j = \log [f(\hat{\theta}_j, \theta_j) + 1] \quad (3)$$

333 where  $f$  is either the relative error (Eq. 1) or Mohn's  $\rho$  (Eq. 2) for simulation  $j$ , so that  
334 values are unbounded. For relative errors,  $y_j$  is the log-scale error. We omitted simulations  
335 where estimated attributes equal to zero (RE = -1). For all regressions we fit separate models  
336 with just individual OM and EM factors included, with all factors included, with all second  
337 order interactions, and with all third order interactions. For the multinomial regression,  
338 we used the `vglm` function from the VGAM package (Yee 2008; Yee 2015). We tabulated  
339 percent reduction in residual deviance for each of the regression fits. We did not perform  
340 formal statistical analyses of effects of OM and EM attributes on results (e.g., ANOVA)  
341 because of the lack of independence of the "observations" that results from fitting multiple  
342 EMs to each simulated data set.

343 The second method involved fitting classification and regression trees (Breiman et al. 1984)  
344 to show how the OM and EM attributes, and their interactions, partition the values for each  
345 measure of reliability (e.g., Gonzalez et al. 2018; Collier et al. 2022). We used classification  
346 trees for categorical measures (convergence and AIC) and regression trees for the other  
347 measures with continuous scales (relative error and Mohn's  $\rho$ ). The response variables were  
348 the same as the regressions for the deviance reduction analyses. We used the `rpart` function  
349 in the `rpart` package (Therneau and Atkinson 2025) to fit trees. Full trees were determined  
350 using default settings except that we increased the number of cross-validations to 100. For  
351 clarity, we manually pruned the full trees to show just the primary branches.

352 We also provide detailed results for all measures of reliability at each combination of OM  
353 and EM attributes in the Supplementary Materials. For confidence intervals of probability of  
354 convergence, we used the Clopper-Pearson exact method (Clopper and Pearson 1934; Thulin  
355 2014). For AIC selection of process error source we provide estimates of the proportions of  
356 simulations where each EM type was selected. For AIC selection of the SRR (a binary indi-  
357 cator for each simulated data set), we fit logistic regressions and present resulting predicted  
358 probabilities of correctly selecting the SRR as a function of SSB variability (log SDSSB de-  
359 scribed above). We estimated bias as the median of the relative errors across all simulations

360 for a given OM and EM combination. We constructed 95% confidence intervals for the me-  
361 dian relative bias, and Mohn's  $\rho$  using the binomial distribution approach (Thompson 1936)  
362 as in Miller and Hyun (2018) and Stock and Miller (2021).

## 363 Results

### 364 Convergence performance

365 For probability of convergence, the EM process error assumption was the single attribute  
366 that resulted in the largest percent reduction in deviance (14-28%) for all OM process error  
367 sources other than R+S OMs where the EM median natural mortality rate assumption  
368 (estimated or known) explained the most residual deviance (>11%; Table 1). However,  
369 including interactions of OM and EM factors also provided large reductions in residual  
370 deviance (35-47%), suggesting successful convergence depended on a combination OM and  
371 EM attributes.

372 Classification trees for each OM process error source all had the primary branch defined  
373 using the same attribute that provided the largest reduction in deviance (Figure 1). EMs  
374 that assumed R+S process errors converged poorly for all OMs that were simulated with  
375 the alternative process error assumptions (R, R+M, R+Sel, and R+q OMs). For all trees,  
376 branches based on the OM fishing mortality history showed better convergence when the OM  
377 included a change in fishing pressure. Branches based on whether the Beverton-Holt SRR  
378 was assumed or not, showed better convergence when it was not estimated and branches  
379 based on the median natural mortality rate assumption showed better convergence when  
380 it was treated as known. For some R+M and R+Sel OMs, better convergence was also  
381 observed when there was lower observation uncertainty.

382 When convergence is defined by a gradient threshold, the primary factor explaining deviance  
383 reduction is the same that for Hessian-based convergence for all OM process error sources,

384 but there are some differences in deviance reduction for secondary factors (Table S6), and  
385 probability of convergence, overall, was lower (Figure S2). We found a wide range of maxi-  
386 mum absolute values of gradients for models that had invertible Hessians (Figure S3). The  
387 largest value observed for a given EM and OM combination was typically  $< 10^{-3}$ , but many  
388 converged models had values greater than 1. For many OMs, EMs that assumed the correct  
389 process error source and did not estimate median natural mortality or the Beverton-Holt  
390 SRR produced the lowest gradient values.

## 391 AIC performance

### 392 Process error source

393 For AIC selection of the correct process error configuration, the magnitude of observation  
394 and process error variation were the attributes that resulted in the largest percent reductions  
395 in deviance across OM process error sources other than R OMs (Table 2). Both sources of  
396 variation explained large reductions in deviance for R+S (17-22%) and R+Sel (8-26%) OMs,  
397 whereas variance of process errors provided the major reductions for R+M ( $>9\%$ ) and R+q  
398 ( $>13\%$ ) OMs. Comparatively, none of the OM or EM attributes explained particularly large  
399 reductions in deviance for R OMs, but fishing history, whether a SRR was estimated, and  
400 whether median natural mortality was known or estimated provided similar and the largest  
401 reductions (approximately 5-6%). Inclusion of second and third order interactions, did not  
402 provide large reductions in deviance for any of the OM process error sources.

403 For all OM process error sources other than R OMs, the attributes defining the primary  
404 branches of classification trees matched those that provided the largest reductions in deviance  
405 (Figure 2). Across all OMs, AIC was more accurate for the process error source when process  
406 error variability was greater and when observation error was lower. For R+S OMs, there  
407 was a tendency to select R OMs when observation error was higher and apparent survival  
408 variation was lower ( $\sigma_{2+} = 0.25$ ), but accuracy for the process error source was otherwise

409 highly accurate. Larger variability of process error relative to observation error was also  
410 required for accurate identification of the correct correlation structure for R+M, R+q, and  
411 R+Sel OM<sub>s</sub> (Figure S4). No branches were estimated for classification trees fit to the R  
412 OM<sub>s</sub>, likely because accuracy was high across all simulations (0.94), although inspection of  
413 the fine-scale results shows there is some degradation in AIC selection when an SRR and  
414 median natural mortality rate are estimated for R OM<sub>s</sub> with constant fishing pressure and  
415 high observation error (Figure S4, top left).

#### 416 Stock-recruit relationship

417 Logistic regressions for AIC selection of the Beverton-Holt SRR, showed OM fishing history  
418 and log SD<sub>SSB</sub> provided substantial reductions in deviance for R+M (>13%), R+Sel (>26%),  
419 and R+q (>24%) OM<sub>s</sub> (Table 3). For R OM<sub>s</sub>, fishing history provided the largest reduction  
420 in deviance (>9%), whereas none of the attributes individually provided large reductions  
421 in deviance for R+S OM<sub>s</sub> (all <5%). However, inclusion of all attributes provided larger  
422 reductions in deviance than the sum of individual contributions for both R (>30%) and  
423 R+S (~19%) OM<sub>s</sub>. Further fits for R and R+S OM<sub>s</sub> that including different combinations  
424 of two factors additively showed fits that included log SD<sub>SSB</sub> and recruitment variation only  
425 provided essentially the same reduction in deviance as the models with all factors. For all  
426 OM process error sources, inclusion of interaction terms provided relatively little reduction  
427 in residual deviance.

428 Attributes defining the primary branches of classification trees for AIC selection of the SRR  
429 assumption were the same as those explaining the largest reductions in deviance for the lo-  
430 gistic regression models (Figure 3). All branches based on log SD<sub>SSB</sub> showed better accuracy  
431 with larger variability in SSB and all branches based on fishing history showed better accu-  
432 racy when there was contrast in fishing pressure. Branches based on OM observation error  
433 or recruitment variability (R and R+S OM<sub>s</sub>) showed better accuracy when they were lower.

434 For R OMs, a combination of lower recruitment variability, contrast in fishing pressure, and  
435 higher SSB variability produced AIC accuracy over 0.8. For R+S OMs, lower recruitment  
436 variability and observation error and higher SSB variability produced AIC accuracy of 0.79.  
437 For R+M, R+Sel, and R+q OMs, accuracy of 0.87 to 0.94 was observed with just increased  
438 SSB variability.

## 439 Bias

### 440 Terminal year spawning stock biomass, fishing mortality, and recruitment

441 Regression models for log-scale errors in SSB that included the various OM and EM factors  
442 showed little reduction in deviance (<5%) for any of the factors across all OM process error  
443 sources (Table 4). The attributes producing the largest reductions were the EM assumption  
444 for median natural mortality (known or estimated) for R, R+M, R+Sel, and R+q OMs (1-  
445 3%), EM process error assumption for R+S OMs (4%) and fishing history for all OM process  
446 error sources (1-5%). Including second order interactions provided the largest reductions  
447 in residual deviance (10- 26%). Including third order interactions also provided further  
448 reductions for R, R+S, and R+q OMs between 5 and 11%.

449 In all regression trees, branches based on fishing history and level of observation error gener-  
450 ally showed less bias in SSB with contrast in fishing and lower observation error (Figure 4).  
451 For scenarios where there was bias, it was generally positive (over-estimation). For branches  
452 based on treatment of median natural mortality rate, bias was generally less when it was  
453 known rather than estimated. For some R+Sel and R+q OMs, less bias in SSB was shown  
454 when the EM process error assumption was correct.

455 Results for bias in fishing mortality and recruitment generally matched those for SSB, except  
456 that directions of bias for fishing mortality were opposite to those for SSB and recruitment.  
457 Effects of individual OM and EM factors on regression models were similarly small as mea-

458 sured by reduction in deviance (Tables S7 and S8). Factors defining the primary branches  
459 of regression trees were in most cases identical to those for SSB (Figures S5 and S6).

#### 460 Stock-recruit parameters

461 Regression models for log-scale errors of estimates of both the Beverton-Holt  $a$  and  $b$  param-  
462 eters showed none of the factors explained large percent reductions in deviance (Table 5).  
463 The OM fishing history provided the largest deviance reduction for most OM process error  
464 sources for both parameters, but reductions were generally less than 6%. Exceptions were  
465 the R+Sel OMs where  $a$  and  $b$  were reduced by approximately 11% and 8%, respectively,  
466 and the R+q OMs where  $b$  was reduced by 10%. The EM process error assumption provided  
467 similar reductions in deviance for both parameters for R OMs. Including interactions also  
468 did not produce important reductions in deviance.

469 For regression trees of log-scale errors in Beverton-Holt  $a$  and  $b$  parameter estimates, less  
470 bias was indicated with contrast in OM fishing pressure for all branches in trees for each  
471 OM process error source (Figures 5 and 6). For all branches based on recruitment variability  
472 in trees for R and R+S OMs, less bias in both  $a$  and  $b$  was observed with less recruitment  
473 variability. For R OMs with contrast in fishing pressure and greater recruitment variability  
474 EMs that assumed the incorrect R+M process errors produced less bias in both  $a$  and  $b$   
475 than other process error assumptions. Across all combinations of OM and EM attributes,  
476 some bias was observed for both parameters, but there was generally less bias and(or) lower  
477 variability in estimation of the  $a$  parameter than the  $b$  parameter (Figure S7).

#### 478 Median natural mortality rate

479 Fitted regression models for log-scale errors in median natural mortality rate showed largest  
480 percent reductions in residual deviance for R+S and R+M models (Table 6). The largest  
481 reductions for a single attribute was the EM process error assumption (>20%) and fishing

history ( $>15\%$ ) for R+S OMs. Fishing history also provided  $>10\%$  reduction for R+M OMs, but reductions for all factors in R, R+Sel, and R+q OMs were relatively low ( $<6\%$ ). Interactions of OM and EM factors also provided substantial further reductions for R+S and R+M OMs (between 8 and 15% for second order interactions).  
Regression trees with branches based on fishing history showed less bias in median natural mortality rate with contrast in fishing pressure and branches based on level of observation error showed less bias with more precise observations (Figure 7). For R OMs, branches based on EM process error assumption showed less bias with EMs assuming the correct R and the incorrect R+S assumption. For R+S and R+M OMs, branches based on EM process error showed only the correct EM process error assumption with less bias.

## 492 Mohn's $\rho$

Regression models for Mohn's  $\rho$  of SSB showed little reduction in deviance for any of the OM and EM attributes ( $<2\%$ ; Table 7). The lack of explanatory power is also reflected in the regression trees where median Mohn's  $\rho$  values are near zero unless a large combinations of OM and EM conditions occur (Figure 8). For example, in R+S OMs, with constant fishing pressure, high observation error, and higher apparent survival process error, EMs that assume R+M process errors have a median Mohn's  $\rho = -0.068$ .

Similarly, poor explanatory power of the OM and EM attributes occurred when we fit regression models for Mohn's  $\rho$  of fishing mortality and recruitment (Tables S9 and S10). Regression trees for Mohn's  $\rho$  of fishing mortality were similar to those for SSB in that median values of Mohn's  $\rho$  were close to zero for most combinations of OM and EM attributes (Figure S8). However, we observed median Mohn's  $\rho$  for recruitment greater than 0.1 at branches much closer to the base of the trees with fewer interactions of the OM and EM attributes (Figure S9). These branches with consistently large retrospective patterns were typically defined by larger OM observation error, OM constant fishing pressure, or

507 incorrect EM process error configuration. Comparing regression model and regression tree  
508 fits, attributes defining the primary branches for all regression trees of all Mohn's  $\rho$  values  
509 (SSB, fishing mortality, and recruitment) generally matched those that explained the largest  
510 reductions in deviance.

## 511 Discussion

### 512 Assessing convergence

513 Poor convergence was common in our results when the incorrect process error source was  
514 assumed. Li et al. (2024) found that convergence could be a useful diagnostic especially for  
515 separating the correct simpler process error assumption from overly complex models. Poor  
516 convergence often occurs when parameter estimates are at their bounds (Carvalho et al.  
517 2021). However, even when the Hessian is invertible for a converged model, parameters that  
518 are poorly informed will have extremely large variance estimates. This further inspection  
519 can lead to a more appropriate and often more parsimonious model configuration where the  
520 problematic parameters are not estimated. For example, process error variance parameters  
521 in state-space models that are estimated close to 0 indicates that the random effects are  
522 estimated to have little or no variability and removing these process errors is warranted.  
523 Our experiments did not aim to emulate the practitioner decision process in determining  
524 an appropriate model configurations, but evaluating the efficacy of such a decision process  
525 when applying EMs might be important in closed loop simulations aimed at quantifying  
526 management performance (e.g., a management strategy evaluation).

527 It is common during the assessment model fitting process to check that the maximum ab-  
528 solute gradient component is less than some threshold prior to inspecting the Hessian of  
529 the optimized likelihood for invertibility (Carvalho et al. 2021), but we found reliance on  
530 magnitude of the gradient values for fitted models as a convergence criterion questionable.

531 There is no accepted standard for the gradient threshold (e.g., Lee et al. 2011; Hurtado-  
532 Ferro et al. 2014; Rudd and Thorson 2018), but the Hessian at the optimized log-likelihood  
533 was often invertible when the maximum absolute gradient was much larger than what might  
534 be perceived to be a sensible threshold in some of our simulations. Therefore, the gradient  
535 criterion could exclude models that in fact have an invertible Hessian.

536 A factor affecting the convergence criteria, particularly for maximum likelihood estimation  
537 of models with random effects, is numerical accuracy. All optimizations performed in these  
538 simulations are of the Laplace approximation of the marginal likelihood and, therefore, gra-  
539 dients and Hessians are also with respect to this approximation (see TMB::sdreport in the  
540 Template Model Builder package). Functionality within the Template Model Builder pack-  
541 age exists (i.e., TMB::checkConsistency) to check the validity of the Laplace approximation  
542 and the utility of this as a diagnostic for state-space assessment models should be explored  
543 further. Furthermore, numerical methods are used to calculate and invert the Hessian for  
544 variance estimation for models with random effects. Our results, along with the potential  
545 lack of accuracy imposed by these approximations, suggest at least investigating whether  
546 the Hessian is positive definite when the calculated absolute gradients are not terribly large  
547 (e.g, < 1).

## 548 Configuring process error

549 We found accuracy of marginal AIC-based selection for the correct process error source  
550 required only low observation error for R, R+S, R+Sel, and R+q OMs. R+M OMs further  
551 required higher process error variability, but this also improved accuracy for the other OM  
552 process errors sources when there was higher observation error. These results seem consistent  
553 with Li et al. (2024). Their simulation studies investigated models with multiple process  
554 error sources and found good accuracy of AIC in detecting correct process error assumptions  
555 for simulations based on two stocks (Gulf of Maine cod and Southern New England-Mid-

556 Atlantic yellowtail founder) that are well sampled by NEUS bottom trawl surveys used as  
557 indices in the respective assessments and poor accuracy for Atlantic mackerel, a semi-pelagic  
558 species that is observed relatively poorly.

## 559 Stock recruitment relationships

560 Variation in SSB was the most important factor for using marginal AIC to correctly distin-  
561 guish the Beverton-Holt SRR from the null model without an SRR. For R+M, R+Sel, and  
562 R+q OMs, the SRR was accurately detected when the CV of SSB over the time series was  
563 at least 40 to 50% ( $\log SD_{SSB} = -0.9$  to  $-0.7$ ) regardless of any other OM or EM attributes.  
564 Detection of the SRR for R and R+S OMs required lower recruitment variability, but this  
565 lower level ( $\sigma_R = 0.5$ ) was assumed for all of the other OM process error source and repre-  
566 sents the lower range of estimates from recent NEUS stock assessments. Our results assumed  
567 that the EM process error configuration was correct, but this may not be a strong limitation  
568 given the ability of AIC to distinguish the process error source in many scenarios.

569 Although we did not compare models with alternative SRRs (e.g., Ricker vs. Beverton-Holt),  
570 we do not expect AIC to perform any better distinguishing between relationships and may  
571 be more difficult than distinguishing from the null model even with larger variability in SSB.  
572 Our finding that AIC tended to choose simpler recruitment models in many cases contrasts  
573 with the noted bias in AIC for more complex models (Shibata 1976; Katz 1981; Kass and  
574 Raftery 1995). However, these earlier findings apply to the much more common comparison  
575 of models that are fit to raw and independent observations, whereas our comparisons of  
576 state-space models account for observation error and separately estimate process errors in  
577 latent variables.

578 Our results comport with those of de Valpine and Hastings (2002) who found AIC could not  
579 distinguish among state-space SRRs that were fit just to SSB and recruitment observations  
580 (i.e., not within an assessment model). Similarly, Britten et al. (In review) found AIC could

581 not reliably distinguish the Beverton-Holt SRR from no SRR, nor identify alternative envi-  
582 ronmental effects on SRR parameters. However, Miller et al. (2016) did find AIC to prefer  
583 an SRR with environmental effects when applied to data for the Southern New England-  
584 Mid-Atlantic yellowtail flounder stock and AIC also selected an environmental covariate on  
585 an SRR for the most recent stock assessment of Georges Bank yellowtail flounder (NEFSC  
586 2025). Both of these yellowtail flounder stocks have large changes in stock size and the  
587 values of environmental covariates over time. Additionally, this species is well-observed by  
588 the bottom trawl survey that is used for an index in assessment models.

589 Estimation of SRR parameters was only moderately reliable in ideal scenarios of low obser-  
590 vation error and contrast in fishing for R+Sel and R+M OMs with large temporal variability  
591 in process errors. Otherwise, SRR parameter estimation was biased and(or) highly variable.  
592 We found substantial bias in estimated SRR parameters in R and R+S OMs particularly  
593 with high variability in recruitment and apparent survival process errors, suggesting that  
594 practitioners should be cautious with SRR inferences when fitted assessment models have  
595 these properties. We only evaluated effects of SSB variability on accuracy of AIC in identi-  
596 fying the SRR, but those results suggests we might find less bias for the SRR parameters in  
597 such cases as well. Another condition that could improve perception of bias in our simulation  
598 studies is restricting results to fits that converged with Hessian-based standard errors for all  
599 parameters, but Britten et al. (In review) did not find less SRR parameter bias when re-  
600 stricting estimates using a gradient-based criterion. A simulation study by Stock and Miller  
601 (2021) examining configurations of environmental covariate effects on a Beverton-Holt SRR  
602 for the previously mentioned, well-observed, Southern New England-Mid-Atlantic yellowtail  
603 flounder stock found little or no bias for the density-independent mortality parameter  $a$ , but  
604 still biased estimation of the density-dependent parameter  $b$ .

605 **Estimating assessment model quantities**

606 As expected, bias in parameters, SSB, and other assessment output was generally improved  
607 with lower observation error. Estimation of median natural mortality was reliable in many  
608 OM scenarios with contrast in fishing pressure, consistent with Hoenig et al. (2025). How-  
609 ever, we found poor accuracy in terminal SSB estimation when estimating median natural  
610 mortality in many OMs when there was no contrast in fishing pressure over time and higher  
611 observation error. Therefore, estimating median natural mortality should be approached  
612 with caution in state-space assessment models, particularly given its significant impact on  
613 determination of reference point and stock status (Li et al. 2024).

614 **Negligible retrospective patterns**

615 Incorrect EM process error assumptions did not produce strong retrospective patterns for  
616 SSB for any OMs regardless of whether median natural mortality or an SRR was esti-  
617 mated, although some weak patterns occurred when observation error was high and there  
618 was contrast in fishing pressure. However, retrospective patterns tended to be more variable  
619 for recruitment and were sometimes large even when the EM was correct. Therefore, we  
620 recommend de-emphasis on inspection of patterns for recruitment, but further research on  
621 retrospective patterns in other assessment model parameters, management quantities such  
622 as biological reference points, and projections may be beneficial (Brooks and Legault 2016).

623 The general lack of retrospective patterns with mis-specified process errors is perhaps to be  
624 expected. Retrospective patterns are often induced in simulation studies by rapid changes  
625 in a quantity such as index catchability, natural mortality, or perceived catch during years  
626 toward the end of the time series (Legault 2009; Miller and Legault 2017; Huynh et al. 2022;  
627 Breivik et al. 2023). In our simulations, the process errors changing over time may have  
628 trends in certain simulations, particularly when strong autocorrelation is imposed, but the  
629 random effects have no trend on average across simulations. Szuwalski et al. (2018) and

630 Li et al. (2024) also found relatively small retrospective patterns when the source of mis-  
631 specification was temporal variation in demographic attributes. Indeed, it is common for  
632 the flexibility provided by temporal random effects to reduce retrospective patterns (Miller  
633 et al. 2018; Stock et al. 2021; Stock and Miller 2021), though it does not necessarily  
634 indicate a more accurate assessment model (Perretti et al. 2020; Li et al. 2024; Liljestrand  
635 et al. 2024). Our results together with the existing literature seem to suggest that when  
636 a strong retrospective pattern is observed in an assessment it is more likely to be due to a  
637 mis-specification of a rapid shift in some model attribute rather than whether a particular  
638 process is assumed to be randomly varying temporally.

## 639 Summarization approach

640 We found the use of regression models and classification and regression trees extremely useful  
641 in understanding the most important OM and EM attributes explaining variation in the  
642 measures of reliability we examined across all simulations. The classification and regression  
643 trees are generally a good tool for determining the OM and EM attributes that produce better  
644 or worse measures of reliability. However, determining the combination of attributes that  
645 produce the best or worst measures of reliability can be challenging using the trees alone. For  
646 example, in the regression tree for median natural mortality rate estimates in R OMs (Figure  
647 7), both of the first branches imply bias is low regardless of OM fishing history, but when  
648 OM fishing pressure is constant, results are much better when OM observation error is low  
649 (median RE about -6%) than when OM observation error is high (median RE about 40%).  
650 The default pruning of the trees can exclude these lower branches. However, inspection of  
651 deviance explained by various regression models shows the ~9% reduction in residual deviance  
652 by including second order interaction of all OM and EM factors (Table 6), indicating that the  
653 interaction of factors may be important, thereby complimenting the regression tree analysis.  
654 Higher order interactions of some factors could also provide reductions in deviance and,

655 therefore, inspection of results for each combinations of OM and EM factors, as provided in  
656 the Supplementary Materials, can also be important.

657 **Recommendations and conclusions**

658 Our findings regarding model convergence suggests practitioners using state-space models  
659 and maximum marginal likelihood for estimation should not heavily weight the magnitude  
660 of the gradient values in determining convergence as long as the maximum absolute value  
661 is around 1 or lower. Instead, positive-definiteness of the Hessian of the minimized negative  
662 log-likelihood should be evaluated.

663 Unfortunately, whether the practitioner includes a Beverton-Holt SRR will often depend on  
664 biological plausibility of this particular SRR because using AIC to determine its validity  
665 required a combination of low recruitment variability, contrast in fishing pressure, large  
666 variation in SSB over time, and lower observation error, which applies to a limited number  
667 of managed stocks. Furthermore, some bias in estimation of the SRR parameters (and MSY-  
668 based reference points should be expected. Because bias in terminal SSB and retrospective  
669 patterns were indifferent to whether or not the SRR was estimated, the prevalence of bias in  
670 SRR parameter estimation, and often better convergence without the SRR, we recommend  
671 a sensible default is to exclude an SRR when fitting assessment models, as also suggested by  
672 Brooks (2024).

673 We found marginal AIC can, in many cases, accurately distinguished models with process  
674 errors. We saw the best accuracy for models with process errors on recruitment only (R), re-  
675 cruitment and apparent survival (R+S), and recruitment and selectivity (R+Sel), especially  
676 with lower observation error. However, AIC could also distinguish R+M and R+q process  
677 errors when variability of those processes was greater. The R+S assumption for process er-  
678 rors is common in applications of WHAM in the NEUS and the SAM assessment framework  
679 (Nielsen and Berg 2014) in ICES, and we can have some confidence that practitioners are

680 correctly arriving at this assumption over other sources of process error using marginal AIC.

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Fig. 1. Classification trees indicating primary factors determining convergence as defined by providing Hessian-based standard errors for R, R+S, R+M, R+Sel and R+q OMs. Nodes denote percent convergence (top) and number of fits (bottom) for the corresponding subset. Lower or higher convergence rates are indicated by more red or green polygons, respectively

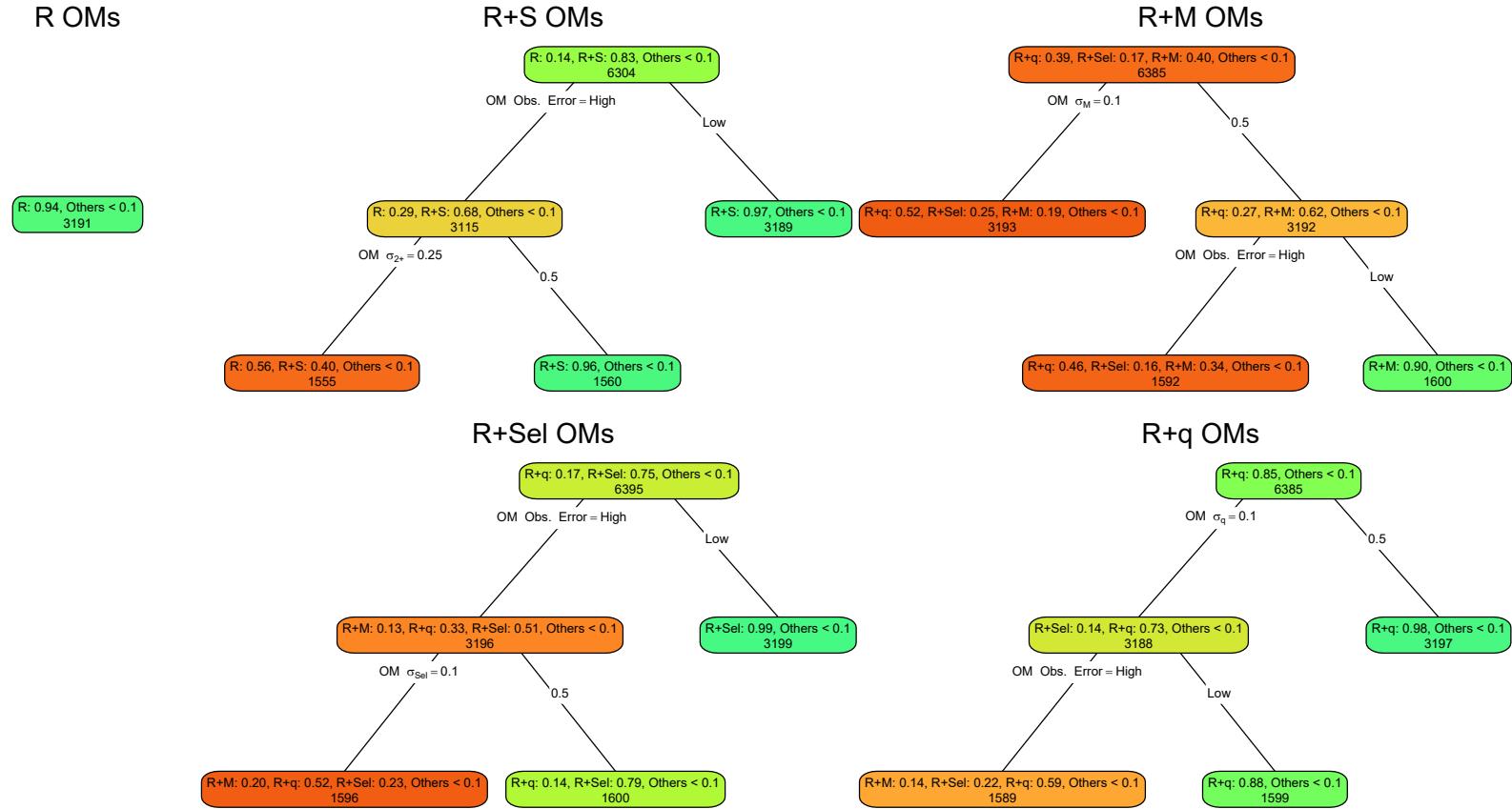


Fig. 2. Classification trees indicating primary factors determining which EM process error assumption provides the lowest AIC for R+S, R+M, R+Sel and R+q OM. Each node shows the proportion of EM process error models with lowest AIC (top) and number of observations (bottom) for the corresponding subset. Lower or higher accuracy of the process error assumption are indicated by more red or green polygons, respectively.

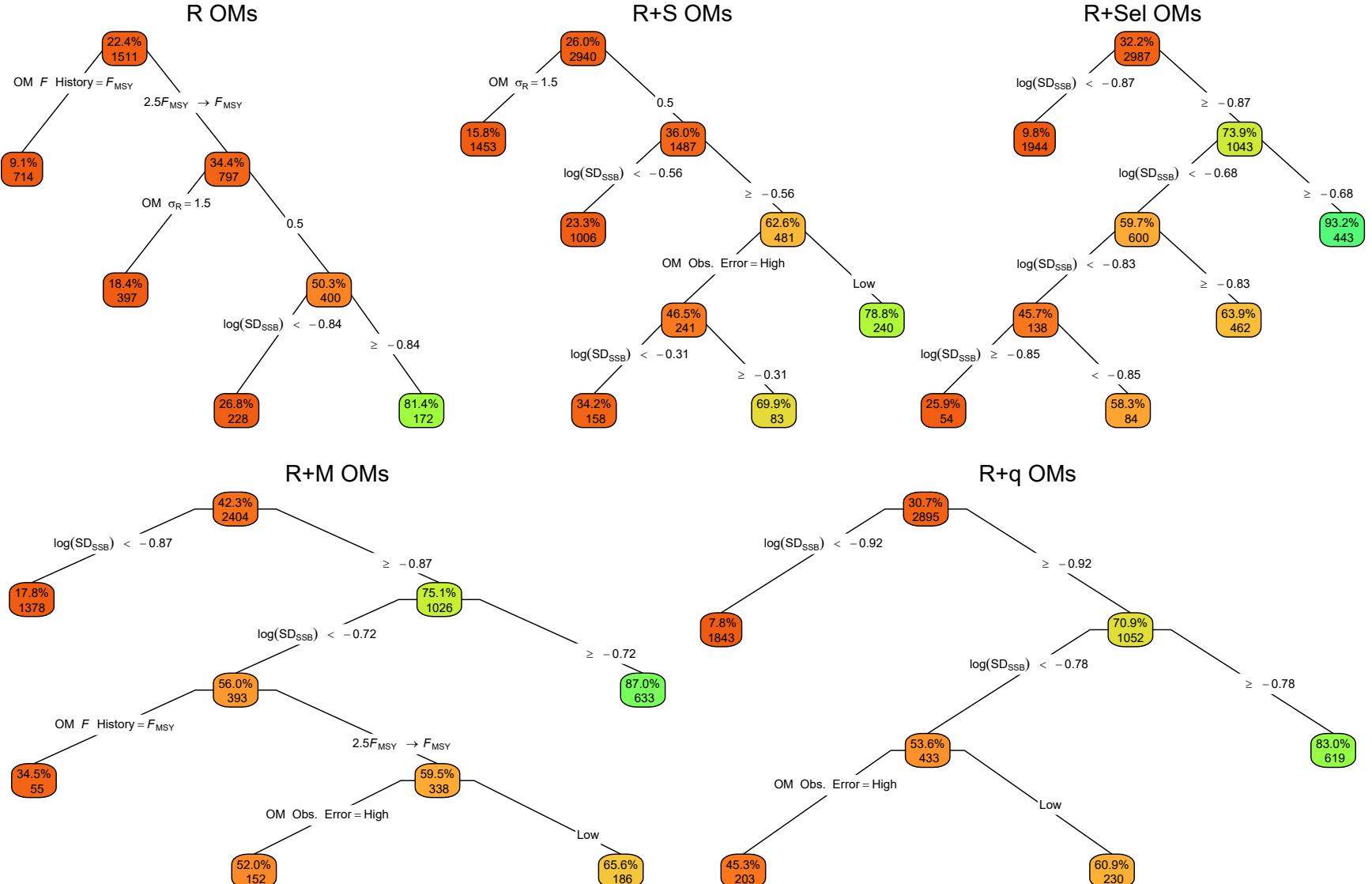


Fig. 3. Classification trees indicating primary factors determining which EM SRR assumption (none or Beverton-Holt) provides the lowest AIC for R, R+S, R+M, R+Sel and R+q OMs. All EMs assume the correct process error source. Nodes denote the percentage of EMs that assume the SRR with lowest AIC (top) and number of observations (bottom) for the corresponding subset. Lower or higher accuracy of the process error assumption are indicated by more red or green polygons, respectively.

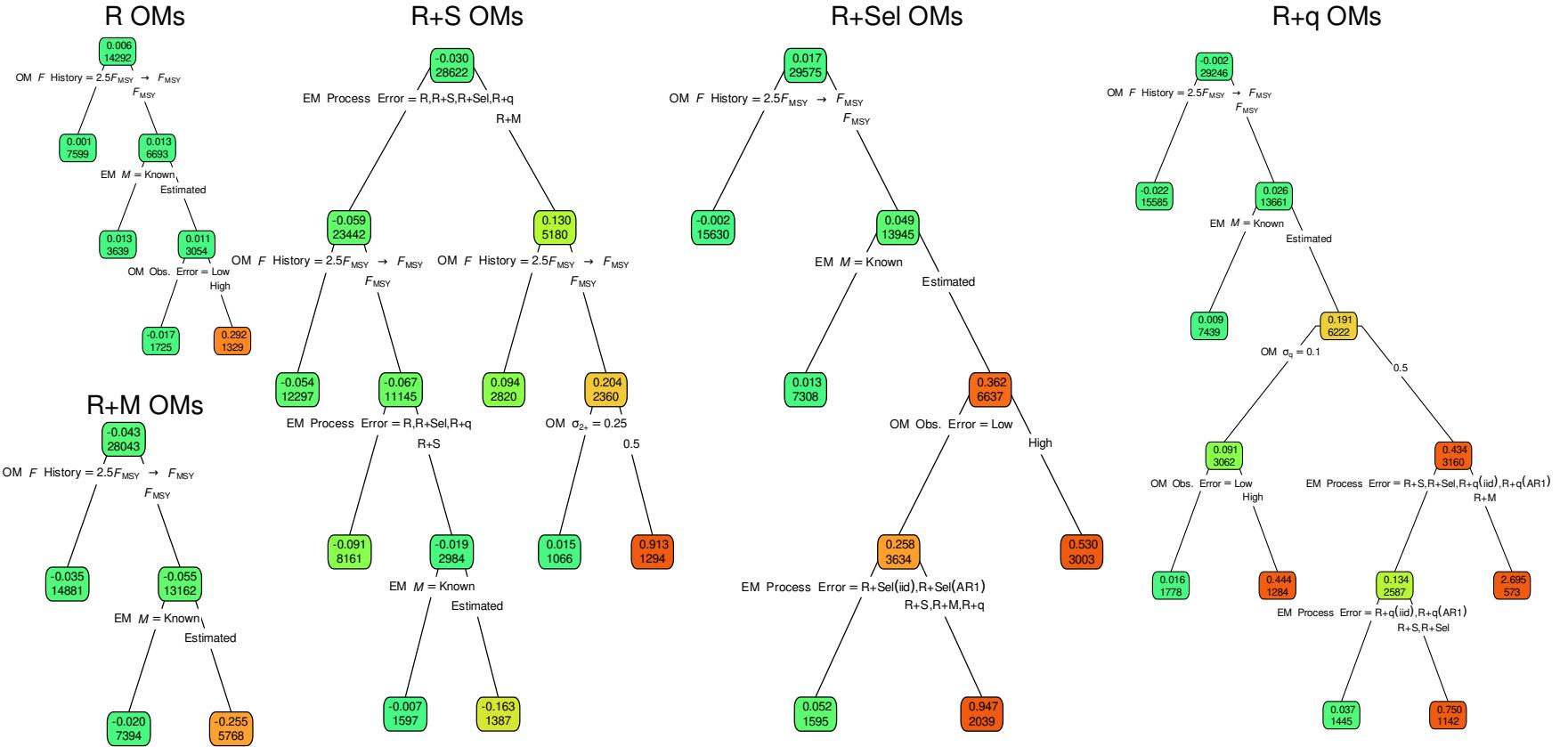


Fig. 4. Regression trees indicating primary factors determining reductions in sums of squares of errors measured by Eq. 3 for terminal year SSB for R+S, R+M, R+Sel and R+q OM. Each node shows the median error (top) and number of observations (bottom) for the corresponding subset. Median errors closer to or further from zero are indicated by more green or red polygons, respectively.

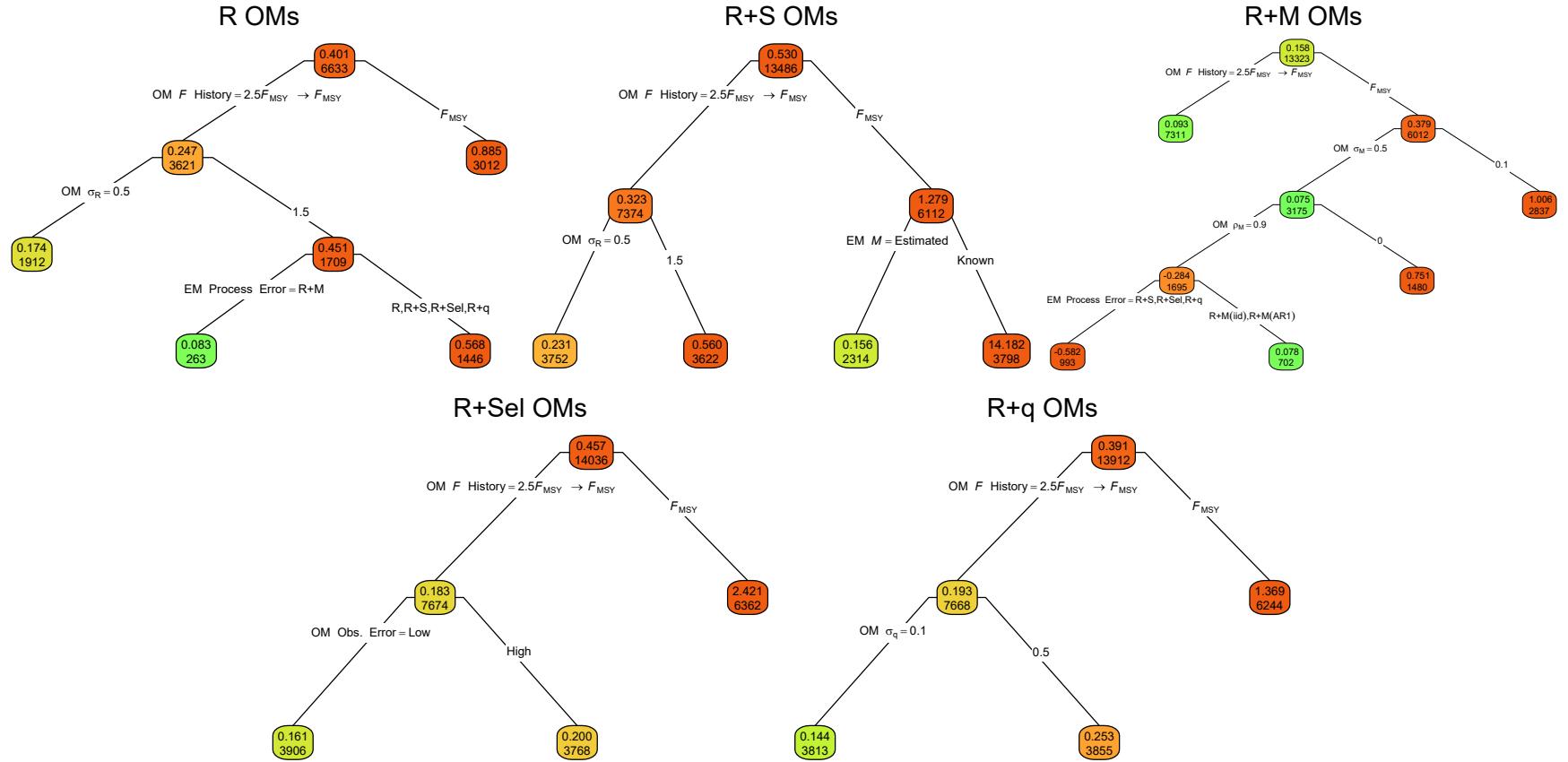


Fig. 5. Regression trees indicating primary factors determining reductions in sums of squares of errors in estimation measured by Eq. 3 for the Beverton-Holt SRR parameter  $a$  for R+S, R+M, R+Sel and R+q OMs. Each node shows the median error (top) and number of observations (bottom) for the corresponding subset. Lower or higher median absolute errors of the process error assumption are indicated by more green or red polygons, respectively.

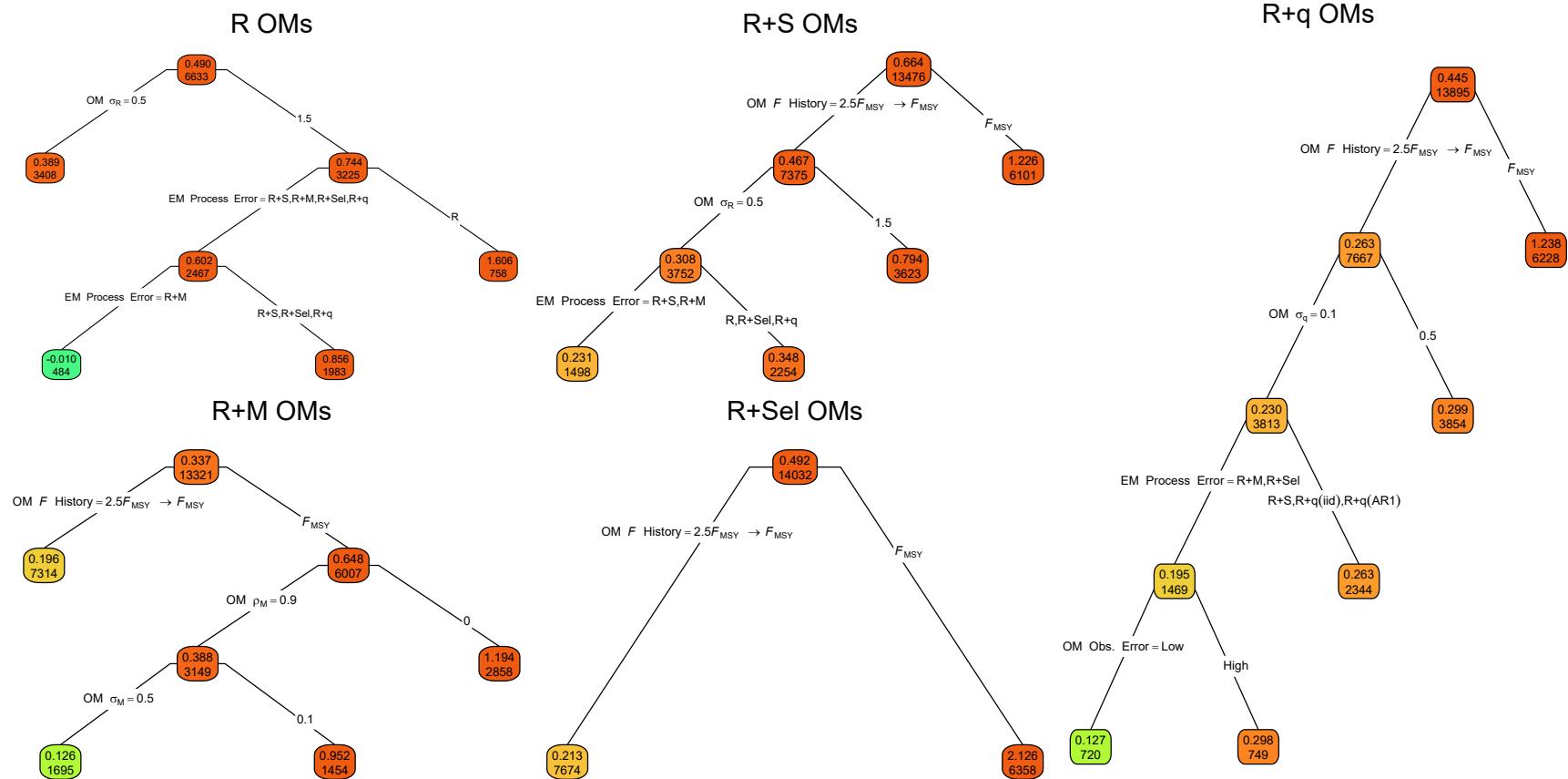


Fig. 6. Regression trees indicating primary factors determining reductions in sums of squares of errors in estimation measured by Eq. 3 for the Beverton-Holt SRR parameter  $b$  for R+S, R+M, R+Sel and R+q OMs. Each node shows the median error (top) and number of observations (bottom) for the corresponding subset. Lower or higher median absolute errors of the process error assumption are indicated by more green or red polygons, respectively.

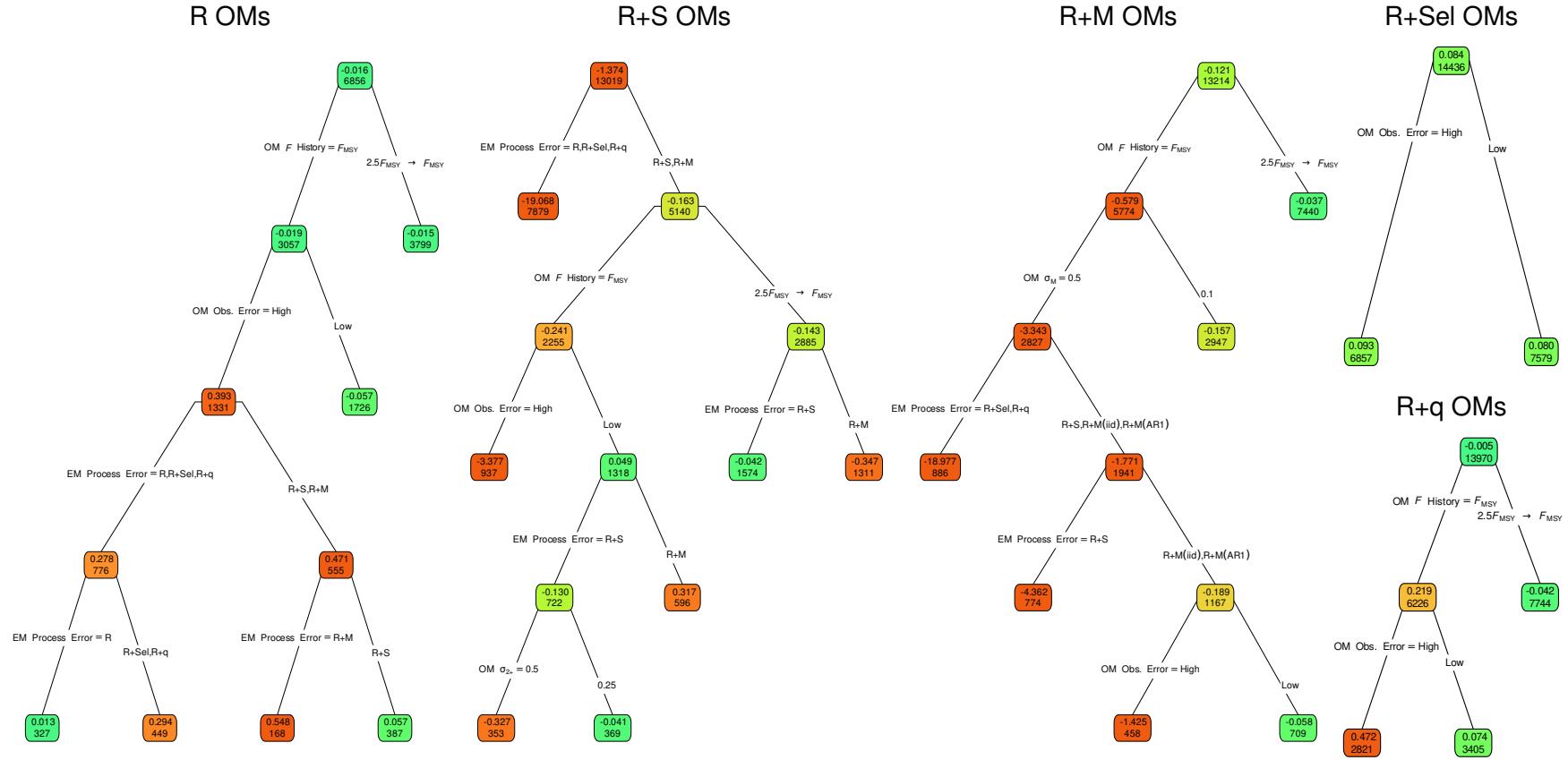


Fig. 7. Regression trees indicating primary factors determining reductions in sums of squares of errors in estimation measured by Eq. 3 for the median natural mortality rate for R+S, R+M, R+Sel and R+q OM. Each node shows the median error (top) and number of observations (bottom) for the corresponding subset. Lower or higher median absolute errors of the process error assumption are indicated by more green or red polygons, respectively.

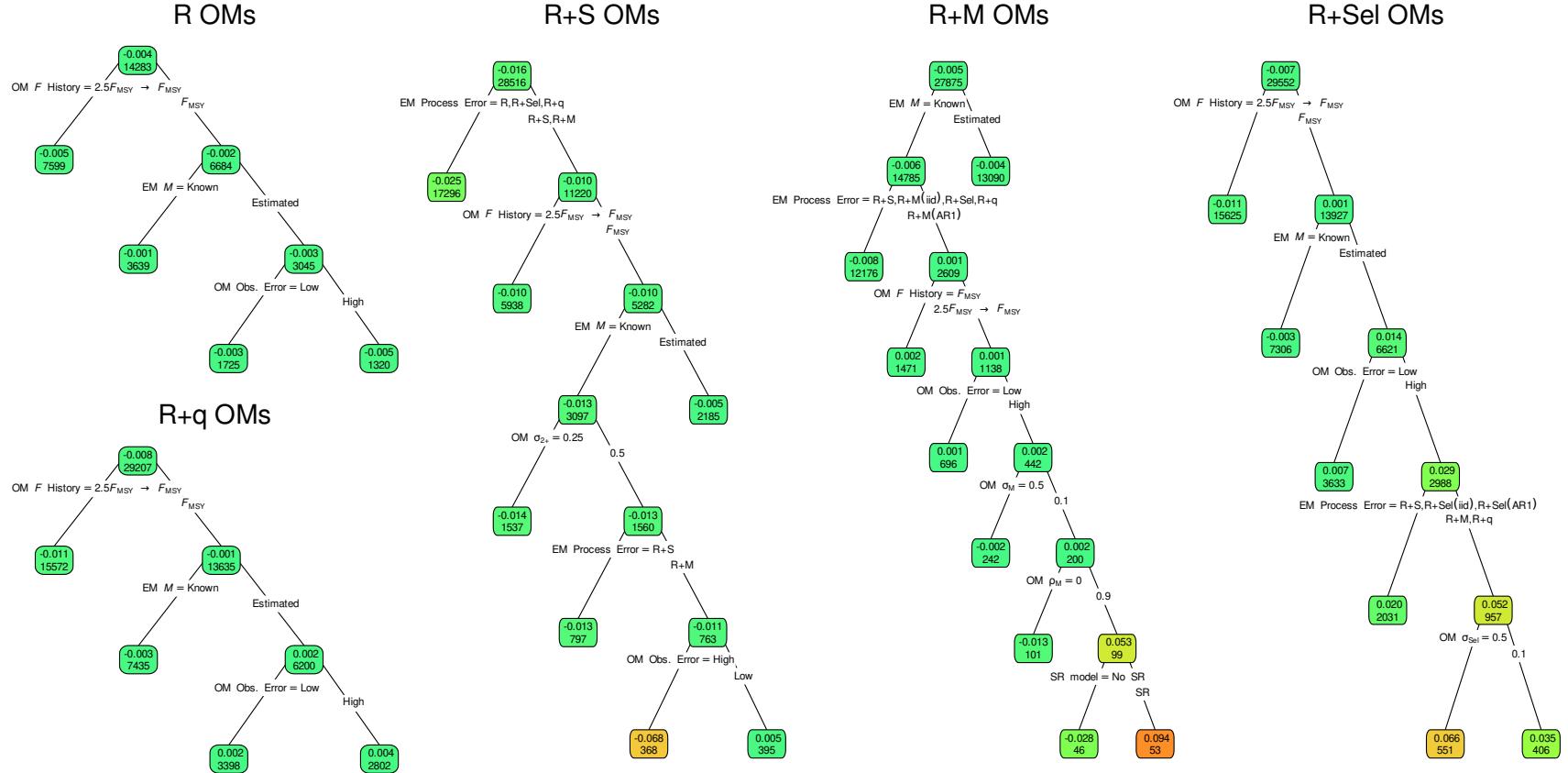


Fig. 8. Regression trees indicating primary factors determining reductions in sums of squares of errors in transformed Mohn's  $\rho$  (Eq. 3) for SSB for R+S, R+M, R+Sel and R+q OMs. Each node shows the median Mohn's  $\rho$  (top) and number of observations (bottom) for the corresponding subset. Median Mohn's  $\rho$  closer to or further from zero are indicated by more green or red polygons, respectively.

Table 1. For each OM process error source (columns), percent reduction in deviance for logistic regression models fit to indicators of convergence (providing Hessian-based standard errors) with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM Process Error	27.95	4.58	14.68	17.24	24.66
EM $M$ Assumption	1.07	11.43	2.45	0.56	1.46
EM SR Assumption	2.88	3.30	1.24	2.47	1.59
OM Obs. Error	0.75	4.64	2.06	4.54	1.60
OM $F$ History	2.32	3.37	1.63	3.30	2.59
OM $\sigma_R$	0.10	0.02	—	—	—
OM $\sigma_{2+}$	—	0.40	—	—	—
OM $\sigma_M$	—	—	0.22	—	—
OM $\rho_M$	—	—	0.17	—	—
OM $\sigma_{Sel}$	—	—	—	1.81	—
OM $\rho_{Sel}$	—	—	—	0.02	—
OM $\sigma_q$	—	—	—	—	0.34
OM $\rho_q$	—	—	—	—	<0.01
All factors	39.54	31.46	24.85	34.83	36.31
+ All Two Way	45.03	39.89	35.20	42.81	43.70
+ All Three Way	47.02	44.57	37.88	45.51	46.87

Table 2. For each OM process error source (columns), percent reduction in deviance for multinomial logistic regression models fit to indicators of EM process error assumption with lowest AIC with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	5.52	1.05	0.52	0.61	1.32
EM SR Assumption	5.60	0.75	1.13	0.93	1.95
OM Obs. Error	2.96	22.46	3.42	25.67	5.03
OM $F$ History	5.77	0.62	0.94	0.91	2.05
OM $\sigma_R$	0.10	0.66	—	—	—
OM $\sigma_{2+}$	—	16.86	—	—	—
OM $\sigma_M$	—	—	9.06	—	—
OM $\rho_M$	—	—	0.38	—	—
OM $\sigma_{Sel}$	—	—	—	7.59	—
OM $\rho_{Sel}$	—	—	—	0.60	—
OM $\sigma_q$	—	—	—	—	13.50
OM $\rho_q$	—	—	—	—	0.75
All factors	20.98	46.12	16.58	40.83	25.99
+ All Two Way	22.02	48.94	21.63	44.08	30.17
+ All Three Way	22.05	49.98	22.36	44.54	31.38

Table 3. For each OM process error source (columns), percent reduction in deviance for logistic regression models fit to indicators of EM SRR assumption (none or Beverton-Holt) with lowest AIC with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	0.04	0.21	0.18	0.02	0.01
OM Obs. Error	<0.01	0.65	0.14	0.04	0.02
OM $F$ History	9.17	3.79	13.08	26.56	24.60
OM $\sigma_R$	3.54	4.74	—	—	—
OM $\sigma_{2+}$	—	0.14	—	—	—
OM $\sigma_M$	—	—	1.14	—	—
OM $\rho_M$	—	—	0.05	—	—
OM $\sigma_{Sel}$	—	—	—	0.02	—
OM $\rho_{Sel}$	—	—	—	0.17	—
OM $\sigma_q$	—	—	—	—	0.36
OM $\rho_q$	—	—	—	—	0.02
log (SD <sub>SSB</sub> )	4.11	1.59	33.39	41.36	39.23
All factors	31.52	18.99	34.23	43.77	42.31
+ All Two Way	34.79	22.24	35.99	45.84	44.04
+ All Three Way	35.41	23.09	37.57	46.39	44.63

Table 4. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to errors in estimation measured by Eq. 3 for the terminal year SSB with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	2.28	1.15	1.04	2.92	3.26
EM SR assumption	0.10	0.06	0.08	0.06	0.08
EM Process Error	0.43	4.28	0.40	0.11	1.05
OM Obs. Error	1.63	0.07	0.78	0.32	<0.01
OM $F$ History	2.62	3.15	1.28	3.22	4.72
OM $\sigma_R$	0.03	0.01	—	—	—
OM $\sigma_{2+}$	—	0.93	—	—	—
OM $\sigma_M$	—	—	0.18	—	—
OM $\rho_M$	—	—	0.01	—	—
OM $\sigma_{Sel}$	—	—	—	0.16	—
OM $\rho_{Sel}$	—	—	—	0.04	—
OM $\sigma_q$	—	—	—	—	1.02
OM $\rho_q$	—	—	—	—	0.06
All factors	7.59	9.86	3.93	7.04	10.64
+ All Two Way	17.99	25.56	10.06	13.44	22.43
+ All Three Way	23.39	36.74	13.76	16.55	31.11

Table 5. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to errors in estimation measured by Eq. 3 for the Beverton-Holt SRR parameters with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	Beverton-Holt <i>a</i>					Beverton-Holt <i>b</i>				
	R	R+S	R+M	R+Sel	R+q	R	R+S	R+M	R+Sel	R+q
EM <i>M</i> Assumption	0.02	1.05	0.02	0.11	0.02	0.05	1.06	0.03	0.01	0.40
EM Process Error	2.74	0.18	0.20	1.25	1.90	2.29	1.21	0.12	1.40	3.06
OM Obs. Error	0.16	<0.01	0.01	0.04	<0.01	<0.01	0.01	0.05	0.01	0.01
OM <i>F</i> History	3.15	3.34	5.60	11.37	10.00	1.16	1.17	2.01	7.97	3.87
OM $\sigma_R$	2.31	0.74	—	—	—	1.67	0.52	—	—	—
OM $\sigma_{2+}$	—	0.29	—	—	—	—	0.01	—	—	—
OM $\sigma_M$	—	—	0.30	—	—	—	—	0.13	—	—
OM $\rho_M$	—	—	0.51	—	—	—	—	0.22	—	—
OM $\sigma_{Sel}$	—	—	—	0.13	—	—	—	—	0.05	—
OM $\rho_{Sel}$	—	—	—	0.07	—	—	—	—	0.04	—
OM $\sigma_q$	—	—	—	—	0.04	—	—	—	—	0.10
OM $\rho_q$	—	—	—	—	<0.01	—	—	—	—	<0.01
All factors	8.07	5.15	6.73	12.64	11.79	4.91	3.75	2.55	9.12	7.22
+ All Two Way	9.96	7.37	9.76	13.59	13.65	7.55	7.15	4.32	10.08	12.16
+ All Three Way	11.22	8.15	11.13	14.48	14.87	9.78	9.02	5.26	11.08	14.73

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Table 6. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to errors in estimation measured by Eq. 3 for the median natural mortality rate parameter with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM SR assumption	0.21	0.38	0.11	0.26	0.43
EM Process Error	1.98	20.36	3.16	0.94	1.31
OM Obs. Error	4.74	0.79	0.40	2.23	1.88
OM $F$ History	5.07	15.11	10.65	0.24	2.38
OM $\sigma_R$	<0.01	0.01	—	—	—
OM $\sigma_{2+}$	—	5.04	—	—	—
OM $\sigma_M$	—	—	5.32	—	—
OM $\rho_M$	—	—	0.85	—	—
OM $\sigma_{Sel}$	—	—	—	1.30	—
OM $\rho_{Sel}$	—	—	—	0.37	—
OM $\sigma_q$	—	—	—	—	0.46
OM $\rho_q$	—	—	—	—	0.06
All factors	12.64	40.10	21.29	5.54	6.52
+ All Two Way	21.17	48.12	36.19	9.87	11.71
+ All Three Way	23.03	50.38	42.82	11.58	14.64

Table 7. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to transformed Mohn's  $\rho$  values for each simulation (Eq. 3) for SSB with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	0.79	0.18	0.15	0.95	1.24
EM SR assumption	<0.01	0.01	<0.01	<0.01	<0.01
EM Process Error	<0.01	0.22	0.14	0.08	0.04
OM Obs. Error	0.12	0.03	0.05	0.18	0.21
OM $F$ History	0.84	0.14	0.07	1.08	1.56
OM $\sigma_R$	0.01	0.01	—	—	—
OM $\sigma_{2+}$	—	0.02	—	—	—
OM $\sigma_M$	—	—	0.01	—	—
OM $\rho_M$	—	—	<0.01	—	—
OM $\sigma_{Sel}$	—	—	—	0.01	—
OM $\rho_{Sel}$	—	—	—	0.02	—
OM $\sigma_q$	—	—	—	—	0.01
OM $\rho_q$	—	—	—	—	0.01
All factors	1.89	0.63	0.43	2.43	3.29
+ All Two Way	3.63	1.10	0.91	4.75	6.22
+ All Three Way	4.27	1.65	1.50	5.73	7.53

<sub>910</sub> **Supplementary Materials**

911 Referenced Figures

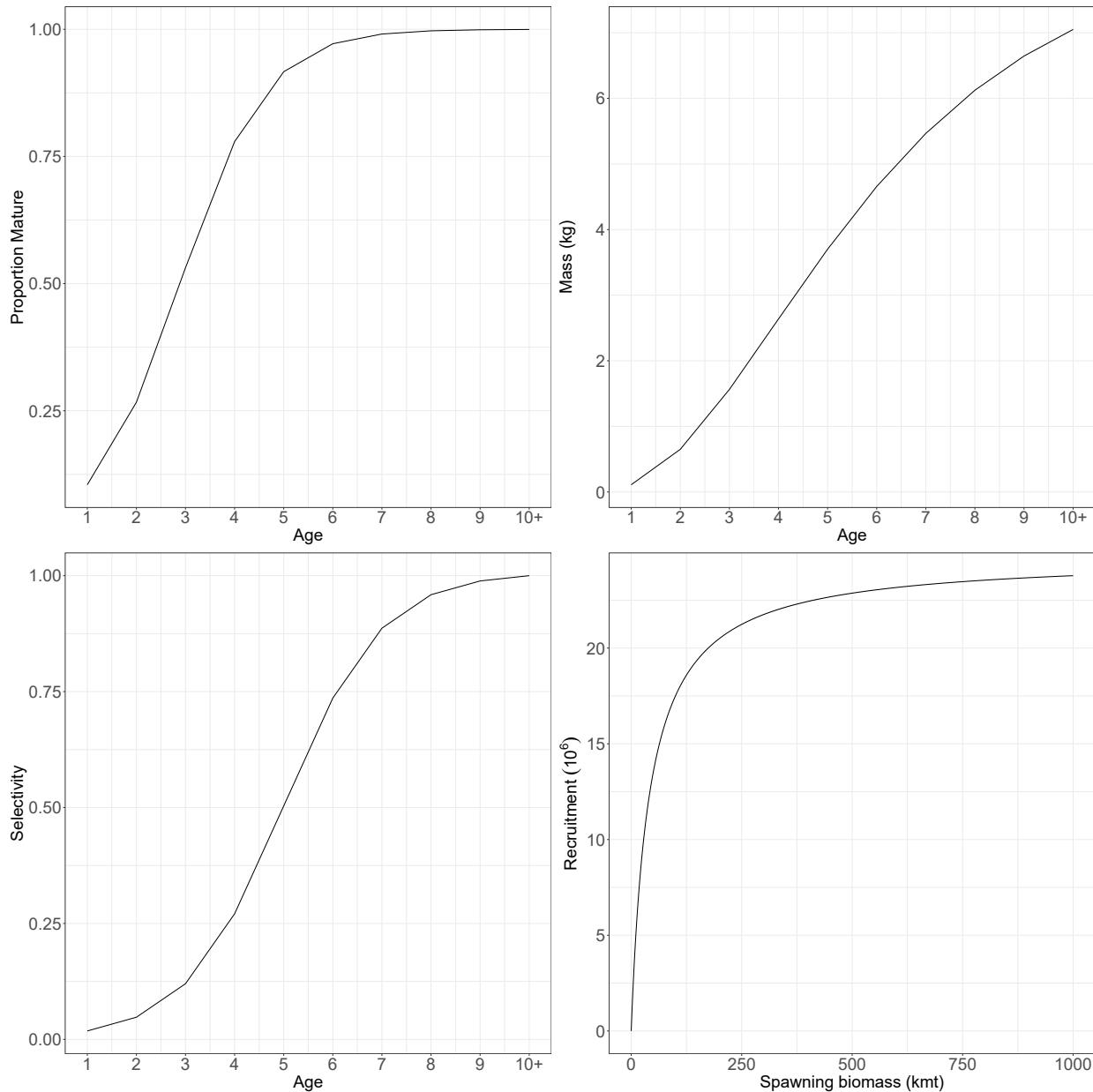


Fig. S1. The proportion mature at age, weight at age, fleet and index selectivity at age, and Beverton-Holt SRR assumed for the population in all OMs. For OMs with random effects on fleet selectivity, this represents the selectivity at the mean of the random effects.

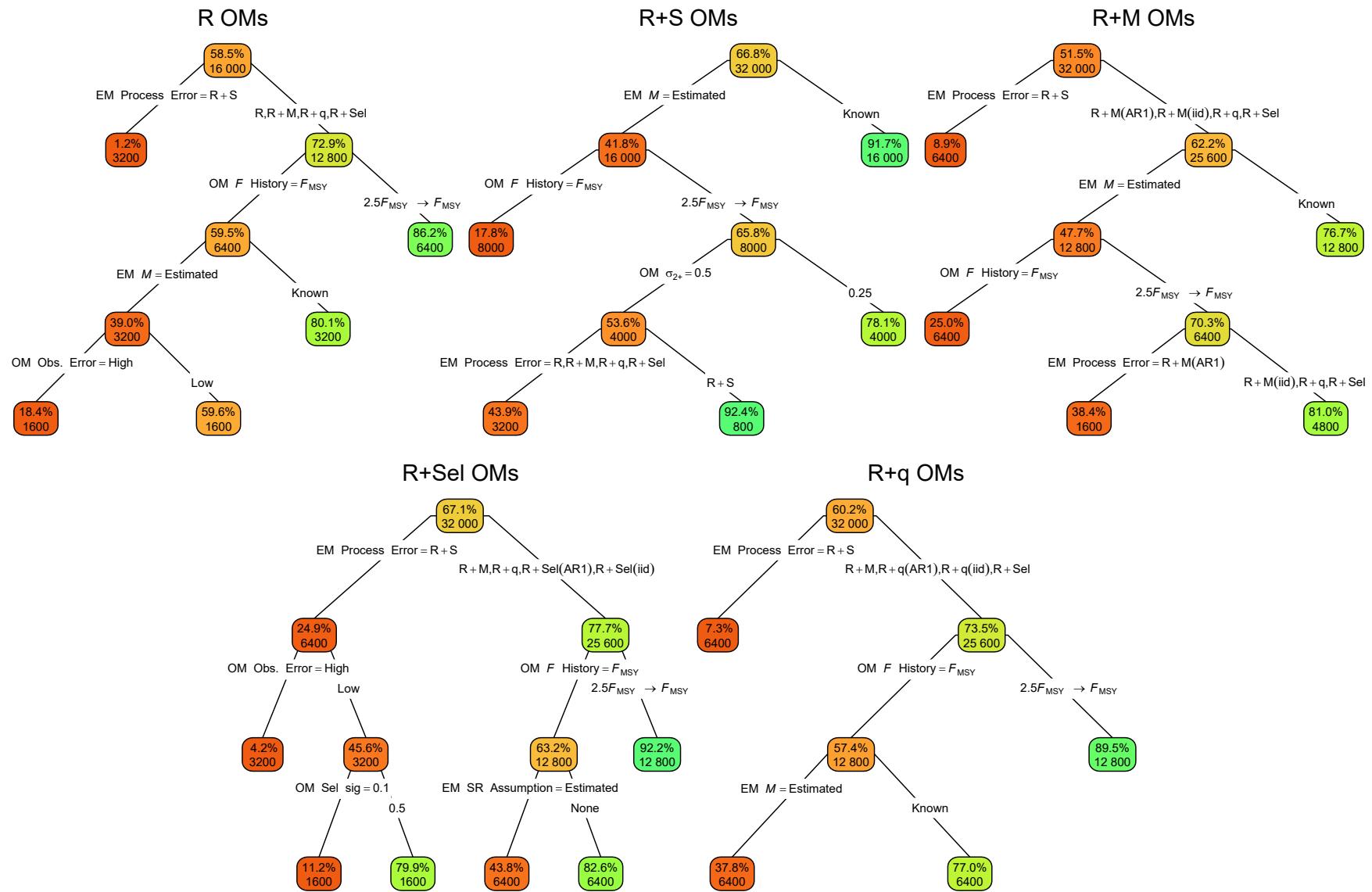


Fig. S2. Classification trees indicating primary factors determining convergence as defined by a maximum absolute gradient  $< 10^{-6}$  for R, R+S, R+M, R+Sel and R+q OMs. Nodes denote percent convergence (top) and number of fits (bottom) for the corresponding subset. Lower or higher convergence rates are indicated by more red or green polygons, respectively

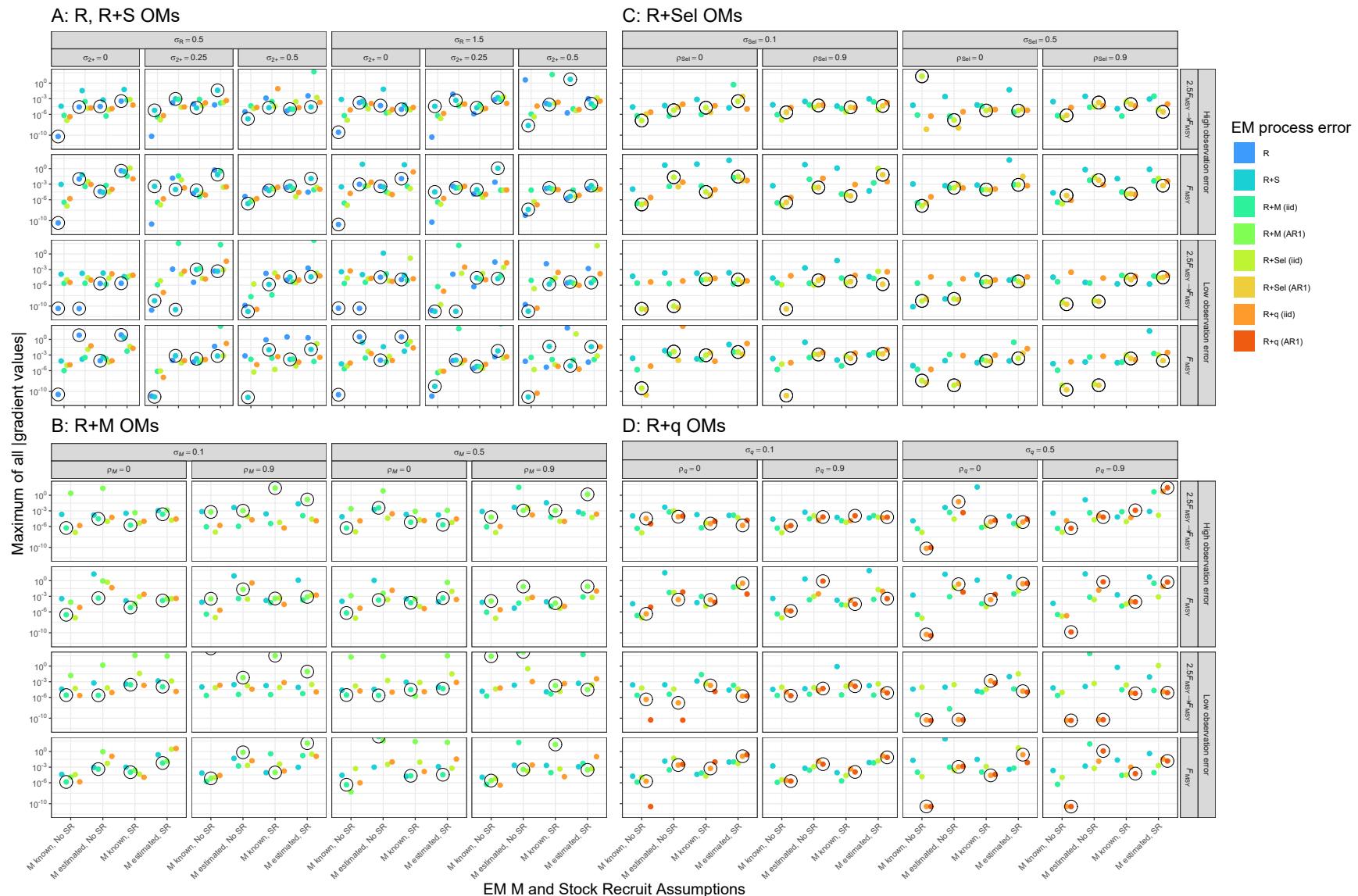


Fig. S3. The maximum of the absolute values of all gradient values for all fits that provided Hessian-based standard errors across all simulated data sets of a given OM configuration (A: R and R+S, B: R+M, C: R+Sel, or D: R+q). Results are conditional on EM fits with alternative process error assumptions (colored points and lines), median natural mortality (estimated or known) and recruitment assumptions (Beverton-Holt SRR or not). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

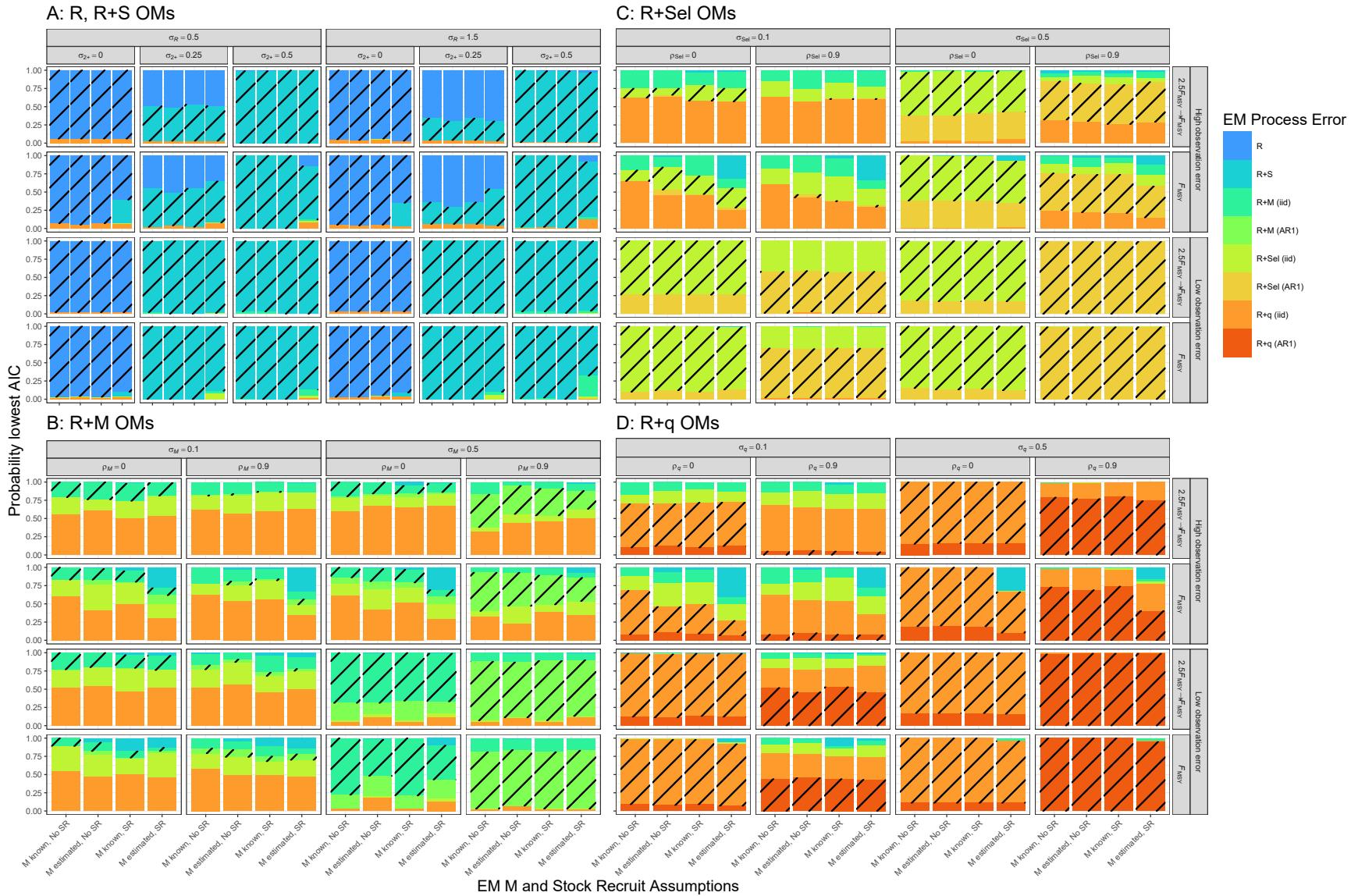


Fig. S4. Estimated probability of lowest AIC for EMs assuming alternative process error assumptions (colored bars) conditional on alternative assumptions for median natural mortality (estimated or known) and Beverton-Holt SRR (estimated or not; along x-axis) when fitted to OMs that have R and R+S (A), R+Sel (B), R+M (C), or R+q (D) process error sources. Striped bars indicate results where the EM process error structure matches that of the OM.

G1

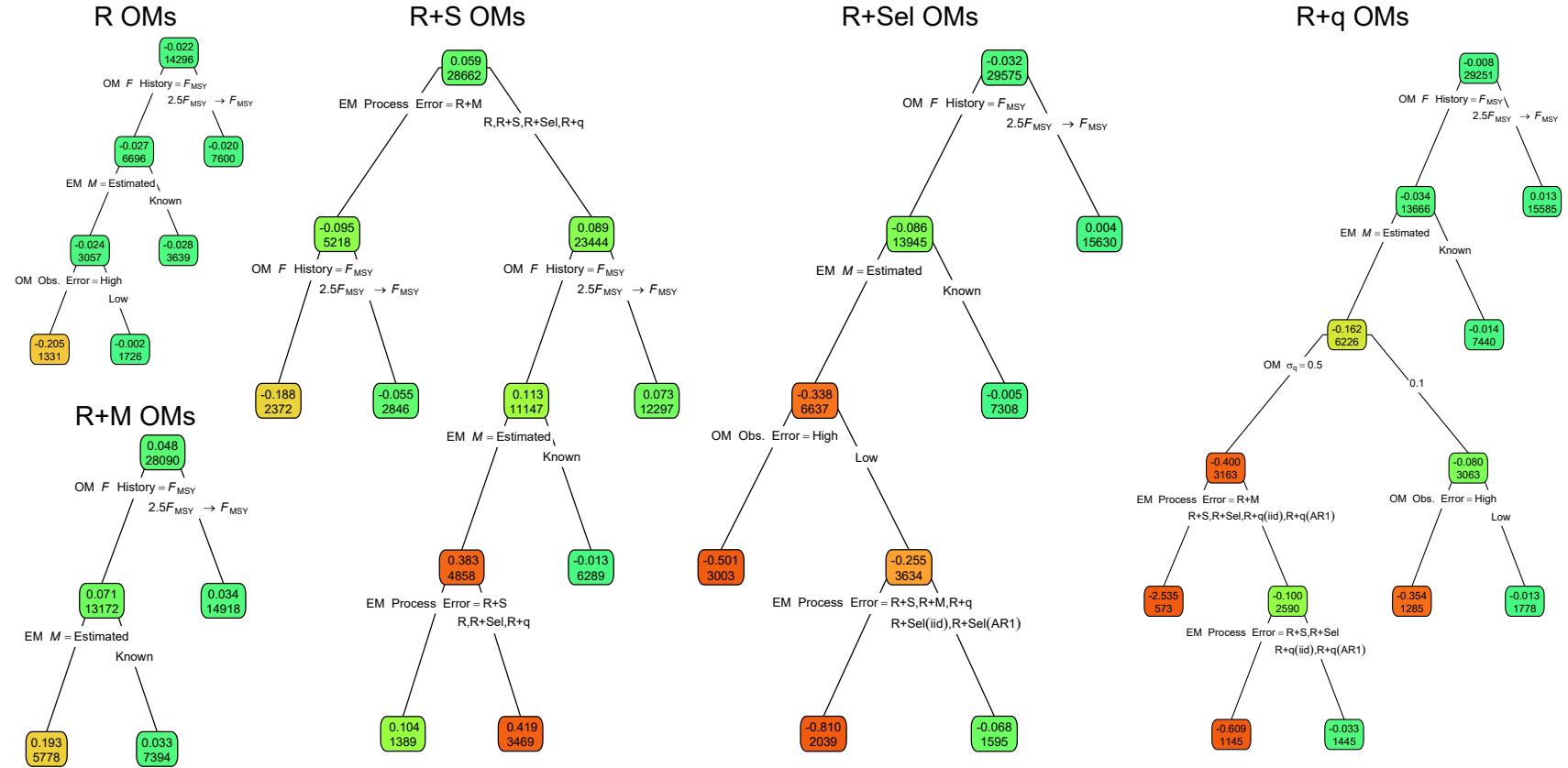


Fig. S5. Regression trees indicating primary factors determining reductions in sums of squares of errors in estimation measured by Eq. 3 for terminal year fully-selected fishing mortality for R+S, R+M, R+Sel and R+q OM models. Each node shows the median error (top) and number of observations (bottom) for the corresponding subset. Median errors closer to or further from zero are indicated by more green or red polygons, respectively.

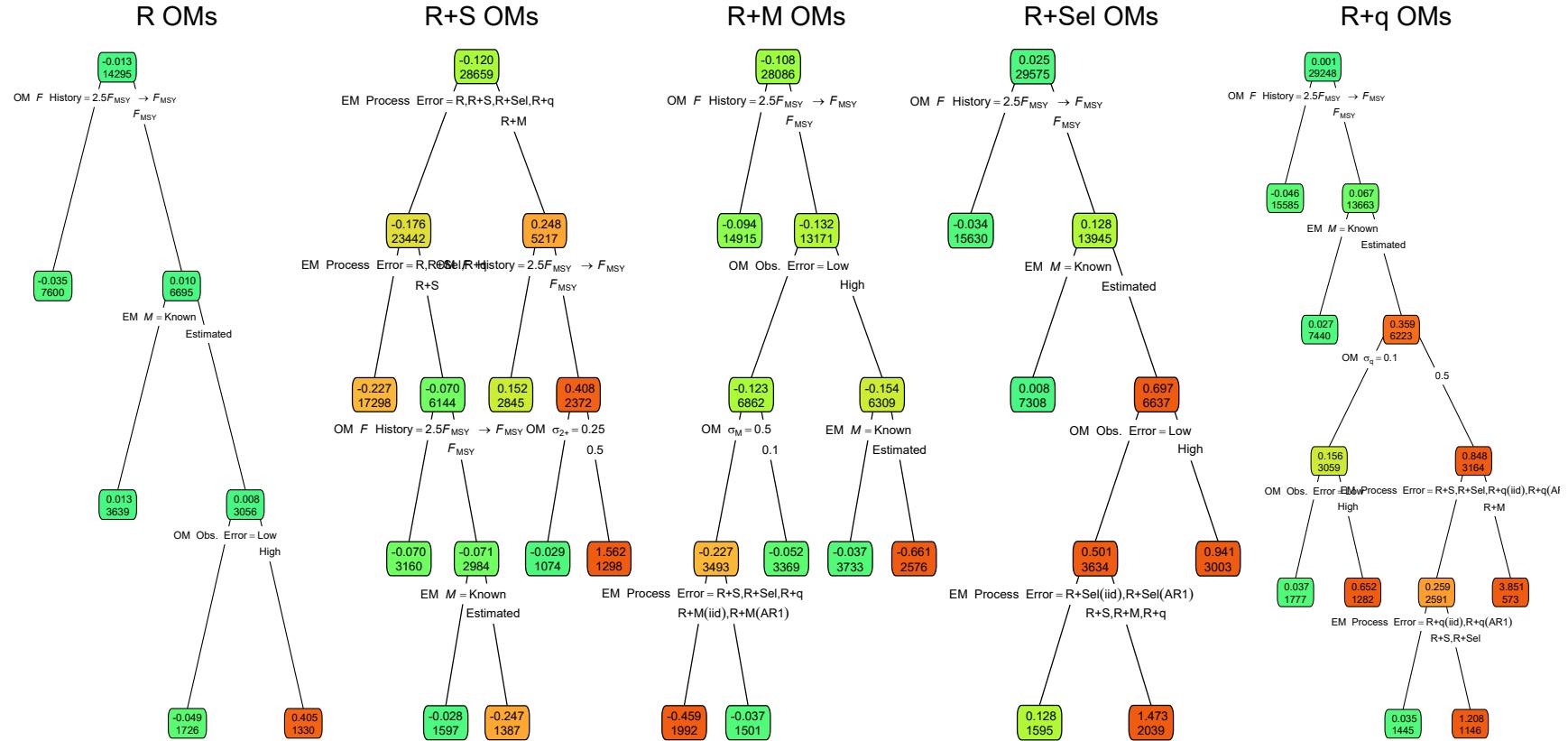


Fig. S6. Regression trees indicating primary factors determining reductions in sums of squares of errors in estimation measured by Eq. 3 for terminal year recruitment for R+S, R+M, R+Sel and R+q OM scenarios. Each node shows the median error (top) and number of observations (bottom) for the corresponding subset. Median errors closer to or further from zero are indicated by more green or red polygons, respectively.

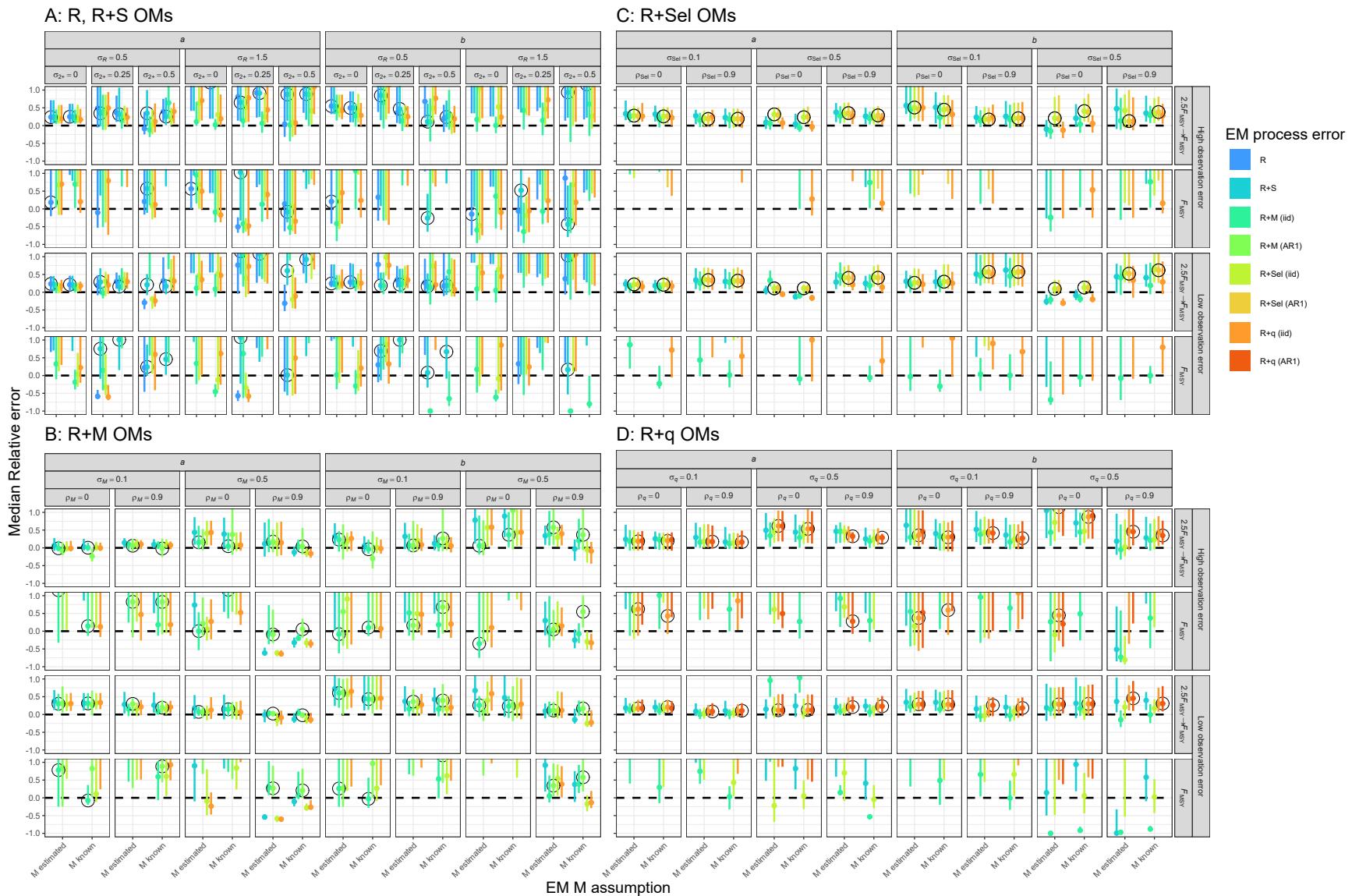


Fig. S7. Median relative error of Beverton-Holt SRR parameters (*a* and *b*) for EMs fitted to data sets simulated with alternative process error structures: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

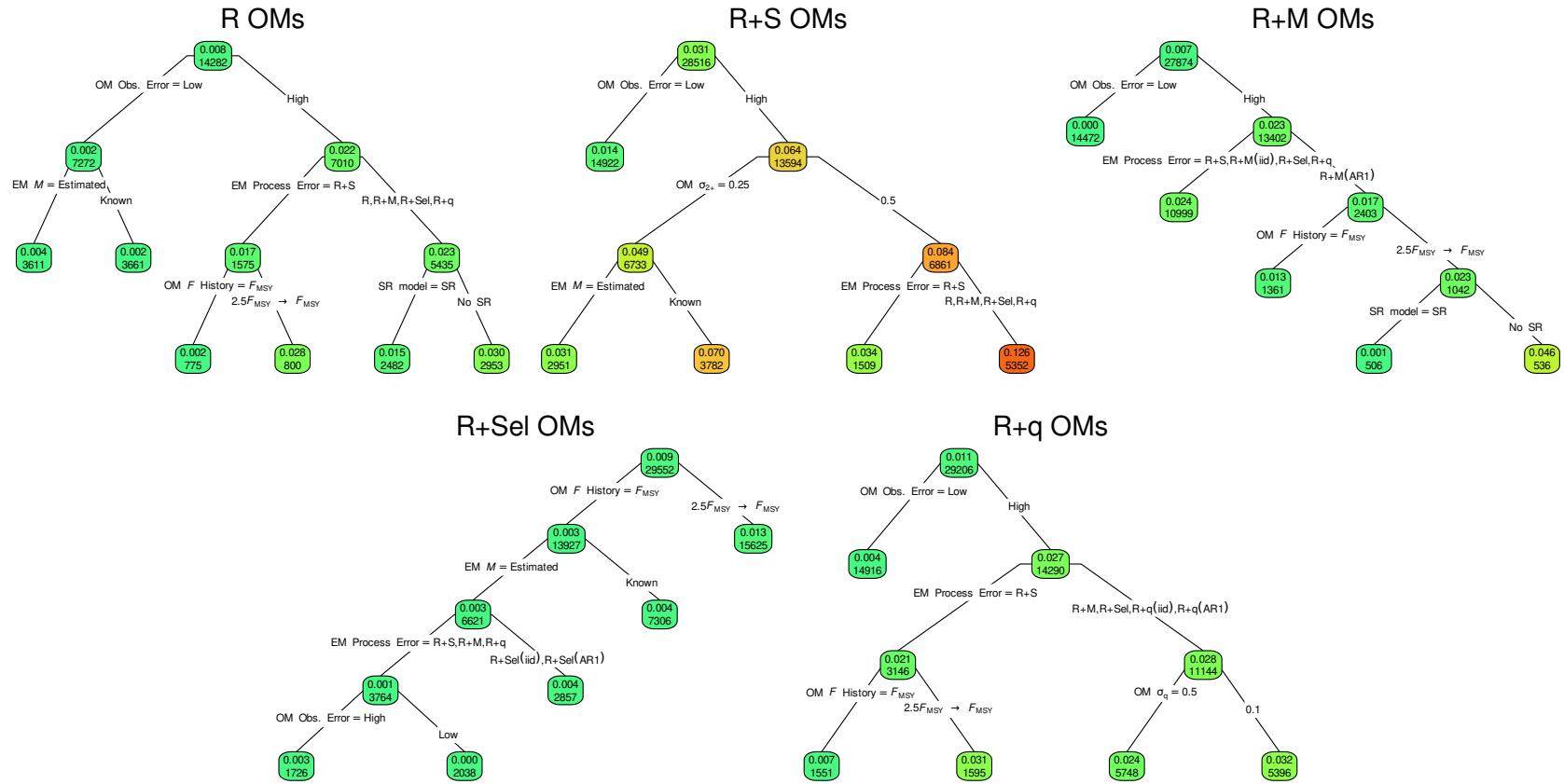


Fig. S8. Regression trees indicating primary factors determining reductions in sums of squares of errors in transformed Mohn's  $\rho$  (Eq. 3) for fishing mortality averaged over all age classes for R+S, R+M, R+Sel and R+q OM categories. Each node shows the median Mohn's  $\rho$  (top) and number of observations (bottom) for the corresponding subset. Median Mohn's  $\rho$  closer to or further from zero are indicated by more green or red polygons, respectively.

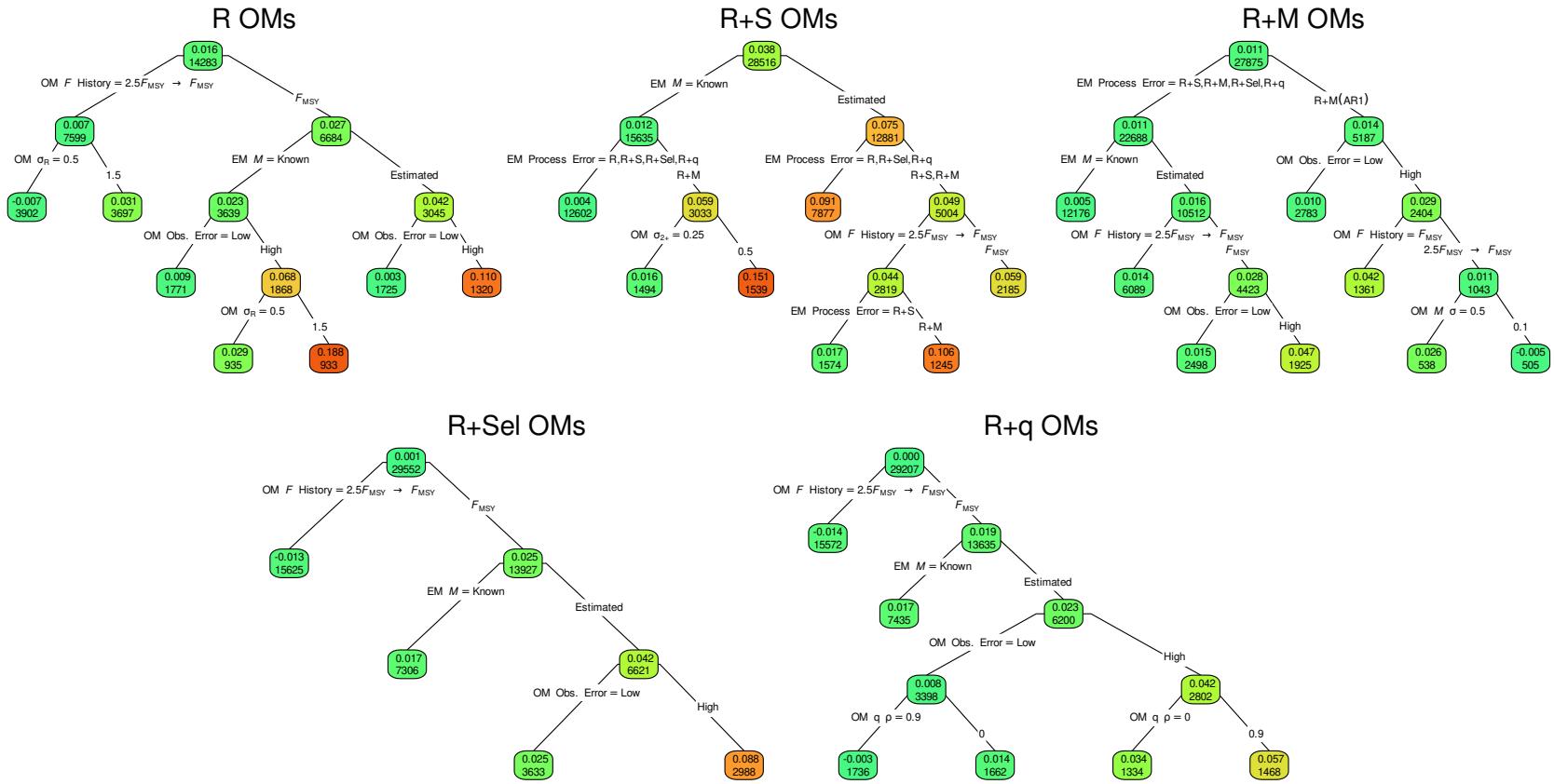


Fig. S9. Regression trees indicating primary factors determining reductions in sums of squares of errors in transformed Mohn's  $\rho$  (Eq. 3) for recruitment for R+S, R+M, R+Sel and R+q OMs. Each node shows the median Mohn's  $\rho$  (top) and number of observations (bottom) for the corresponding subset. Median Mohn's  $\rho$  closer to or further from zero are indicated by more green or red polygons, respectively.

<sub>912</sub> **Referenced Tables**

Table S1. Distinguishing characteristics of the OMs with random effects on recruitment and apparent survival (R, R+S). When observation uncertainty is low, standard deviations for log-normal distributed indices and logistic normal distributed age composition observations are 0.1 and 0.3, respectively, and when it is high, standard deviations are 0.4 and 1.5, respectively. Fishing mortality either changes from  $2.5F_{\text{MSY}}$  to  $F_{\text{MSY}}$  after year 20 (of 40) or is constant at  $F_{\text{MSY}}$  over all years.

Model	$\sigma_R$	$\sigma_{2+}$	Fishing History	Observation Uncertainty
1	0.5		$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
2	1.5		$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
3	0.5	0.25	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
4	1.5	0.25	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
5	0.5	0.50	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
6	1.5	0.50	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
7	0.5		$F_{\text{MSY}}$	Low
8	1.5		$F_{\text{MSY}}$	Low
9	0.5	0.25	$F_{\text{MSY}}$	Low
10	1.5	0.25	$F_{\text{MSY}}$	Low
11	0.5	0.50	$F_{\text{MSY}}$	Low
12	1.5	0.50	$F_{\text{MSY}}$	Low
13	0.5		$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
14	1.5		$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
15	0.5	0.25	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
16	1.5	0.25	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
17	0.5	0.50	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
18	1.5	0.50	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
19	0.5		$F_{\text{MSY}}$	High
20	1.5		$F_{\text{MSY}}$	High
21	0.5	0.25	$F_{\text{MSY}}$	High
22	1.5	0.25	$F_{\text{MSY}}$	High
23	0.5	0.50	$F_{\text{MSY}}$	High
24	1.5	0.50	$F_{\text{MSY}}$	High

Table S2. Distinguishing characteristics of the OMs with random effects on recruitment and natural mortality (R+M). When observation uncertainty is low, standard deviations for log-normal distributed indices and logistic normal distributed age composition observations are 0.1 and 0.3, respectively, and when it is high, standard deviations are 0.4 and 1.5, respectively. Fishing mortality either changes from  $2.5F_{\text{MSY}}$  to  $F_{\text{MSY}}$  after year 20 (of 40) or is constant at  $F_{\text{MSY}}$  over all years. For AR1 process errors,  $\sigma_M$  is defined for the marginal distribution of the processes.

Model	$\sigma_R$	$\sigma_M$	$\rho_M$	Fishing History	Observation Uncertainty
1	0.5	0.1	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
2	0.5	0.5	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
3	0.5	0.1	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
4	0.5	0.5	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
5	0.5	0.1	0.0	$F_{\text{MSY}}$	Low
6	0.5	0.5	0.0	$F_{\text{MSY}}$	Low
7	0.5	0.1	0.9	$F_{\text{MSY}}$	Low
8	0.5	0.5	0.9	$F_{\text{MSY}}$	Low
9	0.5	0.1	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
10	0.5	0.5	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
11	0.5	0.1	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
12	0.5	0.5	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
13	0.5	0.1	0.0	$F_{\text{MSY}}$	High
14	0.5	0.5	0.0	$F_{\text{MSY}}$	High
15	0.5	0.1	0.9	$F_{\text{MSY}}$	High
16	0.5	0.5	0.9	$F_{\text{MSY}}$	High

Table S3. Distinguishing characteristics of the OMs with random effects on recruitment and selectivity (R+Sel). When observation uncertainty is low, standard deviations for log-normal distributed indices and logistic normal distributed age composition observations are 0.1 and 0.3, respectively, and when it is high, standard deviations are 0.4 and 1.5, respectively. Fishing mortality either changes from  $2.5F_{\text{MSY}}$  to  $F_{\text{MSY}}$  after year 20 (of 40) or is constant at  $F_{\text{MSY}}$  over all years. For AR1 process errors,  $\sigma_{\text{Sel}}$  is defined for the marginal distribution of the processes.

Model	$\sigma_R$	$\sigma_{\text{Sel}}$	$\rho_{\text{Sel}}$	Fishing History	Observation Uncertainty
1	0.5	0.1	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
2	0.5	0.5	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
3	0.5	0.1	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
4	0.5	0.5	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
5	0.5	0.1	0.0	$F_{\text{MSY}}$	Low
6	0.5	0.5	0.0	$F_{\text{MSY}}$	Low
7	0.5	0.1	0.9	$F_{\text{MSY}}$	Low
8	0.5	0.5	0.9	$F_{\text{MSY}}$	Low
9	0.5	0.1	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
10	0.5	0.5	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
11	0.5	0.1	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
12	0.5	0.5	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
13	0.5	0.1	0.0	$F_{\text{MSY}}$	High
14	0.5	0.5	0.0	$F_{\text{MSY}}$	High
15	0.5	0.1	0.9	$F_{\text{MSY}}$	High
16	0.5	0.5	0.9	$F_{\text{MSY}}$	High

Table S4. Distinguishing characteristics of the OMs with random effects on recruitment and catchability ( $R+q$ ). When observation uncertainty is low, standard deviations for log-normal distributed indices and logistic normal distributed age composition observations are 0.1 and 0.3, respectively, and when it is high, standard deviations are 0.4 and 1.5, respectively. Fishing mortality either changes from  $2.5F_{\text{MSY}}$  to  $F_{\text{MSY}}$  after year 20 (of 40) or is constant at  $F_{\text{MSY}}$  over all years. For AR1 process errors,  $\sigma_q$  is defined for the marginal distribution of the processes.

Model	$\sigma_R$	$\sigma_q$	$\rho_q$	Fishing History	Observation Uncertainty
1	0.5	0.1	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
2	0.5	0.5	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
3	0.5	0.1	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
4	0.5	0.5	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	Low
5	0.5	0.1	0.0	$F_{\text{MSY}}$	Low
6	0.5	0.5	0.0	$F_{\text{MSY}}$	Low
7	0.5	0.1	0.9	$F_{\text{MSY}}$	Low
8	0.5	0.5	0.9	$F_{\text{MSY}}$	Low
9	0.5	0.1	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
10	0.5	0.5	0.0	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
11	0.5	0.1	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
12	0.5	0.5	0.9	$2.5F_{\text{MSY}} \rightarrow F_{\text{MSY}}$	High
13	0.5	0.1	0.0	$F_{\text{MSY}}$	High
14	0.5	0.5	0.0	$F_{\text{MSY}}$	High
15	0.5	0.1	0.9	$F_{\text{MSY}}$	High
16	0.5	0.5	0.9	$F_{\text{MSY}}$	High

Table S5. Distinguishing characteristics of the EMs and indication (+) of which OM process error sources (R, R+S, R+M, R+Sel, R+q) each EM configuration was fit.

Model	Recruitment model	Median $M$	Process error	R,R+S OM <sub>s</sub>	R+M OM <sub>s</sub>	R+Sel OM <sub>s</sub>	R+q OM <sub>s</sub>
1	Mean recruitment	0.2	R ( $\sigma_{2+} = 0$ )	+			
2	Beverton-Holt	0.2	R ( $\sigma_{2+} = 0$ )	+			
3	Mean recruitment	Estimated	R ( $\sigma_{2+} = 0$ )	+			
4	Beverton-Holt	Estimated	R ( $\sigma_{2+} = 0$ )	+			
5	Mean recruitment	0.2	R+S ( $\sigma_{2+}$ estimated)	+	+	+	+
6	Beverton-Holt	0.2	R+S ( $\sigma_{2+}$ estimated)	+	+	+	+
7	Mean recruitment	Estimated	R+S ( $\sigma_{2+}$ estimated)	+	+	+	+
8	Beverton-Holt	Estimated	R+S ( $\sigma_{2+}$ estimated)	+	+	+	+
9	Mean recruitment	0.2	R+M ( $\rho_M = 0$ )	+	+	+	+
10	Beverton-Holt	0.2	R+M ( $\rho_M = 0$ )	+	+	+	+
11	Mean recruitment	Estimated	R+M ( $\rho_M = 0$ )	+	+	+	+
12	Beverton-Holt	Estimated	R+M ( $\rho_M = 0$ )	+	+	+	+
13	Mean recruitment	0.2	R+Sel ( $\rho_{Sel} = 0$ )	+	+	+	+
14	Beverton-Holt	0.2	R+Sel ( $\rho_{Sel} = 0$ )	+	+	+	+
15	Mean recruitment	Estimated	R+Sel ( $\rho_{Sel} = 0$ )	+	+	+	+
16	Beverton-Holt	Estimated	R+Sel ( $\rho_{Sel} = 0$ )	+	+	+	+
17	Mean recruitment	0.2	R+q ( $\rho_q = 0$ )	+	+	+	+
18	Beverton-Holt	0.2	R+q ( $\rho_q = 0$ )	+	+	+	+
19	Mean recruitment	Estimated	R+q ( $\rho_q = 0$ )	+	+	+	+
20	Beverton-Holt	Estimated	R+q ( $\rho_q = 0$ )	+	+	+	+
21	Mean recruitment	0.2	R+M ( $\rho_M$ estimated)		+		
22	Beverton-Holt	0.2	R+M ( $\rho_M$ estimated)		+		
23	Mean recruitment	Estimated	R+M ( $\rho_M$ estimated)		+		
24	Beverton-Holt	Estimated	R+M ( $\rho_M$ estimated)		+		
25	Mean recruitment	0.2	R+Sel ( $\rho_{Sel}$ estimated)			+	
26	Beverton-Holt	0.2	R+Sel ( $\rho_{Sel}$ estimated)			+	
27	Mean recruitment	Estimated	R+Sel ( $\rho_{Sel}$ estimated)			+	
28	Beverton-Holt	Estimated	R+Sel ( $\rho_{Sel}$ estimated)			+	
29	Mean recruitment	0.2	R+q ( $\rho_q$ estimated)				+
30	Beverton-Holt	0.2	R+q ( $\rho_q$ estimated)				+
31	Mean recruitment	Estimated	R+q ( $\rho_q$ estimated)				+
32	Beverton-Holt	Estimated	R+q ( $\rho_q$ estimated)				+

Table S6. For each OM process error source (columns), percent reduction in deviance for logistic regression models fit to indicators of convergence (maximum absolute gradient  $< 10^{-6}$ ) with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM Process Error	30.40	0.45	17.57	16.04	24.03
EM $M$ Assumption	2.38	24.11	4.42	1.02	2.66
EM SR Assumption	1.80	0.32	0.96	3.38	2.13
OM Obs. Error	0.12	0.77	0.33	1.76	0.28
OM $F$ History	3.51	6.33	2.36	5.86	5.30
OM $\sigma_R$	<0.01	<0.01	—	—	—
OM $\sigma_{2+}$	—	<0.01	—	—	—
OM $\sigma_M$	—	—	0.39	—	—
OM $\rho_M$	—	—	0.09	—	—
OM $\sigma_{\text{Sel}}$	—	—	—	1.08	—
OM $\rho_{\text{Sel}}$	—	—	—	0.01	—
OM $\sigma_q$	—	—	—	—	0.06
OM $\rho_q$	—	—	—	—	<0.01
All factors	43.69	35.72	29.33	34.57	40.69
+ All Two Way	50.53	42.99	43.91	45.93	48.62
+ All Three Way	52.30	48.41	46.81	47.71	50.40

Table S7. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to errors in estimation measured by Eq. 3 for the terminal year fully-selected fishing mortality with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	2.26	1.33	1.26	2.93	3.26
EM SR assumption	0.11	0.07	0.08	0.07	0.09
EM Process Error	0.46	4.18	0.38	0.13	1.02
OM Obs. Error	1.61	0.06	0.86	0.41	<0.01
OM $F$ History	2.49	3.23	1.42	3.22	4.55
OM $\sigma_R$	0.02	0.02	—	—	—
OM $\sigma_{2+}$	—	0.87	—	—	—
OM $\sigma_M$	—	—	0.16	—	—
OM $\rho_M$	—	—	0.01	—	—
OM $\sigma_{\text{Sel}}$	—	—	—	0.24	—
OM $\rho_{\text{Sel}}$	—	—	—	0.05	—
OM $\sigma_q$	—	—	—	—	1.03
OM $\rho_q$	—	—	—	—	0.05
All factors	7.42	9.96	4.37	7.26	10.43
+ All Two Way	17.63	25.76	10.94	13.88	22.07
+ All Three Way	22.97	37.03	14.74	17.32	30.74

Table S8. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to errors in estimation measured by Eq. 3 for the terminal year recruitment with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	1.96	0.40	0.69	3.52	3.03
EM SR assumption	0.06	0.02	0.05	0.02	0.05
EM Process Error	0.39	4.74	0.41	0.12	1.16
OM Obs. Error	1.47	0.08	0.64	0.18	<0.01
OM $F$ History	2.54	2.66	1.11	4.18	5.06
OM $\sigma_R$	0.03	0.01	—	—	—
OM $\sigma_{2+}$	—	1.05	—	—	—
OM $\sigma_M$	—	—	0.36	—	—
OM $\rho_M$	—	—	0.02	—	—
OM $\sigma_{\text{Sel}}$	—	—	—	0.23	—
OM $\rho_{\text{Sel}}$	—	—	—	0.06	—
OM $\sigma_q$	—	—	—	—	1.09
OM $\rho_q$	—	—	—	—	0.06
All factors	6.90	9.01	3.43	8.58	10.90
+ All Two Way	16.48	24.64	9.73	15.76	22.75
+ All Three Way	21.46	35.60	13.56	19.07	31.15

<sub>913</sub> **Further Results**

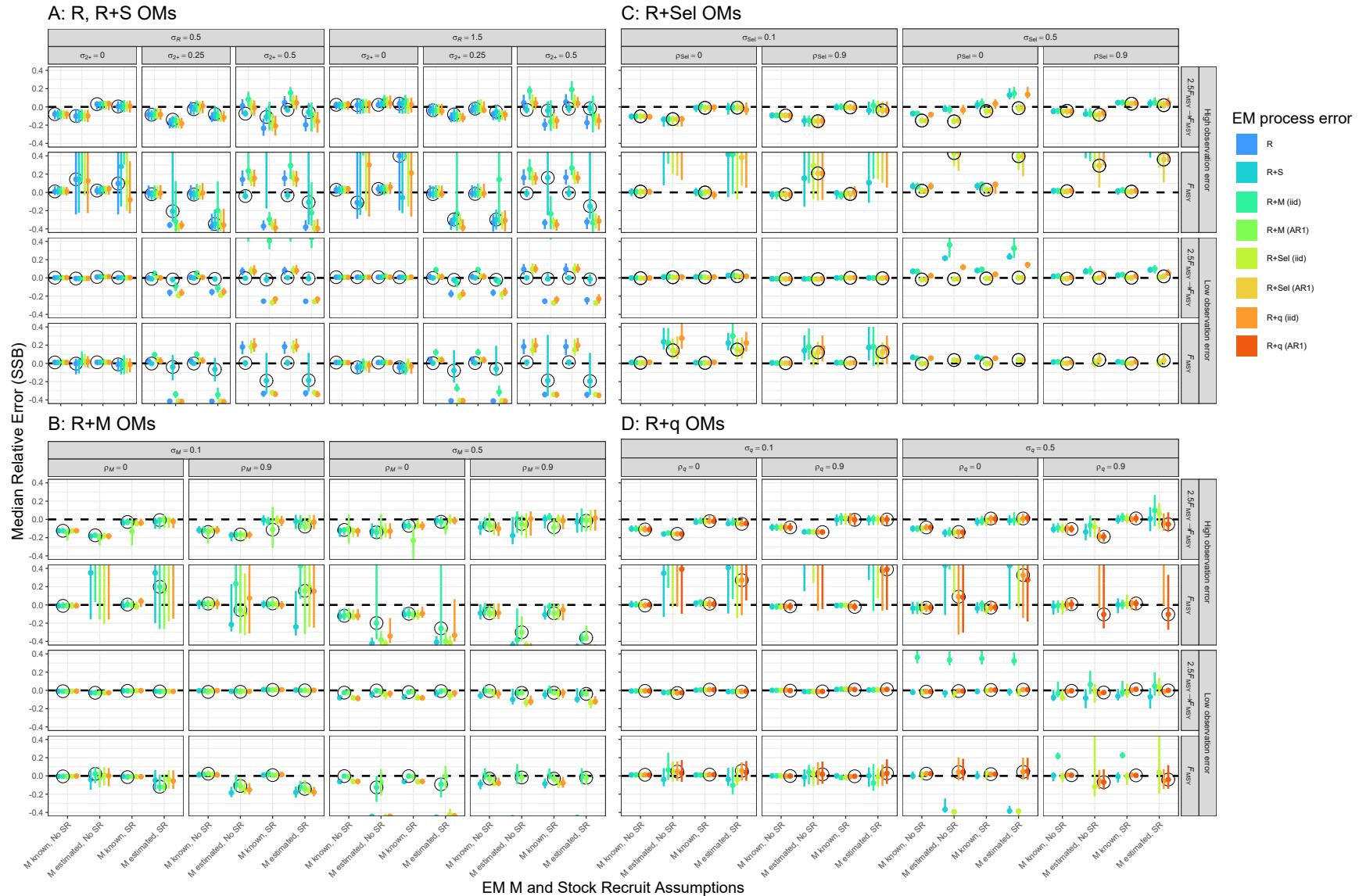


Fig. S10. Median relative error of terminal year SSB for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

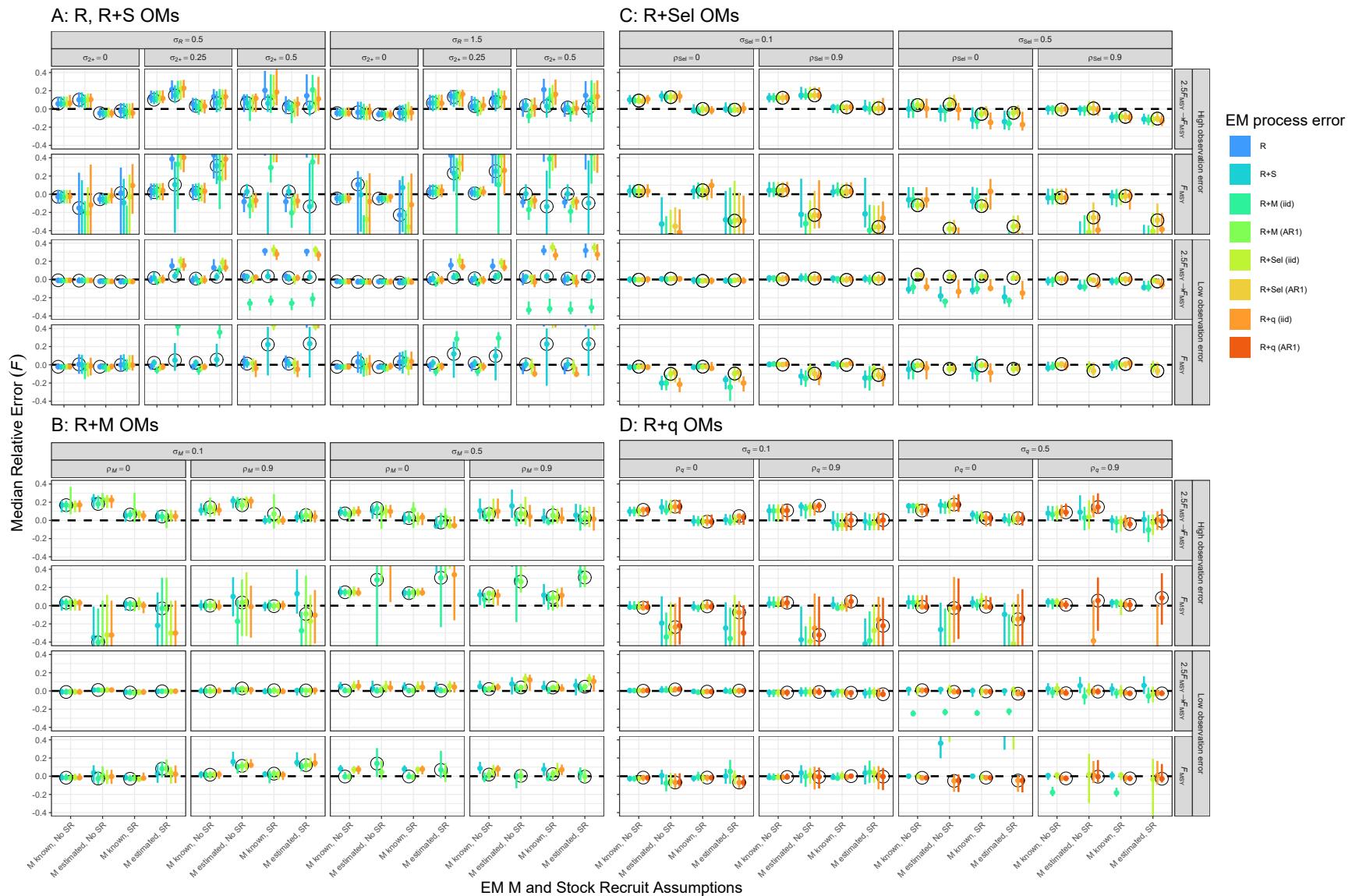


Fig. S11. Median relative error of terminal year fully-selected fishing mortality for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

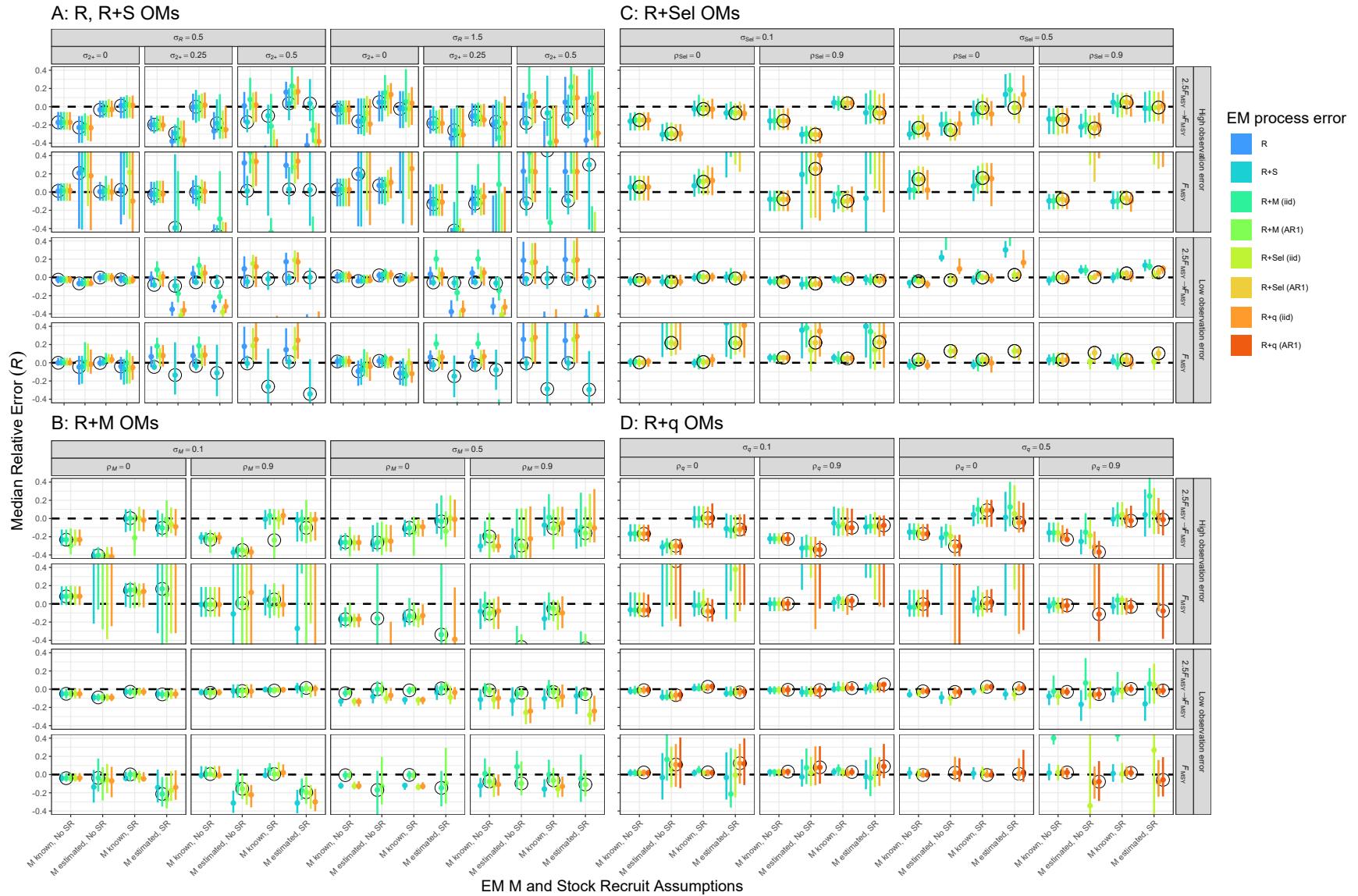


Fig. S12. Median relative error of terminal year recruitment for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

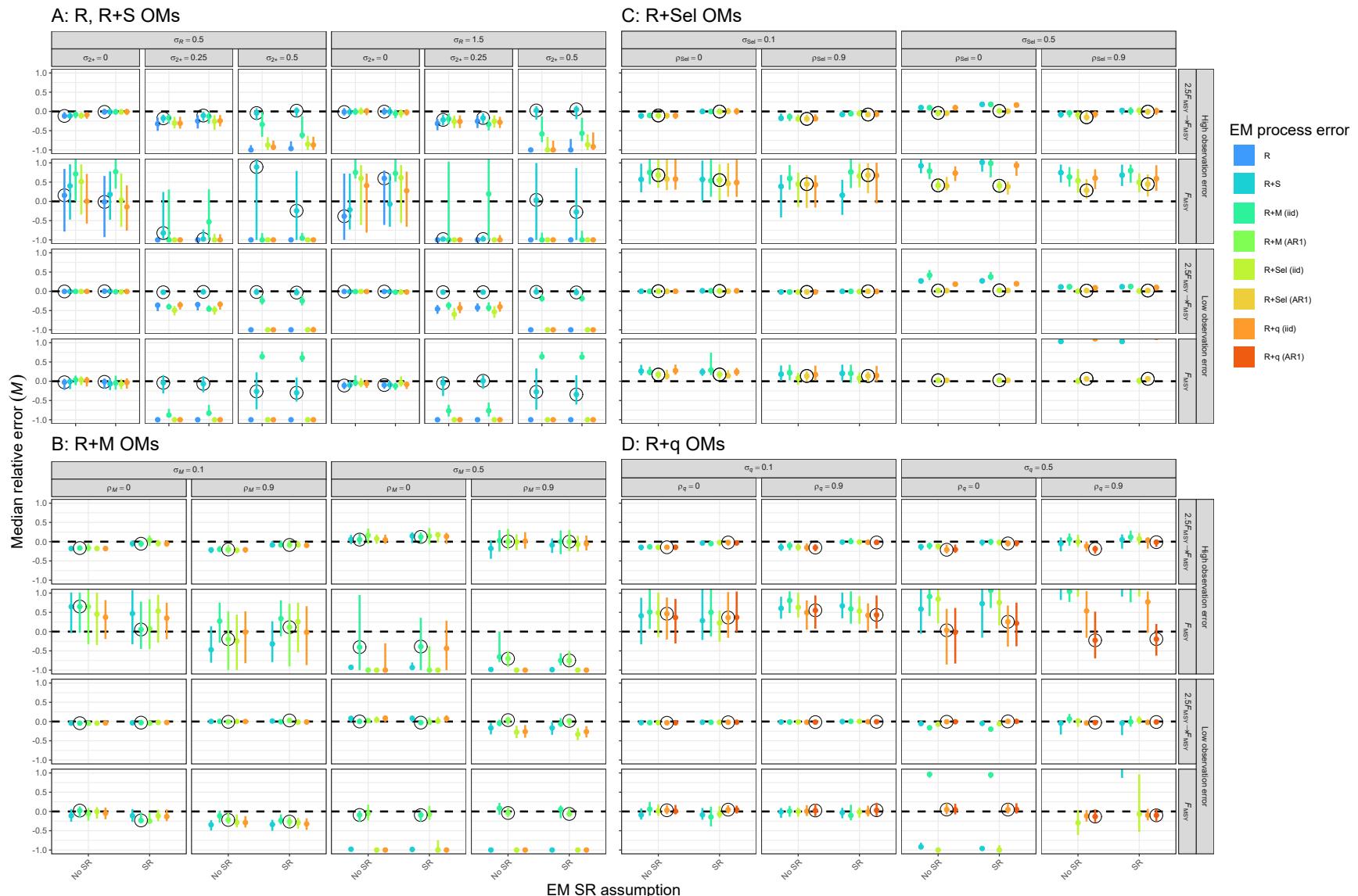


Fig. S13. Median relative error of median natural mortality for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

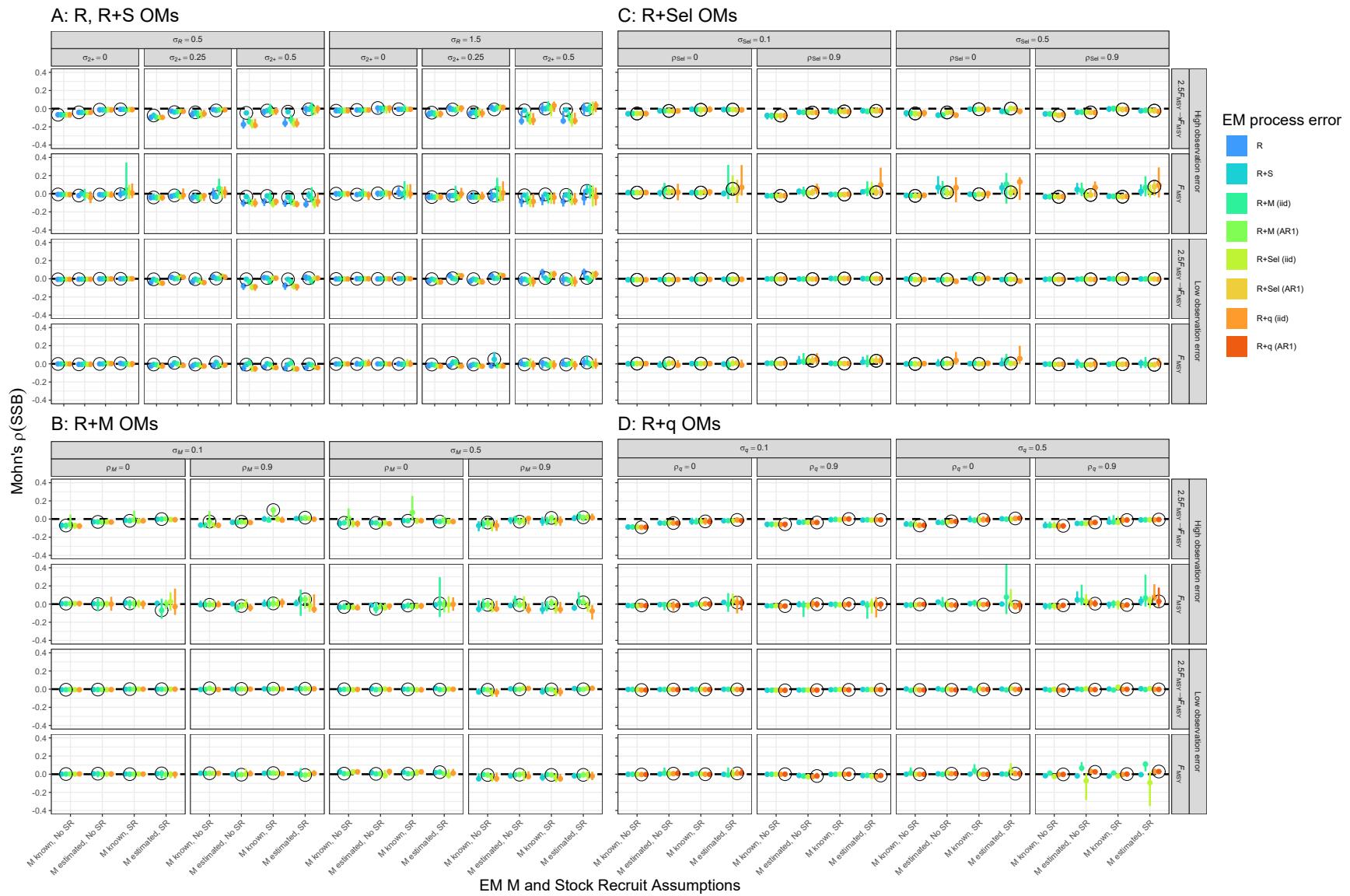


Fig. S14. Median Mohn's  $\rho$  for SSB for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

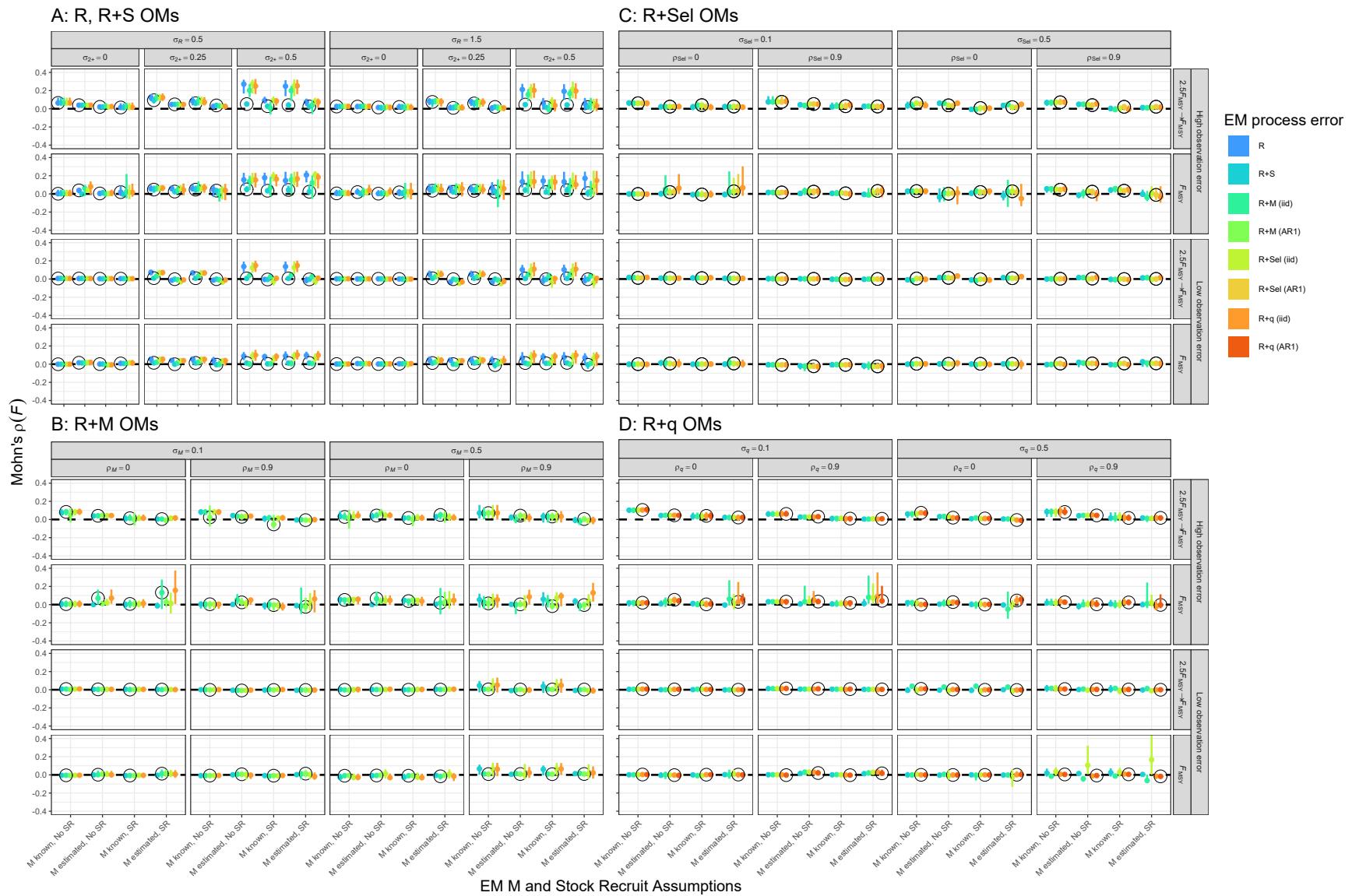


Fig. S15. Median Mohn's  $\rho$  of fishing mortality averaged over all age classes for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.



Fig. S16. Median Mohn's  $\rho$  of recruitment for EMs fitted to data sets simulated with alternative process error sources: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.



Fig. S17. Probability of EMs providing Hessian-based standard errors with alternative process error (colored points and lines), and median natural mortality (estimated or known) and Beverton-Holt SRR (estimated or not; along x-axis) assumptions when fitted to OMs that have R and R+S (A), R+Sel (B), R+M (C), or R+q (D) process error sources. Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

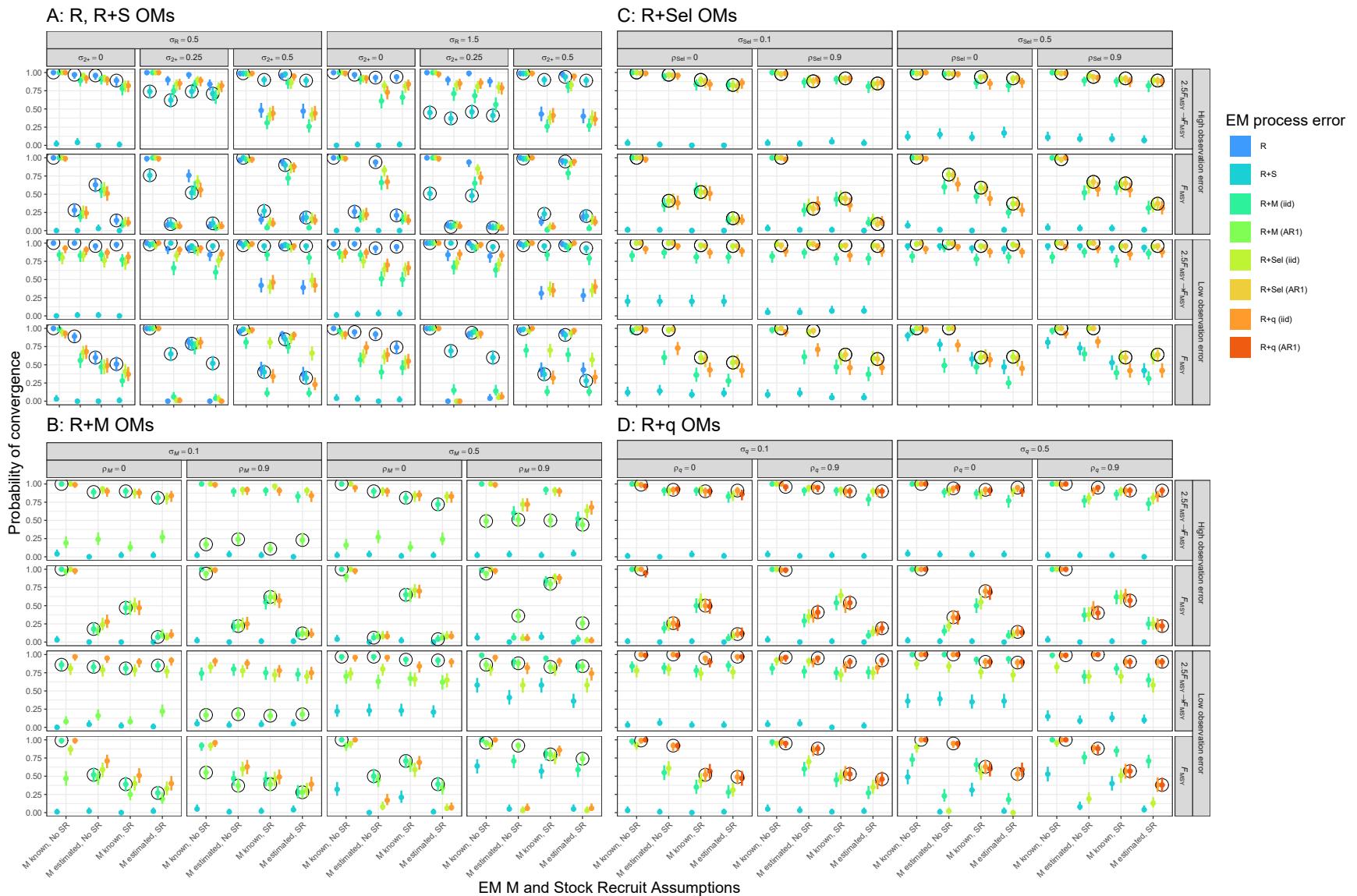


Fig. S18. Probability of EMs providing maximum absolute values of gradients less than  $10^{-6}$  with alternative process error (colored points and lines), and median natural mortality (estimated or known) and Beverton-Holt SRR (estimated or not; along x-axis) assumptions when fitted to OMs that have R and R+S (A), R+Sel (B), R+M (C), or R+q (D) process error sources. Circled values indicate results where the EM process error structure matches that of the OM and vertical lines represent 95% confidence intervals.

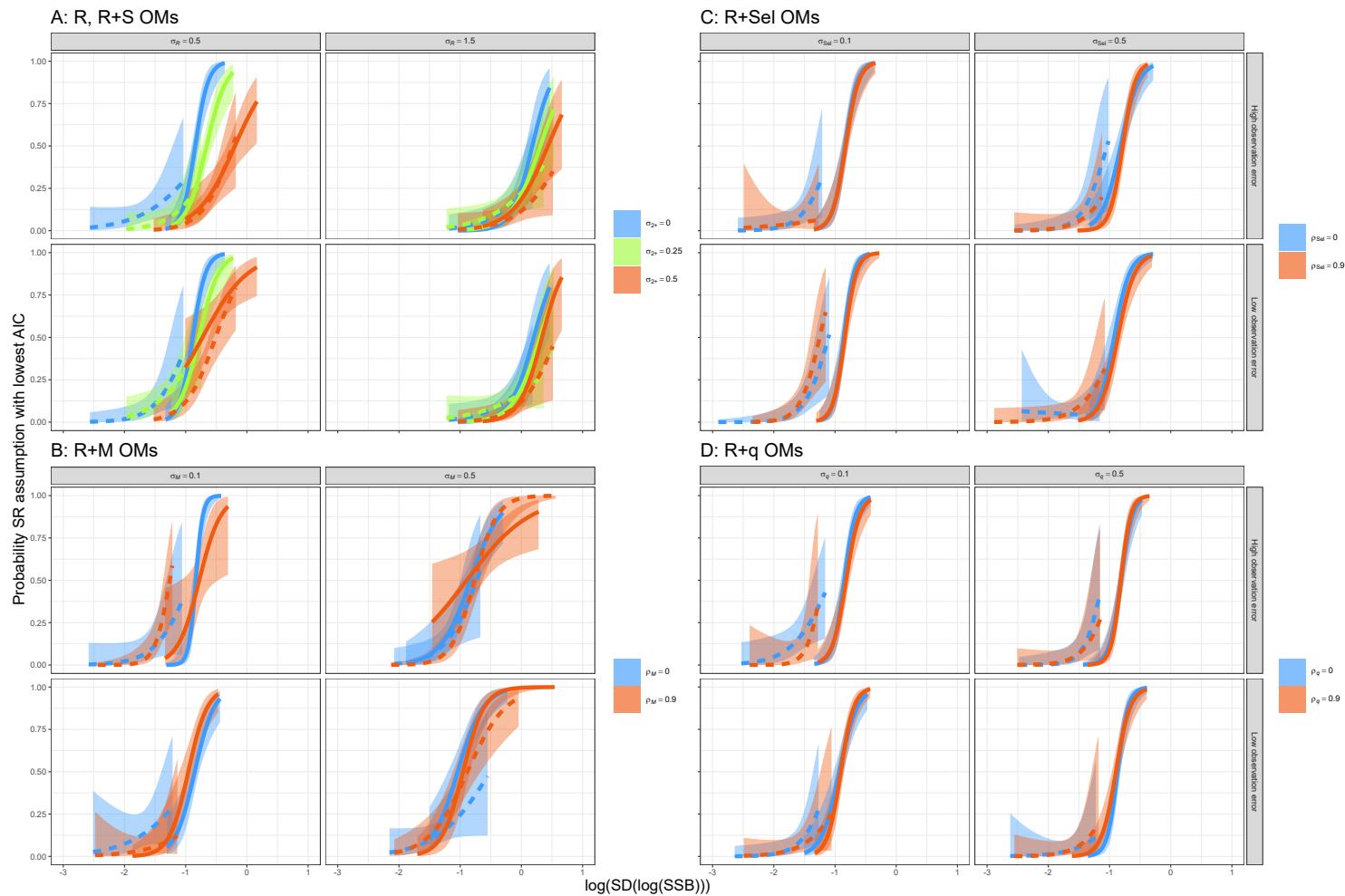


Fig. S19. Probability of lowest AIC from logistic regression on the log-standard deviation of the true  $\log(\text{SSB})$  in each simulation for EM with Beverton-Holt SRRs, rather than the otherwise equivalent EM without the SRR. Results are conditional on median M is known in the EM and alternative assumptions EMs having the correct process error structure: R and R+S (A), R+Sel (B), R+M (C), or R+q (D), and median M is assumed known in the EM. Solid and dashed lines are for OMs with and without temporal contrast in fishing pressure, respectively, and polygons represent 95% confidence intervals. Range of results indicates the range of log-standard deviation of  $\log(\text{SSB})$  for simulations of the particular OM.

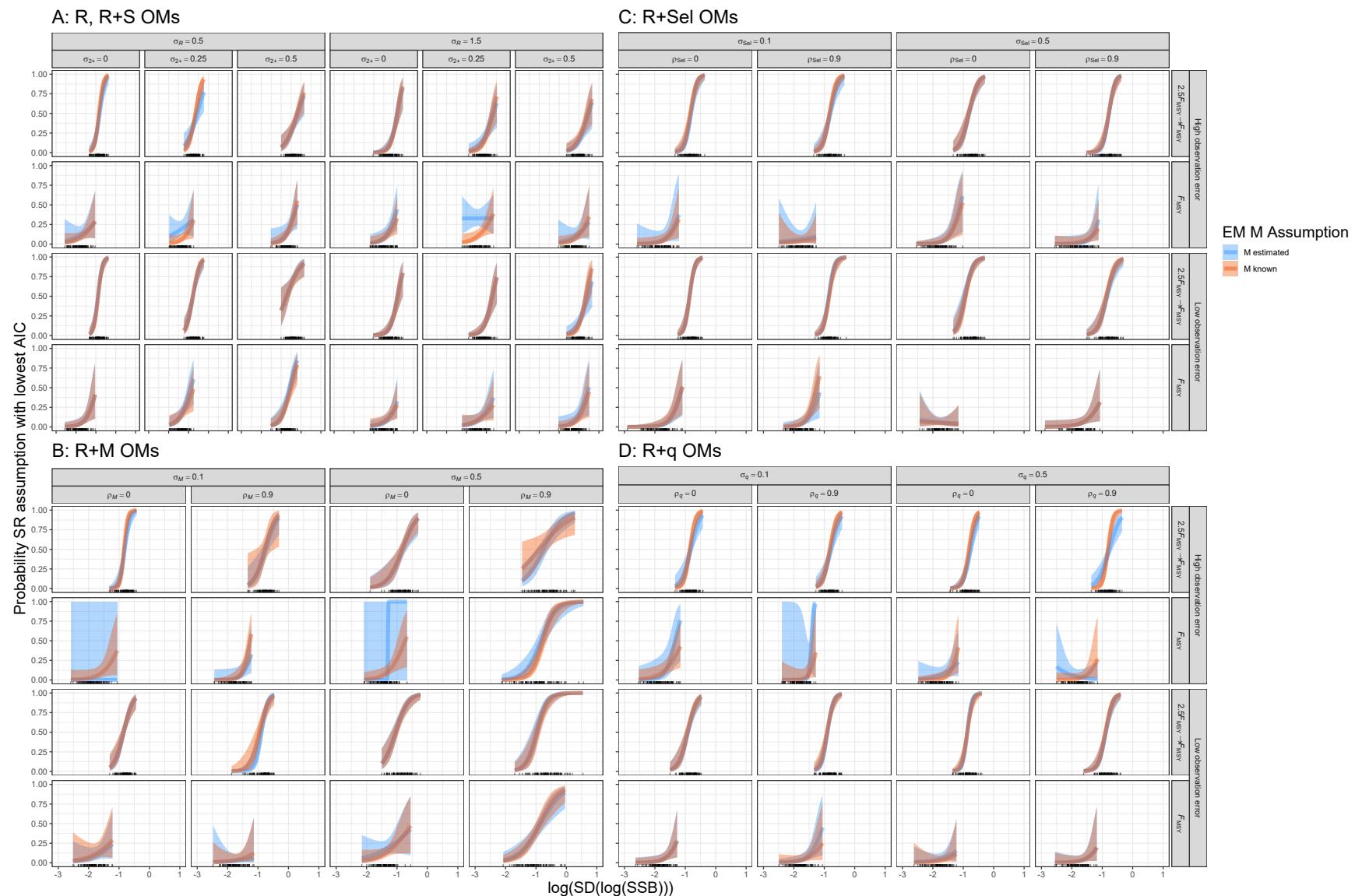


Fig. S20. Estimated probability of lowest AIC from logistic regression on the log-standard deviation of the true  $\log(\text{SSB})$  in each simulation for EM with Beverton-Holt SRRs, rather than the otherwise equivalent EM without the SRR. Results are conditional on alternative assumptions for median natural mortality (estimated or known) and on EMs having the correct process error structure: R and R+S (A), R+Sel (B), R+M (C), or R+q (D). Rug along x-axis denotes  $SD(\log(\text{SSB}))$  values for each simulation and polygons represent 95% confidence intervals.

Table S9. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to transformed Mohn's  $\rho$  values for each simulation (Eq. 3) for fishing mortality averaged over all age classes with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	0.06	0.09	0.01	0.12	0.01
EM SR assumption	0.01	<0.01	0.01	0.02	0.01
EM Process Error	0.03	0.07	0.02	0.06	0.03
OM Obs. Error	0.16	0.10	0.05	0.02	0.07
OM $F$ History	0.07	0.02	0.03	0.24	0.03
OM $\sigma_R$	<0.01	0.01	—	—	—
OM $\sigma_{2+}$	—	0.09	—	—	—
OM $\sigma_M$	—	—	<0.01	—	—
OM $\rho_M$	—	—	<0.01	—	—
OM $\sigma_{Sel}$	—	—	—	0.01	—
OM $\rho_{Sel}$	—	—	—	<0.01	—
OM $\sigma_q$	—	—	—	—	<0.01
OM $\rho_q$	—	—	—	—	0.01
All factors	0.32	0.38	0.12	0.48	0.15
+ All Two Way	0.65	0.67	0.30	0.95	0.43
+ All Three Way	1.18	1.11	0.63	1.34	0.90

Table S10. For each OM process error source (columns), percent reduction in deviance for linear regression models fit to transformed Mohn's  $\rho$  values for each simulation (Eq. 3) for recruitment with each OM and EM factor (rows) included individually, combined, and with second and third order interactions.

Factor	R	R+S	R+M	R+Sel	R+q
EM $M$ Assumption	0.86	0.56	0.16	1.00	1.27
EM SR assumption	<0.01	0.02	0.01	0.01	0.01
EM Process Error	0.01	0.59	0.18	0.07	0.04
OM Obs. Error	0.34	0.01	0.08	0.24	0.27
OM $F$ History	0.91	0.22	0.06	1.20	1.67
OM $\sigma_R$	<0.01	0.14	—	—	—
OM $\sigma_{2+}$	—	0.11	—	—	—
OM $\sigma_M$	—	—	0.01	—	—
OM $\rho_M$	—	—	<0.01	—	—
OM $\sigma_{Sel}$	—	—	—	0.01	—
OM $\rho_{Sel}$	—	—	—	0.01	—
OM $\sigma_q$	—	—	—	—	0.01
OM $\rho_q$	—	—	—	—	0.01
All factors	2.28	1.74	0.51	2.66	3.51
+ All Two Way	4.20	2.74	1.08	5.08	6.51
+ All Three Way	4.83	3.79	1.79	6.03	7.82