- How reliable are inferences from state-space age-structured assessment models?
- Timothy J. Miller¹, Britten, Brooks, Fay, Legault, Stock,
- ⁴ ¹corresponding author: timothy.j.miller@noaa.gov, Northeast Fisheries Science Center,
- 5 Woods Hole Laboratory, 166 Water Street, Woods Hole, MA 02543 USA

1

- 7 Abstract
- 8 Keywords

₉ 1 Introduction

- 10 Application of state-space models in fisheries stock assessment and management has ex-
- panded dramatically within ICES, Canada and the Northeast US (Nielsen and Berg, 2014;
- ¹² Cadigan, 2016; Stock and Miller, 2021).
- Much is known about the reliability of state-space models that are linear or Gaussian (Ae-
- berhard et al., 2018), but applications in fisheries management are nonlinear and typically
- include multiple types of observations with varying distributional assumptions. We know
- relatively little about the statistical reliability of such models. Also, there is a wide range
- of potential random effects structures in assessment models and we know little about the
- ability of information criteria to distinguish among such alternative structures.
- But those studies focus primarily on Gaussian linear models. review literature on reliability
- of hidden/latent process models. Primarily in other fields.

2 Methods

- Used the WHAM package (Stock and Miller, 2021, commit 77bbd94) (Miller and Stock
- 23 2020). This packages has also been used to configure operating and estimating models for
- 24 closed loop simulations evaluating index-based assessment methods (Legault et al., In press).
- ²⁵ We completed a simulation study with a number of operating models that can be categorized
- based on where random effects are assumed: abundance at age, natural mortality, fleet
- 27 selectivity, or index catchability. For each operating model assumptions about variance of
- process errors and observations are required and the values we used were based on a review
- of the range of estimates from recent applications of WHAM in management of stocks of
- haddock, butterfish, and American plaice in the NE US.
- We simulated 100 data sets for each operating model. For each simulated data from each

- operating model we fit a set of estimating models.
- 33 Y estimating models fit to each

$_{34}$ 2.1 Operating models

- 35 common to all:
- ages = 1 to 10+, M maturity
- marginal standard deviations for random effects are defined in tables of operating models.

38 2.1.1 Population

- There are 10 age classes: ages 1 to 10+.
- Spawning was assumed to occur 1/4 of the way through the year.
- Natural mortality rate was assumed 0.2 when it was constant and the mean of the time series
- process for operating models with M random effects. maturity a50 = 2.89, slope = 0.88
- Weight at age was generated with a LVB growth

$$L_a = L_\infty \left(1 - e^{-k(a - t_0)} \right)$$

where $t_0 = 0$, $L_{\infty} = 85$, and k = 0.3, and a L-W relationship such that

$$W_a = \theta_1 L_a^{\theta_2}$$

- where $\theta_1 = e^{-12.1}$ and $\theta_2 = 3.2$.
- We assumed a Beverton-Holt stock recruit function with constant pre-recruit mortality pa-
- 47 rameters for all operating models. All post-recruit productivity components are constant in
- the NAA and survey catchability process error operating models. Therefore steepness and

unfished recruitment are also constant over the time period for those operating models (Miller and Brooks 2021). We specified unfished recruitment = $R_0 = e^{10}$ and $F_{\rm MSY} = F_{40} = 0.348$ equated to a steepness of 0.69 and $\alpha = 0.60$ and $\beta = 2.4 \times 10^{-5}$ for the

$$N_{1,y} = \frac{\alpha SSB_{y-1}}{1 + \beta SSB_{y-1}}$$

Beverton-Holt parameterization.

The magnitude of the overfishing assumptions is based on average estimates of overfishing for NE groundfish stocks from Wiedenmann et al. (20XX). Legault et al. (2023) also used similar approaches to defining fishing mortality histories for operating models. Initial population was configured at the equilibrium distribution fishing at either $F=2.5 \times$ F_{MSY} or $F=F_{\mathrm{MSY}}$ for the two alternative fishing histories. That is for a deterministic model, the age composition would not change over time when the fishing mortality was constant at the respective level. 59 For operating models with time-varying random effects for M, steepness is not constant, but 60

we used the same alpha and beta parameters as other operating models this equates to a 61 steepness and R0 at the mean of the time series process for M. For operating models with time-varying random effects for fishery selectivity, Fmsy is also not constant however we use the same F history as other operating models which corresponds to Fmsy at the mean selectivity parameters.

2.1.2**Fleets**

We assumed a single fleet operating year round for catch observations with logistic selectivity for the fleet with $a_{50} = 5$ and slope = 1. This selectivity is was used to define $F_{\rm MSY}$ for the Beverton-Holt stock recruitment parameters above. We assumed a logistic-normal distribution for the age-composition observations for the fleet.

71 2.1.3 Fishing histories

- All operating models assumed one of two different fishing histories. One: Fishing mortality
- is equal to Fmsy (0.348) for the whole 40 year period. Two: Fishing mortality is 2.5 times
- Fmsy for the first 20 years then changes to Fmsy for the last 20 years.

75 2.1.4 Indices

- 76 Two time series of surveys are assumed and observed in numbers rather than biomass for
- the entire 40 year period with one occurring in the spring (0.25 way through the year) and
- one in the fall (0.75 way through the year). Actually we have it currently configured that
- both occur 0.5 way through the year. Catchability of both surveys are assumed to be 0.1.
- We assumed logistic selectivity for both indices with $a_{50} = 5$ and slope = 1. We assumed a
- 81 logistic-normal distribution for the age-composition observations.

82 2.1.5 Observation Uncertainty

- Standard deviation for log-aggregate catch was 0.1. There were two levels of observation error
- variance for indices and age composition for both indices and fleet catch. A low uncertainty
- 85 specification assumed standard deviation of both series of log-aggregate index observations
- was 0.1 and the standard deviation of the logistic-normal for age composition observations
- was 0.3 In the high uncertainty specification the standard deviation for log-aggregate indices
- was 0.4 and that for the age composition observations was 1.5.

2.1.6 Operating models with random effects on numbers at age

- ⁹⁰ 24 operating models, 16 Sel re operating models and 16 q re operating models. Table of
- 91 process error assumptions

92 2.1.7 Operating models with random effects on natural mortality

- 93 16 operating models Table of process error assumptions
- NOTE: inv_trans_rho function in set_M.R is mis-defined. Will affect correlation parame-
- 95 ters assigned in operating models?

⁹⁶ 2.1.8 Operating models with random effects on fleet selectivity

97 16 operating models Table of process error assumptions

⁹⁸ 2.1.9 Operating models with random effects on index catchability

99 16 operating models Table of process error assumptions

2.2 Estimating models

- 101 32 estimating models Table of estimating models
- 1-20 fit to each NAA RE operating model 5-24 fit to each M RE operating model 5-20,25-28
- to each sel RE operating model 5-20, 29-32 to each q RE operating model
- 104 SR estimation or not
- 105 Make plot of S-R curve, Fmsy = F40 Initial values for BH parameters are the true values.
- 106 Initial values for mean R model = true R0.
- 107 M estimation or not
- NAA re Random effects on Recruitment only or random effects on recruitment and transi-
- tions among older numbers at age.
- 110 M_re Random effects on Recruitment only, M constant across age.
- sel re Random effects on Recruitment only, fleet logistic selectivity RE model?

- 112 q_re Random effects on Recruitment only, one survey catchability RE model?
- Simulations were all carried out on the University of Massachussetts Green High-Performance
- 114 Computing Cluster. Code for completing the simulations and summarization of results can be
- found at github.com/timjmiller/SSRTWG/Project_0. We used the wham package version
- 1.1.X.X (commit XXXXX).

117 3 Results

- Do each of these by type of operating model (Naa, M, sel, q) Convergence performance
- 119 AIC performance
- SR estimation? M estimation?
- 121 Bias, Mean Square error
- 122 Certain basic parameters (stock-recruit pars, M, variance parameters) SSB, F, R

- 3.1 Numbers at age operating models
- $^{124}\,$ 3.1.1 Estimating models include alternative random effects options: NAA, M, $^{125}\,$ sel, q

Table 1. NAA operating models, estimating models all assume a B-H stock recruit relationship and M is fixed at the true value.

σ_R	σ_N	F-history	Obs Error	R only	NAA	M	Sel	 q
0.5		H-MSY	L	96	0	0	0	4
1.5		H-MSY	${ m L}$	96	0	0	0	4
0.5	0.25	H-MSY	${ m L}$	0	100	0	0	0
1.5	0.25	H-MSY	${ m L}$	0	100	0	0	0
0.5	0.50	H-MSY	${ m L}$	0	96	4	0	0
1.5	0.50	H-MSY	${ m L}$	0	100	0	0	0
0.5		MSY	${ m L}$	97	0	0	0	3
1.5		MSY	${ m L}$	96	0	0	0	4
0.5	0.25	MSY	${ m L}$	0	99	1	0	0
1.5	0.25	MSY	${ m L}$	0	99	1	0	0
0.5	0.50	MSY	${ m L}$	0	100	0	0	0
1.5	0.50	MSY	${ m L}$	0	99	1	0	0
0.5		H-MSY	Н	94	0	0	0	6
1.5		H-MSY	Н	94	0	0	0	6
0.5	0.25	H-MSY	Н	46	50	0	0	4
1.5	0.25	H-MSY	Н	65	30	0	0	5
0.5	0.50	H-MSY	Н	1	99	0	0	0
1.5	0.50	H-MSY	Н	0	98	0	0	2
0.5		MSY	Н	94	0	0	0	6
1.5		MSY	Н	95	0	0	0	5
0.5	0.25	MSY	Н	45	52	0	0	3
1.5	0.25	MSY	Н	63	28	0	0	9
0.5	0.50	MSY	Н	0	100	0	0	0
1.5	0.50	MSY	Н	0	98	1	0	1

Table 2. NAA operating models, estimating models all assume a B-H stock recruit relationship and M is estimated.

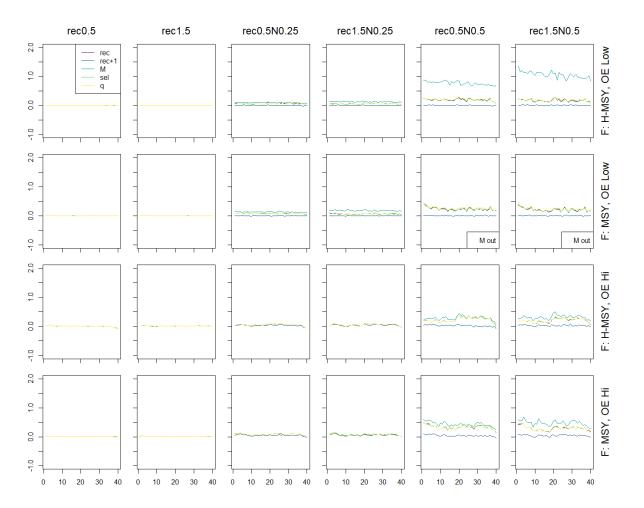
σ_R	σ_N	F-history	Obs Error	R only	NAA	M	Sel	q
0.5		H-MSY	L	96	0	0	0	4
1.5		H-MSY	${ m L}$	96	0	0	0	4
0.5	0.25	H-MSY	${f L}$	0	98	1	1	0
1.5	0.25	H-MSY	${f L}$	0	100	0	0	0
0.5	0.50	H-MSY	${ m L}$	0	97	3	0	0
1.5	0.50	H-MSY	${ m L}$	0	96	2	2	0
0.5		MSY	${f L}$	95	1	0	0	4
1.5		MSY	${ m L}$	93	3	0	0	4
0.5	0.25	MSY	${f L}$	0	94	1	5	0
1.5	0.25	MSY	${f L}$	0	85	5	3	0
0.5	0.50	MSY	${f L}$	0	91	7	1	1
1.5	0.50	MSY	${ m L}$	0	77	20	0	1
0.5		H-MSY	Н	94	0	0	0	6
1.5		H-MSY	Н	96	0	0	0	4
0.5	0.25	H-MSY	Н	50	47	0	0	3
1.5	0.25	H-MSY	Н	68	28	0	0	4
0.5	0.50	H-MSY	Н	1	99	0	0	0
1.5	0.50	H-MSY	Н	0	97	1	0	2
0.5		MSY	Н	78	15	0	1	4
1.5		MSY	Н	69	21	0	2	6
0.5	0.25	MSY	Н	45	41	0	0	6
1.5	0.25	MSY	Н	37	44	1	0	8
0.5	0.50	MSY	Н	3	79	0	0	11
1.5	0.50	MSY	Н	4	69	7	1	13

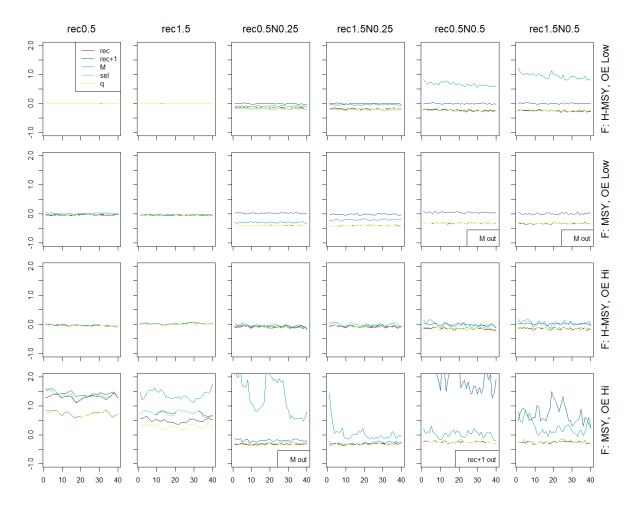
Table 3. NAA operating models, estimating models all estimate a mean recruitment and M is fixed at the true value.

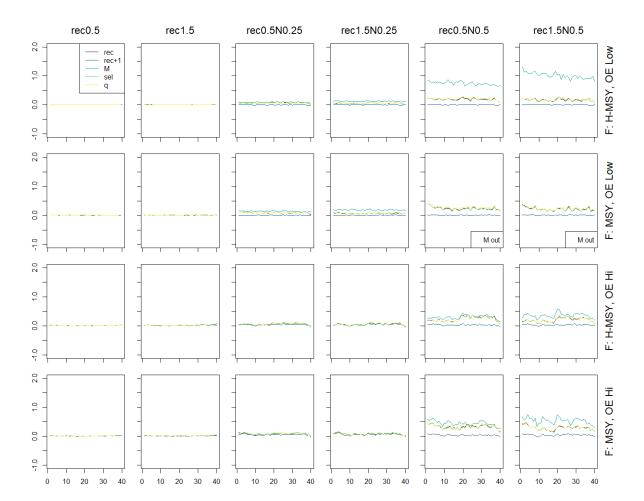
σ_R	σ_N	F-history	Obs Error	R only	NAA	Μ	Sel	q
0.5		H-MSY	L	96	0	0	0	4
1.5		H-MSY	${ m L}$	96	0	0	0	4
0.5	0.25	H-MSY	${ m L}$	0	99	0	1	0
1.5	0.25	H-MSY	${ m L}$	0	100	0	0	0
0.5	0.50	H-MSY	${ m L}$	0	99	1	0	0
1.5	0.50	H-MSY	${ m L}$	0	97	3	0	0
0.5		MSY	${ m L}$	97	0	0	0	3
1.5		MSY	${ m L}$	96	0	0	0	4
0.5	0.25	MSY	${ m L}$	0	100	0	0	0
1.5	0.25	MSY	${ m L}$	0	100	0	0	0
0.5	0.50	MSY	${ m L}$	0	100	0	0	0
1.5	0.50	MSY	${ m L}$	0	100	0	0	0
0.5		H-MSY	Н	94	0	0	0	6
1.5		H-MSY	Н	94	0	0	0	6
0.5	0.25	H-MSY	Н	48	48	0	0	4
1.5	0.25	H-MSY	Н	65	30	0	0	5
0.5	0.50	H-MSY	Н	0	99	1	0	0
1.5	0.50	H-MSY	Н	0	99	0	0	1
0.5		MSY	Н	94	0	0	0	6
1.5		MSY	Н	95	0	0	0	5
0.5	0.25	MSY	Н	46	51	0	0	3
1.5	0.25	MSY	Н	63	28	0	0	9
0.5	0.50	MSY	Н	0	100	0	0	0
1.5	0.50	MSY	Н	0	98	1	0	1

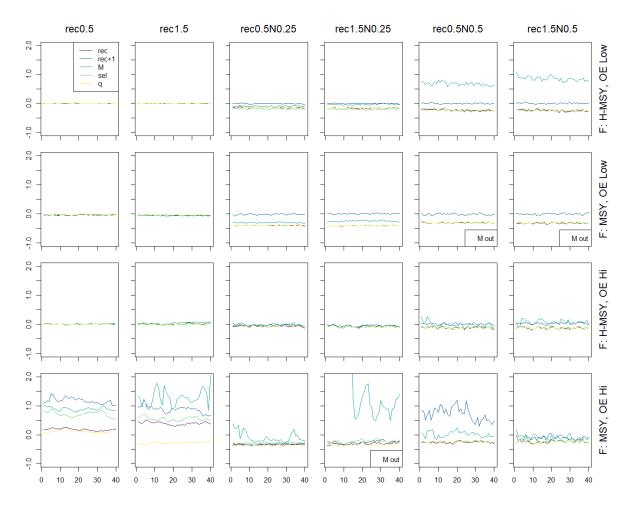
Table 4. NAA operating models, estimating models all estimate a mean recruitment and \mathcal{M} estimated.

σ_R	σ_N	F-history	Obs Error	R only	NAA	Μ	Sel	q
0.5		H-MSY	L	96	0	0	0	4
1.5		H-MSY	${ m L}$	96	0	0	0	4
0.5	0.25	H-MSY	${ m L}$	0	99	0	1	0
1.5	0.25	H-MSY	${ m L}$	0	100	0	0	0
0.5	0.50	H-MSY	${ m L}$	0	99	1	0	0
1.5	0.50	H-MSY	${ m L}$	0	97	3	0	0
0.5		MSY	${ m L}$	97	0	0	0	3
1.5		MSY	${ m L}$	96	0	0	0	4
0.5	0.25	MSY	${ m L}$	0	100	0	0	0
1.5	0.25	MSY	${ m L}$	0	100	0	0	0
0.5	0.50	MSY	${ m L}$	0	100	0	0	0
1.5	0.50	MSY	${ m L}$	0	100	0	0	0
0.5		H-MSY	Н	94	0	0	0	6
1.5		H-MSY	Н	94	0	0	0	6
0.5	0.25	H-MSY	Н	48	48	0	0	4
1.5	0.25	H-MSY	Н	65	30	0	0	5
0.5	0.50	H-MSY	Н	0	99	1	0	0
1.5	0.50	H-MSY	Н	0	99	0	0	1
0.5		MSY	Н	94	0	0	0	6
1.5		MSY	Н	95	0	0	0	5
0.5	0.25	MSY	Н	46	51	0	0	3
1.5	0.25	MSY	Н	63	28	0	0	9
0.5	0.50	MSY	Н	0	100	0	0	0
1.5	0.50	MSY	Н	0	98	1	0	1









126 3.1.2 Estimating models include NAA random effects and estimation assumes
127 mean R or BH SR

Table 5. Operating models and estimation models all assume RE on recruitment only, estimating models assume mean recruitment or a B-H stock recruit relationship and M is fixed at the true value.

σ_R	σ_N	F-history	Obs Error	R only	ВН
0.5		H-MSY	L	46	54
1.5		H-MSY	${ m L}$	82	18
0.5		MSY	${ m L}$	71	29
1.5		MSY	${ m L}$	85	15
0.5		H-MSY	Н	51	49
1.5		H-MSY	Н	82	18
0.5		MSY	Н	72	28
1.5		MSY	Н	86	14

Table 6. Operating models and estimation models all assume RE on recruitment only, estimating models assume mean recruitment or a B-H stock recruit relationship and M is estimated.

σ_R	σ_N	F-history	Obs Error	R only	ВН
0.5		H-MSY	L	45	55
1.5		H-MSY	${ m L}$	82	18
0.5		MSY	${ m L}$	70	30
1.5		MSY	${ m L}$	87	13
0.5		H-MSY	Н	56	44
1.5		H-MSY	Н	82	18
0.5		MSY	Н	75	25
1.5		MSY	Н	84	16

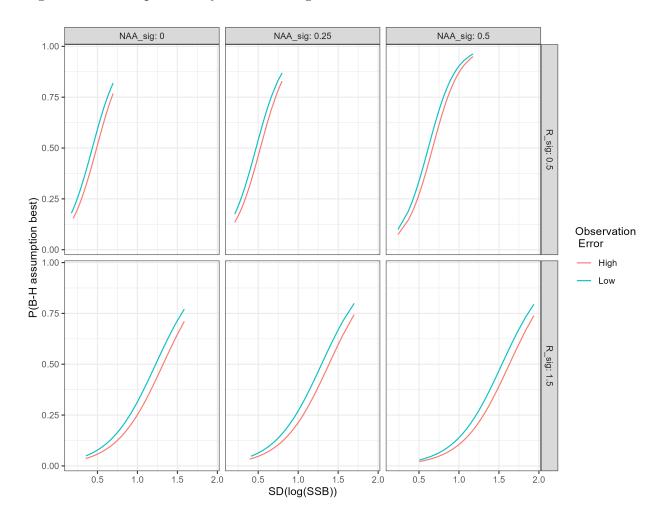
Table 7. Operating models and estimation models all assume RE on all abundances at age, estimating models assume mean recruitment or a B-H stock recruit relationship and M is fixed at the true value.

σ_R	σ_N	F-history	Obs Error	R only	ВН
0.5	0.25	H-MSY	${ m L}$	43	57
1.5	0.25	H-MSY	${ m L}$	84	16
0.5	0.50	H-MSY	${ m L}$	33	67
1.5	0.50	H-MSY	${ m L}$	77	23
0.5	0.25	MSY	${ m L}$	69	31
1.5	0.25	MSY	${ m L}$	88	12
0.5	0.50	MSY	${ m L}$	55	45
1.5	0.50	MSY	${ m L}$	87	13
0.5	0.25	H-MSY	Н	57	43
1.5	0.25	H-MSY	Н	84	16
0.5	0.50	H-MSY	Н	66	34
1.5	0.50	H-MSY	Н	79	21
0.5	0.25	MSY	Н	78	22
1.5	0.25	MSY	Н	88	12
0.5	0.50	MSY	Н	73	27
1.5	0.50	MSY	Н	83	17

Table 8. Operating models and estimation models all assume RE on all abundances at age, estimating models assume mean recruitment or a B-H stock recruit relationship and M is estimated.

σ_R	σ_N	F-history	Obs Error	R only	ВН
0.5	0.25	H-MSY	L	44	56
1.5	0.25	H-MSY	${ m L}$	84	16
0.5	0.50	H-MSY	${ m L}$	31	69
1.5	0.50	H-MSY	${ m L}$	80	20
0.5	0.25	MSY	${ m L}$	68	32
1.5	0.25	MSY	${ m L}$	88	12
0.5	0.50	MSY	${ m L}$	55	45
1.5	0.50	MSY	${ m L}$	86	14
0.5	0.25	H-MSY	Н	59	41
1.5	0.25	H-MSY	Н	81	19
0.5	0.50	H-MSY	Н	67	33
1.5	0.50	H-MSY	Н	80	20
0.5	0.25	MSY	Н	66	34
1.5	0.25	MSY	Н	74	26
0.5	0.50	MSY	Н	74	26
1.5	0.50	MSY	Н	87	13





3.2 M operating models

129 3.2.1 Estimating models include NAA random effects and estimation assumes 130 mean R or BH SR

Table 9. M random effects operating models.

σ_M	$ ho_M$	F-history	Obs Error	R (M fix)	BH (M fix)	R (M est)	BH (M est)
0.1	0.0	H-MSY	L	38	62	38	62
0.5	0.0	H-MSY	${ m L}$	42	58	42	58
0.1	0.0	MSY	${ m L}$	66	34	66	34
0.5	0.0	MSY	${ m L}$	70	30	58	41
0.1	0.0	H-MSY	Н	45	55	47	53
0.5	0.0	H-MSY	Н	56	43	54	45
0.1	0.0	MSY	Н	66	34	66	33
0.5	0.0	MSY	Н	72	28	57	42
0.1	0.9	H-MSY	${f L}$	31	69	33	64
0.5	0.9	H-MSY	${f L}$	15	73	16	64
0.1	0.9	MSY	${f L}$	44	56	41	47
0.5	0.9	MSY	${f L}$	12	76	10	69
0.1	0.9	H-MSY	Н	32	68	47	44
0.5	0.9	H-MSY	Н	10	78	21	51
0.1	0.9	MSY	Н	40	60	38	28
0.5	0.9	MSY	Н	22	64	22	49

131 4 Discussion

The estimating models assumed variances of aggregate catch and index observations was known. This approximation may be appropriate for indices where we have a reliable estimate of uncertainty based on the survey design (), but there may be better approaches for the aggregate catch such as an informed prior on the standard errors with realistic bounds.

136 Acknowledgements

137 This work was funded by NOAA Fisheries Northeast Fisheries Science Center.

References

- Aeberhard, W. H., Mills Flemming, J., and Nielsen, A. 2018. Review of State-Space Models for Fisheries Science 5(1): 215–235, doi: 10.1146/annurev-statistics-031017-100427.
- Cadigan, N. G. 2016. A state-space stock assessment model for northern cod, including under-
- reported catches and variable natural mortality rates. Canadian Journal of Fisheries and
- Aquatic Sciences 73(2): 296–308, doi: 10.1139/cjfas-2015-0047.
- Legault, C. M., Wiedenmann, J., Deroba, J. J., Fay, G., Miller, T. J., Brooks, E. N., Bell,
- R. J., Langan, J. A., Cournane, J. M., Jones, A. W., and Muffley, B. In press. Data-
- rich but model-resistant: an evaluation of data-limited methods to manage fisheries with
- failed age-based stock assessments. Canadian Journal of Fisheries and Aquatic Sciences
- Doi: 10.1139/cjfas-2022-0045.
- Nielsen, A. and Berg, C. W. 2014. Estimation of time-varying selectivity in stock assessments using state-space models. Fisheries Research 158: 96–101, doi:
- 10.1016/j.fishres.2014.01.014.

153

- Stock, B. C. and Miller, T. J. 2021. The Woods Hole Assessment Model (WHAM): A general
 - state-space assessment framework that incorporates time- and age-varying processes via
- random effects and links to environmental covariates. Fisheries Research 240: 105967,
- doi: 10.1016/j.fishres.2021.105967.