- ¹ Chainsweep-based efficiency of bottom trawl surveys and biomass
- estimates for flatfish, red hake, and goosefish stocks in Northwest
- Atlantic waters of the United States
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9 Abstract

- Using a general hierarchical model we estimated relative efficiency of chain sweep to the rockhopper sweep used by the NEFSC bottom trawl survey for from studies carried out between 2015 and 2017 aboard the F/V Karen Elizabeth twin-trawl vessel. Aside from the sweeps, the rest of the trawl gear is the same. We compared a set of models with different assumptions about variation of relative efficiency between paired gear tows, size and diel effects on the relative efficiency, and extra-binomial variation of observations within paired gear tows.
- Using a general hierarchical model we estimated relative efficiency of chain sweep to the rockhopper sweep used by the NEFSC bottom trawl survey for winter and windowpane flounder stocks and red hake stocks from studies carried out between 2015 and 2017 aboard the F/V Karen Elizabeth twin-trawl vessel. Aside from the sweeps, the rest of the trawl gear is the same. We compared a set of models with different assumptions about variation of relative efficiency between paired gear tows, size and diel effects on the relative efficiency, and extra-binomial variation of observations within paired gear tows. Diel effects provided improved model performance for all three species. We used the best performing model to make annual chain sweep-based swept area biomass and abundance-at-length estimates. We estimated uncertainty in all results using bootstrap procedures for each data component.

25 Keywords

26 hieararchical models, spline regression, gear efficiency, abundance estimation

₇ 1 Introduction

- 28 Paired-gear studies have long been used to estimate the efficiency of one fishing gear relative to another (e.g.,
- ²⁹ Gulland, 1964; Bourne, 1965). These types of studies are critical for informing abundance time series from
- 50 fishery independent surveys when there are changes in the vessel and(or) gears over time due to gear failures
- or improved technology.
- Within the northeast US there has been a heightened focus on trawl survey operations and gear efficiency.
- 33 This focus has in part resulted from low quotas for a number of grounfish limiting fishing opportunities.
- To help provide clarity on the trawl operations and build trust in survey indies the New England Fisheries
- 35 Management Council developed a Northeast Trawl Advisory Panel. This panel is composed of members from
- 36 industry, regional academics, as well as state and federal scientists. Together the group designed a set of
- 37 experiments to explore the differences in efficiency between survey and trawl gear (hereafter referred to as
- ³⁸ 'chain sweep' experiments).
- 39 The goal of these chain sweep experiments was to provide estimates of what absolute abundance might be, so
- that this could be used for assessment processes. For example, developing an estimate of absolute abundance
- 41 allows for some swept-area biomass calculations at the region scale. These estimates can then be compares
- to other index-based empirical assessment methods. This is especially valuable for species where limited
- commercial harvest occurs, but assessments suggest the species is in poor status (e..g, red hake).
- In conducting paired-gear studies it is ideal to have the two gears deployed as close together spatially and
- 45 temporally as possible to reduce variation between the gears in densities of the species being captured.
- 46 One fishing method that approaches this ideal is the twin-trawl rigging where two trawls can be fished
- 47 simultaneously (ICES, 1996). The basic methods we used here are based on those used by Miller (2013)
- to estimate size effects on relative catch efficiency of the Henry B. Bigelow to the Albatrosss IV. Similar
- 49 approaches were used to make similar estimates for groundfish, TRAC stocks and summer flounder (Miller
- et al., 2017a,b). The methods here are the same as those used for red hake for the red hake research track
- assessments (Miller et al., 2020).
- Importance of biomass or (catchability) efficiency estimates for both index-based methods as well as age-
- 53 structured models with low contrast.

$_{54}$ 2 Methods

$_{55}$ 2.1 Data collection

Data were collected during three field experiments carried out in 2015, 2016, and 2017, respectively, aboard the F/V Karen Elizabeth, a 78ft stern trawler capable of towing two trawls simultaneously side by side. However, red hake were only observed during the 2017 field experiments. One side of the twin-trawl rig towed a NEFSC standard 400 x 12 cm survey bottom trawl rigged with the NEFSC standard rockhopper sweep (Politis et al., 2014) (Figure 1). The other side of the twin-trawl rig towed a version the NEFSC 400 x 12cm survey bottom trawl modified to maximize the capture of flatfish. The trawl was modified by reducing the headline flotation from 66 to 32, 20cm, spherical floats, reducing the port and starboard top wing-end extensions by 50cm each and utilizing a chain sweep. The chain sweep was constructed of 1.6cm (5/8in) trawl 63 chain covered by 12.7cm diameter x 1cm thick rubber discs on every other chain link (Figure 2). Two rows of 1.3cm (1/2in) tickler chains were attached to the 1.6cm trawl chain by 1.3cm shackles (Figure 2). To ensure equivalent net geometry of each gear, 32m restrictor ropes, made of 1.4cm (9/16in) buoyant, Polytron rope, were attached between each of the trawl doors and the center clump. 3.4m2 Thyboron Type 4 trawl doors 67 were used to provide enough spreading force to ensure the restrictor ropes remained taut throughout each tow. Each trawl used the NEFSC standard 36.6m bridles. All tows followed the NEFSC standard survey towing protocols of 20 minutes at 3.0 knots. In 2015, 108 (45 day, 63 night) paired tows were conducted in eastern Georges Bank and off of southern New England (Figure 3). In 2016, 117 (74 day, 43 night) paired 71 tows were conducted in western Gulf of Maine and northern edge of Georges Bank (Figure 4). In 2017, 103 72 (61 day, 42 night) paired tows were conducted in waters off of southern New England (Figure 5). Paired tows were denoted as "day" and "night" by whether the sun was above or below the horizon at the time of the tow. Winter flounder were caught in 171 paired tows (97 day, 74 night). Overall 6,449 winter flounder were 75 measured for length. The subsampling fractions implied an estimated 6,586 winter flounder were captured across all paired tows. 3805 and 2644 length measurements were made for the chainsweep and rockhopper 77 gears, respectively. During the day, 2385 and 1220 winter flounder were measured in catches by the respective gears whereas during the night 1420 and 1424 were measured in catches by the respective gears. Windowpane flounder were caught in 195 paired tows (100 day, 95 night). Overall 13,014 windowpane were measured for length. The subsampling fractions implied an estimated 15,310 windowpane were captured across all paired tows. 9854 and 3160 length measurements were made for the chainsweep and rockhopper gears, respectively. During the day, 5443 and 778 windowpane were measured in catches by the respective

- gears whereas during the night 4411 and 2382 were measured in catches by the respective gears.
- 85 Red hake were caught in 73 paired tows (40 day, 33 night). Overall 12,585 red hake were measured for length.
- The subsampling fractions implied an estimated 47,275 red hake were captured across all paired tows. 8587
- and 3998 length measurements were made for the chainsweep and rockhopper gears, respectively. During the
- day, 4908 and 1706 red hake were measured in catches by the respective gears whereas during the night 3679
- and 2292 were measured in catches by the respective gears.

2.2 Paired-tow analysis

- We use the hierarchical modeling approach from Miller (2013) to estimate the relative efficiency of chain sweep to the rockhopper sweep used by the NEFSC bottom trawl survey for six species from three studies carried out aboard a twin trawl vessel. Aside from the sweeps the rest of the trawl gear is the same. As in Miller (2013), we compared a set of models with different assumptions about variation of relative efficiency between paired gear tows, size effects on the relative efficiency, and extra-binomial variation of observations within paired gear tows. We began with the same 13 models considered by Miller (2013). Models BI_1 to BI_4 and BB₁ to BB₈ in Table ?? provides a descriptions of the models fitted for all species and pseudo-formulas 97 comparable to those used for fitting models in R and the mgcv package (R Core Team, 2019; Wood, 2006). We then also included diel effects on relative catch efficiency and intereactions with size effects with the best performing model of the original 13 models for each species. For red hake, these are the same analyses provided in Miller et al. (2020) and the new analyses for winter and windowpane flounder are analogous. The 101 analyses here and in Miller et al. (2020) are similar to those by Miller et al. (2017a), Miller et al. (2017b), and Miller et al. (2018), but a more generalized model has been implemented that allows multiple smooth 103 effects on relative catch efficiency so that models do not have to be fit separately to observations occurring during the day and night. Therefore, diel effects on relative catch efficiency and interactions with size effects 105 can be considered while allowing other parameters to be the same for all observations. 106
- If the best model included regression splines of length and smooth parameters estimated linear functions of length (on the transformed scale), then simpler linear models were assumed for further models that included diel effects on relative efficiency. One less parameter (smoothing parameter) for these models.
- Red hake: had to assume station-specific random effects that corresponded to the population-level fixed effects were uncorrelated because of convergence issues.

$_{12}$ 2.3 Length-weight analysis

We fit length-weight relationships to the length and weight observations for each survey each year. We assumed weight observation j from survey i, was log-normal distributed,

$$\log W_{ij} \sim N \left(\log \alpha_i + \beta_i \log L_{ij} - \frac{\sigma_i^2}{2}, \sigma_i^2 \right)$$
 (1)

We used a bias correction to ensure the expected weight $E(W_{ij}) = \alpha_i L_{ij}^{\beta_i}$. We estimated parameters by maximizing the model likelihood programmed in TMB (Kristensen et al., 2016) and R (R Core Team, 2019). Like the relative catch efficiency, bootstrap predictions of weight at length were made by sampling with replacement the length-weight observations within each annual survey and refitting the length-weight relationship to each of the bootstrap data sets.

2.4 Biomass estimation

We estimated biomass for each annual survey in terms of chainsweep efficiency by scaling the survey tow observations by the relative efficiency of the chainsweep and rockhopper sweep gears. First the tow-specific catches at length are rescaled,

$$\widetilde{N}_{hi}(L) = N_{hi}(L)\,\widehat{\rho}_i(L) \tag{2}$$

where $N_{hi}(L)$ is the number at length L in tow i from stratum h and $\widehat{\rho}_i(L)$ is the relative efficiency of the chain sweep to rockhopper sweep at length L estimated from the twin trawl observations, that may depend on the diel characteristic of tow i if that factor is in the best model fitted to the twin-trawl observations.

Note that we have omitted any subscripts denoting the year or survey.

The stratified abundance estimate is then calculated using the design-based estimator,

$$\widehat{N}(L) = \sum_{h=1}^{H} \frac{A_h}{An_h} \sum_{i=1}^{n_h} \widetilde{N}_{hi}(L)$$
(3)

where A_h is the area of stratum h, $A = \sum_{h=1}^{H} A_h$, and n_h is the number of tows that were made in stratum h. The corresponding biomass estimate is then

$$\widehat{B} = \sum_{l=1}^{n_L} \widehat{N}(L=l)\widehat{w}(L=l) \tag{4}$$

where $\widehat{w}(L=l)$ is the estimated weight at length from fitting length-weight observations described above.

Length is typically measured to the nearest cm so n_L indicates the number of 1 cm length categories that were observed during the survey.

To estimate uncertainty in biomass, we used bootstrap results for the relative catch efficiency and weight at length estimates along with bootstrap samples of the survey data. Bootstrap data sets for each of the annual surveys respected the stratified random designs by resampling with replacement within each stratum (Smith, 1997). For each of the 1000 combined bootstraps, survey observations for bootstrap b were scaled with the corresponding bootstrap estimates of relative cookie sweep to rockhopper sweep efficiency and predicted weight at length, using Eqs. 3 and 4.

As measured by AIC, the best performing model for winter flounder before considering day/night effects was the conditional binomial model BI₄ (Table ??). Allowing smooth size-effects on relative catch efficiency and

140 3 Results

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3.1 Winter flounder

variation in these effects among paired-tows provided primary improvements in model performance. Including diel effects on relative efficiency for the twin-trawl observations improved performance of the binomial model 145 (BI₅), however the model allowing the size effects on relative efficiency to differ between day and night (BI₆) would not converge. The relative efficiency of the chain sweep gear to the rockhopper sweep gear is greatest at 147 the smallest sizes of winter flounder, but is fairly constant over over sizes greater than 25 cm. The minimum relative efficiency is between 1.5 and 2 during the day, but efficiencies of the two sweeps are approximately 149 equal efficiency at night (Figure ??). 150 Stock-specific biomass estimates from 2009 to 2019 for the NEFSC spring and fall survey were variable. 151 Georges Bank winter flounder biomass estimates range between 1800 and 9400 mt in the spring and 3000 and 152 24,000 mt in the fall and are lower in recent years than those in the early years (Figure ?? and Table ??). 153 However, we note that the estimates of biomass made here were determined in the 2019 assessment to be 154 problematic because of the larger sizes that predominate in the Georges Bank stock area than other stock 155 areas and the low number of observations in the chainsweep study of these larger individuals (NEFSC, 2020). Gulf of Maine winter flounder biomass estimates are constrained to the segment of the population at least 30 157 cm in length. The spring biomass estimates have been fairly stable ranging between 900 and 2700 mt whereas the fall estimates were greater at the beginning of the time series than recent years and range between 1900 159 and 4300 mt (Figure?? and Table??). Southern New England winter flounder biomass estimates are also

lower in recent years than the beginning of the time series for both seasons and spring and fall estimates range from 1300 to 8500 mt and 2100 to 47,500 mt, respectively (Figure ?? and Table ??).

The efficiency of the rockhopper gear relative to the chainsweep in terms of biomass changes from year to year due primarily to corresponding changes in the estimated numbers at length (Table ??). Annual biomass relative efficiency for Georges Bank winter flounder varied between 0.55 and 0.79 in the spring and 0.61 and 0.92 in the fall. Relative efficiencies for the Gulf of Maine stock range between 0.54 and 0.70 for the spring and 0.63 and 0.88 in the fall. Relative efficiencies for the Southern New England stock range between 0.64 and 0.91 for the spring and 0.60 and 1.0 for the fall.

Because the length-weight relationship which is used with the numbers at length to estimate biomass is
estimated by survey and year there is a possibility that poor sampling in a given year could adversely affect the
biomass estimates. We therefore calculated the ratios of the annual uncalibrated biomass estimates using just
the aggregate catch data to the biomass estimates made using the numbers at length and estimated weight at
length (i.e., Eqs. 3 and 4 without the relative efficiency at size). These ratios should be approximately 1.
The ratios for all years and seasons for all three stocks of winter flounder varied from 0.94 to 1.04 (Table ??).

$_{\scriptscriptstyle{175}}$ 3.2 Windowpane flounder

As measured by AIC, the best performing model for windowpane flounder before considering day/night effects
was the conditional binomial model BI₄ (Table ??). Allowing smooth size-effects on relative catch efficiency
and variation in these effects among paired-tows provided primary improvements in model performance.

Including diel effects on relative efficiency at size for the twin-trawl observations improved performance of the
binomial model (BI₆). The relative efficiency of the chain sweep gear to the rockhopper sweep gear decreases
with size of windowpane flounder. The minimum relative efficiency is between 4.5 and 21 during the day, and
between 1.8 and 2.9 at night (Figure ??).

Stock-specific biomass estimates from 2009 to 2019 for the NEFSC spring and fall survey were variable.

Georges Bank-Gulf of Maine windowpane flounder biomass estimates range between 3000 and 20,300 mt in the spring and 4700 and 18,300 mt in the fall and are lower in recent years than those in the early years (Figure ?? and Table ??). Southern New England-Mid-Atlantic Bight windowpane flounder biomass estimates in the spring ranged between 7300 and 15,600 mt whereas the fall estimates ranged between 7300 and 14,700 mt (Figure ?? and Table ??).

The efficiency of the rockhopper gear relative to the chainsweep in terms of biomass changes from year to year due primarily to corresponding changes in the estimated numbers at length (Table ??). Annual biomass

relative efficiency for Georges Bank-Gulf of Maine windowpane flounder varied between 0.21 and 0.36 in the spring and 0.19 and 0.42 in the fall. Relative efficiencies for the Southern New England-Mid-Atlantic Bight stock ranged between 0.22 and 0.36 for the spring and 0.26 and 0.35 in the fall.

Because the length-weight relationship which is used with the numbers at length to estimate biomass is
estimated by survey and year there is a possibility that poor sampling in a given year could adversely affect the
biomass estimates. We therefore calculated the ratios of the annual uncalibrated biomass estimates using just
the aggregate catch data to the biomass estimates made using the numbers at length and estimated weight at
length (i.e., Eqs. 3 and 4 without the relative efficiency at size). These ratios should be approximately 1. The
ratios for all years and seasons for both stocks of windowpane flounder varied from 0.97 to 1.04 (Table ??).

$_{200}$ 3.3 Red hake

For red hake, the best performing model before considering day/night effects was the conditional beta-binomial 201 model BB₆ (Table ??). The best beta-binomial model had an AIC more than 13 units lower than the best 202 binomial model. Allowing variation in smooth size-effects on relative catch efficiency among paired-tows and 203 extra-binomial variation withing paired-tows (overdispersion via the beta-binomial assumption) provided 204 primary improvements in model performance. Including diel effects on relative efficiency for the twin-trawl observations improved performance of the beta-binomial model. Initially separate smooth size effects for 206 day and night tows were considered for the beta-binomial model (BB₈), but the correlation of non-smoother related random effects across stations was not estimable. Those random effects were therefore assumed 208 uncorrelated (BB₉). Allowing different smooth size effects of relative efficiency for day and night observations was considerd (BB₁₀), but it did not improve model performance. The relative efficiency of the chain sweep 210 gear to the rockhopper sweep gear generally declines with increased size whether the tow occurred during day or night, but the increase in efficiency of the chainsweep was generally greater for tows occurring during the 212 day (Figure ??). 213

Stock-specific trends in annual biomass estimates from 2009 to 2019 for the NEFSC spring and fall survey were generally the same. For northern red hake both the spring and fall biomass estimates increased in 2014 and have remained higher than previous years (Figure ?? and Table ??). The scale of the biomass estimates is also similar for the spring and fall surveys. For southern red hake, the spring biomass generally declined until 2017 and then has increased for the last two years whereas the fall biomass has remained relatively stable (Figure ?? and Table ??).

The efficiency of the rockhopper gear relative to the chainsweep in terms of biomass changes from year to

year due primarily to corresponding changes in the estimated numbers at length (Table ??). Annual biomass relative efficiency for northern red hake varied between 0.19 and 0.25 in the spring and 0.21 and 0.33 in the fall. Values range between 0.15 and 0.26 for the spring and 0.19 and 0.39 in the fall for southern red hake.

Because the length-weight relationship which is used with the numbers at length to estimate biomass is estimated by survey and year there is a possibility that poor sampling in a given year could adversely affect the biomass estimates. We therefore calculated the ratios of the annual uncalibrated biomass estimates using just the aggregate catch data to the biomass estimates made using the numbers at length and estimated weight at length (i.e., Eqs. 3 and 4 without the relative efficiency at size). These ratios should be approximately 1. The ratios for all years and seasons for both northern and southern red hake varied from 0.96 to 1.04 (Table ??).

²³⁰ 4 Discussion

²³¹ Compare greater or lesser smoothness within stations with Pedersen et al. 2019.

232 Acknowledgements

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Fig. 1. Diagram of the standard Northeast Fisheries Science Center rockhopper sweep center and wing sections.

ROCKHOPPER CENTER SECTION Section = 890cm, 100lbs Lead

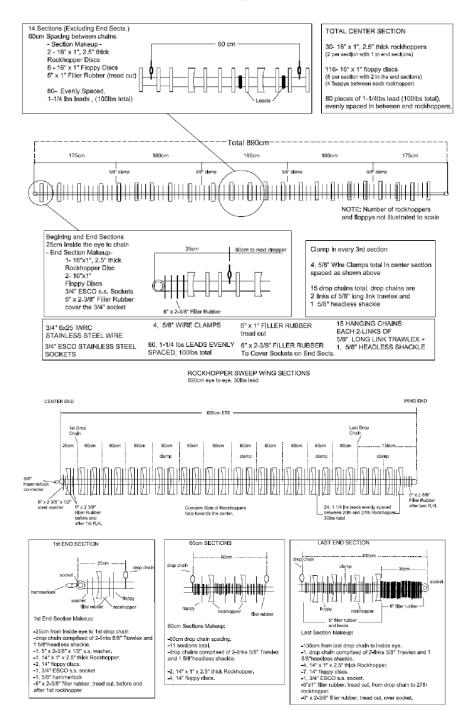


Fig. 2. Diagram of the chain sweep designed maximize bottom contact and flatfish capture.

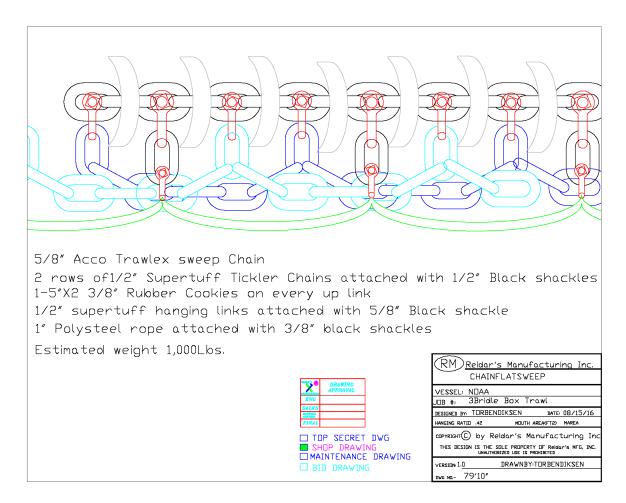
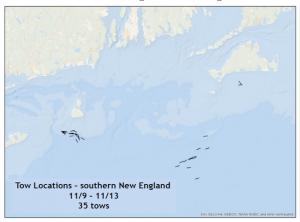


Fig. 3. Locations of stations in 2015 where the F/V Karen Elizabeth conducted twin-trawl sets with the standard bottom trawl gear and the gear with a chain sweep instead of the rockhopper sweep.



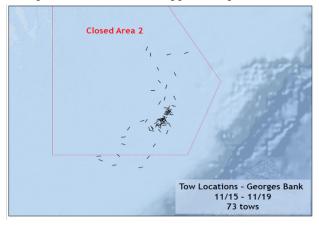
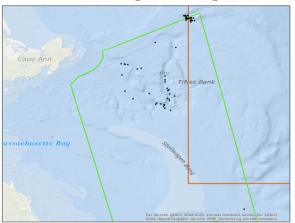


Fig. 4. Locations of stations in 2016 where the F/V Karen Elizabeth conducted twin-trawl sets with the standard bottom trawl gear and the gear with a chain sweep instead of the rockhopper sweep.



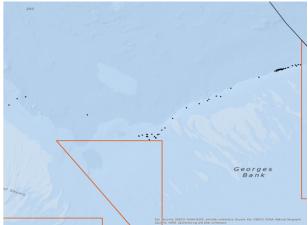


Fig. 5. Locations of stations in 2017 where the F/V Karen Elizabeth conducted twin-trawl sets with the standard bottom trawl gear and the gear with a chain sweep instead of the rockhopper sweep.

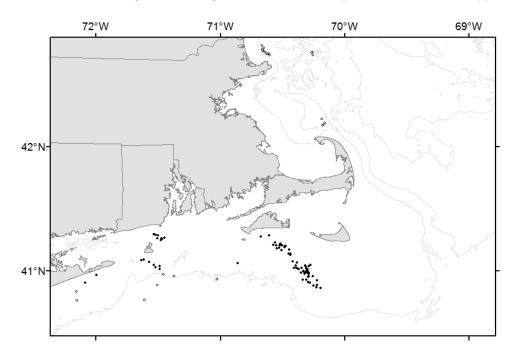


Table 1. Description of relative catch efficiency (ρ) and beta-binomial dispersion (ϕ) parameterizations for binomial and beta-binomial models and number of marginal likelihood parameters (n_p) for the 13 base models from Miller (2013) and fit to paired chainsweep and rockhoppersweep tow data for each species.

Model	$\log\left(ho ight)$	$\log\left(\phi\right)$	n_p	Description
BI_0	~ 1	_	1	population-level mean for all observations
BI_1	$\sim 1 + 1 \text{pair}$	_	2	population- and random station-level ρ
BI_2	$\sim s(length)$	_	3	population-level smooth size effect on ρ
BI_3	$\sim s(length) + 1 pair$	_	4	population-level smooth size effect and random station-level intercept for ρ
BI_4	$\sim s(length) + s(length) pair$	_	7	population-level and random station-level smooth size effects for ρ
BB_0	~ 1	~ 1	2	population-level ρ and ϕ
BB_1	$\sim 1 + 1 \text{pair}$	~ 1	3	population-level and random station-level intercept for ρ and population-level ϕ
BB_2	$\sim s(length)$	~ 1	4	population-level smooth size effect on ρ and population-level ϕ
BB_3	$\sim s(length)$	$\sim s(length)$	6	population-level smooth size effect on ρ and ϕ
BB_4	$\sim s(length) + 1 pair$	~ 1	5	population-level smooth size effect and random station-level intercept for ρ and population-level ϕ
BB_5	$\sim s(length) + 1 pair$	$\sim s(length)$	7	population-level smooth size effect on ρ and ϕ and random station-level intercepts for ρ
BB_6	$\sim s(length) + s(length) pair$	~ 1	8	population-level and random station-level smooth size effects on ρ and population-level ϕ
BB ₇	\sim s(length) + s(length) pair	$\sim s(length)$	10	population-level and random station-level smooth size effects on ρ and population-level smooth size effects on ϕ

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Table 2. Difference in AIC for each of the 13 models described in Table 1 from the best model (0) by species.

	BI_0	BI_1	BI_2	BI_3	BI_4	BB_0	BB_1	BB_2	BB_3	BB_4	BB_5	BB_6	BB_7
Summer flounder	27.96	13.53	8.9	0		28.64	15.45	10.59					
American plaice	821.11	546.54	743.34	494.92	415.63	179.48	71.76	141.44		37.06		0.71	0
Windowpane	1045.06	38.51	1029.72	17.03	0	585.7	32.22	572.73		15.27			
Winter flounder	216.47	15.73	200.33	3.02	0	163.31	16.63	151.66	151.01	4.21	6.78	1.41	
Yellowtail flounder	727.15	97.93	727.36	51.84	10.96	394.94	70.2	391.13	371.13	31.85		0	3.33
Witch flounder	1424.17	212.64	1372.66		35.33	881.28	142.53	844.47		81.37		0	
Red hake	1884.51	295.85		170.75		627.33	166.43	590.92		95.8	59.31	0	0.83
Goosefish	227.67	87.23	80.37	0		219.13		76.54					
Barndoor skate	36.51	10.01	31.34	2.72	0	36.23	11.99	29.03		4.6			
Thorny skate	39.04	8.57	32.65	3.44	1.15	22.38	5.84	18.66		1.38	5.19	0	

	Model	$\log{(ho)}$	$\log(\phi)$	n_p	$\Delta { m AIC}$
Summer flounder					
	BI_3	$\sim s(length) + 1 pair$	_	4	22.92
	BI_{3a}	$\sim dn + s(length) + 1 pair$	_	5	0
	BI_{3b}	\sim dn * s(length) + 1 pair	_	7	1.74
American plaice					
	BB_7	$\sim s(length) + s(length) pair$	$\sim s(length)$	10	0
	BB_{7a}	$\sim dn + s(length) + s(length) pair$	$\sim s(length)$	11	1.43
	BB_{7b}	\sim dn * s(length) + s(length) pair	$\sim s(length)$	13	2.95
Windowpane					
	BI_4	$\sim s(length) + s(length) pair$	_	7	152.1
	BI_{4a}	$\sim dn + length + s(length) pair$	_	7	4.06
	BI_{4b}	\sim dn * length + s(length) pair	_	8	0
Winter flounder					
	BI_4	$\sim s(length) + s(length) pair$	_	7	50.68
	BI_{4a}	$\sim dn + s(length) + length pair$	_	7	0.3
	BI_{4b}	\sim dn * s(length) + length pair	_	9	0
Yellowtail flounder					
	BB_6	$\sim s(length) + s(length) pair$	~ 1	8	3.84
	BB_{6a}	$\sim dn + s(length) + s(length) pair$	~ 1	9	0
	BB_{6b}	\sim dn * s(length) + s(length) pair	~ 1	11	3.48
Witch flounder					
	BB_6	$\sim s(length) + s(length) pair$	~ 1	8	19.68
	BB_{6a}	$\sim dn + length + s(length) pair$	~ 1	8	0
	BB_{6b}	\sim dn * length + s(length) pair	~ 1	9	1.52
Red hake					
	BB_6	$\sim s(length) + s(length) pair$	~ 1	8	32.35
	BB_{6a}	$\sim dn + s(length) + s(length) pair$	~ 1	8	0
	BB_{6b}	\sim dn * s(length) + s(length) pair	~ 1	10	3.18
Goosefish					
	BI_3	$\sim s(length) + 1 pair$	_	4	5.44
	BI_{3a}	$\sim dn + s(length) + 1 pair$	_	5	0
	BI_{3b}	\sim dn * s(length) + 1 pair	_	7	6.8
Barndoor skate					
	BI_4	$\sim s(length) + s(length) pair$	_	7	15.57
	BI_{4a}	$\sim dn + length + length pair$	_	5	0
	BI_{4b}	\sim dn * length + length pair	_	6	1.83
Thorny skate					
	BB_6	$\sim s(length) + s(length) pair$	~ 1	8	15.51
	BB_{6a}	$\sim dn + length + length pair$	~ 1	7	0
	BB_{6b}	\sim dn * length + length pair	~ 1	8	1.38