

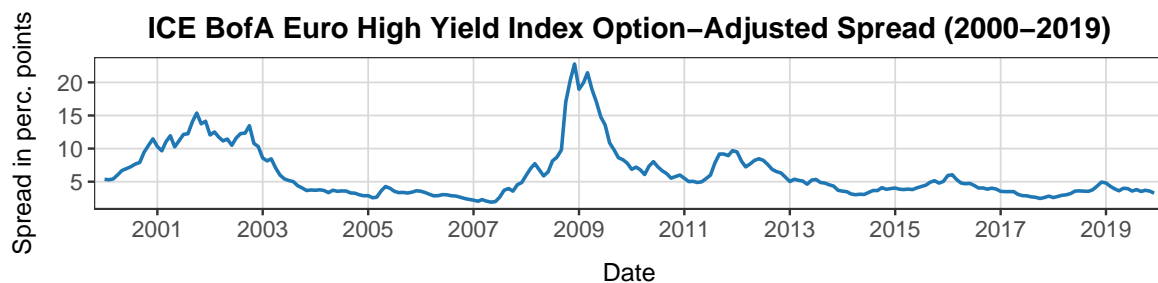
# Econometrics 2B: Time Series Analysis - Homework

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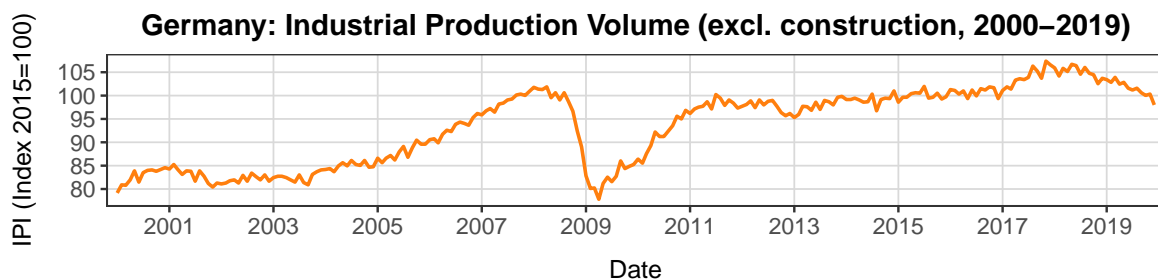
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## Exercise 1 - Univariate Analysis

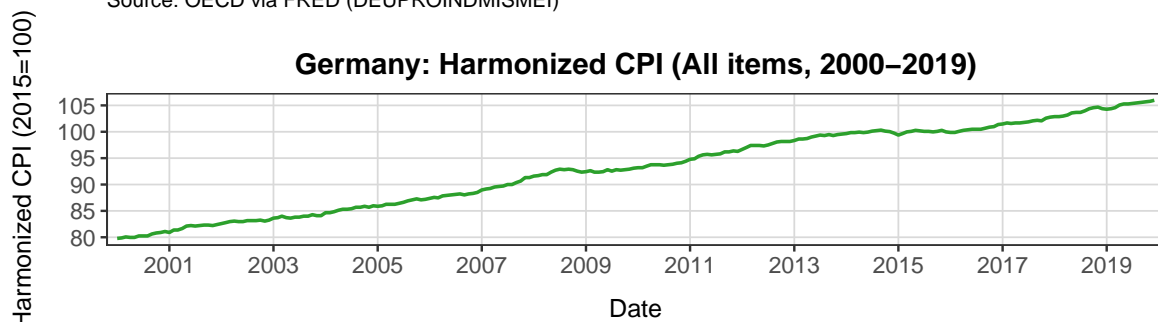
**Exercise 1.1:** Plot each time-series in levels before applying any transformations



Source: ICE Data Indices via FRED (BAMLHE00EHYIOAS)



Source: OECD via FRED (DEUPROINDMISMEI)



Source: OECD via FRED (DEUCPIALLMINMEI)

**Comment on these time series Plots**

### Credit Spread Plot

Before turning to the first plot, we briefly introduce the nature and construction of this time series, as it is less conventional than the other two, which most Economists should be familiar with. The ICE

BofA Euro High Yield Index Option-Adjusted Spread (OAS) measures the additional risk premium that investors require, over the spot treasury curve, to hold euro-denominated corporate bonds rated below investment grade (i.e., lower than BB by Fitch or Ba1 by Moody's).

The plot shows that the credit spread generally fluctuates within a 3–5 percentage point band during stable periods. Sharp spikes in the spread coincide with major episodes of financial turmoil. The elevated spread in 2001–2003, peaking around 15%, reflects heightened risk perceptions during the burst of the “dot-com-bubble” and the post-9/11 recession. The most pronounced increase occurs during the global financial crisis (2007–2009), with a peak above 20% following the collapse of the US-Bank Lehman Brothers in September 2008. The final surge in our time series between 2011 and 2013 reflects the European sovereign debt crisis.

However, it is important to note that the index only includes high-yield corporate bonds issued by firms domiciled in countries with investment-grade sovereign ratings, such as Germany. The observed increase in spreads during the European debt crisis thus primarily reflects broader market risk aversion and heightened perceptions of credit risk for core Eurozone Countries.

For our time series analysis, visually inspecting the series we see the series exhibits strong mean-reversion around a constant level and no visible trend, suggesting weak stationarity.

### **Industrial Production Index**

The second plot shows Germany's industrial production index (excluding construction) from 2000 to 2019, expressed in real terms with 2015 as the base year. We can divide the evolution of the series into several key phases. From 2003 to mid-2008, the index displays a steady and almost linear upward trend, reflecting sustained industrial growth. This is followed by a sharp contraction of over 20% during the global financial crisis. The recovery begins in early 2009 but remains gradual and volatile. Pre-crisis output levels are only reached again by late 2015, an astounding 7 years after the GFC began. After 2017, the series begins to decline again, with little evidence of structural growth, indicating a potential stagnation of the German industrial sector in the face of increasing global uncertainty.

Visual inspection suggests that the series is clearly non-stationary, characterized by both a deterministic trend and a shift in level post GFC. To obtain a stationary series, we take the first difference of the outcome. Additionally, we will use a logarithmic transformation as log-differences can be interpreted as month-over-month growth rates in industrial production.

### **Consumer Price Index**

The third plot shows the harmonized consumer price index (HICP) for Germany from 2000 to 2019, with 2015 as the base year. Over the entire sample period, the series exhibits a smooth and almost linear upward trend, increasing from approximately 80 to 105. Assuming linearity, this corresponds to an average annual growth rate of roughly 1.25 percentage points, which is consistent with the broader macroeconomic environment of low and stable inflation during this time period. Notably, the sample ends just before two major inflationary shocks: the COVID-19 pandemic and the 2022 energy crisis triggered by Russia's invasion of Ukraine—both of which led to significant price pressures in subsequent years.

Throughout the period shown, the index displays no signs of mean reversion, and inflation appears largely unaffected by the external shocks visible in the other two series. Based on visual inspection, the series clearly exhibits a deterministic trend component.

## **Exercise 1.2: Conduct unit root and stationarity tests for each series**

Given our previous results, we now propose to conduct unit root and stationarity tests in the following order:

- 1) We log-transform CPI and IPI to linearize the relationships and for better interpretability (log differences can be interpreted as MoM growth rates)
- 2) We proceed by conducting standard unit root and stationarity tests in the following order: First, apply the tests to the original (non-differenced). If these tests suggest non-stationarity, we continue with integration until we find stationary series.

## Level Series without integration:

Table 1: Unit Root and Stationarity Tests—Level Series

Series	Test	Specification	Test.Statistic	X1..Crit..Val.	X5..Crit..Val.	X10..Crit..Val.
<b>Industrial Production (log)</b>						
Industrial Production (log)	ADF	Trend	-3.317	-3.99	-3.43	-3.13
	PP	Trend	-2.783	-4	-3.43	-3.138
	KPSS	Trend	0.131	0.22	0.146	0.119
<b>CPI (log)</b>						
CPI (log)	ADF	Trend	-1.483	-3.99	-3.43	-3.13
	PP	Trend	-1.59	-4	-3.43	-3.138
	KPSS	Trend	0.831	0.22	0.146	0.119
<b>Credit Spread</b>						
Credit Spread	ADF	Drift	-2.538	-3.46	-2.88	-2.57
	PP	Drift	-13.076	-	-	-
	KPSS	Level	0.798	0.739	0.463	0.347

Notes:

ADF and PP:  $H_0$  = unit root present

KPSS:  $H_0$  = series stationary

**Log Industrial Production** We obtain mixed results regarding the stationarity of the log industrial production series. Both the ADF and PP tests failed to reject a unit root at standard confidence levels, indicating non-stationarity. However, the KPSS test indicates stationarity at the 1% and 5% levels, though it was borderline at 10%. Given this conflicting evidence and the general tendency to conclude non-stationarity in such cases, we lean towards the safer option and conclude that the series is non-stationary, requiring first-order integration.

**Log CPI** Both the ADF ( $-1.537$ ) and PP ( $-1.564$ ) test statistics are far above the critical values, confirming failure to reject the unit root. The KPSS test statistic ( $0.83$ ) strongly exceeds all critical values, clearly rejecting trend stationarity. Together, the tests provide robust evidence that CPI (log) is non-stationary in levels, which aligns with expectations for price indices.

**Credit Spread** The ADF test statistic ( $-2.606$ ) does not exceed the 5% critical value ( $-2.88$ ), so we fail to reject the unit root. The KPSS test ( $0.807 >$  all critical values) also rejects stationarity. However, the PP test shows an extremely large negative statistic ( $-13.002$ ) with a near-zero p-value, strongly rejecting the null of a unit root. This conflicting evidence suggests caution, but overall, ADF and KPSS both support non-stationarity.

## I(1) Series:

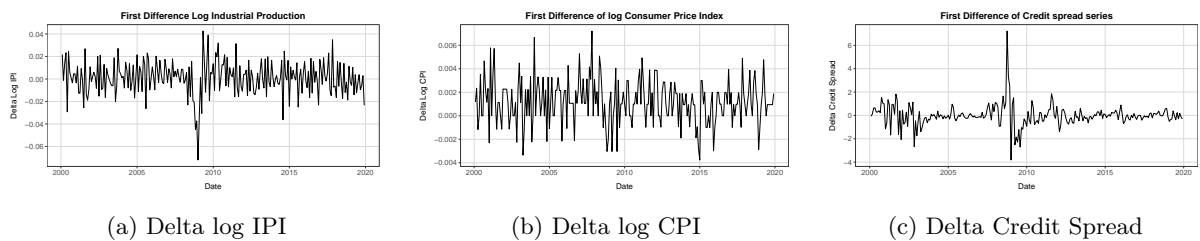


Figure 1: First Differences of the Three Stationary Series

First before we do the unit root tests we again plot the time series of the integrated processes for inspection and conclude the following about the appropriate setup for unit root tests:

- **Industrial Production (Delta log IPI):** The series fluctuates around a non-zero constant mean without a trend, justifying the use of drift specifications for ADF/PP and a level null in KPSS.

- **CPI (Delta log CPI):** The differenced price index series also shows no trend, only short-term fluctuations around a stable mean. This supports the same test setup.
- **Credit Spread (Delta):** Although more volatile, especially around 2009, the series remains mean-reverting without trend, making the constant-only specification reasonable.

Table 2: Unit Root and Stationarity Tests—First Differences

Series	Test	Specification	Test.Statistic	X1..Crit..Val.	X5..Crit..Val.	X10..Crit..Val.
<b>Delta Industrial Production (log)</b>						
Delta Industrial Production (log)	ADF	Drift	-5.539	-3.46	-2.88	-2.57
	PP	Drift	-344.498	-	-	-
	KPSS	Level	0.09	0.739	0.463	0.347
<b>Delta CPI (log)</b>						
Delta CPI (log)	ADF	Drift	-9.902	-3.46	-2.88	-2.57
	PP	Drift	-252.96	-	-	-
	KPSS	Level	0.199	0.739	0.463	0.347
<b>Delta Credit Spread</b>						
Delta Credit Spread	ADF	Drift	-6.284	-3.46	-2.88	-2.57
	PP	Drift	-184.129	-	-	-
	KPSS	Level	0.048	0.739	0.463	0.347

Notes:

ADF and PP:  $H_0$  = unit root present

KPSS:  $H_0$  = series stationary

Delta denotes first difference

After doing the tests, we conclude the following: -  **$\Delta \log$  Industrial Production:** All three tests now clearly point toward stationarity. ADF and PP strongly reject the unit root, while the KPSS test fails to reject level stationarity. This confirms that first differencing was sufficient to achieve stationarity for the industrial production series.

- **$\Delta \log$  CPI:** The test results are consistent and conclusive. Both the ADF and PP tests strongly reject the null of a unit root, and the KPSS test does not reject level stationarity. We therefore conclude that the first-differenced log CPI series is stationary.
- **$\Delta$  Credit Spread:** As with the other two series, all tests align. ADF and PP reject the presence of a unit root by a wide margin, and KPSS indicates no violation of level stationarity. This supports the conclusion that the differenced credit spread series is stationary.

**Exercise 1.3: Identify and estimate candidate AR(p) and ARMA(p,q) models using the ACF and PACF. Which model would you choose according to information criteria? Comment the results**

#### ACF, PACF Plots and Residual Diagnostics

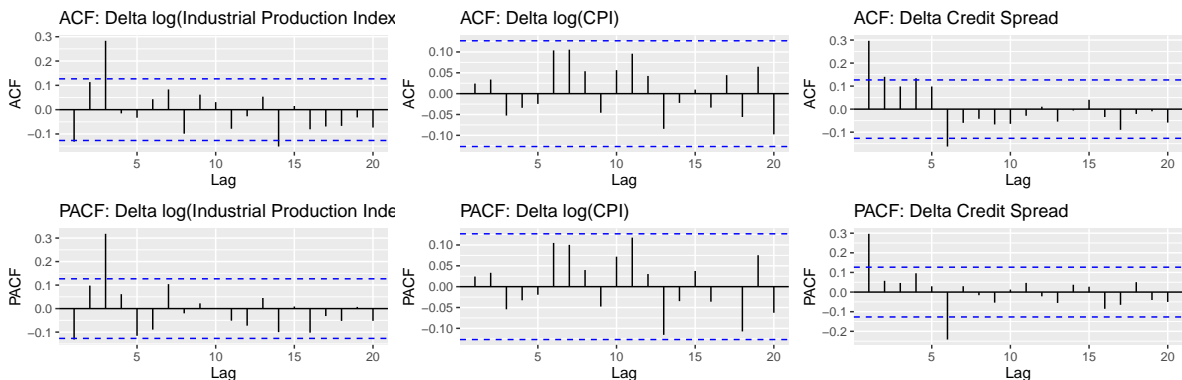


Table 3: Residual diagnostics for top ARMA models by BIC and AIC

Series	Criterion	Model	LB Stat	LB p-val	JB Stat	JB p-val
Industrial Production Index	BIC	ARMA(0,3)	13.77	0.842	31.16	0.000
Industrial Production Index	AIC	ARMA(5,7)	5.99	0.999	53.95	0.000
Core Inflation	BIC	ARMA(0,0)	18.95	0.525	1.29	0.525
Core Inflation	AIC	ARMA(2,2)	12.59	0.894	1.43	0.490
Credit Spread	BIC	ARMA(1,0)	23.52	0.264	3649.07	0.000
Credit Spread	AIC	ARMA(1,6)	8.55	0.988	4865.13	0.000

**Industrial Production Index:**

**Comment:** Inspecting the PACF plot, the pattern appears somewhat irregular. We observe a significant spike at lag 1, a non-significant lag 2, followed by another significant spike at lag 3. This suggests an autoregressive process of order between 1 and 3. As a conservative choice, we initially lean toward an AR(3) specification. This is further supported by the ranking of optimal candidates by the Bayesian Information Criterion (BIC), where the AR(3) model appears as the fourth-best candidate, performing only marginally worse than the top models.

Based on the information criteria, the BIC selects an MA(3) process as the optimal model, while the AIC favors a much more complex ARMA(5,7) specification. (*Reminder: since we are modeling the  $I(1)$  series, this corresponds to an ARIMA(5,1,7) on the original series.*) Once again, this illustrates AIC's tendency to prefer more heavily parameterized models that were not clearly supported by the ACF or PACF plots. We therefore select the MA(3) model as our preferred specification—it performs nearly as well under AIC and is more parsimonious. The MA(3) Model was also chosen by the Hyndman-Khandakar-Algorithm when optimizing with respect to the BIC.

Residual diagnostics (see final table in Exercise 1.3) confirm that the MA(3) model is well-specified. The Ljung–Box test fails to reject the null hypothesis of no autocorrelation. While the Jarque–Bera test rejects normality, this is common in empirical macroeconomic applications and not a major concern, especially since we are interested in forecasting and not inference.

**Consumer Price Index:**

**Comment:** Looking at the MoM inflation rate (log-differenced CPI), the ACF and PACF plots show no significant autocorrelation at any lag, as all values remain well within the confidence bands. Based on visual inspection alone, this pattern is most consistent with a simple white noise process.

This impression is confirmed by the BIC, which selects an ARMA(0,0) model, i.e. pure white noise. The AIC, on the other hand, again favors a more complex model (*in this case, an ARMA(2,2) process*). However, even under AIC, the improvement in fit relative to ARMA(0,0) is marginal and does not justify the added complexity, especially given the lack of support from the correlogram.

Turning to residual diagnostics, we fail to reject both null hypotheses of the Ljung–Box test (no autocorrelation) and the Jarque–Bera test (normality) for the white noise model. These results provide further evidence for our initial conclusion that the CPI time series—after differencing—can reasonably be modeled as a white noise process.

**Credit Spread Index:**

**Comment:** Inspecting the ACF and PACF plots for the credit spread change (i.e. first difference) series again reveals a somewhat non-standard pattern. The ACF shows a large significant spike at lag 1, followed by additional significant values at lags 2 and 4, as well as a highly negative spike at lag 6. The PACF similarly exhibits a strong positive spike at lag 1 and a large negative spike at lag 6. While not a textbook case, this pattern is most plausibly associated with an AR(1) or possibly an AR(6) process.

Turning to the information criteria, the BIC selects an ARMA(1,0) process, i.e. an AR(1), as the preferred specification. The next-best BIC candidate is an MA(1), but the visual evidence does not support a

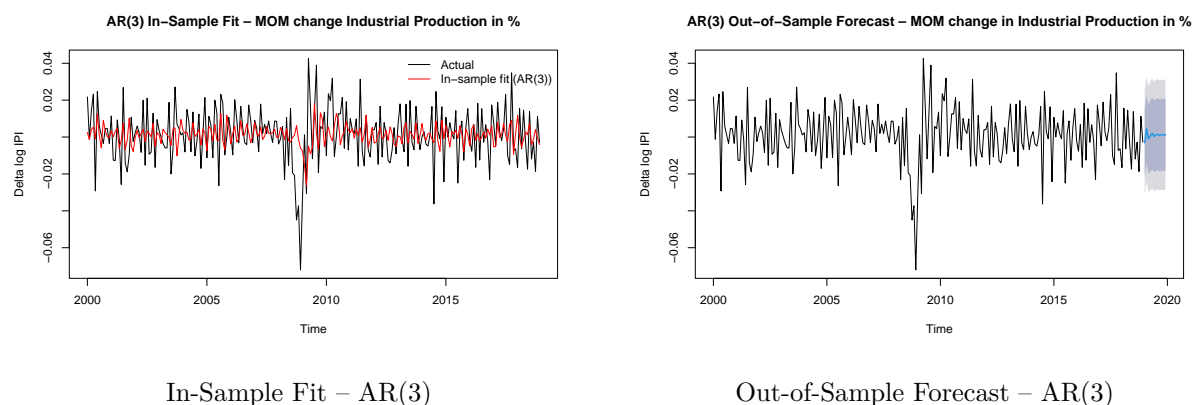
pure MA process. The AIC, as before, chooses a more complex model—namely, an ARMA(1,6)—which comes with a considerable reduction in AIC relative to the AR(1) model. Nevertheless, for reasons of parsimony and interpretability, we adopt **AR(1)** as our baseline model.

Finally, examining the residual diagnostics, we find that the AR(1) model passes the Ljung–Box test (i.e., we fail to reject the null of no autocorrelation), while the Jarque–Bera test again rejects normality, typical for Macroeconometrics. Based on these results, we conclude that the AR(1) specification sufficiently captures the serial dependence in the credit spread series.

## Residual Diagnostics:

**Exercise 1.4: For one of the series, plot the in-sample and out-of-sample forecasts from your best model. Comment the results**

We now plot the in-sample and out-of-sample forecasts for the MOM growth of the Industrial Production series. While the MA(3) initially performed best in terms of BIC, MA models are generally less suited for forecasting since they rely on unobservable future shocks. By contrast, AR processes only depend on past information, making them operationally more robust. Given that the AR(3) process performs nearly as well on the BIC and passes key residual diagnostics (Ljung–Box), we proceed with it for this exercise.



## Comment on the Plots:

### In-Sample Fit

The first plot compares the AR(3) model’s in-sample predictions (red) with the actual data (black). Overall, the model captures the general direction and persistence in  $\Delta \log \text{IPI}$  reasonably well. However, the fit is clearly smoother than the actual series, particularly drastic shocks, around the 2009 GFC, are not fully reflected. This is expected: linear autoregressive models tend to average over past fluctuations and are typically not well-suited to capture crisis dynamics. Still, the model offers a decent approximation of the underlying process.

### Out-of-Sample Forecast

The second plot presents the out-of-sample forecast with confidence intervals. The forecast shows some minor variation early on but quickly reverts to a constant mean, as expected for a stationary AR(p) process. Since we’re using an AR(3) model for a 12-month horizon, real input data beyond the first few periods becomes unavailable, limiting dynamic response. The wide confidence bands indicate high uncertainty, which is not surprising given the volatility of the series. In short, the model suggests short-term stability but lacks precision for medium- or long-run projections.

### Conclusion

The AR(3) model provides a reasonable short-term baseline, capturing autocorrelation but smoothing over extreme movements. For more accurate or structural insights, models with additional indicators (e.g., VAR) would be more appropriate. To better understand crisis episodes, nonlinear time series methods should be considered, as linear models struggle to capture such dynamics.

## Exercise 2 - : Multivariate analysis

### Exercise 2.1: Select the optimal lag length for your multivariate model

Table 4: VAR Lag-Order Selection by Information Criteria

Criterion	Selected Lag
Lag-Order Criteria	
Criterion	SelectedLag
AIC(n)	6
HQ(n)	3
SC(n)	1
FPE(n)	6

#### Comment:

The lag selection criteria point to different optimal values: both AIC (*Akaike Information Criterion*) and FPE (*Final Prediction Error*) suggest a lag length of 6, while HQ (*Hannan–Quinn*) selects 3 and SC (*Schwarz Criterion*) selects 1. Following standard practice, we prioritize the more parsimonious criteria, HQ and SC, which recommend lag orders of 3 and 1, respectively.

Among these, we choose lag 3, as selected by the HQ criterion. While this includes fewer lags than the AIC-optimal specification, it still ensures that residuals are approximately serially uncorrelated (as confirmed in Question 2), which is essential for valid inference and for interpreting impulse response functions. In addition, a more parsimonious model reduces the risk of overfitting, which is particularly important in finite samples.

### Exercise 2.2: Estimate the model and verify that the residuals satisfy standard properties

Table 5: Residual Diagnostics for VAR Model

	Test Statistic	DF	P-value
Portmanteau (no serial corr.)	62.79	54	$1.9 \times 10^{-1}$
ARCH (no ARCH effects)	352.55	180	$2.7 \times 10^{-13}$
Normality (Jarque–Bera)	73927.10	2	$< 2.2 \times 10^{-16}$

#### Comment:

We estimated the VAR(6) model in the standard way in the preceding code chunk. As is common in applied macroeconomic work, we do not report the estimated coefficients here, since our focus lies not on reduced-form parameters but on the dynamic relationships captured by **Impulse Response Functions (IRFs)**, which we will analyze in a later section. (Granger causality could be of interest in some cases, but is not required here and is thus omitted.)

#### Redisual diagnostics:

- **Portmanteau Test for Serial Correlation**

With a p-value of 0.193, we do *not reject* the null of no residual autocorrelation at standard confidence levels. This supports the chosen lag length and confirms that the model captures the joint dynamics of the series sufficiently well. This is a necessary condition for valid inference using IRFs and forecasts.

- **ARCH Test for Conditional Heteroskedasticity**

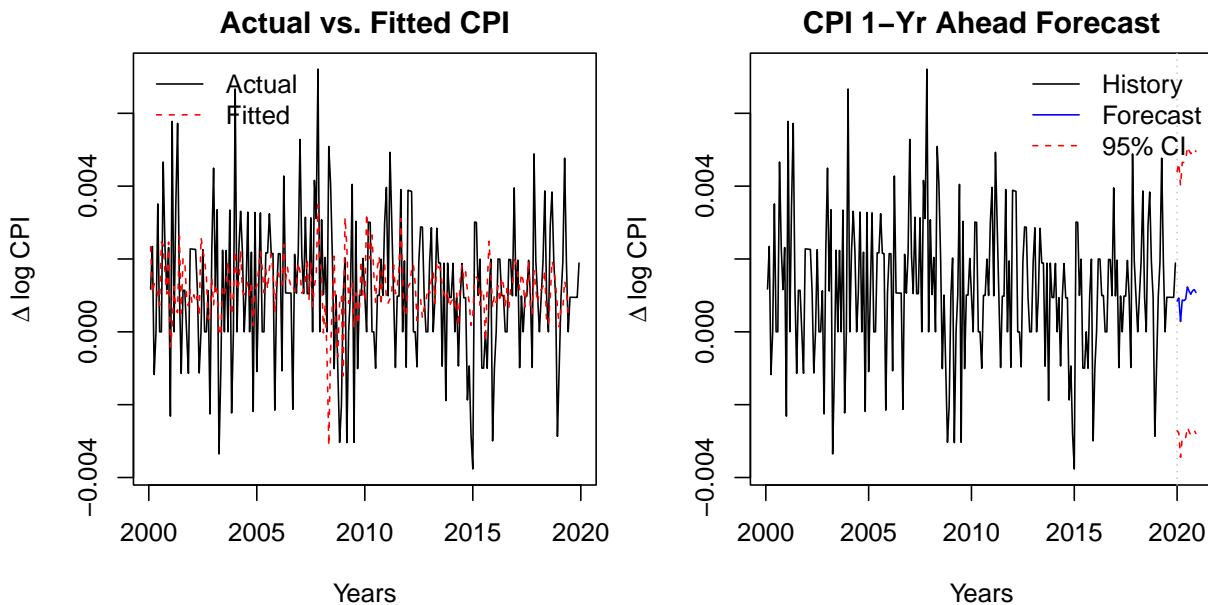
The null of no ARCH effects is *strongly rejected* ( $p \approx 0$ ), indicating time-varying volatility in

the residuals. While this does not bias coefficient estimates, it does invalidate inference based on homoskedastic standard errors. This is why we will rely on *bootstrapped IRFs* in the next step.

- **Jarque–Bera Test for Normality**

We also *strongly reject* the null of normally distributed residuals. This likely reflects skewness or heavy tails. While non-normality limits the applicability of asymptotic theory, most procedures we apply (e.g. bootstrapping) are robust to such deviations.

### Exercise 2.3: Plot the in-sample and out-of-sample forecasts for one of the series



#### Panel 1: Actual vs. Fitted CPI

We estimate a VAR(6) model to capture the joint dynamics of the system. The solid black line shows the observed month-over-month inflation rate in Germany ( $\Delta \log \text{CPI}$ ), while the red dashed line represents the fitted values produced by the VAR(6) model over the estimation window. This plot illustrates the in-sample fit—that is, how well the model explains the data it was trained on.

Overall, the model captures the general trend and propagation of inflation reasonably well. However, the fitted series is noticeably smoother than the actual data, highlighting the model’s inability to match the observed volatility. This limitation is particularly visible during periods of economic disruption, for instance, the 2008–2009 Global Financial Crisis and the 2015 deflationary episode (likely driven by the collapse in global oil prices). These episodes are better understood as nonlinear shocks or “black-swan” events, which simple linear models like VARs are not designed to capture.

Despite this, there is no evidence of persistent over- or underprediction bias. The residuals fluctuate around zero, suggesting the model effectively tracks low-frequency dynamics, even if it fails to capture high-frequency noise and sudden shocks.

#### Panel 2: CPI 1-Year Ahead Forecast

The right panel shows the out-of-sample forecast. The black line again plots observed MoM inflation, while the blue line represents the 12-month-ahead forecast from the VAR(6) model. The red dashed lines indicate the 95% confidence interval.

As expected, the confidence band widens over the forecast horizon, reflecting the accumulating uncertainty the further we forecast into the future. The point forecast itself is conservative, hovering slightly



above zero. This reflects the model's expectation of stable inflation dynamics in the near term, given past information.

However, caution is warranted. These confidence intervals are analytic, and do not account for the non-Gaussian features of the residuals. As we discuss later, bootstrapped intervals (not shown here) are more robust in the presence of heteroskedasticity and fat tails, which are typical in macroeconomic data.

Importantly, the confidence bands are wide—allowing for outcomes ranging from high deflation ( $-0.3\%$  MoM  $\sim 3.7\%$  p.a.) to high inflation ( $0.5\%$  MoM  $\sim 6.7\%$  p.a.). Given this wide range, the point forecast offers limited practical guidance. The high degree of uncertainty simply reflects the noisy nature of monthly inflation, and points to the limitations of simple linear VAR models in predictive settings.

### Exercise 2.4: Using the Cholesky decomposition, explain the reasoning behind your chosen ordering of variables

We apply the following Cholesky ordering to our three variables:

$$\Delta\text{Credit Spread} \longrightarrow \Delta\text{Industrial Production} \longrightarrow \Delta\text{CPI}$$

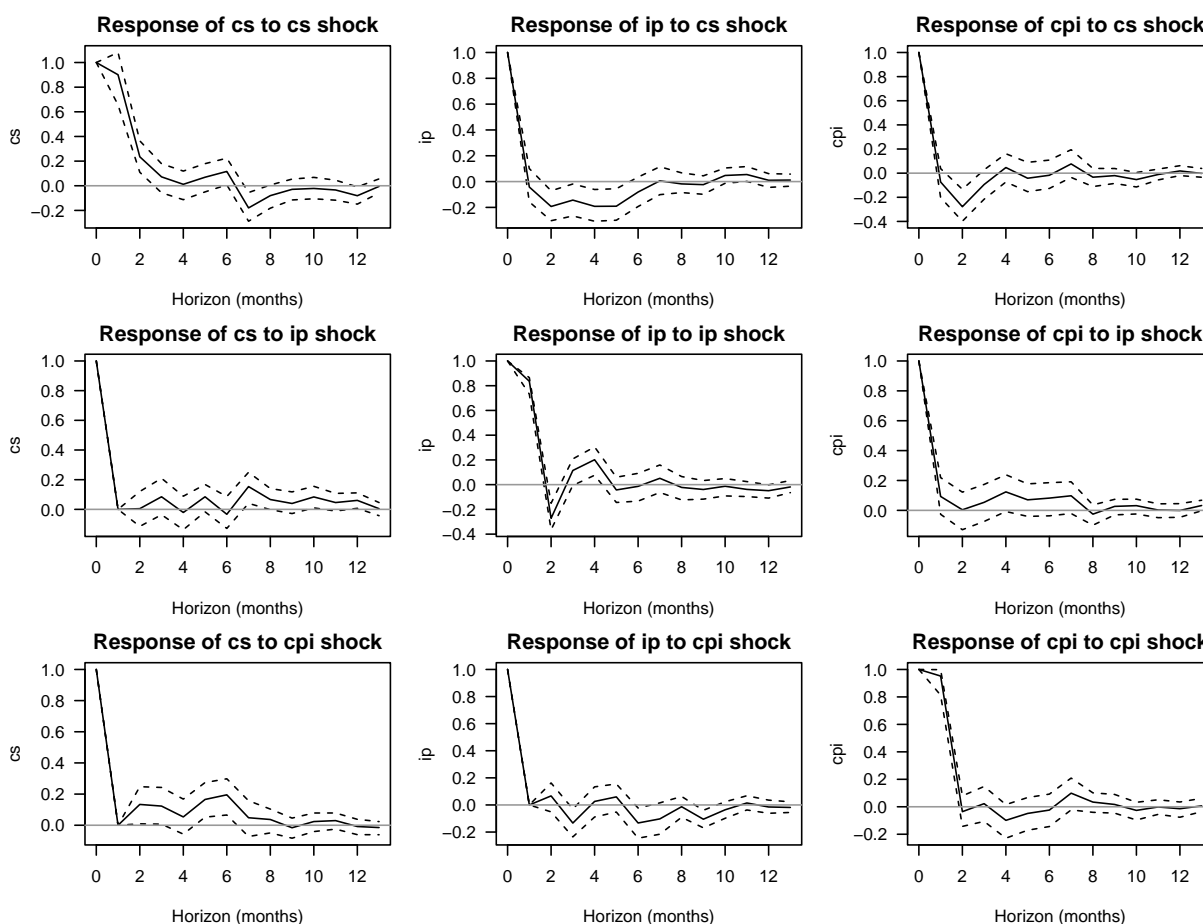
This recursive ordering reflects the assumed speed at which each variable responds to exogenous shocks or new information. The structure is consistent with standard economic intuition.

We place **credit spreads** first, since financial markets, under the assumption of at least partial informational efficiency, are expected to react almost instantaneously to new information. As such, we treat changes in credit spreads as contemporaneously exogenous, allowing them to influence the other variables within the same month but not vice versa.

**Industrial production** is ordered second. Real economic activity typically responds to changes in financial conditions with a short delay (within the month), for example through adjustments in investment or inventory decisions. Moreover, industrial production data is often published with a lag, whereas credit spreads reflect real-time market information. This asymmetry in data availability further supports the chosen ordering.

Lastly, we place **consumer prices** at the end. Prices are generally sticky and slow to adjust due to nominal rigidities such as wage contracts, menu costs, or pricing norms. It is therefore plausible to assume that inflation does not contemporaneously affect either credit markets or real activity. However, inflation itself may respond within the same period to shocks in credit spreads and output.

**Exercise 2.5: Show the orthogonalized impulse response functions for your system**



**Response to a 1 SD increase in Credit Spread change** The credit spread (CS) jumps sharply on impact, as expected, and gradually decays back toward zero by month 3–4. This suggests short-lived persistence of shocks in the growth rate of credit spreads.

Industrial production (IP) growth responds notably: it falls sharply over the first two months (peak drop around  $-0.3$  SD), then slowly recovers, returning close to baseline around month 6–8.

Inflation (CPI) growth also dips initially (trough around  $-0.25$  SD at month 2) but recovers more quickly—already by month 3, effects are minor and mostly indistinguishable from zero.

Overall, a one-standard-deviation tightening in financial conditions (wider credit spread) leads to a short-run contraction in both output and prices. Even though the effects on growth rates are transitory, all series are  $I(1)$ , meaning that in levels, both IP and CPI are pushed onto a lower trajectory. This implies persistent real-side consequences from temporary financial stress.

**Response to a 1 SD increase in MoM output growth (IP)** Credit spreads exhibit no notable response to an output growth shock—this is largely mechanical due to the Cholesky ordering, which assumes output does not contemporaneously affect spreads.

The response of inflation is modest and delayed, peaking at around  $+0.1$  standard deviations in month 4 before gradually reverting to zero. However, given the width of the confidence bands, we cannot conclude that this effect is statistically distinguishable from zero.

Industrial production growth displays the familiar overshooting pattern: a slight dip below zero in months 1–2, followed by a return to baseline around month 6. This is consistent with a temporary acceleration in output growth that gradually normalizes.

**Response to a 1 SD increase in MoM inflation (CPI)** Neither credit spreads nor industrial production growth show any meaningful response to a CPI shock. This is consistent with the imposed cholesky ordering.

Even the CPI growth rate itself shows no persistence: it initially overshoots and then quickly reverts. The lack of amplification implies that CPI shocks are largely absorbed without broader macro spillovers.

## General Comments

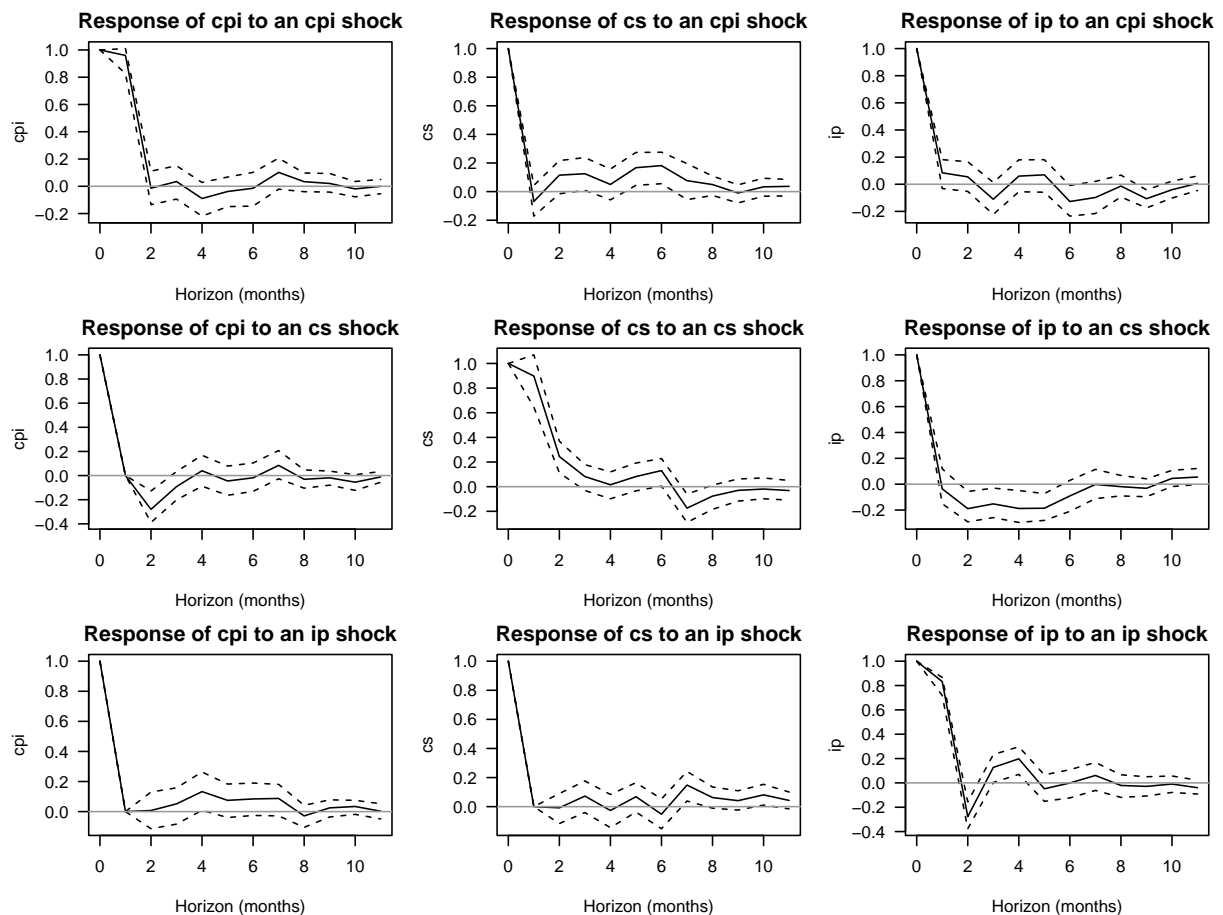
Across all responses, impulse effects are modest and short-lived—most return to zero within 6–8 months. Since the VAR was estimated in first differences, this implies the level variables experience small but permanent shifts.

Importantly, the Cholesky ordering (CS → IP → CPI) shapes the results. By placing CS first, we assume financial conditions affect the real and nominal sides contemporaneously, but not the other way around. This assumption helps identify financial shocks cleanly, but alternative orderings could change estimated effects especially for inflation dynamics.

Finally, while the magnitudes are not large (typically around 0.1–0.3 SD), they are meaningful given the monthly frequency. The real-side response to financial shocks is consistent with what we would expect from the literature, even if the estimated effects are not dramatic.

*NB: Since all series are non-stationary, we had to apply first differencing before estimating the VAR. While this ensures statistical validity, it also makes the results somewhat harder to interpret economically.*

## Exercise 2.6: Modify the ordering of the variables and comment how this affects your results



As an alternative Cholesky ordering, we test **CPI → Credit Spread → Industrial Production**. The idea is that inflation shocks arrive first, prompting an immediate reaction in financial markets. Real

activity responds last, adjusting only after observing both the inflation surprise and its impact on credit conditions.

**Comment on the impact of a shock to MoM CPI growth rate:**

CPI jumps sharply on impact and reverts to baseline within 2–3 months, followed by a small and statistically insignificant rebound. Credit spreads respond mildly, with a delayed increase of about +0.1 SD around months 3–5, before fading out. Industrial production declines modestly, reaching a trough of –0.15 SD in month 2, then gradually returns to baseline by month 6. However, the responses of both credit spreads and industrial production are not statistically different from zero.

**Interpretation:** While the direction of effects aligns with economic intuition, tightening spreads and lower output, none of the responses are statistically significant. We therefore find no strong evidence of meaningful transmission following a CPI shock.

**Comment on the impact of a shock to the credit spread change:**

Credit spreads spike on impact and gradually decline over 4–5 months, indicating a persistent tightening in financial conditions. CPI falls briefly by about –0.3 SD, but the response is not statistically significant—likely a result of the imposed Cholesky structure. Industrial production reacts more strongly, declining to around –0.25 SD by month 4 and remaining below zero throughout most of the horizon.

**Interpretation:** Financial tightening has a clear and persistent effect dampening effect on output growth. Additionally, financial tightening seems somewhat persistent.

**Comment on the impact of an shock to the Industrial-production MoM growt rate**

IP growth shows the standard transitory pattern—sharp increase on impact, then an undershoot and return to baseline by month 6. Given the Cholesky ordering, neither CPI nor credit spreads respond significantly.