$$\frac{\Delta(n-1)}{\Delta(n)} = \frac{d+n-2}{d(d+n-2)-(n-1)} = \frac{d+(n-2)}{(d-1)[d+(n-1)]}$$

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$$\Delta(n) \;=\; (d-1)^{n-1}(d+n-1)$$