

1. Set up but do not evaluate the double integrals to compute the areas of the following:

(a) (10 points) The unit semicircle above the x -axis.

Solution:

$$\int_{-1}^1 \int_0^{\sqrt{1-x^2}} 1 \, dy dx$$

(b) (10 points) The region bounded by $x = y^2$ and $y = x - 2$.

Solution:

$$\int_1^4 \int_{y^2}^{y+2} 1 \, dx dy$$

2. (20 points) Compute

$$\int_0^1 \int_y^1 e^{-x^2} \, dx dy$$

Here is a guided approach that you may optionally follow.

- (a) (5 points) Draw and shade the region
 (b) (5 points) Exchange the integrals with the aid of the picture drawn in the previous part.
 (c) (10 points) Compute the iterated integrals $\iint_R e^{-x^2} \, dy dx$.

Solution:

$$\int_0^1 \int_y^1 e^{-x^2} \, dx dy = \int_0^1 \int_0^x e^{-x^2} \, dy dx = \int_0^1 x e^{-x^2} \, dx$$

Then use the u -sub $u = -x^2$.

3. (20 points) For the region R bounded by the curves $x = y^2$ and $y = x$, compute

$$\iint_R 3x + 2y \, dA$$

Solution:

$$\iint_R 3x + 2y \, dA = \int_0^1 \int_{y^2}^y 3x + 2y \, dx dy$$

or

$$= \int_0^1 \int_x^{\sqrt{x}} 3x + 2y \, dy dx$$