

AP PHYSICS C: UNIVERSAL GRAVITATION

Directions: Each of the questions or incomplete statements below is followed by five suggested answers or completions. Select the one that is best in each case and place the letter of your choice in the corresponding box on the student answer sheet.

Note: To simplify calculations, you may use $g = 10\text{ m/s}^2$ in all problems.

1. A 70 kg astronaut floats at a distance of 10 m from a 50 000 kg spacecraft. What is the force of attraction between the astronaut and spacecraft?
(A) $2.4 \times 10^{-6}\text{ N}$
(B) $2.4 \times 10^{-5}\text{ N}$
(C) Zero; there is no gravity in space.
(D) $2.4 \times 10^5\text{ N}$
(E) $2.4 \times 10^6\text{ N}$

2. The Earth is at an average distance of 1 AU from the Sun and has an orbital period of 1 year. Jupiter orbits the Sun at approximately 5 AU. About how long is the orbital period of Jupiter?
(A) 1 year
(B) 2 years
(C) 5 years
(D) 11 years
(E) 125 years

3. A proposed “space elevator” can lift a 1000 kg payload to an orbit of 150 km above the Earth’s surface. The radius of the Earth is $6.4 \times 10^6\text{ m}$, and the Earth’s mass is $6.0 \times 10^{24}\text{ kg}$. What is the gravitational potential energy of the payload when it reaches orbit?
(A) $1.0 \times 10^3\text{ J}$
(B) $2.7 \times 10^6\text{ J}$
(C) $6.1 \times 10^{10}\text{ J}$
(D) $2.7 \times 10^{12}\text{ J}$
(E) $1.0 \times 10^{15}\text{ J}$

4. A satellite orbits the Earth at a distance of 200 km. If the mass of the Earth is $6.0 \times 10^{24}\text{ kg}$ and the Earth’s radius is $6.4 \times 10^6\text{ m}$, what is the satellite’s speed?
(A) $1.0 \times 10^3\text{ m/s}$
(B) $3.5 \times 10^3\text{ m/s}$
(C) $7.8 \times 10^3\text{ m/s}$
(D) $5 \times 10^6\text{ m/s}$
(E) $6.1 \times 10^7\text{ m/s}$

5. Mars orbits the Sun at a distance of $2.3 \times 10^{11}\text{ m}$. The mass of the Sun is $2.0 \times 10^{30}\text{ kg}$, and the mass of Mars is $6.4 \times 10^{23}\text{ kg}$. Approximately what is the gravitational force that the Sun exerts on Mars?
(A) $1.6 \times 10^{20}\text{ N}$
(B) $1.6 \times 10^{21}\text{ N}$
(C) $3.7 \times 10^{21}\text{ N}$
(D) $3.7 \times 10^{32}\text{ N}$
(E) $3.7 \times 10^{42}\text{ N}$

6. The mass of a planet is 1/4 that of Earth and its radius is half of Earth’s radius. The acceleration due to gravity on this planet is most nearly
(A) 2 m/s^2
(B) 4 m/s^2
(C) 5 m/s^2
(D) 10 m/s^2
(E) 20 m/s^2

7. When climbing from sea level to the top of Mount Everest, a hiker changes elevation by 8848 m. By what percentage will the gravitational field of the Earth change during the climb? (The Earth’s mass is $6.0 \times 10^{24}\text{ kg}$, and its radius is $6.4 \times 10^6\text{ m}$.)
(A) It will increase by approximately 0.3 %.
(B) It will decrease by approximately 0.3 %.
(C) It will increase by approximately 12 %.
(D) It will decrease by approximately 12 %.
(E) The gravitational field strength will not change.

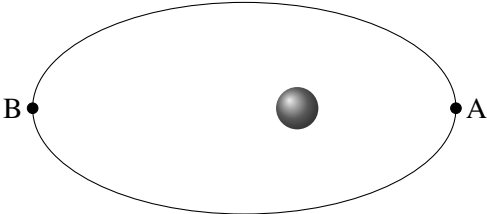
8. Four planets, A through D, orbit the same star. The relative masses and distances from the star for each planet are shown in the table. For example, Planet A has twice the mass of Planet B, and Planet D has three times the orbital radius of Planet A. Which planet has the highest gravitational attraction to the star?

Planet	Relative mass	Relative distance
A	$2m$	r
B	m	$0.1r$
C	$0.5m$	$2r$
D	$4m$	$3r$

(A) Planet A
(B) Planet B
(C) Planet C
(D) Planet D
(E) All have the same gravitational attraction to the star.

9. A satellite orbits the Earth at a distance that is four times the radius of the Earth. If the acceleration due to gravity near the surface of the Earth is g , the acceleration of the satellite is most nearly
(A) zero
(B) $\frac{g}{2}$
(C) $\frac{g}{4}$
(D) $\frac{g}{8}$
(E) $\frac{g}{16}$

10. A satellite orbits the Earth in an elliptical orbit, with point A being close to the Earth and point B farther away. As the satellite moves from point A to point B, which of the following is true of the angular momentum and kinetic energy of the satellite?

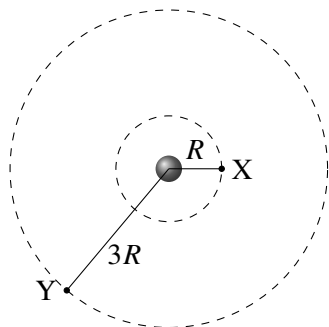


	Angular momentum	Kinetic energy
(A)	Increases	Remains constant
(B)	Remains constant	Increases
(C)	Decreases	Remains constant
(D)	Remains constant	Decreases
(E)	Remains constant	Remains constant

11. Two planets of mass M and $9M$ are in the same solar system. The radius of the planet of mass M is R . In order for the acceleration due to gravity to be the same for each planet, the radius of the planet of mass $9M$ would have to be
(A) $\frac{R}{2}$
(B) R
(C) $2R$
(D) $3R$
(E) $9R$

12. A satellite is in a stable circular orbit around the Earth at a radius R and speed v . At what radius would the satellite travel in a stable orbit with a speed $2v$?
(A) $\frac{R}{4}$
(B) $\frac{R}{2}$
(C) R
(D) $2R$
(E) $4R$

13. Two planets, X and Y, orbit a star. Planet X orbits at a radius R , and Planet Y orbits at a radius $3R$. Which of the following best represents the relationship between the acceleration a_X of Planet X and the acceleration a_Y of Planet Y?



- (A) $a_X = 9a_Y$
 (B) $9a_X = a_Y$
 (C) $a_X = 3a_Y$
 (D) $3a_X = a_Y$
 (E) $a_X = a_Y$
14. A planet orbits at a radius R around a star of mass M . The period of orbit of the planet is

- (A) $\sqrt{\frac{4\pi^2 R^2}{GM}}$
 (B) $\frac{4\pi^2 R^3}{GM}$
 (C) $\sqrt{\frac{4\pi^2 R^3}{GM}}$
 (D) $\sqrt{\frac{4\pi^2 R}{GM}}$
 (E) $\frac{GM}{4\pi^2 R}$

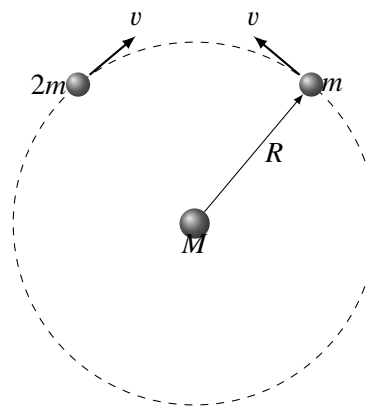
15. A moon orbits a large planet in an elliptical orbit, with its closest approach at a distance a , and its farthest distance b . The speed of the moon at point b is v . The speed at point a is

- (A) $\frac{av}{b}$
 (B) $\frac{bv}{a}$
 (C) $\frac{(a+b)v}{b}$
 (D) $\frac{(b-a)v}{b}$
 (E) $\frac{2bv}{a}$

16. A satellite orbits the Earth in an elliptical orbit. Which of the following statements is true?
- (A) The angular velocity of the satellite increases as it travels farther from the Earth.
 (B) The acceleration of the satellite increases as it travels closer to the Earth.
 (C) The angular momentum of the satellite increases as it travels closer to the Earth.
 (D) The potential energy of the satellite is equal to its kinetic energy at all points in the orbit.
 (E) The speed of the satellite must remain constant for it to remain in orbit around the Earth.

Questions 17–18

Two moons of mass m and $2m$ orbit a planet of mass M at the same radius R and speed v toward each other, as shown. The moons collide and stick together without destroying either moon.



17. The total momentum of the moons after the collision is

- (A) mv
 (B) $2mv$
 (C) $3mv$
 (D) $6mv$
 (E) zero

18. The velocity of the two masses after the collision above is

- (A) v counterclockwise
 (B) $v/2$ counterclockwise
 (C) $v/2$ clockwise
 (D) $v/3$ counterclockwise
 (E) $v/3$ clockwise

19. A satellite of mass m travels in an elliptical orbit around a planet of mass M . The satellite has a speed v when it is closest to the planet at a distance r . Work is done by the engines of the satellite to change its orbit to a circular orbit when it is at this distance r . Which of the following statements is true of the transition from an elliptical orbit to a circular orbit?

- (A) The work done by the satellite engines to change the orbit is equal to the change in kinetic energy of the satellite.
 (B) The work done by the satellite engines to change the orbit is equal to the change in potential energy of the satellite.
 (C) The work done by the satellite engines to change the orbit is equal to the change in angular momentum of the satellite.
 (D) The work done by the satellite engines to change the orbit is equal to the change in speed of the satellite.
 (E) The work done by the satellite engines to change the orbit is equal to the change in orbital radius of the satellite.

20. A satellite of mass m orbits the Earth with a potential energy U and a kinetic energy K . Which of the following statements would have to be true for the satellite to escape the Earth's gravity completely?
- (A) The kinetic energy of the satellite would have to be equal to the potential energy between the Earth and the satellite.
 (B) The potential energy between the Earth and the satellite would have to be greater than the kinetic energy of the satellite.
 (C) The total energy of the satellite would have to be greater than the kinetic energy of the satellite.
 (D) The kinetic energy of the satellite would have to be greater than the potential energy of the satellite.
 (E) The total energy of the satellite would have to be equal to the potential energy of the satellite.

AP PHYSICS C: UNIVERSAL GRAVITATION
SECTION II
4 Questions

Directions: Answer all questions. The parts within a question may not have equal weight. All final numerical answers should include appropriate units. Credit depends on the quality of your solutions and explanations, so you should show your work. Credit also depends on demonstrating that you know which physical principles would be appropriate to apply in a particular situation. Therefore, you should clearly indicate which part of a question your work is for.

**I NEED ONE MORE FREE-RESPONSE QUESTION
FROM PREVIOUS EXAMS SO THAT I CAN REMOVE
SOME OF THE SHORTER QUESTIONS.
WANT TOTAL OF 4 QUESTIONS**

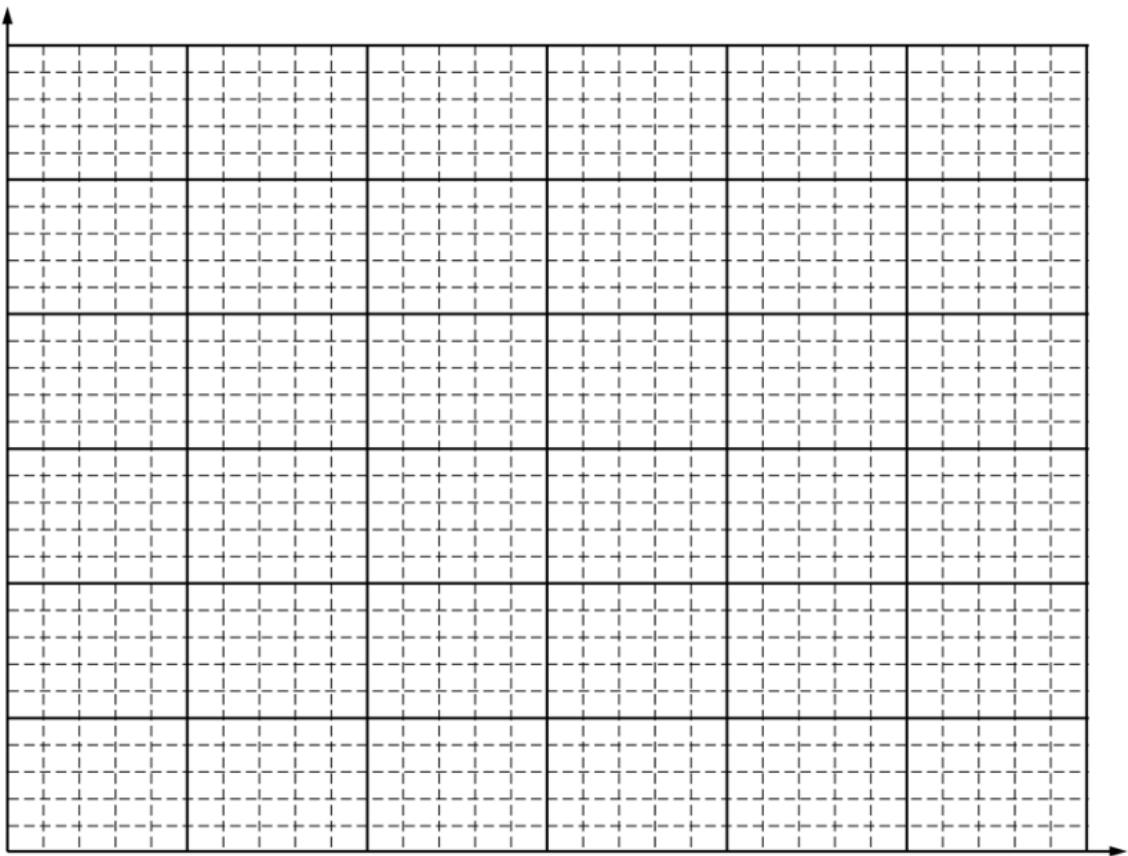
1. In March 1999 the Mars Global Surveyor (GS) entered its final orbit about Mars, sending data back to Earth. Assume a circular orbit with a period of 1.18×10^2 minutes = 7.08×10^3 s and orbital speed of 3.40×10^3 m/s. The mass of the GS is 930 kg and the radius of Mars is 3.43×10^6 m.
- (a) Calculate the radius of the GS orbit.
 - (b) Calculate the mass of Mars.
 - (c) Calculate the total mechanical energy of the GS in this orbit.
 - (d) If the GS was to be placed in a lower circular orbit (closer to the surface of Mars), would the new orbital period of the GS be greater than or less than the given period? Justify your answer.

_____ Greater than _____ Less than
 - (e) In fact, the orbit the GS entered was slightly elliptical with its closest approach to Mars at 3.71×10^5 m above the surface and its furthest distance at 4.36×10^5 m above the surface. If the speed of the GS at closest approach is 3.40×10^3 m/s, calculate the speed at the furthest point of the orbit.

2. A student is given the set of orbital data for some of the moons of Saturn shown below and is asked to use the data to determine the mass M_S of Saturn. Assume the orbits of these moons are circular.

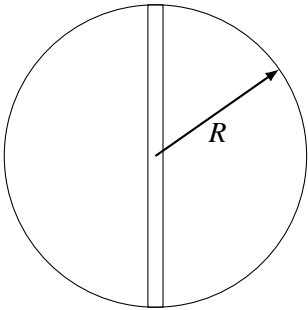
Orbital Period, T (seconds)	Orbital Radius, R (meters)		
8.14×10^4	1.85×10^8		
1.18×10^5	2.38×10^8		
1.63×10^5	2.95×10^8		
2.37×10^5	3.77×10^8		

- (a) Write an algebraic expression for the gravitational force between Saturn and one of its moons.
- (b) Use your expression from part (a) and the assumption of circular orbits to derive an equation for the orbital period T of a moon as a function of its orbital radius R .
- (c) Which quantities should be graphed to yield a straight line whose slope could be used to determine Saturn’s mass?
- (d) Complete the data table by calculating the two quantities to be graphed. Label the top of each column, including units.
- (e) Plot the graph on the axes below. Label the axes with the variables used and appropriate numbers to indicate the scale.



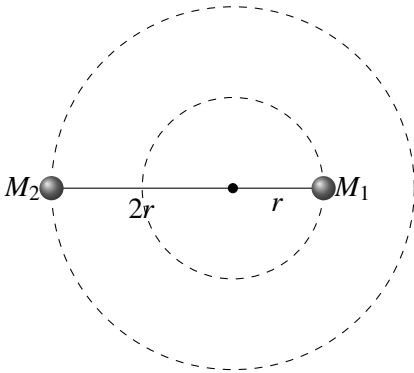
- (f) Using the graph, calculate a value for the mass of Saturn.

3. A planet of mass M , radius R , and uniform density has a small tunnel drilled through the center of the planet, as shown below. When the mass is inside the tunnel, it experiences a force of $F = (GmM/R^3)r$, whereas when the mass is outside of the planet, it experiences a gravitational force of $F = GmM/r^2$.



- (a) Setting the potential energy of the mass to be zero at the planet's center, calculate the mass's potential energy as a function of distance from the center of the planet $U(r)$, for values $r < R$. Sketch this potential function.
- (b) If the mass is dropped from R from the center of the planet, how long will it take until it returns to its original position?
- (c) If the mass is dropped from $R/2$ from the center of the planet, will it require more, or less, or the same amount of time to return to its original position compared to if it was dropped from R ?
- (d) If the mass is dropped from $2R$ from the center of the planet, will it require more, or less, or the same amount of time to return to its original position compared to if it was dropped from R ?

4. Two stars of unequal mass orbit each other about their common center of mass as shown. The star of mass M_1 orbits in a circle of radius r , and the star of mass M_2 orbits in a circle of radius $2r$.



- (a) Determine the ratio of masses M_1/M_2 .
- (b) Determine the ratio of the acceleration a_1 of M_1 to the acceleration a_2 of M_2 .
- (c) Determine the ratio of the period T_1 of M_1 to the period T_2 of M_2 .