



sphere with uniform charge density ρ

total charge

$$Q = \rho V = \frac{4}{3}\pi R^3 \rho \rightarrow \rho = \frac{3Q}{4\pi R^3} \quad \left. \begin{array}{l} \text{positive.} \\ \text{constant.} \end{array} \right\}$$

1. What is the electric field inside the sphere?
2. What is the electric field outside of the sphere?

1. Gaussian surface inside the sphere at radius $r < R$

$$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E(A) = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{Q}{\epsilon_0 R^3} \rho r^3$$

$$E = \frac{Q}{4\pi\epsilon_0 R^3} r$$

$$E \propto r$$

$$E = \frac{kQ}{R^3} r$$

$$\rho V = \left(\frac{3Q}{4\pi R^3} \right) \left(\frac{4}{3}\pi r^3 \right) = \frac{Q}{R^3} r^3$$

2. Gaussian surface outside of the sphere at radius $r > R$

$$\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E(A) = \frac{Q_{\text{enc}}}{\epsilon_0}$$

$$E(4\pi r^2) = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{4\pi\epsilon_0 r^2} \rightarrow \frac{kQ}{r^2}$$

looks a point charge.

