# **Topic 17: Nuclear Physics**

AP Physics 2

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Olympiads School

# Nucleus of the Atom

#### The Rutherford-Bohr Model

In the Rutherford-Bohr atomic model, an atom consists of

- A dense positively-charged nucleus
- Negatively-charged electrons "orbiting" the nucleus in predefined energy levels
- Most of the atom is empty space

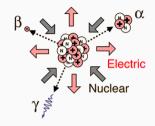
Most of the atom is empty space, although almost all the mass is concentrated at the nucleus

#### **Nucleus of an Atom**

The nucleus—where most of the mass of the atom is concentrated—are made up of **nucleons** which are:

- Positively charged protons, and
- Electrically neutral neutrons

## **Balancing Fundamental Forces**



The nucleus of an atom is held together by balancing two fundamental forces:

- Electromagnetic force: the repulsive force between protons
  - The force drop off as the square of the distance (inverse square law)
- Nuclear strong force: short-distance force holding nucleons together
  - ullet Attractive between nucleons at about 1 fm ( $10^{-15}\,\mathrm{m}$ )
  - Insignificant at distances beyond 2.5 fm
  - Repulsive at distances below 0.7 fm

## **Atomic Properties**

The nucleus of an atom is identified by two numbers:



- Atomic number (Z): the number of protons
  - · Determines what element it is, and
  - its chemical properties
- Mass number (A): number of nucleons
- The number of neutrons (N) is therefore N = A Z

### **Isotopes**

Carbon has three common **isotopes**, all with the same atomic numbers, but different number of neutrons (called "carbon-12", "carbon-13" and "carbon-14" respectively). The atomic number is sometimes omitted.

$$^{12}C$$
  $^{13}C$   $^{14}C$ 

Hydrogen also has three common isotopes (hydrogen, deuterium and tritium)

$$^{1}H$$
  $^{2}H$   $^{3}H$ 

On average, there are 2.6 isotopes for each element.

6

#### Mass of the Nucleus

The **unified atomic mass unit** (u)<sup>1</sup> is defined as 1/12 of the rest mass of a carbon-12 atom in its nuclear ground state:

$$1 \, \mathrm{u} = \frac{1}{12} m(^{12}\mathrm{C}) \approx 1.660 \, 54 \times 10^{-27} \, \mathrm{kg}$$

The rest mass of the elementary particles can be expressed in this unit:

<b>Particle</b>	Mass (u)	Mass (kg)
Proton	1.007 276	$1.672614 \times 10^{-27}$
Neutron	1.008 665	$1.674920\times10^{-27}$
Electron	0.000 549	$9.10956\times10^{-31}$

<sup>&</sup>lt;sup>1</sup>It replaces the "atomic mass unit" (amu) which is no longer used. The atomic mass value in the periodic table is a weighted average across all isotopes.

**Mass Defect & Nuclear Binding** 

**Energy** 

## Mass-Energy Equivalence

One of the discoveries in special relativity<sup>2</sup> is the fundamental equivalence of mass and energy. While it is based on *relativistic kinematics*, it also applies to *quantum mechanics*, from which nuclear physics is based on.

$$E = mc^2$$

Quantity	Symbol	SI Unit
Energy	E	J
Rest mass of a particle	m	kg
Speed of light	С	m/s

The speed of light is a universal constant:  $c = 2.998 \times 10^8$  m/s.

<sup>&</sup>lt;sup>2</sup>Einstein, A., "Does the Inertia of a Body Depend Upon Its Energy Content?", *Annelen der Physik*, 18(13):639-641, 21 November, 1905.

## Mass-Energy Equivalence

Any change in energy is *always* accompanied by a change in mass, and vice versa.

$$E = mc^2 \longrightarrow \Delta E = \Delta mc^2$$

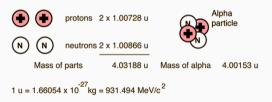
- The concept is difficult to visualize in everyday life. Example: A baseball moving at  $160 \, \mathrm{km/h}$  is more massive than a baseball travelling at  $20 \, \mathrm{km/h}$ , but the  $\Delta m$ s is too small to measure.
- But in cases when
  - speeds approaches the speed of light (v > 0.3c), or when
  - the masses are small (e.g. electrons, protons, neutrons)

the difference significant

9

#### **Mass Defect**

The sum of the masses of the nucleons are always higher than the mass of the nucleus itself. **Example:** the mass of the alpha particle (helium nucleus) is lower than 2 protons plus 2 neutrons:



#### **Mass Defect**

This difference in mass is called the **mass defect**  $\Delta m$ , which can be calculated with a simple equation:

$$\Delta m = [Zm_P + (A - Z)m_N] - m_A$$

Quantity	Symbol	SI Unit
Mass defect	$\Delta m$	kg
Atomic number and mass numbers	Z, A	
Rest mass of a proton and neutron	$m_P, m_N$	kg
Rest mass of the nucleus	$m_A$	kg

11

#### **Mass Defect**

Mass defect exists in all nuclei because the nucleus of an atom is always in a lower energy state than the individual nucleons alone

#### Similar examples:

- The total energy of a planet orbiting the Sun is lower than the planet and the Sun individually
- An electron orbiting the nucleus is at a lower energy state also

## **Nuclear Binding Energy**

The amount of energy that is equivalent to the mass defect is called the **nuclear binding** energy  $E_b$ , defined as:

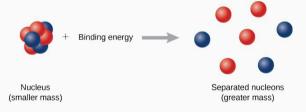
$$E_b = (\Delta m)c^2$$

Quantity	Symbol	SI Unit
Nuclear binding energy	$E_b$	J
Mass defect	$\Delta m$	kg
Speed of light	С	m/s

- The energy required to break up the nucleus into its individual nucleons
- Generally expressed in electron volts (eV) where  $1\,\text{eV}=1.602\times 10^{-19}\,\text{J}$ , rather than in joules

## **Nuclear Binding Energy**

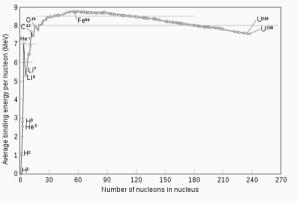
The nuclear binding energy is the amount of work required to separate the nucleons



The higher the binding energy, the more *tightly bound* a nucleus is, therefore more work is required to separate the nucleons

## Nuclear Binding Energy & Stability of the Nucleus

The nuclear binding energy is highest for iron-56 ( $E_b = 492.275 \,\text{MeV}$ , or  $8.7906 \,\text{MeV}$  per nucleon)



It means that the nucleus

- requires the most energy to separate the nucleons
- most tightly bound
- most stable

To achieve greater stability in the nucleus

- Heavier atoms can split into lighter nuclei, while
- Lighter atoms can combine into heavier nuclei

**Radioactivity** 

## **Radioactive Decay**

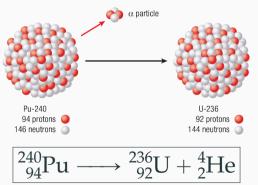
**Radioactivity**<sup>3</sup> is the spontaneously disintegration of a nucleus. There are *three* types of radioactive decay:

- Alpha decay, or  $\alpha$ -decay
- **Beta decay**, or  $\beta$ -decay
- Gamma decay, or  $\gamma$ -decay

<sup>&</sup>lt;sup>3</sup>Or radioactive decay

## **Alpha Decay**

In  $\alpha$ -decay, an **alpha particle** (a helium-4 nucleus, with 2 protons and 2 neutrons), is spontaneously emitted from the nucleus. Example: plutonium-240 nucleus decays into a uranium-236 nucleus, emitting an alpha particle



Note the binding energy in the helium-4 nucleus in previous slides

## General Formula for Alpha Decay

The general formula for an  $\alpha$ -decay is shown by the equation:

$$\begin{bmatrix} {}^{A}_{Z}X \longrightarrow {}^{A-4}_{Z-2}Y + {}^{4}_{2}He \end{bmatrix}$$

The **parent atom** (X) is the "reactant", and the **daughter atom** (Y) is the "product". This reaction is called a **transmutation**, because a new element is formed.

- The nuclear binding energy of the daughter atom and the alpha particle are *higher* than the parent atom.
- The combined mass of the daughter atom plus the alpha particle is *lower* than the parent atom, meaning that energy is released

### **Beta Decays**

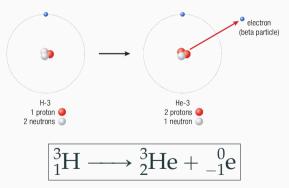
**Beta decays** involve the emission/capture of a **beta particle** (electron or a positron). There are three types of beta decays:

- Beta-negative decay (emission of an electron)
- Beta-positive decay (emission of an positron)
- Electron capture

Beta decays generally occur in smaller (less massive) nuclei

## **Beta-Negative Decay**

In a **beta-negative decay** ( $\beta^-$ -decay), a neutron spontaneously decays into a proton and an electron, and the electron is ejected from the nucleus. For example, the  $\beta^-$ -decay of a tritium atom is:



## **Beta-Negative Decay**

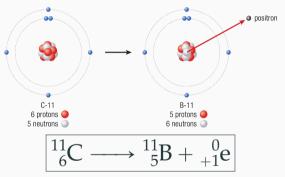
The general form for  $\beta^-$ -decay is given by:

$${}^{A}_{Z}X \longrightarrow {}^{A}_{Z+1}Y + {}^{0}_{-1}e$$

The daughter atom has a higher nuclear binding energy than the parent atom. This decay is also a transmutation because a new element is formed.

### **Beta-Positive Decay**

In **beta-positive decay** ( $\beta^+$ -decay), a proton spontaneously decays into a neutron and a positron. Example: decay of carbon-11 into boron-11:



A positron has the same mass as an electron, but with a *positive* elementary charge. It is not a stable particle.

22

### **Beta-Positive Decay**

The general equation for  $\beta^+$ -decay is given by:

$${}^{A}_{Z}X \longrightarrow {}^{A}_{Z-1}Y + {}^{0}_{+1}e$$

Similar to a  $\beta^-$  decay, the daughter nucleus has a higher nuclear binding energy than the parent nucleus (i.e. lower energy state). This decay is also a transmutation because a new element is formed.

#### **Electron-Positron Annihilation**

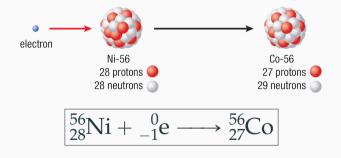
The positron released in the decay will be (almost) immediately *annihilated*<sup>4</sup> by another electron, releasing a pair of gamma particle (photons with no mass), each with an energy of 0.511 MeV, moving in opposite directions at the speed of light:

$$\boxed{ {}^{0}_{+1} e + {}^{0}_{-1} e \longrightarrow 2 \left( {}^{0}_{0} \gamma \right) }$$

<sup>&</sup>lt;sup>4</sup>It means that the two particles collide, and all of their masses are converted into energy

## **Electron Capture**

**Electron capture** is a rarer form of beta decay where an electron is absorbed by a nucleus and combines with a proton to form a neutron. For example, a nickel-56 nucleus can capture an electron to form a cobalt-56 nucleus:



## **Electron Capture**

The general equation for electron capture is given by:

$$\begin{bmatrix} {}^{A}_{Z}X + {}^{0}_{-1}e & \longrightarrow {}^{A}_{Z-1}Y \end{bmatrix}$$

The electron that is absorbed usually comes from the lowest energy shell (n = 1, or "K-shell") that is closest to the nucleus, so it is often called *K-capture*.

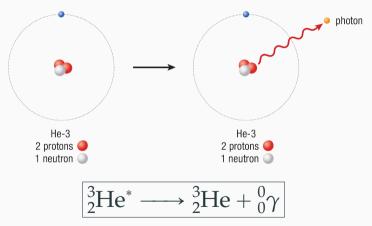
#### **Gamma Radiation**

**Gamma decay** ( $\gamma$ -decay) occurs after a nuclear reaction (e.g.  $\alpha$  or  $\beta$  decay)

- The daughter nucleus is in a high-energy (excited) state
- The nucleus spontaneously releases energy in a **gamma particle** to return to a lower (therefore more stable) energy state.
- A gamma particle:
  - is a highly energetic form of electromagnetic radiation that is emitted as a **photon**
  - Has zero mass

### **Gamma Radiation**

As an example, the  $\gamma$ -decay of a helium-3 atom is given by:



#### **Gamma Radiation**

The general equation for  $\gamma$ -decay is:

- The parent and daughter nuclei are identical
- Only the energy level of the nucleus has changed
  - The asterisk indicates that the parent an excited state
- Notice that the mass number and atomic number of a gamma ray  $\binom{0}{0}\gamma$  are both zero.

## **Energies of Radiation**

Radioactive particles post danger to living tissues, because

- they can ionize (or strip the electrons from) atoms
- $\bullet$   $\alpha$  particles have strongest ionizing ability, but can only travel a relatively short distance before becoming absorbed
- $\beta$  particles and  $\gamma$  rays have a greater penetrating range in air and must be shielded against

Туре	Radiation	Charge	Penetrating Ability
α-decay	Alpha particle (He-4 nucleus)	+2	Skin or paper
$eta^-$ -decay	Beta particle (electron)	-1	thin sheet of aluminum
$eta^+$ -decay	Beta particle (positron)	+1	thin sheet of aluminum
$e^-$ capture	None	N/A	N/A
$\gamma$ -decay	Gamma particle (photon)	0	Few centimetres of lead

#### Half-Life

While the radioactive decay of a single atom is *random* (like all quantum mechanics, radioactivity is driven by probability), when there are a large number of atoms, the overall rate of decay is very predictable.

$$N(t) = N_0 \left(\frac{1}{2}\right)^{\frac{t}{\tau}}$$

Quantity	Symbol	SI Unit
Amount of radioactive material	N(t)	kg
Initial sample amount	$N_0$	kg
Time	t	S
Half-life	τ	S

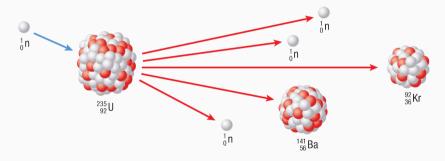
**Half-life:** the time it requires for a radioactive material to decay to half of its original amount.

## **Half-Life of Radioactive Isotopes**

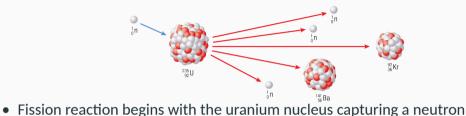
The half-life of radioactive substance can vary from a fraction of a second to billions of years.

Substance	Half-Life $(t_0)$
Polonium-215	0.0018 s
Bismuth-212	60.5  s
Sodium-24	15 h
Iodine-131	$8.07\mathrm{d}$
Cobalt-60	5.26 yr
Radium-226	1600 yr
Uranium-238	$4.5  imes 10^9\mathrm{yr}$

The release of energy in a nuclear reaction primarily comes from **nuclear fission**, where a heavier atomic is split into lighter atoms. For example, the fission reaction of uranium-235 splitting into krypton-92 and barium-141 atoms:



$$^{235}_{92}U + ^{1}_{0}n \longrightarrow ^{92}_{36}Kr + ^{141}_{56}Ba + 3 (^{1}_{0}n) + energy$$



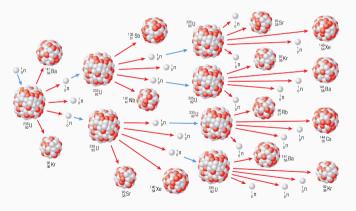
- The addition of the neutron defense the neutron into a device lead (dues) of the
- The addition of the neutron deforms the nucleus into a double-loped "drop" shape
- The attractive nuclear strong force can no longer hold the two fragments together, and they electrically repel each other away
- In splitting the atom, several neutrons are released from the nucleus
- The neutrons may be captured by other uranium-235 atoms, causing further reaction

- By probability, a nuclear fission is usually binary (two daughter nuclei in the process)
- Nuclear fuels can be
  - Fissile: the capture of any neutron will be sufficient to cause fission, e.g. <sup>235</sup>U or <sup>239</sup>Pu
  - **Fissionable:** requires additional energy from a fast-moving neutron to cause fission to begin, e.g. <sup>238</sup>U
- $\bullet$  Fission products usually cluster masses of  $95\pm15~\text{u}$  and  $135\pm15~\text{u}$

#### **Chain Reaction**

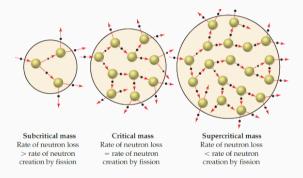
A chain reaction is a series of reactions that can repeat over several cycles

• Reactions occur without requiring any material being added to the system



#### **Critical Mass**

The amount of fuel required to sustain a chain reaction is called **critical mass** 



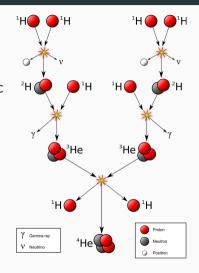
**Nuclear Fusion** 

#### **Proton-Proton Reaction**

The simplest fusion reaction occurs under high temperature about  $4\times 10^7$  K is the proton-proton chain. In most the basic form, it is written as:

$$4\begin{pmatrix} {}^{1}_{1}H\end{pmatrix} \longrightarrow {}^{4}_{2}He + 2\begin{pmatrix} {}^{0}_{+1}e\end{pmatrix} + energy$$

In each p-p reaction, 26.732 MeV is released. The exact mechanism for the p-p chain is shown in the right.



## **CNO Cycle**

A fusion reaction that occurs in even higher temperatures (between 1.5 to  $1.7 \times 10^7$  K) is the carbon-nitrogen-oxygen (CNO) cycle. The total energy released in one cycle is 26.73 MeV.

• The core temperature of the sun is about  $1.56\times10^7$  K, so only 1.7% of helium-4 nuclei produced in the Sun are from this process

