

```

1  #!/usr/bin/env python3
2  # vim: ts=2 sw=2 sts=2 et :
3
4  /sublime.py [OPTIONS]
5  (c)2022 Tim Menzies <timm@ieee.org>, BSD license
6  S.U.B.L.I.M.E. =
7  Sublime's unsupervised bifurcation: let's infer minimal explanations.
8
9  OPTIONS:
10
11  -Max      max numbers to keep      : 512
12  -Some     find 'far' in this many eggs : 512
13  -cautious On any crash, stop+show stack: False
14  -data     data file                 : data/aut093.csv
15  -enough   min leaf size             : 5
16  -help     show help                 : False
17  -far      how far to look in 'Some' : 9
18  -p        distance coefficient       : 2
19  -seed     random number seed        : 10019
20  -todo     start up task              : nothing
21  -xsmall   Cohen's small effect       : .35
22
23  ## See Also
24
25  [issues](https://github.com/timm/sublime/issues)
26  :: [repo](https://github.com/timm/sublime)
27  :: [view source](https://github.com/timm/sublime/blob/main/docs/pdf)
28
29  
30  
31  
32  <a href=https://github.com/timm/sublime/actions/workflows/main.yml><img
33  src=https://github.com/timm/sublime/actions/workflows/main.yml/badge.svg></a>
34  (https://doi.org/10.5281/zenodo.5912461)
35
36  ## Algorithm
37
38  Stochastic clustering to generate tiny models. Uses random projections
39  to divide the space. Then, optionally, explain the clusters by
40  unsupervised iterative dichotomization using ranges that most
41  distinguish sibling clusters.
42
43  ### Example1: just bi-cluster on two distant points
44  ...
45  /sublime.py -c -s $RANDOM -t cluster
46
47  .. : 398
48  .. : 199
49  .. : 99
50  .. : 49 Lbs- Acc+ Mpg+
51  .. : 24 : [2255, 15.5, 30]
52  .. : 25 : [2575, 16.4, 30]
53  .. : 50
54  .. : 25 : [2110, 16.4, 30] <== best
55  .. : 25 : [2205, 16, 30]
56  .. : 100
57  .. : 50
58  .. : 25 : [2234, 15.5, 30]
59  .. : 25 : [2278, 16.5, 30]
60  .. : 50
61  .. : 25 : [2220, 15.5, 30]
62  .. : 25 : [2320, 15.8, 30]
63  .. : 199
64  .. : 99
65  .. : 49
66  .. : 24 : [2451, 16.5, 20]
67  .. : 25 : [3021, 15.5, 20]
68  .. : 50
69  .. : 25 : [3425, 17.6, 20]
70  .. : 25 : [3155, 16.7, 20]
71  .. : 100
72  .. : 50
73  .. : 25 : [4141, 13.5, 10]
74  .. : 25 : [4054, 13.2, 20]
75  .. : 50
76  .. : 25 : [4425, 11, 10]
77  .. : 25 : [4129, 13, 10]
78  ...
79
80  ### Example2: as above but split on range that most divides data
81  ...
82  /sublime.py -c -s $RANDOM -t xplain
83
84  .. Lbs- Acc+ Mgg+
85  .. : 398 : [2807, 15.5, 20]
86  198 <= Lbs < 454 : 167 : [3725, 14.5, 20]
87  .. Modl < 72 : 34 : [3609, 13, 20]
88  .. Modl >= 72 : 133 : [3735, 14.9, 20]
89  .. Cylr < 8 : 56 : [3336, 17, 20]
90  .. 77 <= Modl < 82 : 22 : [3410, 17.1, 20]
91  .. Modl < 77 or Modl >= 82 : 34 : [3233, 17, 20]
92  .. Cylr >= 8 : 77 : [4129, 13.2, 20]
93  .. Modl < 75 : 37 : [4274, 13, 10]
94  .. Modl >= 75 : 40 : [3962, 13.5, 20]
95  .. Lbs >= 302 : 35 : [4054, 13.2, 20]
96  Lbs < 198 or Lbs >= 454 : 231 : [2290, 16, 30] <== best
97  ...
98
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100
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118  NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
119  SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
120
121  """
122  import traceback, random, copy, math, sys, re
123  from random import random as r
124  from typing import Any

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125 #
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130 #
131 #
132
133 def any(a:list) -> Any:
134     "Return a random item."
135     return a[anywhere(a)]
136
137 def anywhere(a:list) -> int:
138     "Return a random index of list 'a'."
139     return random.randint(0, len(a)-1)
140
141 big = sys.maxsize
142
143 def atom(x):
144     "Return a number or trimmed string."
145     x=x.strip()
146     if x=="True": return True
147     elif x=="False": return False
148     else:
149         try: return int(x)
150         except: return float(x)
151         except: return x.strip()
152
153 def demo(do,all):
154     "Maybe run a demo, if we want it, resetting random seed first."
155     todo = dir(all)
156     if do and do != "all":
157         todo = [x for x in dir(all) if x.startswith(do)]
158     for one in todo:
159         fun = all.__dict__.get(one,"")
160         if type(fun)==type(demo):
161             random.seed(the.seed)
162             doc = re.sub(r'\n\s+', "\n", fun.__doc__ or "")
163             try:
164                 fun()
165                 print("PASS:", doc)
166             except Exception as e:
167                 all.fails += 0
168                 if the.cautious: traceback.print_exc(); exit(1)
169             else:
170                 print("FAIL:", doc, e)
171     exit(all.fails)
172
173 def file(f):
174     "Iterator. Returns one row at a time, as cells."
175     with open(f) as fp:
176         for line in fp:
177             line = re.sub(r'(\n|\r|\t)|#.*', '', line)
178             if line:
179                 yield [cell.strip() for cell in line.split(",")]
180
181 def first(a:list) -> Any:
182     "Return first item."
183     return a[0]
184
185 def merge(b4:list) -> list:
186     "While we can find similar adjacent things, merge them."
187     j,n,now = -1,len(b4),[]
188     while j < n-1:
189         j += 1
190         a = b4[j]
191         if j < n-2:
192             if merged := a.merge(b4[j+1]):
193                 a = merged
194                 j += 1 # we will continue, after missing one
195         now += [a]
196     # if 'now' is same size as 'b4', look for any other merges.
197     return b4 if len(now)==len(b4) else merge(now)
198
199 class o(object):
200     "Class that can pretty print its slots, with fast inits."
201     def __init__(i, **d): i.__dict__.update(**d)
202     def __repr__(i):
203         pre = i.__class__.__name__ if isinstance(i,o) else ""
204         return pre+'('+' '.join([f"{k} {v}" for k, v in
205                                 sorted(i.__dict__.items()) if str(k)[0] != "_"])]+')?'
206
207 def options(doc:str) -> o:
208     """Convert 'doc' to options dictionary using command line args.
209     Args cause two 'shortands': (1) boolean flags have no arguments (and mentioning
210     those on the command line means 'flip the default value'; (2) args need only
211     mention the first few of a key (e.g. -s is enough to select for -seed)."""
212     d={}
213     for line in doc.splitlines():
214         if line and line.startswith(" -"):
215             key, *_ = line.strip()[1:].split("#") # get 1st,last word on each line
216             for j,flag in enumerate(sys.argv):
217                 if flag and flag[0]=="-" and key.startswith(flag[1:]):
218                     x= "True" if x=="False" else "False" if x=="True" else sys.argv[j+1])
219             d[key] = atom(x)
220     if d["help"]: exit(print(re.sub(r'\n#.*', "", doc, flags=re.S)))
221     return o(**d)
222
223 def r() -> float:
224     "Return random number 0..1"
225     return random.random()
226
227 def rn(x:float, n=3) -> float:
228     "Round a number to three decimals."
229     return round(x,n)
230
231 def rN(a:list, n=3) -> list:
232     "Round a list of numbers to three decimals."
233     return [rn(x,n=n) for x in a]
234
235 def second(a:list) -> Any:
236     "Return second item."
237     return a[1]

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238 #
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250 #
251 class Span(o):
252     """Given two 'Sample's and some 'x' range 'lo..hi'.
253     a 'Span' holds often that range appears in each 'Sample'."""
254     def __init__(i,col, lo, hi, ys=None):
255         i.col, i.lo, i.hi, i.ys = col, lo, hi, ys or Sym()
256
257     def add(i, x:float, y:Any, inc=1) -> None:
258         "y' is a label identifying one 'Sample' or another."
259         i.lo = min(x, i.lo)
260         i.hi = max(x, i.hi)
261         i.ys.add(y,inc)
262
263     def merge(i, j): # -> Span|None
264         "If the merged span is simpler, return that merge."
265         a, b, c = i.ys, j.ys, i.ys.merge(j.ys)
266         if (i.ys.n==0 or j.ys.n==0 or
267             c.div()*.99 <= (a.n*a.div() + b.n*b.div())/(a.n + b.n)):
268             return Span(i.col, min(i.lo,j.lo),max(i.hi,j.hi), ys=c)
269
270     def selects(i,row:list) -> bool:
271         "True if the range accepts the row."
272         x = row[i.col.at]; return x=="?" or i.lo<=x and x< i.hi
273
274     def show(i, positive=True) -> None:
275         "Show the range."
276         txt = i.col.txt
277         if positive:
278             if i.lo == i.hi: return f"[{txt}] == {i.lo}"
279             elif i.lo == -big: return f"[{txt}] < {i.hi}"
280             elif i.hi == big: return f"[{txt}] >= {i.lo}"
281             else: return f"[{i.lo}] <= {txt] < {i.hi}"
282         else:
283             if i.lo == i.hi: return f"[{txt}] != {i.lo}"
284             elif i.lo == -big: return f"[{txt}] >= {i.hi}"
285             elif i.hi == big: return f"[{txt}] < {i.lo}"
286             else: return f"[{txt}] < {i.lo} or {txt] >= {i.hi}"
287
288     def support(i) -> float:
289         "Returns 0..1."
290         return i.ys.n / i.col.n
291
292     @staticmethod
293     def sort(spans : list) -> list:
294         "Good spans have large support and low diversity."
295         divs, supports = Num(512), Num(512)
296         sn = lambda s: supports.norm( s.support())
297         dn = lambda s: divs.norm( s.ys.div())
298         f = lambda s: ((1 - sn(s))*2 + dn(s)**2)**.5/2***.5
299         for s in spans:
300             divs.add( s.ys.div())
301             supports.add(s.support())
302         return sorted(spans, key=f)
303
304 #
305 #
306 #
307 #
308 #
309 class Col(o):
310     "Summarize columns."
311     def __init__(i,at=0,txt=""):
312         i.n,i.at,i.txt,i.w=0,at,txt,(-1 if "-" in txt else 1)
313
314     def dist(i,x:Any, y:Any) -> float:
315         return 1 if x=="?" and y=="?" else i.dist1(x,y)
316
317 #
318 #
319 #
320 #
321 #
322 class Sym(Col):
323     "Summarize symbolic columns."
324     def __init__(i,**kw):
325         super().__init__(**kw)
326         i.has, i.mode, i.mode = {}, None, 0
327
328     def add(i, x:str, inc:int=1) -> str:
329         "Update symbol counts in 'has', updating 'mode' as we go."
330         if x != " ":
331             i.n += inc
332             tmp = i.has[x] = inc + i.has.get(x,0)
333             if tmp > i.mode: i.mode, i.mode = tmp, x
334         return x
335
336     def dist(i,x:str, y:str) -> float:
337         "Distance between two symbols."
338         return 0 if x==y else 1
339
340     def div(i):
341         "Return diversity of this distribution (using entropy)."
342         p = lambda x: x / (i.n-1 + i.n)
343         return sum( -p(x)*math.log(p(x),2) for x in i.has.values() )
344
345     def merge(i,j):
346         "Merge two 'Sym's."
347         k = Sym(at=i.at, txt=i.txt)
348         for x,n in i.has.items(): k.add(x,n)
349         for x,n in j.has.items(): k.add(x,n)
350         return k
351
352     def mid(i) -> Any:
353         "Return central tendency of this distribution (using mode)."
354         return i.mode
355
356     def prep(i,x) -> Any:
357         "Return 'x' as anything at all."
358         return x
359
360     def spans(i,j, _bins, out):
361         """For each symbol in 'i' and 'j', count the
362         number of times we see it on either side."""
363         xys = [(x,"this",n) for x,n in i.has.items()] + [
364             (x,"that",n) for x,n in j.has.items()]
365         one, last = None, None
366         all = []
367         for x,y,n in sorted(xys, key=first):
368             if x != last:
369                 last = x
370                 one = Span(i, x,x)
371                 all += [one]
372             one.add(x,y,n)
373         if len(all) > 1 : out += all

```

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374 #
375 #
376 #
377 #
378 class Num(Col):
379     "Summarize numeric columns."
380     def __init__(i,size,**kw):
381         super().__init__(**kw)
382         i._all, i.lo, i.hi, i.max, i.ok = [], 1E32, -1E32, size, False
383
384     def add(i,x:float,inc=1):
385         "Reservoir sampler. If 'all' is full, sometimes replace an item at random."
386         if x != "":
387             i.n += inc
388             i.lo = min(x,i.lo)
389             i.hi = max(x,i.hi)
390             if len(i._all) < i.max : i.ok=False; i._all += [x]
391             elif r() < i.max/i.n: i.ok=False; i._all[anywhere(i._all)] = x
392         return x
393
394     def all(i):
395         "Return 'all'. sorted."
396         if not i.ok: i.ok=True; i._all.sort()
397         return i._all
398
399     def dist1(i,x,y):
400         if x=="?": y=i.norm(y); x=(1 if y<.5 else 0)
401         elif y=="?": x=i.norm(x); y=(1 if x<.5 else 0)
402         else : x,y = i.norm(x), i.norm(y)
403         return abs(x-y)
404
405     def div(i):
406         """Report the diversity of this distribution (using standard deviation).
407         &pm;2, 2.56, 3 &sigma; is 66,90,95%, of the mass. 2&sigma;. So one
408         standard deviation is (90-10)th divide by 2.4 times &sigma;."""
409         return (i.per(.9) - i.per(.1)) / 2.56
410
411     def merge(i,j):
412         "Return two Num's."
413         k = Num(i.max, at=i.at, txt=i.txt)
414         for x in i._all: k.add(x)
415         for x in j._all: k.add(x)
416         return k
417
418     def mid(i):
419         "Return central tendency of this distribution (using median)."
420         return i.per(.5)
421
422     def norm(i,x):
423         "Normalize 'x' to the range 0..1."
424         return 0 if i.hi-i.lo < 1E-9 else (x-i.lo)/(i.hi-i.lo)
425
426     def per(i,p:float=.5) -> float:
427         "Return the p-th ranked item."
428         a = i.all(); return a[ int(p*len(a)) ]
429
430     def prep(i,x):
431         "Return 'x' as a float."
432         return x if x=="?" else float(x)
433
434     def spans(i,j, bins, out):
435         """Divide the whole space 'lo' to 'hi' into, say, 'xsmall'=16 bin.
436         then count the number of times we the bin on other side.
437         Then merge similar adjacent bins."""
438         lo = min(i.lo, j.lo)
439         hi = max(i.hi, j.hi)
440         gap = (hi-lo) / bins
441         xys = [(x,"this",1) for x in i._all] + [
442             (x,"that",1) for x in j._all]
443         one = Span(i.lo,lo)
444         all = [one]
445         for x,y,n in sorted(xys, key=first):
446             if one.hi - one.lo > gap:
447                 one = Span(i, one.hi,x)
448                 all += [one]
449             one.add(x,y,n)
450         all = merge(all)
451         all[0].lo = -big
452         all[-1].hi = big
453         if len(all) > 1: out += all
454 #
455 #
456 #
457 #
458 #
459
460 class Explain(o):
461     "Tree with 'yes','no' branches for samples that do/do not match a 'span'."
462     def __init__(i,here):
463         i.here, i.span, i.yes, i.no = here, None, None, None
464
465     def show(i,pre=""):
466         if not pre:
467             tmp = i.here.mid(i.here.y)
468             print(f"[{pre:40}]: {len(i.here.rows):5} : {tmp}")
469         if i.yes:
470             s=f"[pre]{i.span.show(True)}"
471             tmp = i.yes.here.mid(i.yes.here.y)
472             print(f"[s:40]: {len(i.yes.here.rows):5} : {tmp}")
473             i.yes.show(pre + "|.")
474         if i.no:
475             s=f"[pre]{i.span.show(False)}"
476             tmp = i.no.here.mid(i.no.here.y)
477             print(f"[s:40]: {len(i.no.here.rows):5} : {tmp}")
478             i.no.show(pre + "|.")
479
480 #
481 #
482 #
483 #
484 #
485
486 class Cluster(o):
487     "Tree with 'left','right' samples, broken at median between far points."
488     def __init__(i,here,x=None,y=None,c=None,mid=None):
489         i.here,i.x,i.y,i.c,i.mid,i.left,i.right = here,x,y,c,mid,None,None
490
491     def show(i,pre=""):
492         s = f"[pre:40]: {len(i.here.rows):5}"
493         print(f"[s]{s}" if i.left else f"[s] : {i.here.mid(i.here.y)}")
494         for kid in [i.left,i.right]:
495             if kid: kid.show(pre + "|.")
496 #
497 #
498 #
499 #
500
501 class Sample(o):
502     "Load, then manage, a set of examples."
503
504     def __init__(i, the, inits=[]):
505         i.the = the
506         i.rows, i.cols, i.x, i.y, i.klass = [], [], [], [], None
507         if str ==type(inits): [i.add(row, True) for row in file(inits)]
508         if list==type(inits): [i.add(row) for row in inits]
509
510     def add(i, a, raw=False):
511         pre = lambda a,c: c.prep(a[c.at]) if raw else a[c.at]
512         nump = lambda x : x[0].isupper()
513         skipp = lambda x : x[-1]=="."
514         klassp = lambda x : "[ " in x
515         goalp = lambda x : "+" in x or "-" in x or klassp(x)
516         #-----
517         def col(at,txt):
518             now = Num(i.the.Max,at=at,txt=txt) if nump(txt) else Sym(at=at,txt=txt)
519             where = i.y if goalp(txt) else i.x
520             if not skipp(txt):
521                 where += [now]
522                 if klassp(txt): i.klass = now
523             return now
524         #-----
525         if i.cols: i.rows += [[col.add(pre(a,col)) for col in i.cols]]
526         else: i.cols = [col(at,txt) for at,txt in enumerate(a)]
527
528     def clone(i, inits=[]):
529         out = Sample(i.the)
530         out.add([col.txt for col in i.cols])
531         [out.add(x) for x in inits]
532         return out
533
534     def cluster(i, top=None):
535         """Split the data using random projections. Find the span that most
536         separates the data. Divide data on that span."""
537         here = Cluster(i)
538         top = top or i
539         if len(i.rows) >= 2*(len(top.rows)**i.the.enough):
540             left,right,x,y,c,mid = i.half(top)
541             if len(left.rows) < len(i.rows):
542                 here = Cluster(i,x,y,c,mid)
543             here.left = left.cluster(top)
544             here.right = right.cluster(top)
545             return here
546
547     def dist(i,x,y):
548         d = sum( col.dist(x[col.at], y[col.at])**i.the.p for col in i.x )
549         return (d/len(i.x)) ** (1/i.the.p)
550
551     def div(i,cols=None):
552         return [col.div() for col in (cols or i.all)]
553
554     def far(i, x, rows=None):
555         tmp = sorted([(i.dist(x,y),y) for y in (rows or i.rows)],key=first)
556         return tmp[ int(len(tmp)*i.the.far) ]
557
558     def half(i, top=None):
559         "Using two faraway points 'x,y' break data at median distance."
560         some = i.rows if len(i.rows)<i.the.Some else random.choices(i.rows, k=the.Some)
561         top = top or i
562         w = any(some)
563         _,x= top.far(w, some)
564         c,y= top.far(x, some)
565         tmp = [r for _,r in sorted([(top.proj(r,x,y,c),r)
566                                     for r in i.rows],key=first))]
567         mid= len(tmp)//2
568         return i.clone(tmp[:mid]), i.clone(tmp[mid:]), x, y, c, tmp[mid]
569
570     def mid(i,cols=None):
571         return [col.mid() for col in (cols or i.all)]
572
573     def proj(i, row,x,y,c):
574         "Find the distance of a 'row' on a line between 'x' and 'y'."
575         a = i.dist(row,x)
576         b = i.dist(row,y)
577         return (a**2 + c**2 - b**2) / (2*c)
578
579     def xplain(i,top=None):
580         """Split the data using random projections. Find the span that most
581         separates the data. Divide data on that span."""
582         here = Explain(i)
583         top = top or i
584         tiny = len(top.rows)**i.the.enough
585         if len(i.rows) >= 2*tiny:
586             left, right,*_ = i.half(top)
587             spans = []
588             [lcol.spans(rcol,6/i.the.xsmall,spans) for lcol,rcol
589              in zip(left.x, right.x)]
590
591             if len(spans) > 0:
592                 here.span = Span.sort(spans)[0]
593                 yes, no = i.clone(), i.clone()
594                 [(yes if here.span.selects(row) else no).add(row) for row in i.rows]
595                 if tiny <= len(yes.rows) < len(i.rows): here.yes = yes.xplain(top=top)
596                 if tiny <= len(no.rows) < len(i.rows): here.no = no.xplain(top=top)
597             return here

```

```

597 #
598 #
599 #
600 #
601 #
602 #
603 #
604
605 class Demos:
606     "Possible start-up actions."
607     fails=0
608     def opt():
609         "show the config."
610         print(the)
611
612     def seed():
613         "seed"
614         assert .494 <= r() <= .495
615
616     def num():
617         "check 'Num'."
618         n = Num(512)
619         for _ in range(100): n.add(r())
620         assert .30 <= n.div() <= .31, "in range"
621
622     def sym():
623         "check 'Sym'."
624         s = Sym()
625         for x in "aaaabbc": s.add(x)
626         assert 1.37 <= s.div() <= 1.38, "entropy"
627         assert 'a' == s.mid(), "mode"
628
629     def rows():
630         "count rows in a file."
631         assert 399 == len([row for row in file(the.data)])
632
633     def sample():
634         "sampling."
635         s = Sample(the, the.data)
636         print(the.data, len(s.rows))
637         assert 398 == len(s.rows), "length of rows"
638         assert 249 == s.x[-1].has['l'], "symbol counts"
639
640     def dist():
641         "distance between rows"
642         s = Sample(the, the.data)
643         assert .84 <= s.dist(s.rows[1], s.rows[-1]) <= .842
644
645     def far():
646         "distant items"
647         s = Sample(the, the.data)
648         for _ in range(32):
649             a,_ = s.far(any(s.rows))
650             assert a>.5, "large?"
651
652     def clone():
653         "cloning"
654         s = Sample(the, the.data)
655         s1 = s.clone(s.rows)
656         d1,d2 = s.x[0].__dict__, s1.x[0].__dict__
657         for k,v in d1.items():
658             assert d2[k] == v, "clone test"
659
660     def half():
661         "divide data in two"
662         s = Sample(the, the.data)
663         s1,s2,*_ = s.half()
664         print(s1.mid(s1.y))
665         print(s2.mid(s2.y))
666
667     def cluster():
668         "divide data in two"
669         s = Sample(the, the.data)
670         s.cluster().show(); print("")
671
672     def xplain():
673         "divide data in two"
674         s = Sample(the, the.data)
675         s.xplain().show(); print("")
676
677 #-----
678 the=options(__doc__)
679 if __name__ == "__main__": demo(the.todo,Demos)
680
681 """
682 Example class
683 """

```