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155 #
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163
164 def any(a: list) -> Any:
165     "Return a random item."
166     return a[anywhere(a)]
167
168
169 def anywhere(a: list) -> int:
170     "Return a random index of list 'a'."
171     return random.randint(0, len(a)-1)
172
173
174 big = sys.maxsize
175
176
177 def atom(x):
178     "Return a number or trimmed string."
179     x = x.strip()
180     if x == "True":
181         return True
182     elif x == "False":
183         return False
184     else:
185         try:
186             return int(x)
187         except:
188             try:
189                 return float(x)
190             except:
191                 return x.strip()
192
193
194 def demo(do, all):
195     "Maybe run a demo, if we want it, resetting random seed first."
196     todo = dir(all)
197     if do and do != "all":
198         todo = [x for x in dir(all) if x.startswith(do)]
199     for one in todo:
200         fun = all.__dict__.get(one, "")
201         if type(fun) == type(demo):
202             Random.seed(the.seed)
203             doc = re.sub(r'\n\s+', "\n", fun.__doc__ or "")
204             try:
205                 fun()
206                 print("PASS:", doc)
207             except Exception as e:
208                 all.fails += 1
209                 if the.cautious:
210                     traceback.print_exc()
211                     exit(1)
212             else:
213                 print("FAIL:", doc, e)
214     exit(all.fails)
215
216
217 def file(f):
218     "Iterator. Returns one row at a time, as cells."
219     with open(f) as fp:
220         for line in fp:
221             line = re.sub(r'([\n\r\v])', '#.').strip()
222             if line:
223                 yield [atom(cell.strip()) for cell in line.split(",")]
224
225
226 def first(a: list) -> Any:
227     "Return first item."
228     return a[0]
229
230
231 def merge(b4: list) -> list:
232     "While we can find similar adjacent things, merge them."
233     j, n, now = -1, len(b4), []
234     while j < n-1:
235         j += 1
236         a = b4[j]
237         if j < n-2:
238             if merged := a.merge(b4[j+1]):
239                 a = merged
240                 j += 1 # we will continue, after missing one
241         now += [a]
242     # if 'now' is same size as 'b4', look for any other merges.
243     return b4 if len(now) == len(b4) else merge(now)
244
245
246 class o(object):
247     "Class that can pretty print its slots, with fast inits."
248     def __init__(i, **d): i.__dict__.update(**d)
249
250     def __repr__(i):
251         pre = i.__class__.__name__ if isinstance(i, o) else ""
252         return pre+str(
253             {k: v for k, v in sorted(i.__dict__.items()) if str(k)[0] != "_"})
254
255
256 def options(doc: str) -> o:
257     """Convert 'doc' to options dictionary using command line args.
258     Args cause two 'shorthands': (1) boolean flags have no arguments (and mentioning
259     those on the command line means 'flip the default value'; (2) args need only
260     mention the first few of a key (e.g. -s is enough to select for -seed)."""
261     d = {}
262     for line in doc.splitlines():
263         if line and line.startswith("-"):
264             # get 1st, last word on each line
265             key, x = line.strip()[1:].split(" ")
266             for j, flag in enumerate(sys.argv):
267                 if flag and flag[0] == "-" and key.startswith(flag[1:]):
268                     x = "True" if x == "False" else "False" if x == "True" else sys.argv[j+1]
269             d[key] = atom(x)
270     if d["help"]:
271         exit(print(re.sub(r'\n#.*', "", doc, flags=re.S)))
272     return o(**d)
273
274
275
276 def r() -> float:
277     "Return random number 0..1"
278     return random.random()
279
280
281 def rn(x: float, n=3) -> float:
282     "Round a number to three decimals."
283     return round(x, n)
284
285
286 def rN(a: list, n=3) -> list:
287     "Round a list of numbers to three decimals."
288     return [rn(x, n=n) for x in a]
289
290

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291 def second(a: list) -> Any:
292     "Return second item."
293     return a[1]

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307 #
308 class Span(o):
309     """Given two 'Sample's and some 'x' range 'lo..hi'.
310     a 'Span' holds often that range appears in each 'Sample'."""
311     def __init__(i, col, lo, hi, ys=None,):
312         i.col, i.lo, i.hi, i.ys = col, lo, hi, ys or Sym()
313
314     def add(i, x: float, y: Any, inc=1) -> None:
315         "y' is a label identifying one 'Sample' or another."
316         i.lo = min(x, i.lo)
317         i.hi = max(x, i.hi)
318         i.ys.add(y, inc)
319
320     def merge(i, j): # -> Span|None
321         "If the merged span is simpler, return that merge."
322         a, b, c = i.ys, j.ys, i.ys.merge(j.ys)
323         if (i.ys.n == 0 or j.ys.n == 0 or
324             c.div()*.99 <= (a.n*a.div() + b.n*b.div())/(a.n + b.n)):
325             return Span(i.col, min(i.lo, j.lo), max(i.hi, j.hi), ys=c)
326
327     def selects(i, row: list) -> bool:
328         "True if the range accepts the row."
329         x = row[i.col.at]
330         return x == "?" or i.lo <= x and x < i.hi
331
332     def show(i, positive=True) -> None:
333         "Show the range."
334         txt = i.col.txt
335         if positive:
336             if i.lo == i.hi:
337                 return f"[{txt}] == {i.lo}"
338             elif i.lo == -big:
339                 return f"[{txt}] < {i.hi}"
340             elif i.hi == big:
341                 return f"[{txt}] >= {i.lo}"
342             else:
343                 return f"[{i.lo} <= {txt} < {i.hi}]"
344         else:
345             if i.lo == i.hi:
346                 return f"[{txt}] != {i.lo}"
347             elif i.lo == -big:
348                 return f"[{txt}] >= {i.hi}"
349             elif i.hi == big:
350                 return f"[{txt}] < {i.lo}"
351             else:
352                 return f"[{txt} < {i.lo} or {txt} >= {i.hi}]"
353
354     def support(i) -> float:
355         "Returns 0..1."
356         return i.ys.n / i.col.n
357
358     @staticmethod
359     def sort(spans: list) -> list:
360         "Good spans have large support and low diversity."
361         divs, supports = Num(), Num()
362         def sn(s): return supports.norm(s.support())
363         def dn(s): return divs.norm(s.ys.div())
364         def f(s): return ((1 - sn(s))**2 + dn(s)**2)**.5/2**.5
365         for s in spans:
366             divs.add(s.ys.div())
367             supports.add(s.support())
368         return sorted(spans, key=f)
369
370 #
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375 #
376 class Col(o):
377     "Summarize columns."
378     def __init__(i, at=0, txt=""):
379         i.n, i.at, i.txt, i.w = 0, at, txt, (-1 if "-" in txt else 1)
380
381     def dist(i, x: Any, y: Any) -> float:
382         return 1 if x == "?" and y == "?" else i.dist1(x, y)
383
384 #
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388 #
389 #
390 class Sym(Col):
391     "Summarize symbolic columns."
392     def __init__(i, **kw):
393         super().__init__(**kw)
394         i.has, i.mode, i.most = {}, None, 0
395
396     def add(i, x: str, inc: int = 1) -> str:
397         "Update symbol counts in 'has', updating 'mode' as we go."
398         if x != "?":
399             i.n += inc
400             tmp = i.has[x] = inc + i.has.get(x, 0)
401             if tmp > i.most:
402                 i.most, i.mode = tmp, x
403             return x
404
405     def dist(i, x: str, y: str) -> float:
406         "Distance between two symbols."
407         return 0 if x == y else 1
408
409     def div(i):
410         "Return diversity of this distribution (using entropy)."
411         def p(x): return x / (1E-31 + i.n)
412         return sum(-p(x)*math.log(p(x), 2) for x in i.has.values())
413
414     def merge(i, j):
415         "Merge two 'Sym's."
416         k = Sym(at=i.at, txt=i.txt)
417         for x, n in i.has.items():
418             k.add(x, n)
419         for x, n in j.has.items():
420             k.add(x, n)
421         return k
422
423     def mid(i):
424         "Return central tendency of this distribution (using mode)."
425         return i.mode
426
427     def spans(i, j, out):
428         """For each symbol in 'i' and 'j', count the
429         number of times we see it on either side."""
430
431     xys = [(x, "this", n) for x, n in i.has.items()] + [
432         (x, "that", n) for x, n in j.has.items()]
433     one, last = None, None
434     all = []
435     for x, y, n in sorted(xys, key=first):
436         if x != last:
437             last = x
438             one = Span(i, x, x)
439             all += [one]
440             one.add(x, y, n)
441         if len(all) > 1:
442             out += all
443
444 #
445 #
446 #
447 class Num(Col):
448     "Summarize numeric columns."
449     def __init__(i, **kw):
450         super().__init__(**kw)
451         i._all, i.lo, i.hi, i.max, i.ok = [], 1E32, -1E32, the.Max, False
452
453     def add(i, x: float, inc=1):
454         "Reservoir sampler. If '_all' is full, sometimes replace an item at random."
455         if x != "?":
456             i.n += inc
457             i.lo = min(x, i.lo)
458             i.hi = max(x, i.hi)
459             if len(i._all) < i.max:
460                 i.ok = False
461                 i._all += [x]
462             elif r() < i.max/i.n:
463                 i.ok = False
464                 i._all[anywhere(i._all)] = x
465             return x
466
467     def all(i):
468         "Return '_all'. sorted."
469         if not i.ok:
470             i.ok = True
471             i._all.sort()
472         return i._all
473
474     def dist1(i, x, y):
475         if x == "?":
476             y = i.norm(y)
477             x = (1 if y < .5 else 0)
478         elif y == "?":
479             x = i.norm(x)
480             y = (1 if x < .5 else 0)
481         else:
482             x, y = i.norm(x), i.norm(y)
483         return abs(x-y)
484
485     def div(i):
486         """Report the diversity of this distribution (using standard deviation).
487         &pm;2.256, 3 &sigma; is 66.9095% of the mass. 2&sigma; is 90-10% divide by 2.4 times &sigma;."""
488         return (i.per(.9) - i.per(.1)) / 2.56
489
490     def merge(i, j):
491         "Return two 'Num's."
492         k = Num(at=i.at, txt=i.txt)
493         for x in i._all:
494             k.add(x)
495         for x in j._all:
496             k.add(x)
497         return k
498
499     def mid(i):
500         "Return central tendency of this distribution (using median)."
501         return i.per(.5)
502
503     def norm(i, x):
504         "Normalize 'x' to the range 0..1."
505         return 0 if i.hi-i.lo < 1E-9 else (x-i.lo)/(i.hi-i.lo)
506
507     def per(i, p: float = .5) -> float:
508         "Return the p-th ranked item."
509         a = i.all()
510         return a[int(p*len(a))]
511
512     def spans(i, j, out):
513         """Divide the whole space 'lo' to 'hi' into, say, 'xsmall'=16 bin,
514         then count the number of times we the bin on other side.
515         Then merge similar adjacent bins."""
516         lo = min(i.lo, j.lo)
517         hi = max(i.hi, j.hi)
518         gap = (hi-lo) / (6/the.xsmall)
519         xys = [(x, "this", 1) for x in i._all] + [
520             (x, "that", 1) for x in j._all]
521         one = Span(i, lo, lo)
522         all = [one]
523         for x, y, n in sorted(xys, key=first):
524             if one.hi - one.lo > gap:
525                 one = Span(i, one.hi, x)
526                 all += [one]
527             one.add(x, y, n)
528         all = merge(all)
529         all[0].lo = -big
530         all[-1].hi = big
531         if len(all) > 1:
532             out += all
533
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540 #
541 class Explain(o):
542     "Tree with 'yes','no' branches for samples that do/do not match a 'span'."
543     def __init__(i, here):
544         i.here, i.span, i.yes, i.no = here, None, None, None
545
546     def show(i, pre=""):
547         if not pre:
548             tmp = i.here.mid(i.here.y)
549             print(f"[{pre[:40]}: {len(i.here.rows):5}] : {tmp}")
550         if i.yes:
551             s = f"[pre]{i.span.show(True)}"
552             tmp = i.yes.here.mid(i.yes.here.y)
553             print(f"[s:40]: {len(i.yes.here.rows):5}] : {tmp}")
554             i.yes.show(pre + "[. ")
555         if i.no:
556             s = f"[pre]{i.span.show(False)}"
557             tmp = i.no.here.mid(i.no.here.y)
558             print(f"[s:40]: {len(i.no.here.rows):5}] : {tmp}")
559             i.no.show(pre + "[. ")
560
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566
567
568 class Cluster(o):
569     "Tree with 'left', 'right' samples, broken at median between far points."
570     def __init__(i, here, x=None, y=None, c=None, mid=None):
571         i.here, i.x, i.y, i.c, i.mid, i.left, i.right = here, x, y, c, mid, None, No
572         ne
573
574     def show(i, pre=""):
575         s = f"{pre:40}: {len(i.here.rows):5}"
576         print(f"{s}" if i.left else f"{s} : {i.here.mid(i.here.y)}")
577         for kid in [i.left, i.right]:
578             if kid:
579                 kid.show(pre + "|. ")
580
581 #
582 #
583 #
584
585
586 class Sample(o):
587     "Load, then manage, a set of examples."
588     def __init__(i, inits=[]):
589         i.rows, i.cols, i.x, i.y, i.klass = [], [], [], [], None
590         if str == type(inits):
591             [i.add(row) for row in file(inits)]
592         if list == type(inits):
593             [i.add(row) for row in inits]
594
595     def add(i, a):
596         def col(at, txt):
597             what = Num if txt[0].isupper() else Sym
598             now = what(at=at, txt=txt)
599             where = i.y if "+" in txt or "-" in txt or "!" in txt else i.x
600             if txt[-1] != " ":
601                 where += [now]
602             if "!" in txt:
603                 i.klass = now
604             return now
605         # -----
606         if i.cols:
607             i.rows += [[col.add(a[col.at]) for col in i.cols]]
608         else:
609             i.cols = [col(at, txt) for at, txt in enumerate(a)]
610
611     def clone(i, inits=[]):
612         out = Sample()
613         out.add([col.txt for col in i.cols])
614         [out.add(x) for x in inits]
615         return out
616
617     def cluster(i, top=None):
618         """Split the data using random projections. Find the span that most
619         separates the data. Divide data on that span."""
620         here = Cluster(i)
621         top = top or i
622         if len(i.rows) >= 2*(len(top.rows)**the.enough):
623             left, right, x, y, c, mid = i.half(top)
624             if len(left.rows) < len(i.rows):
625                 here = Cluster(i, x, y, c, mid)
626             here.left = left.cluster(top)
627             here.right = right.cluster(top)
628             return here
629
630     def dist(i, x, y):
631         d = sum(col.dist(x[col.at], y[col.at])**the.p for col in i.x)
632         return (d/len(i.x)) ** (1/the.p)
633
634     def div(i, cols=None):
635         return [col.div() for col in (cols or i.all)]
636
637     def far(i, x, rows=None):
638         tmp = sorted([(i.dist(x, y), y) for y in (rows or i.rows)], key=first)
639         return tmp[int(len(tmp)*the.far)]
640
641     def half(i, top=None):
642         "Using two faraway points 'x,y' break data at median distance."
643         some = i.rows if len(
644             i.rows) < the.Some else random.choices(i.rows, k=the.Some)
645         top = top or i
646         w = any(some)
647         _, x = top.far(w, some)
648         c, y = top.far(x, some)
649         tmp = [r for _, r in sorted([(top.proj(r, x, y, c), r)
650                                     for r in i.rows], key=first)]
651         mid = len(tmp)//2
652         return i.clone(tmp[:mid]), i.clone(tmp[mid:]), x, y, c, tmp[mid]
653
654     def mid(i, cols=None):
655         return [col.mid() for col in (cols or i.all)]
656
657     def proj(i, row, x, y, c):
658         "Find the distance of a 'row' on a line between 'x' and 'y'."
659         a = i.dist(row, x)
660         b = i.dist(row, y)
661         return (a**2 + c**2 - b**2) / (2*c)
662
663     def xplain(i, top=None):
664         """Split the data using random projections. Find the span that most
665         separates the data. Divide data on that span."""
666         here = Explain(i)
667         top = top or i
668         tiny = len(top.rows)**the.enough
669         if len(i.rows) >= 2*tiny:
670             left, right, *_ = i.half(top)
671             spans = []
672             [lcol.spans(rcol, spans) for lcol, rcol in zip(left.x, right.x)]
673             if len(spans) > 0:
674                 here.span = Span.sort(spans)[0]
675                 yes, no = i.clone(), i.clone()
676                 [(yes if here.span.selects(row) else no).add(row) for row in i.rows]
677                 if tiny <= len(yes.rows) < len(i.rows):
678                     here.yes = yes.xplain(top=top)
679                 if tiny <= len(no.rows) < len(i.rows):
680                     here.no = no.xplain(top=top)
681             return here

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690
691 class Demos:
692     "Possible start-up actions."
693     fails = 0
694
695     def opt():
696         "show the config."
697         [print(f"{k>10}={v}") for k, v in the.__dict__.items()]
698
699     def seed():
700         "seed"
701         assert .494 <= r() <= .495
702
703     def num():
704         "check 'Num'."
705         n = Num()
706         for _ in range(100):
707             n.add(r())
708         assert .30 <= n.div() <= .31, "in range"
709
710     def sym():
711         "check 'Sym'."
712         s = Sym()
713         for x in "aaabbc":
714             s.add(x)
715         assert 1.37 <= s.div() <= 1.38, "entropy"
716         assert 'a' == s.mid(), "mode"
717
718     def rows():
719         "count rows in a file."
720         assert 399 == len([row for row in file(the.data)])
721
722     def sample():
723         "sampling."
724         s = Sample(the.data)
725         assert 398 == len(s.rows), "length of rows"
726         assert 249 == s.x[-1].has[1], "symbol counts"
727
728     def dist():
729         "distance between rows"
730         s = Sample(the.data)
731         assert .84 <= s.dist(s.rows[1], s.rows[-1]) <= .842
732
733     def far():
734         "distant items"
735         s = Sample(the.data)
736         for _ in range(32):
737             a, _ = s.far(any(s.rows))
738             assert a > .5, "large?"
739
740     def clone():
741         "cloning"
742         s = Sample(the.data)
743         s1 = s.clone(s.rows)
744         d1, d2 = s.x[0].__dict__, s1.x[0].__dict__
745         for k, v in d1.items():
746             assert d2[k] == v, "clone test"
747
748     def half():
749         "divide data in two"
750         s = Sample(the.data)
751         s1, s2, *_ = s.half()
752         print(s1.mid(s1.y))
753         print(s2.mid(s2.y))
754
755     def cluster():
756         "divide data in two"
757         s = Sample(the.data)
758         s.cluster().show()
759         print("")
760
761     def xplain():
762         "divide data in two"
763         s = Sample(the.data)
764         s.xplain().show()
765         print("")
766
767 #
768 # -----
769 the = options(__doc__)
770 if __name__ == "__main__":
771     demo(the.todo, Demos)
772
773 """
774 all config local to Sample
775 Example class
776 """

```