```
#!/usr/bin/env python3
# vim: ts=2 sw=2 sts=2 et :
#                                 _.
#                         _.-----'' `\
#             __..-----'''             `.
#            <             `\.          '\
#            :.               `.          `\
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#                `:. L  i  a    ns`.   __.===::::;)
#           I  L E   `: n   t   ____.__>'::::::a:f/'
#      i          X   `.  _,===:::=-'-=-""""''
#  m      n  a         '-/:::''
#                        ''
#           m
"""
./sublime.py [OPTIONS]
(c)2022 Tim Menzies <timm@ieee.org>
S.U.B.L.I.M.E. =
Sublime's unsupervised bifurcation: let's infer minimal explanations.

OPTIONS:

    -Max      max numbers to keep          : 512
    -Some     find 'far' in this many egs  : 512
    -cautious On any crash, stop+show stack : False
    -data     data file                    : data/auto93.csv
    -enough   min leaf size                : .5
    -help     show help                    : False
    -far      how far to look in 'Some'    : .9
    -p        distance coefficient         : 2
    -seed     random number seed           : 10019
    -todo     start up task                : nothing
    -xsmall   Cohen's small effect         : .35

## See Also

[issues](https://github.com/timm/sublime/issues)
:: [repo](https://github.com/timm/sublime)
:: [view source](https://github.com/timm/sublime/blob/main/docs/pdf)

<a href=https://github.com/timm/sublime/actions/workflows/main.yml><img
src=https://github.com/timm/sublime/actions/workflows/main.yml/badge.svg></a>
![](https://img.shields.io/badge/purpose-se--ai-blueviolet)
![](https://img.shields.io/badge/language-python3-orange)
![](https://img.shields.io/badge/platform-osx,linux-pink)
[![DOI](https://zenodo.org/badge/DOI/10.5281/zenodo.5912461.svg)](https://doi.org/10.5281/zenodo.5912461)
## Algorithm

Stochastic clustering to generate tiny models.  Uses random projections
to divide the space. Then, optionally, explain the clusters by
unsupervised iterative dichotomization using ranges that most
distinguish sibling clusters.

### Example1: just bi-cluster on two distant points

```
/sublime.py -c -s $RANDOM -t cluster
                                   :  398
|..                                :  199
|.. |..                            :   99
|.. |.. |..                        :   49   Lbs-   Acc+  Mpg+
|.. |.. |.. |..                    :   24  : [2255, 15.5, 30]
|.. |.. |.. |..                    :   25  : [2575, 16.4, 30]
|.. |.. |..                        :   50
|.. |.. |.. |..                    :   25  : [2110, 16.4, 30] <== best
|.. |.. |.. |..                    :   25  : [2205, 16, 30]
|.. |..                            :  100
|.. |.. |..                        :   50
|.. |.. |.. |..                    :   25  : [2234, 15.5, 30]
|.. |.. |.. |..                    :   25  : [2278, 16.5, 30]
|.. |.. |..                        :   50
|.. |.. |.. |..                    :   25  : [2220, 15.5, 30]
|.. |.. |.. |..                    :   25  : [2320, 15.8, 30]
|..                                :  199
|.. |..                            :   99
|.. |.. |..                        :   49
|.. |.. |.. |..                    :   24  : [2451, 16.5, 20]
|.. |.. |.. |..                    :   25  : [3021, 15.5, 20]
|.. |.. |..                        :   50
|.. |.. |.. |..                    :   25  : [3425, 17.6, 20]
|.. |.. |.. |..                    :   25  : [3155, 16.7, 20]
|.. |..                            :  100
|.. |.. |..                        :   50
|.. |.. |.. |..                    :   25  : [4141, 13.5, 10]
|.. |.. |.. |..                    :   25  : [4054, 13.2, 20]
|.. |.. |..                        :   50
|.. |.. |.. |..                    :   25  : [4425, 11, 10]
|.. |.. |.. |..                    :   25  : [4129, 13, 10]
```

Example2: as above but split on range that most divides data

```
./sublime.py -c -s $RANDOM -t xplain
                                              Lbs-  Acc+  Mgg+
                                   :   398 : [2807, 15.5, 20]
198 <= Lbs < 454                           :   167 : [3725, 14.5, 20]
|.. Modl < 72                          :    34 : [3609, 13,   20]
|.. Modl >= 72                         :   133 : [3735, 14.9, 20]
|.. |.. Cylr < 8                       :    56 : [3336, 17,   20]
|.. |.. |.. 77 <= Modl < 82            :    22 : [3410, 17.1, 20]
|.. |.. |.. Modl < 77 or Modl >= 82    :    34 : [3233, 17,   20]
|.. |.. Cylr >= 8                      :    77 : [4129, 13.2, 20]
|.. |.. |.. Modl < 75                  :    37 : [4274, 13,   10]
|.. |.. |.. Modl >= 75                 :    40 : [3962, 13.5, 20]
|.. |.. |.. |.. Lbs >= 302             :    35 : [4054, 13.2, 20]
Lbs < 198 or Lbs >= 454                    :   231 : [2290, 16,   30] <== best
```

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NEGLIGENCE OR OTHERWISE) ARISING IN ANY WAY OUT OF THE USE OF THIS
SOFTWARE, EVEN IF ADVISED OF THE POSSIBILITY OF SUCH DAMAGE.
"""

import traceback, random, copy, math, sys, re
import random as rnd
from typing import Any
r = rnd.random
```

```
#   ___          __
#  /\_ \    __   /\ \
#  \//\ \  /\_\  \ \ \____
#    \ \ \ \/\ \  \ \ '__`\
#     \_\ \_\ \ \  \ \ \L\ \
#     /\____\\ \_\  \ \_,__/
#     \/____/ \/_/   \/___/

def any(a:list) -> Any:
  "Return a random item."
  return a[anywhere(a)]

def anywhere(a:list) -> int:
  "Return a random index of list ‘a‘."
  return rnd.randint(0, len(a)-1)

big = sys.maxsize

def atom(x):
  "Return a number or trimmed string."
  x=x.strip()
  if   x=="True" : return True
  elif x=="False": return False
  else:
    try: return int(x)
    except:
      try: return float(x)
      except: return x.strip()

def demo(do,all):
  "Maybe run a demo, if we want it, resetting random seed first."
  todo = dir(all)
  if do and do != "all":
    todo = [x for x in dir(all) if x.startswith(do)]
  for one in todo:
    fun = all.__dict__.get(one,"")
    if type(fun)==type(demo):
      rnd.seed(the.seed)
      doc = re.sub(r"\n\s+", "\n", fun.__doc__ or "")
      try:
        fun()
        print("PASS:", doc)
      except Exception as e:
        all.fails += 0
        if the.cautious : traceback.print_exc(); exit(1)
        else            : print("FAIL:", doc, e)
  exit(all.fails)

def file(f):
  "Iterator. Returns one row at a time, as cells."
  with open(f) as fp:
    for line in fp:
      line = re.sub(r'([\n\t\r"\' ]|#.*)', '', line)
      if line:
        yield [cell.strip() for cell in line.split(",")]

def first(a:list) -> Any:
  "Return first item."
  return a[0]

def merge(b4:list) -> list:
  "While we can find similar adjacent things, merge them."
  j,n,now = -1,len(b4),[]
  while j < n-1:
    j += 1
    a  = b4[j]
    if j < n-2:
      if merged := a.merge(b4[j+1]):
        a  = merged
        j += 1 # we will continue, after missing one
    now += [a]
  # if ‘now‘ is same size as ‘b4‘, look for any other merges.
  return b4 if len(now)==len(b4) else merge(now)

class o(object):
  "Class that can pretty print its slots, with fast inits."
  def __init__(i, **d): i.__dict__.update(**d)
  def __repr__(i):
    pre = i.__class__.__name__ if isinstance(i,o) else ""
    return pre+'{'+(' '.join([f":{k} {v}" for k, v in
                   sorted(i.__dict__.items()) if str(k)[0] != "_"]))+'}'

def options(doc:str) ->o:
  """Convert ‘doc‘ to options dictionary using command line args.
 Args canuse two ’shorthands’: (1) boolean flags have no arguments (and mentioning
 those on the command line means ’flip the default value’; (2) args need only
 mention the first few of a key (e.g. -s is enough to select for --seed)."""
  d={}
  for line in doc.splitlines():
    if line and line.startswith("  -"):
       key, *_, x = line.strip()[1:].split(" ") # get 1st,last word on each line
       for j,flag in enumerate(sys.argv):
         if flag and flag[0]=="-" and key.startswith(flag[1:]):
           x= "True" if x=="False" else("False" if x=="True" else sys.argv[j+1])
       d[key] = atom(x)
  if d["help"]: exit(print(re.sub(r'\n#.*',"",doc,flags=re.S)))
  return o(**d)

def r() -> float:
  "Return random number 0..1"
  return rnd.random()

def rn(x:float, n=3) -> float:
  "Round a number to three decimals."
  return round(x,n)

def rN(a:list, n=3) -> list:
  "Round a list of numbers to three decimals."
  return [rn(x,n=n) for x in a]

def second(a:list) -> Any:
  "Return second item."
  return a[1]
#         ___
#        /\_ \
#   ___  \//\ \      __      ____    ____     __    ____
#  /'___\  \ \ \   /'__`\   /',__\  /',__\  /'__`\ /',__\
# /\ \__/   \_\ \_/\ \L\.\_/\__, `\/\__, `\/\  __//\__, `\
# \ \____\  /\____\ \__/.\_\/\____/\/\____/\ \____\/\____/
#  \/____/  \/____/\/__/\/_/\/___/  \/___/  \/____/\/___/

#   ___ _ __  __ _ _ _
#  (_-<| '_ \/ _` | ' \
#  /__/| .__/\__,_|_||_|
#      |_|
class Span(o):
  """Given two ‘Sample‘s and some ‘x‘ range ‘lo..hi‘,
  a ‘Span‘ holds often that range appears in each ‘Sample‘."""
  def __init__(i,col, lo, hi, ys=None,):
    i.col, i.lo, i.hi, i.ys = col, lo, hi,  ys or Sym()

  def add(i, x:float, y:Any, inc=1) -> None:
    "‘y‘ is a label identifying, one ‘Sample‘ or another."
    i.lo = min(x, i.lo)
    i.hi = max(x, i.hi)
    i.ys.add(y,inc)

  def merge(i, j): # -> Span|None
    "If the merged span is simpler, return that merge."
    a, b, c = i.ys, j.ys, i.ys.merge(j.ys)
    if (i.ys.n==0 or j.ys.n==0 or
        c.div()*.99 <= (a.n*a.div() + b.n*b.div())/(a.n + b.n)):
      return Span(i.col, min(i.lo,j.lo),max(i.hi,j.hi), ys=c)

  def selects(i,row:list) -> bool:
    "True if the range accepts the row."
    x = row[i.col.at]; return x=="?" or i.lo<=x and x<i.hi

  def show(i, positive=True) -> None:
    "Show the range."
    txt = i.col.txt
    if positive:
      if   i.lo == i.hi: return f"{txt} == {i.lo}"
      elif i.lo == -big: return f"{txt} < {i.hi}"
      elif i.hi ==  big: return f"{txt} >= {i.lo}"
      else             : return f"{i.lo} <= {txt} < {i.hi}"
    else:
      if   i.lo == i.hi: return f"{txt} != {i.lo}"
      elif i.lo == -big: return f"{txt} >= {i.hi}"
      elif i.hi ==  big: return f"{txt} < {i.lo}"
      else             : return f"{txt} < {i.lo} or {txt} >= {i.hi}"

  def support(i) -> float:
    "Returns 0..1."
    return i.ys.n / i.col.n

  @staticmethod
  def sort(spans : list) -> list:
    "Good spans have large support and low diversity."
    divs, supports = Num(512), Num(512)
    sn = lambda s: supports.norm( s.support())
    dn = lambda s: divs.norm(     s.ys.div())
    f  = lambda s: ((1 - sn(s))**2 + dn(s)**2)**.5/2**.5
    for s in spans:
      divs.add(     s.ys.div())
      supports.add(s.support())
    return sorted(spans, key=f)
#              _
#   __   ___  | |
#  / _| / _ \ | |
#  \__| \___/ |_|

class Col(o):
  "Summarize columns."
  def __init__(i,at=0,txt=""):
    i.n,i.at,i.txt,i.w=0,at,txt,(-1 if "-" in txt else 1)

  def dist(i,x:Any, y:Any) -> float:
    return 1 if x=="?" and y=="?" else i.dist1(x,y)
#   ___  _  _  _ __
#  (_-< | || | | '  \
#  /__/  \_, | |_|_|_|
#        |__/

class Sym(Col):
  "Summarize symbolic columns."
  def __init__(i,**kw):
    super().__init__(**kw)
    i.has, i.mode, i.most = {}, None, 0

  def add(i, x:str, inc:int=1) -> str:
    "Update symbol counts in ‘has‘, updating ‘mode‘ as we go."
    if x != "?":
      i.n += inc
      tmp = i.has[x] = inc + i.has.get(x,0)
      if tmp > i.most: i.most, i.mode = tmp, x
    return x

  def dist(i,x:str, y:str) ->float:
    "Distance between two symbols."
    return 0 if x==y else 1

  def div(i):
    "Return diversity of this distribution (using entropy)."
    p = lambda x: x / (1E-31 + i.n)
    return sum( -p(x)*math.log(p(x),2) for x in i.has.values() )

  def merge(i,j):
    "Merge two ‘Sym‘s."
    k = Sym(at=i.at, txt=i.txt)
    for x,n in i.has.items(): k.add(x,n)
    for x,n in j.has.items(): k.add(x,n)
    return k

  def mid(i) -> Any:
    "Return central tendency of this distribution (using mode)."
    return i.mode

  def prep(i,x) -> Any:
    "Return ‘x‘ as anything at all."
    return x

  def spans(i,j, _bins, out):
    """For each symbol in ‘i‘ and ‘j‘, count the
 number of times we see it on either side."""
    xys = [(x,"this",n) for x,n in i.has.items()] + [
           (x,"that",n) for x,n in j.has.items()]
    one, last = None,None
    all  = []
    for x,y,n in sorted(xys, key=first):
      if x != last:
         last = x
         one  = Span(i, x,x)
         all += [one]
      one.add(x,y,n)
    if len(all) > 1 : out += all
#   _ _  _  _  _ __
#  | ' \| || || '  \
#  |_||_|\_,_||_|_|_|
```

```
class Num(Col):
  "Summarize numeric columns."
  def __init__(i,size,**kw):
    super().__init__(**kw)
    i._all, i.lo, i.hi, i.max, i.ok = [], 1E32, -1E32, size, False

  def add(i,x: float ,inc=1):
    "Reservoir sampler. If ‘_all‘ is full, sometimes replace an item at random."
    if x != "?":
      i.n += inc
      i.lo = min(x,i.lo)
      i.hi = max(x,i.hi)
      if len(i._all) < i.max    : i.ok=False; i._all += [x]
      elif r()       < i.max/i.n: i.ok=False; i._all[anywhere(i._all)] = x
    return x

  def all(i):
    "Return ‘_all‘, sorted."
    if not i.ok: i.ok=True; i._all.sort()
    return i._all

  def dist1(i,x,y):
    if   x=="?": y=i.norm(y); x=(1 if y<.5 else 0)
    elif y=="?": x=i.norm(x); y=(1 if x<.5 else 0)
    else       : x,y = i.norm(x), i.norm(y)
    return abs(x-y)

  def div(i):
    """Report the diversity of this distribution (using standard deviation).
  &pm;2, 2,56, 3 &sigma; is 66,90,95%, of the mass.  28&sigma;. So one
  standard deviation is (90−10)th divide by  2.4 times &sigma;."""
    return (i.per(.9) - i.per(.1)) / 2.56

  def merge(i,j):
    "Return two ‘Num‘s."
    k = Num(i.max, at=i.at, txt=i.txt)
    for x in i._all: k.add(x)
    for x in j._all: k.add(x)
    return k

  def mid(i):
    "Return central tendency of this distribution (using median)."
    return i.per(.5)

  def norm(i,x):
    "Normalize ‘x‘ to the range 0..1."
    return 0 if i.hi-i.lo < 1E-9 else (x-i.lo)/(i.hi-i.lo)

  def per(i,p:float=.5) -> float:
    "Return the p−th ranked item."
    a = i.all(); return a[ int(p*len(a)) ]

  def prep(i,x):
    "Return ‘x‘ as a float."
    return x if x=="?" else float(x)

  def spans(i,j, bins, out):
    """Divide the whole space ‘lo‘ to ‘hi‘ into, say, ‘xsmall‘=16 bin,
  then count the number of times we the bin on other side.
  Then merge similar adjacent bins."""
    lo  = min(i.lo, j.lo)
    hi  = max(i.hi, j.hi)
    gap = (hi-lo) / bins
    xys = [(x,"this",1) for x in i._all] + [
           (x,"that",1) for x in j._all]
    one = Span(i,lo,lo)
    all = [one]
    for x,y,n in sorted(xys, key=first):
      if one.hi - one.lo > gap:
        one  = Span(i, one.hi,x)
        all += [one]
      one.add(x,y,n)
    all = merge(all)
    all[ 0].lo = -big
    all[-1].hi =  big
    if len(all) > 1: out += all
#                                      _
#   ___  __ __  __ _   _ __    _ __  | |  ___
#  / -_) \ \ / / _` | | '  \  | '_ \ | | / -_)
#  \___| /_\_\ \__,_| |_|_|_| | .__/ |_| \___|
#                             |_|
class Example(o):
  def __init__(i,cells):
    "One example stores a list of cells."
    i.cells=cells
  def __getitem__(i,k):
    "Accessor."
    return i.cells[k]

  def dist(i,j, sample):
    "Separation of two examples."
    cols, p = sample.x, sample.the.p
    d = sum(col.dist(i[col.at], j[col.at])**p for col in cols)
    return (d/len(cols)) ** (1/p)

  def better(i,j, sample):
    "Compare different goals."
    n = len(cols)
    for col in cols:
      a,b = col.norm( i[col.at] ), col.norm( j[col.at] )
      s1 -= math.e**(col.w*(a-b)/n)
      s2 -= math.e**(col.w*(b-a)/n)
    return s1/n < s2/n
#                       _           _
#   ___  __ __  _ __   | |  __ _  (_)  _ _
#  / -_) \ \ / | '_ \  | | / _` | | | | ' \
#  \___| /_\_\ | .__/  |_| \__,_| |_| |_||_|
#               |_|
class Explain(o):
  "Tree with ‘yes‘,‘no‘ branches for samples that do/do not match a ‘span‘."
  def __init__(i,here):
    i.here, i.span, i.yes, i.no = here, None, None, None

  def show(i,pre=""):
    "Pretty print"
    if not pre:
      tmp= i.here.mid(i.here.y)
      print(f"{’’:40} : {len(i.here.rows):5} : {tmp}")
    for (status,kid) in [(True,i.yes), (False, i.no)]:
      if kid:
        s=f"{pre}{i.span.show(status)}"
        tmp= kid.here.mid(kid.here.y)
        print(f"{s:40} : {len(kid.here.rows):5} : {tmp}")
        kid.show(pre + "|.. ")
#        _          _
#   __  | |  _  _   ___  | |_   ___   _ _
#  / _| | | | || | (_-<  |  _| / -_) | '_|
#  \__| |_|  \_,_| /__/   \__| \___| |_|
#
class Cluster(o):
  "Tree with ‘left‘,‘right‘ samples, broken at median between far points."
  def __init__(i, sample, top=None):
    i.here,i.left,i.right,i.x,i.y,i.c,i.mid= sample,None,None,None,None,None,Non
e
    top    = top or sample
    if len(sample.rows) >= 2*(len(top.rows)**top.the.enough):
      left, right, i.x, i.y, i.c, i.mid = sample.half(top)
      if len(left.rows) < len(sample.rows):
        i.left  = Cluster(left, top)
        i.right = Cluster(right,top)

  def show(i,pre=""):
    s= f"{pre:40} : {len(i.here.rows):5}"
    print(f"{s}" if i.left  else f"{s} : {i.here.mid(i.here.y)}")
    for kid in [i.left,i.right]:
      if kid: kid.show(pre + "|.. ")
#                               _
#   ___  __ _   _ __    _ __  | |  ___
#  (_-< / _` | | '  \  | '_ \ | | / -_)
#  /__/ \__,_| |_|_|_| | .__/ |_| \___|
#                      |_|
class Sample(o):
  "Load, then manage, a set of examples."

  def __init__(i, the, inits=[]):
    """Samples hold ‘rows‘, summarized in ‘col‘umns. The non−skipped columns
  are stored in ‘x,y‘ lists for independent and dependent columns. Also
  stored is the ‘klass‘ column and ‘the‘ configuration options."""
    i.the = the
    i.rows, i.cols, i.x, i.y, i.klass = [], [], [], [],None
    if str ==type(inits): [i.add(row, True) for row in file(inits)]
    if list==type(inits): [i.add(row) for row in inits]

  def add(i, a, raw=False):
    """If we have no ‘cols‘, this ‘a‘ is the first row with the column names.
  Otherwise ‘a‘ is another row of data."""
    def pre(a,c)     : return c.prep(a[c.at]) if raw else a[c.at]
    def is_num(x)    : return x[0].isupper()
    def is_skip(x)   : return x[-1]==":"
    def is_klass(x)  : return "!" in x
    def is_goal(x)   : return "+" in x or "-" in x or is_klass(x)
    def col(at,txt)  :
      now = Num(i.the.Max,at=at,txt=txt) if is_num(txt) else Sym(at=at,txt=txt)
      where= i.y if is_goal(txt) else i.x
      if not is_skip(txt):
        where += [now]
        if is_klass(txt): i.klass = now
      return now
    #-----------
    if i.cols: i.rows += [Example([col.add(pre(a,col)) for col in i.cols])]
    else:      i.cols  = [col(at,txt) for at,txt in enumerate(a)]

  def clone(i,inits=[]):
    "Generate a new ‘Sample‘ with the same structure as this ‘Sample‘."
    out = Sample(i.the)
    out.add([col.txt for col in i.cols])
    [out.add(x) for x in inits]
    return out

  def cluster(i,top=None):
    """Split the data using random projections. Find the span that most
  separates the data. Divide data on that span."""
    here = Cluster(i)
    top = top or i
    if len(i.rows) >= 2*(len(top.rows)**i.the.enough):
      left,right,x,y,c,mid = i.half(top)
      if len(left.rows) < len(i.rows):
        here       = Cluster(i,x,y,c,mid)
        here.left  = left.cluster(top)
        here.right = right.cluster(top)
    return here

  def far(i,x,rows):
    tmp= sorted([(x.dist(y,i),y) for y in (rows or i.rows)],key=first)
    return tmp[ int(len(tmp)*i.the.far) ]

  def half(i, top=None):
    "Using two faraway points ‘x,y‘ break data at median distance."
    some=i.rows if len(i.rows)<i.the.Some else rnd.choices(i.rows,k=i.the.Some)
    top= top or i
    w  = any(some)
    _,x= top.far(w, some)
    c,y= top.far(x, some)
    tmp= [r for _,r in sorted([(top.proj(r,x,y,c),r)
                               for r in i.rows],key=first)]
    mid= len(tmp)//2
    return i.clone(tmp[:mid]), i.clone(tmp[mid:]), x, y, c, tmp[mid]

  def mid(i,cols=None):
    "Return a list of the mids of some columns."
    return [col.mid() for col in (cols or i.all)]

  def proj(i,row,x,y,c):
    "Find the distance of a ‘row‘ on a line between ‘x‘ and ‘y‘."
    a = row.dist(x,i)
    b = row.dist(y,i)
    return (a**2 + c**2 - b**2) / (2*c)

  def xplain(i,top=None):
    """Split the data using random projections. Find the span that most
  separates the data. Divide data on that span."""
    here = Explain(i)
    top = top or i
    tiny = len(top.rows)**top.the.enough
    if len(i.rows) >= 2*tiny:
      left, right,*_ = i.half(top)
      spans = []
      [lcol.spans(rcol,6/top.the.xsmall,spans) for lcol,rcol
                                           in zip(left.x, right.x)]
      if len(spans) > 0:
        here.span = Span.sort(spans)[0]
        yes, no = i.clone(), i.clone()
        [(yes if here.span.selects(row) else no).add(row) for row in i.rows]
        if tiny <= len(yes.rows) < len(i.rows): here.yes = yes.xplain(top=top)
        if tiny <= len(no.rows ) < len(i.rows): here.no  = no.xplain(top=top)
    return here
```

```
#     _
#    /\ \
#    \_\ \     __    ___ ___     ___     ____
#    /'_` \  /'__`\/' __` __`\  / __`\  /',__\
#   /\ \L\ \/\  __//\ \/\ \/\ \/\ \L\ \/\__, `\
#   \ \___,_\ \____\ \_\ \_\ \_\ \____/\/\____/
#    \/__,_ /\/____/\/_/\/_/\/_/\/___/  \/___/

class Demos:
  "Possible start-up actions."
  fails=0
  "Number of errors; returned to operating system as our exit code"
  def opt():
    "show the config."
    print(the)

  def seed():
    "seed"
    assert .494 <= r() <= .495

  def num():
    "check `Num`."
    n = Num(512)
    for _ in range(100): n.add(r())
    assert .30 <= n.div() <= .31, "in range"

  def sym():
    "check `Sym`."
    s = Sym()
    for x in "aaaabbc": s.add(x)
    assert 1.37 <= s.div() <= 1.38, "entropy"
    assert 'a'  == s.mid(), "mode"

  def rows():
    "count rows in a file."
    assert 399 == len([row for row in file(the.data)])

  def sample():
    "sampling."
    s = Sample(the, the.data)
    print(the.data, len(s.rows))
    print(s.x[3], s.rows[-1])
    assert 398 == len(s.rows),     "length of rows"
    assert 249 == s.x[-1].has['1'], "symbol counts"

  def dist():
    "distance between rows"
    s = Sample(the, the.data)
    assert .84 <= s.rows[1].dist(s.rows[-1],s) <= .842

  def clone():
    "cloning"
    s = Sample(the, the.data)
    s1 = s.clone(s.rows)
    d1,d2 = s.x[0].__dict__, s1.x[0].__dict__
    for k,v in d1.items():
      print(d2[k],v)
      assert d2[k] == v, "clone test"

  def half():
    "divide data in two"
    s = Sample(the, the.data)
    s1,s2,*_ = s.half()
    print(s1.mid(s1.y))
    print(s2.mid(s2.y))

  def cluster():
    "divide data in two"
    s = Sample(the, the.data)
    Cluster(s).show(); print("")

  def xplain():
    "divide data in two"
    s = Sample(the, the.data);
    s.xplain().show(); print("")

#-----------------------------------------------------
the = options(__doc__)
if __name__ == "__main__": demo(the.todo,Demos)

"""
Example class
"""
```