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SAM : Semi-supervised And Multi-objective explainations
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       |___/
-- In this code:
-- - Line strive to be 80 chars (or less)
-- - Two spaces before function argumnets denote optionals.
-- - Four spaces before function argumnets denote local variables.
-- - Private functions start with `_`
-- - Arguments of private functions do anything at all
-- - Local variables inside functions do anything at all
-- - Arguments of public functions use type hints
--   - Variable  `x` is is anything
--   - Prefix `is` is a boolean
--   - Prefix `fun` is a function
--   - Prefix `f` is a filename
--   - Prefix `n` is a string
--   - Prefix `s` is a string
--   - Prefix `c` is a column index
--   - `col` denotes `num` or `sym`
--   - `x` is anything (table or number of boolean or string
--   - `v` is a simple value (number or boolean  or  string)
--   - Suffix `s` is a list of things
--   - Tables are `t` or, using the above, a table of numbers would be `ns`
--   - Type names are lower case versions of constuctors; e.g `col` isa `Cols`.
--
--  All demo functions `eg.fun1` can be called via  `lua eg.lua -e fun1`.
local eg= {}

local l=require"lib"
local _=require"sam"
local o,oo,per,push,rnd = l.o,l.oo,l.per,l.push,l.rnd
local add,adds,dist,div = _.add,_.adds,_.dist,_.div
local mid, records, the = _.mid,_.records,_.the
local Num,Sym      = _.Num, _.Sym

-- Settings come from big string top of "sam.lua"
-- (maybe updated from comamnd line)
function eg.the() oo(the); return true end

-- The middle and diversity of a set of symbols is called "mode"
-- and "entropy" (and the latter is zero when all the symbols
-- are the same).
function eg.ent(  sym,ent)
  sym= adds(Sym(), {"a","a","a","a","b","b","c"})
  ent= div(sym)
  print(ent,mid(sym))
  return 1.37 <= ent and ent <=1.38 end

-- The middle and diversity of a set of numbers is called "median"
-- and "standard deviation" (and the latter is zero when all the nums
-- are the same).
function eg.num(  num)
  num=Num()
  for i=1,100 do add(num,i) end
  local med,ent = mid(num), rnd(div(num),2)
  print(mid(num) ,rnd(div(num),2))
  return 50<= med and med<= 52 and 30.5 <ent and ent <32 end

-- Nums store only a sample of the numbers added to it (and that storage
-- is done such that the kept numbers span the range of inputs).
function eg.bignum(  num)
  num=Num()
  the.nums = 32
  for i=1,1000 do add(num,i) end
  oo(_.nums(num))
  return 32==#num._has end

-- We can read data from disk-based csv files, where row1 lists a
-- set of columns names. These names are used to work out what are Nums, or
-- ro Syms, or goals to minimize/maximize, or (indeed) what columns to ignre.
function eg.records()
 oo(records("../../data/auto93.csv").cols.y); return true end

-- Any two rows have a distance 0..1 that satisfies equality, symmetry
-- and the triangle inequality.
function eg.dist(  data,t)
  data=records("../../data/auto93.csv")
  t={}
  for i=1,100 do
     local A,B,C = l.any(data.rows), l.any(data.rows), l.any(data.rows)
     local a,b,c = dist(data,B,C), dist(data,A,C), dist(data,A,B)
     assert(a<=1 and b<=1 and c<=1)
     assert(a>=0 and b>=0 and c>=0)
     assert( dist(data,A,A) == 0)              -- equality
     assert( dist(data,A,B) == dist(data,B,A)) -- symmetry
     assert(a+b>=c)                            -- triangle inequality
     for _,x in pairs{a} do push(t,rnd(x,2)) end  end
  table.sort(t)
  oo(t)
  return true end

function eg.far(  data)
  data = records("../../data/auto93.csv")
  oo(data.rows[1].cells)
  for i,t in pairs(_.around(data,data.rows[1])) do
    if i>390 or i< 10 then print(o(t.row.cells),t.dist) end end
  oo(_.far(data, data.rows[1]).cells)
  return true end

function eg.half(   data)
  data = records("../../data/auto93.csv")
  _.halves(data)
  --tree(_.halves(data),function(t) tostring(10) end)
  return true end

-- ---------------------------------------------------------------------------
the = l.cli(the)
os.exit( l.runs(the.eg, eg, the))

                                   _
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-- For a list of coding conventions in this file, see
-- [eg.lua](https://github.com/timm/lua/blob/main/src/sam/eg.lua).
local l=require"lib"
local the=l.settings([[
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USAGE: lua eg.lua [OPTIONS]

OPTIONS:
 -b  --bins    number of bins            = 8
 -c  --cohen   small effect              = .35
 -e  --eg      start-up example          = nothing
 -F  --far     far away                  = .95
 -f  --file    file with csv data        = ../../docs/auto93.csv
 -h  --help    show help                 = false
 -m  --min     min size = n^(the.min)    = .5
 -n  --nums    how many numbers to keep  = 256
 -p  --p       distance coeffecient      = 2
 -s  --seed    random number seed        = 10019
 -S  --sample  how many rows to search   = 512]])
-- Commonly used lib functions.
local lt,o,oo,map   = l.lt,l.o,l.oo,l.map
local per,push,sort = l.per, l.push,l.sort

---- ---- ---- ---- Classes
local Data,Cols,Sym,Num,Row
-- Holder of `rows` and their sumamries (in `cols`).
function Data() return {_is = "Data",
                        cols= nil,  -- summaries of data
                        rows= {}    -- kept data
                       } end

-- Holds of summaries of columns.
-- Columns are created once, then may appear in  multiple slots.
function Cols() return {
  _is  = "Cols",
  names={},  -- all column names
  all={},    -- all the columns (including the skipped ones)
  klass=nil, -- the single dependent klass column (if it exists)
  x={},      -- independent columns (that are not skipped)
  y={}       -- depedent columns (that are not skipped)
  } end

-- Summarizers a stream of symbols.
function Sym(c,s)
  return {_is= "Sym",
          n=0,          -- items seen
          at=c or 0,    -- column position
          name=s or "", -- column name
          _has={}       -- kept data
         } end

-- Summarizes a stream of numbers.
function Num(c,s)
  return {_is="Nums",
          n=0,at=c or 0, name=s or "", _has={}, -- as per Sym
          isNum=true,      -- mark that this is a number
          lo= math.huge,   -- lowest seen
          hi= -math.huge,  -- highest seen
          isSorted=true,    -- no updates since last sort of data
          w=(s or ""):find"-$" and -1 or 1 -- minimizing if w=-1
         } end

-- Holds one record
function Row(t) return {_is="Row",
                        cells=t,          -- one record
                        cooked=l.copy(t), -- used if we discretize data
                        isEvaled=false    -- true if y-values evaluated.
                       } end

---- ---- ---- ---- Data Functions
local add,adds,clone,div,mid,norm,nums,record,records,stats
---- ---- ---- Create
-- Generate rows from some `src`.  If `src` is a string, read rows from file;
-- else read rows from a `src`  table. When reading, use row1 to define columns.
function records(src,      data,head,body)
  function head(sNames)
    local cols = Cols()
    cols.names = namess
    for c,s in pairs(sNames) do
      local col = push(cols.all, -- Numerics start with Uppercase.
                       (s:find"^[A-Z]*" and Num or Sym)(c,s))
      if not s:find":$" then -- some columns are skipped
        push(s:find"[!+-]" and cols.y or cols.x, col) -- some cols are goal cols
        if s:find"!$"    then cols.klass=col end end end
    return cols
  end ------------
  function body(t) -- treat first row differently (defines the columns)
    if data.cols then record(data,t) else data.cols=head(t) end
  end ----------
  data =  Data()
  if type(src)=="string" then l.csv(src, body) else
    for _,t in pairs(src or {}) do body(t) end end
  return data end

-- Return a new data with same structure as `data1`. Optionally, oad in `rows`.
function clone(data1,  rows)
  data2=Data()
  data2.cols = _head(data1.cols.names)
  for _,row in pairs(rows or {}) do record(data2,row) end
  return data2 end

---- ---- ---- Update
-- Add one thing to `col`. For Num, keep at most `nums` items.
function add(col,v)
  if v~="?" then
    col.n = col.n + 1
    if not col.isNum then col._has[v] = 1 + (col._has[v] or 0) else
       col.lo = math.min(v, col.lo)
       col.hi = math.max(v, col.hi)
       local pos
       if     #col._has < the.nums           then pos = 1 + (#col._has)
       elseif math.random() < the.nums/col.n then pos = math.random(#col._has) end
```

```lua
      if pos then col.isSorted = false
                  col._has[pos] = tonumber(v) end end end end

-- Add many things to col
function adds(col,t) for _,v in pairs(t) do add(col,v) end; return col end

-- Add a `row` to `data`. Calls `add()` to  updatie the `cols` with new values.
function record(data,xs)
  local row= push(data.rows, xs.cells and xs or Row(xs)) -- ensure xs is a Row
  for _,todo in pairs{data.cols.x, data.cols.y} do
    for _,col in pairs(todo) do
      add(col, row.cells[col.at]) end end end

---- ---- ---- Query
-- Return kept numbers, sorted.
function nums(num)
  if not num.isSorted then num._has = sort(num._has); num.isSorted=true end
  return num._has end

-- Normalized numbers 0..1. Everything else normalizes to itself.
function norm(col,n)
  return x=="?" or not col.isNum and x or  (n-col.lo)/(col.hi-col.lo + 1E-32) end

-- Diversity (standard deviation for Nums, entropy for Syms)
function div(col)
  if  col.isNum then local a=nums(col); return (per(a,.9)-per(a,.1))/2.58 else
    local function fun(p) return p*math.log(p,2) end
    local e=0
    for _,n in pairs(col._has) do if n>0 then e=e-fun(n/col.n) end end
    return e end end

-- Central tendancy (median for Nums, mode for Syms)
function mid(col)
  if col.isNum then return per(nums(col),.5) else
    local most,mode = -1
    for k,v in pairs(col._has) do if v>most then mode,most=k,v end end
    return mode end end

-- For `showCols` (default=`data.cols.x`) in `data`, report `fun` (default=`mid`).
function stats(data,  showCols,fun,    t)
  showCols, fun = showCols or data.cols.y, fun or mid
  t={}; for _,col in pairs(showCols) do t[col.name]=fun(col) end; return t end

---- ---- ---- ---- Discretization
local bins,cook,divs
-- Find ranges within a num (unsupervised).
function bins(num)
  local a, epsilon = nums(num), the.cohen*div(num)
  local enough = #a^the.min
  local one = {lo=a[1], hi=a[1], n=0}
  local t = {one}
  for i,x in pairs(a) do
    if i < #a-enough and x ~= a[i+1] and n > enough and hi-lo > epsilon then
      one = push(t, {lo=one.hi, hi=a[i], n=0})  end
    one.hi = a[i]
    one.n  = 1 + one.n end
  t[1].lo  = -math.huge
  t[#t].ho =  math.huge
  return t end

-- Fill in discretized values (in `cooked`).
function cook(data)
  for _,num in pairs(data.cols.x) do
    if num.isNum then local t = bins(num)
                      for _,row in pairs(data.rows) do
                        local v = row.cells[num.at]
                        if v ~= "?" then
                          for _,bin in pairs(t) do
                            if v > bin.lo and v <= bin.hi then
                              row.cooked[col.at] = bin.lo
                              break end end end end end end end

-- Sum the entropy of the coooked independent columns.
function divs(data,rows)
  local n = 0
  for _,col in pairs(data.cols.x) do
    local sym= Sym()
    for _,row in pairs(rows or data.rows) do
      v = row.cooked[col.at]
      if v ~= "?" then add(s, v) end end
    n = n + div(sym) end
  return n end

---- ---- ---- ---- Distance functions
local around, dist, far, half, halves
-- Distance between rows (returns 0..1). For unknown values, assume max distance.
function dist(data,t1,t2)
  local function fun(col,  v1,v2)
    if   v1=="?" and v2=="?" then return 1 end
    if not col.isNum then return v1==v2 and 0 or 1 end
    v1,v2 = norm(col,v1), norm(col,v2)
    if v1=="?" then v1 = v2<.5 and 1 or 0 end
    if v2=="?" then v2 = v1<.5 and 1 or 0 end
    return math.abs(v1-v2)
  end -------
  local d = 0
  for _,col in pairs(data.cols.x) do
    d = d + fun(col, t1.cells[col.at], t2.cells[col.at])^the.p end
  return (d/#data.cols.x)^(1/the.p) end

-- Sort `rows` (default=`data.rows`) by distance to `row1`.
function around(data,row1,  rows,     fun)
  function fun(row2) print("row2",#row2);return {row=row2, dist=dist(data,row1,row
2)} end
  return sort(map(rows or data.rows,fun),lt"dist") end

-- Return the row that is `the.far` to max distance away from `row`.
function far(data,row,  rows)
  oo{row=row}
  return per(around(data,row,rows), the.far).row end

-- Split `rows` (default=`data.rows`) in half by distance to 2 distant points.
function half(data,rows,  rowAbove)
  local some,left,right,c,lefts,rights,fun
  rows  = rows or data.rows
  some  = l.many(rows, the.sample)
  left  = rowAbove or far(data, l.any(some),some)
  right = far(data, left,some)
  c     = dist(data,left,right)
  lefts,rights = {},{}
  function fun(row) local a = dist(data,row,left)
                    local b = dist(data,row,right)
                    return {row=rows, d=(a^2 + c^2 - b^2) / (2*c)} end
  for i,rowd in pairs(sort(map(rows, fun), lt"d")) do
    push(i <= #rows/2 and lefts or rights, rowd.row) end
  return left,right,lefts,rights,c end

-- Recursively split `rows` (default=`data.rows`) in half.
function halves(data,    stop,fun)
  function fun(rows,  rowAbove,    here,left,right,lefts,rights)
    here = {node=rows}
    print(#rows, stop)
    if #rows >= stop then
      left,right,lefts,rights = half(data, rows,rowAbove)
      here.kids = {fun(lefts,left), fun(rights,right)} end
    return here
  end --------
  stop = (#data.rows)^the.min
  return fun(data.rows) end

function tree(x,  nodeFun,     pre)
  nodeFun = nodeFun or io.write
  pre = pre or "|.. "
  print(pre,nodeFun(x.node))
  for _,kid in pairs(x.kids or {}) do tree(kid, nodeFun, pre.."|.. ") end end


-- ---------------------------------------------------------------------------
-- That's all folks.
return {
  the=the, Data=Data, Cols=Cols, Sym=Sym, Num=Num, Row=Row, add=add,
  adds=adds, around=around, bin=bins,clone=clone,cook=cook,dist=dist, div=div,
  divs=divs, far=far, half=half, halves=halves, mid=mid, nums=nums, records=record
s,
  record=record, stats=stats}
  _   _   _          _                 
 | | (_) | |__      | |  _   _    __ _ 
 | | | | | '_ \  _  | | | | | |  / _` |
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-- lib.lua: misc LUA functions
-- (c)2022 Tim Menzies <timm@ieee.org> BSD-2 licence
local l={}

---- ---- ---- ---- Meta
-- Find rogue locals.
l.b4={}; for k,v in pairs(_ENV) do l.b4[k]=v end
function l.rogues()
  for k,v in pairs(_ENV) do if not l.b4[k] then print("?",k,type(v)) end end end

---- ---- ---- ---- Lists
-- Add `x` to a list. Return `x`.
function l.push(t,x) t[1+#t]=x; return x end

-- Sample one item
function l.any(t) return t[math.random(#t)] end

-- Sample many items
function l.many(t,n,  u)  u={}; for i=1,n do u[1+#u]=l.any(t) end; return u end

-- Deepcopy
function l.copy(t)
  if type(t) ~= "table" then return t end
  local u={}; for k,v in pairs(t) do u[k] = l.copy(v) end
  return setmetatable(u,getmetatable(t))  end

-- Round
function l.rnd(n, nPlaces)
  local mult = 10^(nPlaces or 3)
  return math.floor(n * mult + 0.5) / mult end

-- Deepcopy
function l.copy(t)
  if type(t) ~= "table" then return t end
  local u={}; for k,v in pairs(t) do u[k] = l.copy(v) end
  return u end

-- Return the `p`-th thing from the sorted list `t`.
function l.per(t,p)
  p=math.floor(((p or .5)*#t)+.5); return t[math.max(1,math.min(#t,p))] end

-- Return the list `t` sorted using `fun`.
function l.sort(t,fun)  table.sort(t,fun); return t end

-- Return a function that sorts on `s` , in ascending order.
function l.lt(s) return function(t1,t2) return t1[s] < t2[s] end end

-- Map `fun` over `t1`, returning all not-nil results.
function l.map(t1,fun)
  local t2={}; for _,v in pairs(t1) do t2[1+#t2] = fun(v) end; return t2 end

---- ---- ---- ---- Strings
-- `o` generates a string from a nested table.
function l.o(t)
  if type(t) ~=  "table" then return tostring(t) end
  local function show(k,v)
    if not tostring(k):find"^_"  then
      v = l.o(v)
      return #t==0 and string.format(":%s %s",k,v) or tostring(v) end end
  local u={}; for k,v in pairs(t) do u[1+#u] = show(k,v) end
  return (t._is or "").."{"..table.concat(#t==0 and l.sort(u) or u," ").."}" end

-- `oo` prints the string from `o`.
function l.oo(t) print(l.o(t)) return t end
--
-- Convert string to something else.
function l.coerce(s)
  local function coerce1(s1)
    if s1=="true"  then return true end
    if s1=="false" then return false end
    return s1 end
  return math.tointeger(s) or tonumber(s) or coerce1(s:match"^%s*(.-)%s*$") end

-- Iterator over csv files. Call `fun` for each record in `fname`.
function l.csv(fname,fun)
  local src = io.input(fname)
  while true do
    local s = io.read()
    if not s then return io.close(src) else
      local t={}
      for s1 in s:gmatch("([^,]+)") do t[1+#t] = l.coerce(s1) end
      fun(t) end end end

---- ---- ---- ---- Settings
-- Parse help string looking for slot names and default values
function l.settings(s)
  local t={}
  s:gsub("\n [-][%S]+[%s]+[-][-]([%S]+)[^\n]+= ([%S]+)",
         function(k,x) t[k]=l.coerce(x)end)
  t._help = s
  return t end

-- Update `t` from values after command-line flags. Booleans need no values
-- (we just flip the defeaults).
function l.cli(t)
  for slot,v in pairs(t) do
    v = tostring(v)
    for n,x in ipairs(arg) do
      if x=="-"..(slot:sub(1,1)) or x=="--"..slot then
        v = v=="false" and "true" or v=="true" and "false" or arg[n+1] end end
    t[slot] = l.coerce(v) end
  if t.help then os.exit(print("\n"..t._help.."\n")) end
  return t end

---- ---- ---- ---- Main
-- In this function:
-- - `k`=`ls`  : list all settings
-- - `k`=`all` : run all demos
-- - `k`=x     : run one thing
--
-- For each run, beforehand, reset random number seed. Afterwards,
-- discard and settings changes made during that one run.
-- If any run does not return `true`, increment `fails`.
-- Return fails counter.
function l.runs(k,funs,settings)
  local fails =0
  local function _egs(   t)
    t={}; for k,_ in pairs(funs) do t[1+#t]=k end; table.sort(t); return t end
  if k=="ls" then -- list all
    print("\nExamples -e X):\nX=")
    print(string.format(" %-7s","all"))
    print(string.format(" %-7s","ls"))
    for _,k in pairs(_egs()) do print(string.format(" %-7s",k)) end
  elseif k=="all" then -- run all
    for _,k in pairs(_egs()) do
      fails=fails + (l.runs(k,funs,settings) and 0 or 1) end
  elseif funs[k] then -- run one
    math.randomseed(settings.seed) -- reset seed
    local b4={}; for k,v in pairs(settings) do b4[k]=v end
    local out=funs[k]()
    for k,v in pairs(b4) do settings[k]=v end -- restore old settings
    print("!!!!!!", k, out and "PASS" or "FAIL") end
  l.rogues()
  return fails end

-- ------------------------------------------------
-- That's all folks.
return l
```