```lua
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local b4={}; for k,_ in pairs(_ENV) do b4[k]=k end
local the, help = {}, [[

lua bnbad.lua [OPTIONS]
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OPTIONS:
  -cohen     -c cohen                   = .35
  -far       -f how far to seek poles = .9
  -keep      -k items to keep           = 256
  -minItems  -m min items in a rang e = .5
  -p         -p euclidean coefficient = 3

OPTIONS, other:
  -dump      -d stackdump on error      = false
  -file      -f data file               = ../etc/data/auto93.csv
  -help      -h show help               = false
  -rnd       -r round numbers           = %5.2f
  -seed      -s random number seed      = 10019
  -todo      -t start-up action         = nothing
]]

local any, bestSpan, bins, bins1, bootstrap, firsts, fmt, last
local many, map, new, o, obj, oo, per, push, quintiles, r, rnd, rnds, scottKnot
local selects, settings,slots, smallfx, sort, sum, thing, things, xplains

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new = setmetatable
function obj(s,   t)
  t={__tostring=o,_is=s or ""}; t.__index=t
  return new(t, {__call=function(_,...) return t.new(_,...) end}) end

local Num, Sym, Egs = obj"Num", obj"Sym", obj"Egs"

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function Sym:new(at,name)
    return new({at=at, name=name, most=0,n=0,all={}}, Sym) end

function Num:new(at,name)
    return new({at=at, name=name, _all={}, w=(name or ""):find"-$" and -1 or 1,
               n=0, sd=0, mu=0, m2=0, lo=math.huge, hi=-math.huge}, Num) end

function Egs:new(names,   i,col)
  i = new({all={}, cols={names=names, all={}, x={}, y={}}}, Egs)
  for at,name in pairs(names) do
    col = (name:find"^[A-Z].-" and Num or Sym)(at,name)
    push(i.cols.all, col)
    if not name:find":$" then
      if name:find"!$" then i.cols.class = col end
      push(name:find"[-+!]$" and i.cols.y or i.cols.x, col) end end
  return i end

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function Sym.copy(i) return Sym(i.at, i.name) end

function Num.copy(i) return Num(i.at, i.name) end

function Egs.copy(i,all,    j)
  j = Egs(i.cols.name)
  for _,row in pairs(rows or {}) do i:add(row) end
  return j end

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function Egs.add(i,row)
  i.all[1 + #i.all] = row
  for at,col in pairs(i.cols) do col:add(row[col.at]) end end

function Sym.add(i,x,inc)
  if x ~= "?" then
    inc = inc or 1
    i.n = i.n+inc
    i.all[x] = inc + (i.all[x] or 0)
    if i.all[x] > i.most then i.most, i.mode = i.all[x], x end end end

function Sym.sub(i,x,inc)
  if x ~= "?" then
    inc = inc or 1
    i.n = i.n - inc
    i.all[x] = i.all[x] - inc end end

function Num.add(i,x,_,    d,a)
  if x ~="?" then
    i.n   = i.n + 1
    d     = x - i.mu
    i.mu  = i.mu + d/i.n
    i.m2  = i.m2 + d*(x - i.mu)
    i.sd  = (i.m2<0 or i.n<2) and 0 or ((i.m2/(i.n - 1))^0.5)
    i.lo  = math.min(x, i.lo)
    i.hi  = math.max(x, i.hi)
    a     = i._all
    if      #a  < the.keep     then i.ok=false; push(a,x)
    elseif r() < the.keep/i.n then i.ok=false; a[r(#a)]=x end end end

function Num.sub(i,x,_,    d)
  if x ~="?" then
    i.n   = i.n - 1
    d     = x - i.mu
    i.mu  = i.mu - d/i.n
    i.m2  = i.m2 - d*(x - i.mu)
    i.sd  = (i.m2<0 or i.n<2) and 0 or ((i.m2/(i.n - 1))^0.5) end end

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function Num.sorted(i)
  if not i.ok then table.sort(i._all); i.ok=true end
  return i._all end

function Num.mid(i) return i.mu end
function Sym.mid(i) return i.mode end

function Num.div(i) return i.sd end
function Sym.div(i,  e)
  e=0
  for _,n in pairs(i.all) do
    if n > 0 then e = n/i.n * math.log(n/i.n,2) end end
  return -e end

function Num.norm(i,x)
  return i.hi - i.lo < 1E-32 and 0 or (x - i.lo)/(i.hi - i.lo) end
```

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function Num.dist(i,a,b)
  if     a=="?" and b=="?" then return 1 end
  if     a=="?" then b=i:norm(b); a=b<.5 and 1 or 0
  elseif b=="?" then a=i:norm(a); b=a<.5 and 1 or 0
  else   a,b = i:norm(a), i:norm(b)  end
  return math.abs(a - b) end

function Sym.dist(i,a,b)
  return a=="?" and b=="?" and 1 or a==b and 0 or 1 end

function Egs.dist(i,row1,row2,    d)
  d = sum(i.cols.x, function(c) return c:dist(row1[c.at], row2[c.at])^the.p end)
  return (d/#i.cols.x)^(1/the.p) end

function Egs.dists(i,r1,rows)
   return sort(map(rows,function(s) return{i:dist(r1,r2),r2} end),firsts) end

function Egs.half(i, rows)
  local project,far,some,left,right,c,lefts,rights
  far     = function(r,t)  return per(i:dists(r,t), the.far)[2] end
  project= function(r1,  a,b)
             a,b = i:dist(left,r1), i:dist(right,r1)
             return {(a^2 + c^2 - b^2)/(2*c), r1} end
  some   = many(rows,       the.some)
  left   = i:far(any(some), some)
  right  = i:far(left,      some)
  c      = i:dist(left,right)
  lefts,rights = i:copy(), i:copy()
  for n, projection in pairs(sort(map(rows,project),firsts)) do
    if n==#rows//2 then mid=row end
    (n <= #rows//2 and lefts or rights):add( projection[2] ) end
  return lefts, rights, left, right, mid, c  end

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function Num.spans(i,j, cuts)
  local xys,all = {}, Num
  for _,n in pairs(i._all) do all:add(n); push(xys,{x=n,y="left"}) end
  for _,n in pairs(j._all) do all:add(n); push(xys,{x=n,y="right"})  end
  return bins(i,cuts,
         bins1(sort(xys,first),(#xys)^the.minItems,all.sd*the.cohen,Sym,{})) end

function bins1(col, old,new)
  if #new>1 then
    new[1].lo    = -math.huge
    new[#new].hi =  math.huge
    for _,cut in pairs(new) do cut.col= col; push(old,cut) end end end

function bins1(xys, minItems, cohen, yclass, cuts, b4)
  local lhs, rhs, b4, cut, div, xpect = yclass(), yclass(), b4 or xys[1].x
  function xpect(i,j) return (i.n*i:div() + j.n*j.div()) / (i.n + j.n) end
  for _,xy in pairs(xys) do rhs:add(xy.y) end
  div = rhs:div()
  for j,xy in pairs(xys) do
    lhs:add(xy.y)
    rhs:sub(xy.y)
    if lhs.n >= minItems and rhs.n >= minItems then
      if xy.x ~= xys[j+1].x then
        if xy.x - xys[1].x >= cohen and xys[#xys].x - xy.x >= cohen then
          if xpect(lhs,rhs) < div then
            cut, div = j, xpect(lhs,rhs) end end end end end
  if   cut
  then local l,r = {},{}
       for n,xy in pairs(xys) do push(n<=cut and l or r, xy) end
       bins1(l, minItems, cohen, yclass, cuts, b4)
       bins1(r, minItems, cohen, yclass, cuts, xys[cut].x)
  else push(cuts, {lo=b4, hi=xys[#xys].x, n=#xys, div=div}) end end

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local xplain,xplains,selects,spanShow
function Egs.xplain(i,rows)
  local stop,here,left,right,lefts0,rights0,lefts1,rights1
  rows = rows or i.all
  here = {all=rows}
  stop = (#i.all)^the.minItems
  if #rows >= 2*stop then
    lefts0, rights0, here.left, here.right, here.mid, here.c  = half(i, rows)
    if #lefts0.all < #rows then
      cuts = {}
      for j,col in pairs(lefs0.col.x) do col:spans(rights0.col.x[j],cuts) end
      lefts1,rights1 = {},{}
      for _,row in pairs(rows) do
        push(selects(here.selector, row) and lefts1 or rights1, row) end
      if #lefts1  > stop then here.lefts  = xplain(i,lefts1) end
      if #rights1 > stop then here.rights = xplain(i,rights1) end end end
  return here end

function bestSpan(spans)
  local divs,ns,n,div,stats,dist2heaven = Num(), Num()
  function dist2heaven(s) return {((1 - n(s))^2 + (0 - div(s))^2)^.5,s} end
  function div(s)         return divs:norm( s.all:div() ) end
  function n(s)           return   ns:norm( s.all.n     ) end
  for _,s in pairs(spans) do
    add(divs, s.all:div())
    add(ns,   s.all.n) end
  return sort(map(spans, dist2heaven), firsts)[1][2]  end

function selects(span,row,    lo,hi,at,x)
  lo, hi, at = span.lo, span.hi, span.col.at
  x = row[at]
  if x=="?" then return true end
  if lo==hi then return x==lo else return lo <= x and x < hi end end

function xplains(i,format,t,pre,how,    sel,front)
  pre, how = pre or "", how or ""
  if t then
    pre=pre or ""
    front = fmt("%s%s%s %s",pre,how, #t.all, t.c and rnd(t.c) or "")
    if t.lefts and t.rights then print(fmt("%-35s",front)) else
      print(fmt("%-35s %s",front, o(rnds(mids(i,t.all),format))))
    end
    sel = t.selector
    xplains(i,format,t.lefts,  "|".. pre, spanShow(sel).."":")
    xplains(i,format,t.rights, "|".. pre, spanShow(sel,true) ..":") end end

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function quintiles(ts,width,  nums,out,all,n,m)
  width=width or 32
  nums=Num(); for _,t in pairs(ts) do
                 for _,x in pairs(sort(t)) do add(nums,x) end end
  all,out = nums.all, {}
  for _,t in pairs(ts) do
     local s, where = {}
     where = function(n) return (width*nums:norm(n))//1 end
     for j = 1, width do s[j]=" " end
     for j = where(per(t,.1)), where(per(t,.3)) do s[j]="-" end
     for j = where(per(t,.7)), where(per(t,.9)) do s[j]="-" end
     s[where(per(t, .5))] = "|"
     push(out,{display=table.concat(s),
               data = t,
               pers = map({.1,.3,.5,.7,.9},
                          function(p) return rnd(per(t,p))end)}) end
  return out end

function smallfx(xs,ys,     x,y,lt,gt,n)
  lt,gt,n = 0,0,0
  if #ys > #xs then xs,ys=ys,xs end
  for _,x in pairs(xs) do
    for j=1, math.min(64,#ys) do
      y = any(ys)
      if y<x then lt=lt+1 end
      if y>x then gt=gt+1 end
      n = n+1 end end
  return math.abs(gt - lt) / n <= the.cliffs end

function bootstrap(y0,z0)
  local x, y, z, b4, yhat, zhat, bigger
  local function obs(a,b,    c)
    c = math.abs(a.mu - b.mu)
    return (a.sd + b.sd) == 0 and c or c/((x.sd^2/x.n + y.sd^2/y.n)^.5) end
  local function adds(t, num)
    num = num or Num(); map(t, function(x) add(num,x) end); return num end
  y,z    = adds(y0), adds(z0)
  x      = adds(y0, adds(z0))
  b4     = obs(y,z)
  yhat   = map(y.all, function(y1) return y1 - y.mu + x.mu end)
  zhat   = map(z.all, function(z1) return z1 - z.mu + x.mu end)
  bigger = 0
  for j=1,the.boot do
    if obs( adds(many(yhat,#yhat)),  adds(many(zhat,#zhat))) > b4
    then bigger = bigger + 1/the.boot end end
  return bigger >= the.conf end

--- xxx mid has to be per and
-- XXX implement same
-- XXX need tests for stats
function scottKnot(nums,      all,cohen)
  local mid = function (z) return z.some:mid()
  end --------------------------------
  local function summary(i,j,    out)
    out = copy( nums[i] )
    for k = i+1, j do out = out:merge(nums[k]) end
    return out
  end --------------------------
  local function div(lo,hi,rank,b4,       cut,best,l,l1,r,r1,now)
    best = 0
    for j = lo,hi do
      if j < hi  then
        l   = summary(lo,  j)
        r   = summary(j+1, hi)
        now = (l.n*(mid(l) - mid(b4))^2 + r.n*(mid(r) - mid(b4))^2
              ) / (l.n + r.n)
        if now > best then
          if math.abs(mid(l) - mid(r)) >= cohen then
            cut, best, l1, r1 = j, now, copy(l), copy(r)
    end end end end
    if cut and not l1:same(r1,the) then
      rank = div(lo,    cut, rank, l1) + 1
      rank = div(cut+1, hi,  rank, r1)
    else
      for i = lo,hi do nums[i].rank = rank end end
    return rank
  end -------------------------------------------------------
  table.sort(nums, function(x,y) return mid(x) < mid(y) end)
  all   = summary(1,#nums)
  cohen = all.sd * the.cohen
  div(1, #nums, 1, all)
  return nums end
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r=math.random

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function last(a)        return a[ #a ] end
function per(a,p)       return a[ (p*#a)//1 ] end
function any(a)         return a[ math.random(#a) ] end
function many(a,n,  u) u={}; for j=1,n do push(u,any(a)) end; return u end

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function push(t,x)   t[1 + #t] = x; return x end
function map(t,f, u) u={};for _,v in pairs(t) do push(u,f(v)) end; return u end
function sum(t,f, n)
  f = f or function(x) return x end
  n=0; for _,v in pairs(t) do n = n + f(v) end; return n end

function sort(t,f)   table.sort(t,f); return t end
function firsts(a,b) return a[1] < b[1] end

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function thing(x)
  x = x:match"^%s*(.-)%s*$"
  if x=="true" then return true elseif x=="false" then return false end
  return tonumber(x) or x end

function things(file,      x)
  local function cells(x,  t)
    t={}; for y in x:gmatch("([^,]+)") do push(t, thing(y)) end; return t end
  file = io.input(file)
  return function()
    x=io.read(); if x then return cells(x) else io.close(file) end end end

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fmt = string.format

function oo(t) print(o(t)) end

function o(t,  seen, u)
  if type(t)~="table" then return tostring(t) end
  seen = seen or {}
  if seen[t] then return "..." end
  seen[t] = t
  local function show1(x) return o(x, seen) end
  local function show2(k) return fmt(":%s %s",k,o(t[k],seen)) end
  u = #t>0 and map(t,show1) or map(slots(t),show2)
  return (t._is or "").."{"..table.concat(u," ").."}" end

function slots(t, u)
  u={};for k,v in pairs(t) do if tostring(k):sub(1,1)~="_" then push(u,k)end end
  return sort(u) end

function rnds(t,f) return map(t, function(x) return rnd(x,f) end) end
function rnd(x,f)
  return fmt(type(x)=="number" and (x~=x//1 and f or the.rnd) or "%s",x) end

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function settings(txt,    d)
  d={}
  txt:gsub("\n ([-]([^%s]+))[%s]+(-[^%s]+)[^\n]*%s([^%s]+)",
    function(long,key,short,x)
      for n,flag in ipairs(arg) do
        if flag==short or flag==long then
          x = x=="false" and true or x=="true" and "false" or arg[n+1] end end
       d[key] = x==true and true or thing(x) end)
  return d end

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local go, ok = {fails=0}
function ok(test,msg)
  print(test and "   PASS: "or "   FAIL: ",msg or "")
  if not test then
    go.fails=go.fails+1
    if the.dump then assert(test,msg) end end end

function go.main(todo,seed)
  for k,one in pairs(todo=="all" and slots(go) or {todo}) do
    if k ~= "main" and type(go[one]) == "function" then
      math.randomseed(seed)
      print(fmt(":%s",one))
      go[one]() end end
  for k,v in pairs(_ENV) do if not b4[k] then print("?",k,type(v)) end end
  return go.fails end

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function go.last()
  ok( 30 == last{10,20,30}, "lasts") end

function go.per(  t)
  t={};for i=1,100 do push(t,i*1000) end
  ok(70000 == per(t,.7), "per") end

function go.many(  t)
  t={};for i=1,100 do push(t,i) end; many(t,10) end

function go.sum(  t)
  t={};for i=1,100 do push(t,i) end; ok(5050==sum(t),"sum")end

-- function go.things(  t)
--   t={}; for row in things(the.file) do oo(row) end end

function go.egs( )
  ok(Egs({"name","age","Weight!"}).cols.x,"Egs")   end

function go.sym(  s)
  s=Sym(); map({1,1,1,1,2,2,3}, function(x) s:add(x) end)
  ok(1.378 < s:div() and s:div() < 1.379, "ent") end

function go.num( n)
  n=Num(); map({10, 12, 23, 23, 16, 23, 21, 16},function(x) n:add(x) end)
  ok( 4.89 < n:div() and 4.90 < n:div(), "div") end

function go.nums( num,t,b4)
  t={};for j=1,1000 do push(t,100*r()*j) end
  num=Num()
  b4={};
  for j=1,#t  do
    num:add(t[j])
    if j%100==0 then    b4[j] =  fmt("%.5f",num:div()) end end
  for j=#t,1,-1 do
    if j%100==0 then ok(b4[j] == fmt("%.5f",num:div()),"div"..j) end
    num:sub(t[j]) end end

function go.syms( t,b4,s,sym)
  s="I have gone to seek a great perhaps."
  t={}; for j=1,20 do s:gsub('.',function(x) t[#t+1]=x end) end
  sym=Sym()
  b4={};
  for j=1,#t  do
    sym:add(t[j])
    if j%100==0 then    b4[j] =  fmt("%.5f",sym:div()) end end
  for j=#t,1,-1 do
    if j%100==0 then ok(b4[j] == fmt("%.5f",sym:div()),"div"..j) end
    sym:sub(t[j]) end
  end

--------------------------------------------------------------------------
the = settings(help)
if the.help then print(help) else go.main(the.todo, the.seed) end
```