```
local help = [[
                                                                                                                                                                                                                                                                    -- misc
function distance2Heaven(t,heaven, num,d)
for n,txt in pairs(heaven) do
num = Num(at,txt)
for _,z in pairs(t) do num:add(z.ys[n]) end
for _,z in pairs(t) do z.ys[n] = num:distance2heaven(z.ys[n]) end end
d = function(one) return (sum(one,ys)*fone,ys)*.5 end
return sort(t, function(a,b) return d(a) < d(b) end) end
  15 == a little lab of lots of LUA learning algorithms.
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  USAGE:
lua 15.lua [OPTIONS]
 OPTIONS:
         FIONS:

-cohen F Cohen's delta = .35
-data N data file = etc/data/auto93.csv
-Dump stack dump on assert fails = false
-furthest F far = .9
-Format s format string = $5.2f
-keep P max kept items = 512
-distance coefficient = 2
                                                                                                                                                                                                                                                                                                                                        function new(k,t) k.__index=k; k.__tostring=o; return setmetatable(t,k) end
                                                                                                                                                                                                                                                                        -- COLS: turns list of column names into NUMs, SYMs, or SKIPs
                                                                                                                                                                                                                                                                      function COLS.new(k,row, i)
i= new(k,{all={},x={}},names=row})
for at,txt in ipairs(row) do push(i.all, i:col(at,txt)) end
return i end
  KEY: N=fileName F=float P=posint S=string
                                                                                                                                                                                                                                                                     function COLS.add(i,t)
for _,col in pairs(i.all) do col:add(t[col.at]) end
return t end
         NOTES: This code uses Aha's distance measure [^Ah91] (that can handle numbers and symbols) to recursively divide data based on two distant points (these two are found in linear time using the Fastmap heuristic [Fa95]).
                                                                                                                                                                                                                                                                     function COLS.col(i,at,txt, col)
if ignorep(txt) then return SKIP:new(at,txt) end
col = (nump(txt) and NUM or SYM):new(at,txt)
push(goalp(txt) and i.y or i.x, col)
if klassp(txt) then i.klass = col end
return col end
   -- To avoid spurious outliers, this code use the 90% furthest points.
         To avoid long runtimes, uses a subset of the data to learn where to divide data (then all the data gets pushed down first halves)
                                                                                                                                                                                                                                                                      -- NUM: summarizes a stream of numbers
function NUM.new(k,n,s)
return new(k,fn,e),at=n or 0,txt=s or"",has=SOME:new(),ok=false,
w=lessp(s or "") and -1 or 1, lo=big, hi=-big}) end
         To support explanation, optionally, at each level of recursion, this code reports what ranges can best distinguish sibling clusters C1,C2. The discretizer is inspired by the Childwerge algorithm: numerics are divided into, say, 16 bins. Then, while we can find adjacent bins with the similar distributions in C1,C2, then (a) merge then (b) look for other merges.
                                                                                                                                                                                                                                                                     function NUM.add(i,x)
if x -= "?" then
i.n = i.n + 1
if i.has:add(x) then i.ok=false end
i.lo,i.hi = min(x,i.lo), max(x,i.hi); end end
                                                                                                                                                                                                                                                                     -- Cache current globals, use at end to find roque variables local b4=\{\}; for k,_ in pairs(_ENV) do b4[k]=k end
    -- Defined local names
  local any.asserts,big,cli,csv,fails,firsts,fmt,goalp,ignorep,klassp
local lessp,map,main,many,max,merge,min,morep,new,nump,o,oo,per,pop,push
local r,rows,rnd,rnds,slots,sort,sum,thing,things,unpack
                                                                                                                                                                                                                                                                      function NUM.distance2heaven(x, w)
  return ((i.w>0 and 1 or 0) - i:norm(x))^2 end
         Classes have UPPER CASE names
  function NUM.mid(i) return per(i:sorted(), .5) end
 - ## Settings
- Parse the help text for flags and defaults (e.g. -keep, 512).
- Check for updates on those details from command line
- (and and there,
- some shortcuts are available;
- e.g. _ *N _ & *rArr; 'keep=N';
- and _ -booleanFlag_ & *rArr; 'booleanFlag=not default').

local the={}
help:gsub("\m [-|(|\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{2}|-\frac{n}{
                                                                                                                                                                                                                                                                      function NUM.norm(i,x)
  return math.abs(i.hi-i.lo)<1E-9 and 0 or (x-i.lo)/(i.hi - i.lo) end</pre>
                                                                                                                                                                                                                                                                       function NUM.sorted(i)
  if i.ok==false then table.sort(i.has.all); i.ok=true end
  return i.has.all end
                                                                                                                                                                                                                                                                       -- ROWS: manages 'rows', summarized in 'cols' (columns).

function ROWS.new(k,inits, i)

i = new(k,(rows={},cols=nil})

if type(inits)=="string" then for t in csv(inits) do i:add(t) end end

if type(inits)=="table" then for t in inits do i:add(t) end end
                                                                                                                                                                                                                                                                            return i end
                                                                                                                                                                                                                                                                     function ROWS.add(i,t)
  if i.cols then push(i.rows,i.cols:add(t)) else i.cols=COLS:new(t) end end
 -- this code reads csv files where the words on linel define column types. function ignorep(x) return x:find"\S" end -- columns to ignore function klassp(x) return x:find"\S" end -- symbolic goals to achieve function lessp(x) return x:find"\S" end -- number goals to minimize function nump(x) return x:find"\A-Z\]" end -- numeric goals to maximize function nump(x) return x:find"\A-Z\]" end -- numeric columns
                                                                                                                                                                                                                                                                     function ROWS.clone(i, j) j= ROWS:new(); j:add(i.cols.names);return j end
                                                                                                                                                                                                                                                                     function ROWS.dist(i,row1,row2, d,fun)
function fun(col) return col:dist(row1[col.at], row2[col.at])^the.p end
return (sum(i.cols.x, fun)/ #i.cols.x)^(1/the.p) end
  function goalp(x) return morep(x) or lessp(x) or klassp(x) end
                                                                                                                                                                                                                                                                     function ROWS.furthest(i,row1,rows, fun)
  function fun(row2) return {i:dist(row1,row2), row2} end
  return unpack(per(sort(map(rows,fun),firsts), the.furthest)) end
  -- strings
fmt = string.format
                                                                                                                                                                                                                                                                     function ROWS.half(i, top)
local some, top,c,x,y,tmp,mid,lefts,rights,_
some= many(i.rows, the.keep)
top = top or i
    _,x = top:furthest(any(some), some)
    _,x = top:furthest(any(some), some)
-- maths
big = math.huge
max = math.max
min = math.min
r = math.random
                                                                                                                                                                                                                                                                            __x = top:furthest(any(some), some)
c,y = top:furthest(x, some)
some)
timp = sort(map(i.rows,function(r) return top:fastmap(r,x,y,c) end),firsts)
mid = #i.rows//2
lefts, rights = iclone(), i:clone()
for at,row in pairs(tmp) do (at <=mid and lefts or rights):add(row[2]) end
return lefts,rights,x,y,c, tmp[mid] end
  function \operatorname{rnds}(t,f) return \operatorname{map}(t,\operatorname{function}(x)\operatorname{return}\operatorname{rnd}(x,f)\operatorname{end}) end function \operatorname{rnd}(x,f) return \operatorname{fmt}(\operatorname{type}(x) = \operatorname{"number"}\operatorname{and}(x - \operatorname{x} / 1\operatorname{and} f\operatorname{or}\operatorname{the.Format})\operatorname{or}\operatorname{"%s"},x) end
  pop = table.remove
unpack = table.unpack
function any(t)
function firsts(a,b)
                                                                                                                                                                                                                                                                      function ROWS.mid(i,cols)
  return map(cols or i.cols.all, function(col) return col:mid() end) end
                                                                  return t[r(#t)] end
return a[1] < b[1] end
u={}; for i=1, n do push(u,any(t)) end; return u end
return t[ (#t*(p or .5))//1 ] end
table.insert(t,x); return x end
table.sort(t,f); return t end</pre>
  function many(t,n, u)
function per(t,p)
function push(t,x)
function sort(t,f)
                                                                                                                                                                                                                                                                      function ROWS.fastmap(i, r,x,y,c, a,b) 
 a,b = i : dist(r,x), i : dist(r,y); return \{(a^2 + c^2 - b^2)/(2*c), r\} end
                                                                                                                                                                                                                                                                       -- SKIP: summarizes things we want to ignore (so does nothing)
function SKIP.new(k,n,s) return new(k,{n=0,at=at or 0,txt=s or""}) end
function SKIP.add(i,x) return x end
function SKIP.mid(i) return "?" end
  -- meta
function map(t,f, u) u={}; for k,v in pairs(t) do push(u,f(v)) end; return u end
function sum(t,f, n) n=0; for _,v in pairs(t) do n=n+f(v) end; return n end
function slots(t, u)
                                                                                                                                                                                                                                                                       -- SOME: keeps a random sample on the arriving data function SOME.new(k,keep) return new(k,{n=0,all={}}, keep=keep or the.keep}) end function SOME.add(i,x)
i.n = i.n+1
if #i.all < i.keep then push(i.all,x); return i.all
elseif r() < i.keep/i.n then i.all[r(#i.all)]=x; return i.all end end
        un()
un()
for k,v in pairs(t) do k=tostring(k);if k:sub(1,1)~="_" then push(u,k) end end
return sort(u) end
  -- print tables, recursively
function oo(t) print(o(t)) end
function o(t)
  if type(t)-="table" then return tostring(t) end
  local key=function(k) return fmt(":%%%",k,o(t[k])) end
  local u = ft>0 and map(t,o) or map(slots(t),key)
  return '{'..table.concat(u,"").."}" end
                                                                                                                                                                                                                                                                       -- SYM: summarizes a stream of symbols
function SYM.new(k,n,s)
  return new(k, {n=0,at=n or 0,txt=s or"",has={},most=0}) end
                                                                                                                                                                                                                                                                       function SYM.add(i,x,inc)
                                                                                                                                                                                                                                                                            if x <= """ then
inc = inc or 1
i.n = i.n + inc
i.has[x] = inc + (i.has[x] or 0)
if i.has[x] > i.most then i.most,i.mode=i.has[x],x end end end
  -- strings to things
function csv(file, x)
file = io.input(file)
return function()
x=io.read(); if x then return things(x) else io.close(file) end end end
                                                                                                                                                                                                                                                                      function SYM.dist(i,x,y) return(x=="?" and y=="?" and 1) or(x==y and 0 or 1) end
function SYM.div(i, return i.mode end
function SYM.div(i, p)
  return sum(i.has,function(k) p=-i.has[k]/i.n;return -p*math.log(p,2) end) end
  function thing(x)
x = x:match"%s*(--)%s*$"
if x=="true" then return true elseif x=="false" then return false end
return tonumber(x) or x end
                                                                                                                                                                                                                                                                           unction SYM.merge(i,j, k)

k = SYM:new(i.at,i.txt)
for x,n in pairs(i.has) do k:add(x,n) end
for x,n in pairs(j.has) do k:add(x,n) end
ei, ej, ejk= i:div(), j:div(), k:div()
if i.n==0 or j.n==0 or .99*ek <= (i.n*ei + j.n*ej)/k.n then
return k end end
                                                                                                                                                                                                                                                                       function SYM.merge(i,j,
  function things(x, sep, t)
        t={} for y in x:gmatch(sep or"([^,]+)") do push(t,thing(y)) end return t end
```

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        function CLUSTER.show(i,pre, here)
             inction CLUSTEK.show(i,pre, nere)
pre = pre or ""
here=""
if not i.left and not i.right then here= o(i.here:mid(i.here.cols.y)) end
print(fmt("%6s:%-30s %s", #i.here.rows, pre, here))
for _,kid in pairs(i.left, i.right) do
    if kid then kid:show(pre .. "[.") end end end
        -- SPAN: keeps a random sample on the arriving data function SPAN.new(k, col, lo, hi, has)
return new(k,{col=col,lo=lo,hi=hi or lo,has=has or SYM:new()}) end
        function SPAN.add(i,x,y,n) i.lo,i.hi=min(x,i.lo),max(x,i.hi); i.has:add(y,n) end
function SPAN.merge(i,j)
local has = i.has:merge(j.has)
if now then return SPAN:new(i.col, i.lo, j.hi, has) end end
        function SPAN.select(i,row, x)
             return (x=="?") or (i.lo==i.hi and x==i.lo) or (i.lo <= x and x < i.hi) end</pre>
        function SPAN.score(i) return {i.has.n/i.col.n, i.has:div()} end
      -- EXPLAIN:
function EXPLAIN.new(k,egs,top)
local i,top,want,left,right,spans,best,yes,no
i = new(k,(here = egs))
top = top or egs
want = (#top.rows) 'the.want
if #top.rows >= 2*want then
left,right = egs:half(top)
spans = {}
for n,col in pairs(i.cols.x) do
for _,s in pairs(cl.spans(j.cols.x[n])) do
push(spans,(ys=s:score(),it=s)) end end
best = distance/heaven(spans,("+","-"))[1]
yes,no = egs:clone(), egs:clone(), for _,row in pairs(egs.rows) do
(best:selects(row) and yes or no):add(row) end -- divide data in two
if #yes.rows**Regs.rows then -- make kids if kid size different to parent siz
              if #yes.rows>=want then i.yes=EXPLAIN:new(yes,top) end
if #no.rows>=want then i.no =EXPLAIN:new(no, top) end end end
return i end
        function EXPLAIN.show(i,pre)
             unction EXPLAIN.show(1,pre)
pre = pre or ""
if not pre then
tmp = i.here:mid(i.here.y)
print(fmt("%6s:%-30s %s", #i.here.rows, pre, o(i.here:mid(i.here.cols.y))))
for _,pair in pairs{{true,i.yes}, {false,i.no}} do
status,kid = unpack(pair)
k:shpw(pre .. "|.") end end end
        function SYM.spans(i, j)
            unction SYM.spans(i, j)
local xys,all,one,last,xys,x,c n = {},{}
for x,n in pairs(i.has) do push(xys, (x, "this",n)) end
for x,n in pairs(j.has) do push(xys, (x, "that",n)) end
for _,tmp in ipairs(sort(xys,firsts)) do
    x,c,n = unpack(tmp)
    if x ~= last then
    last = x
        one = push(all, Span(i,x,x)) end
    one.add(x,y,n) end
return all end
        function NUM.spans(i, j)
local xys,all,lo,hi,gap,xys,one,x,c,n = {},{}
lo,hi = min(i.lo, j.lo), max(i.hi,j.hi)
gap = (hi - lo) / (6/the.cohen)
for x,n in pairs(i.has) do push(xys, {x,"this",1}) end
for x,n in pairs(j.has) do push(xys, {x,"this",1}) end
one = Span:new(i,lo,lo)
all = {one}
for_,tmp in ipairs(sort(xys,first)) do
    x,c,n = unpack(tmp)
    if one.hi - one.lo > gap then one = push(all, Span(i, one.hi, x)) end
    one:ad(x,y) end
all = merge(all)
all[i] lo = big
    return all end
```

```
fails=0
function asserts(test, msg)
print(test and "PASS: "or "FAIL: ",msg or "")
if not test then
fails=fails+1
if the.dump then assert(test,msg) end end end
       function EGS.nothing() return true end function EGS.the() oo(the) end function EGS.some(s,t) s=SOME:new(100)
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            s=SOME:new(100)
for i=1,100000 do s:add(i) end
for j,x in pairs(sort(s.all)) do
   --if (j % 10)=0 then print("") ei
   --io.write(fmt("%6s",x)) end end
fmt("%6s",x) end end
       function EGS.clone( r,s)
            nnction EGS.clone( r,s)
r = ROWS:new(the.data)
s = r:clone()
for _,row in pairs(r.rows) do s:add(row) end
asserts(r.cols.x[1].lo==s.cols.x[1].lo, "clone.lo")
asserts(r.cols.x[1].hi==s.cols.x[1].hi, "clone.hi")
end
414 function EGS.data( r)
            r = ROWS:new(the.data)
asserts(r.cols.x[1].hi == 8, "data.columns") end
       function EGS.many(     t)
t={}; for j=1,100 do push(t,j) end
--print(oo(many(t, 10))) end
o(many(t, 10)) end
       function EGS.far(    r,c,row1,row2)
    r = ROWS:new(the.data)
    row1 = r.rows[1]
    c,row2 = r:far(r.rows[1], r.rows) end
    --print(c,"\n",o(row1),"\n", o(row2)) end
       function EGS.half( r,c,row1,row2)
local lefts,rights,x,y,x
r = ROWS:new(the.data)
r:mid(r.cols.y)
lefts,rights,x,y,c = r:half()
lefts:mid(lefts.cols.y)
rights:mid(rights.cols.y)
asserts(true, "half") end
                      ROWS:new(the.data)
             --CLUSTER:new(r):show() end
CLUSTER:new(r) end
      -- start-up
if arg[0] == "s.lua" then
if the help then print(help:gsub("\m\OTES:*\$","")) else
local b4={}; for k,v in pairs(the) do b4{k}=v end
for _rtodo in pairs(the:todo="all" and slots(EGS) or {the.todo}) do
for k,v in pairs(b4) do the{k}=v end
math.randomseed(the.seed)
if type(EGS[todo])=="function" then EGS[todo]() end end
             end
for k,v in pairs(_ENV) do if not b4[k] then print("?",k,type(v)) end end
             os.exit(fails)
           return {CLUSTER=CLUSTER, COLS=COLS, NUM=NUM, ROWS=ROWS, SKIP=SKIP, SOME=SOME, SYM=SYM, the=the, oo=oo, o=o}
       end
-- git rid of SOME for rows
-- nss = NUM | SYM | SKIP
-- nss = NUM | SYM | SKIP
-- COLS = all:[nss]+, x:[nss]*, y:[nss]*, klass;col?
-- ROWS = cols:COLS, rows:SOME
       -- [^Ah91]: Aha, D.W., Kibler, D. & Albert, M.K. Instance-based learning algor ithms. Mach Learn 6, 37âM-^@M-^S66 (1991). https://doi.org/10.1007/BF00153759
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