

```

1  -- <img align=left width=150 src=head.png>
2  --
3  -- **[Repo](https://github.com/timm/lu) &M~&E [Issues](https://github.com/timm
4  -- /lua/issues) &M~&E [copy;2022] (LICENSE.md)** Tim Menzies
5  --
6  -- The next generation of AI-literature software engineers need a deep
7  -- understanding of AI tools. To that end, I've been looking back over
8  -- common themes from my
9  -- AI graduate students (30+ students, over 20 years). The result
10 -- is a
11 -- tool kit small enough to build in a semester, and which can be
12 -- refactored many ways. The code may not be optimal, but it does
13 -- enable a tour through many of the current themes in AI. No, it's
14 -- not a deep learner since I want to build succinct high-level models
15 -- that humans can read, understand, critique, and change.
16 --
17 -- Anyway, my standard "intro to AI" exercise is six
18 -- weeks of homeworks where students rebuild the following code, from
19 -- scratch, in any language they like (except LUA). After that,
20 -- students can review all the assumptions of this code, then read the
21 -- literature looking for other tools that challenge those assumptions.
22 -- That leads to a second a 4-6 week project using these tools as a baseline aga
23 -- inst
24 -- which they can compare other approaches.
25 --
26 -- <hr>
27 --
28 -- Standard supervised learners assume that all examples have labels.
29 -- When this is not true, then we need tools to incrementally
30 -- (a) summarize what has been seen so far; (b) find and focus
31 -- on the most interesting part of that summary, (c) collect
32 -- more data in that region, then (d) repeat.
33 --
34 -- <a href="div.png"></a>
35 -- To make that search manageable, it is useful to exploit a
36 -- manifold assumption; i.e.
37 -- higher-dimensional data can be approximated in a lower dimensional
38 -- manifold without loss of signal [Ch05,Le05].
39 -- Manifolds lead to continuity
40 -- effects; i.e. if there are fewer dimensions, then there are more
41 -- similarities between examples.
42 -- Continuity simplifies clustering
43 -- (and any subsequent reasoning). More similarities means easier
44 -- clustering. And after clustering, reasoning just means reason about
45 -- a handful of examples (maybe even just one) from each cluster.
46 --
47 -- **ASSIGNMENTS**
48 -- **Instance selection**: filter the data down to just a few samples per
49 -- cluster, the reason using just those.
50 -- **Anomaly detection**
51 -- **Explanation**
52 -- Discretize the numeric ranges (\*) at each level of the recursion,
53 -- then divide the data according what range best selects for one half, or the o
54 -- ther
55 -- at the data at this level of recursion.
56 -- **Multi-objective optimization**: This code
57 -- can apply Zitzler's multi-objective ranking predicate [Zit04] to prune the
58 -- worst
59 -- half of the data, then recurs on the rest [Ch18]. Assuming a large over-gener
60 -- ation
61 -- of the initial population (to say, 10,000, examples), this can be just as eff
62 -- ective
63 -- as genetic optimization [Ch18], but runs much faster.
64 -- **Semi-supervised learning**: these applications require only the _2.log(N)
65 -- labels at
66 -- of the pair of furthest points seen at each level of recursion.
67 -- local help = {}
68 --
69 -- l4 == a little LUA learner laboratory.
70 -- (c) 2022, Tim Menzies, BSD 2-clause license.
71 --
72 -- USAGE:
73 -- lua 14.lua [OPTIONS]
74 --
75 -- OPTIONS:
76 -- -cohen F Cohen's delta = .35
77 -- -data N data file = etc/data/auto93.csv
78 -- -Dump stack dump on assert fails = false
79 -- -furthest F far = .9
80 -- -Format s format string = %5.2f
81 -- -keep P max kept items = 512
82 -- -p P distance coefficient = 2
83 -- -seed P set seed = 10019
84 -- -todo S start up action (or 'all') = nothing
85 -- -help show help = false
86 -- -want F recurse until rows^want = .5
87 --
88 -- KEY: N=fileName F=float P=posint S=string
89 --
90 -- NOTES: This code uses Aha's distance measure [Aha91] (that can
91 -- handle numbers and symbols) to recursively divide data based on two
92 -- distant points (these two are found in linear time using the Fastmap
93 -- heuristic [Fa95]).
94 --
95 -- To avoid spurious outliers, this code use the 90% furthest points.
96 --
97 -- To avoid long runtimes, uses a subset of the data to learn where
98 -- to divide data (then all the data gets pushed down first halves).
99 --
100 -- To support explanation, optionally, at each level of recursion,
101 -- this code reports what ranges can best distinguish sibling clusters
102 -- C1,C2. The discretizer is inspired by the ChiMerge algorithm:
103 -- numerics are divided into, say, 16 bins. Then, while we can find
104 -- adjacent bins with the similar distributions in C1,C2, then
105 -- (a) merge then (b) look for other merges.
106 -- ]]
107 --
108 -- ## Namespace
109 --
110 -- Cache current globals, use at end to find rogue variables
111 -- local b4={}; for k,_ in pairs(_ENV) do b4[k]=k end
112 --
113 -- Defined local names.
114 -- local any, asserts, big, cli, csv, fails, firsts, fmt, goalp, ignorep, klassp
115 -- local lessp, map, main, many, max, merge, min, morep, new, nump, o, oo, per, pop, push
116 -- local r, rows, rnd, rnds, slots, sort, sum, thing, things, unpack
117 --
118 -- Classes have UPPER CASE names.
119 -- local CLUSTER, COLS, ESS, NUM, ROWS = {}, {}, {}, {}, {}
120 -- local SKIP, SOME, SPAN, SYM = {}, {}, {}, {}
121 --
122 -- ## Settings
123 -- Parse the help text for flags and defaults (e.g. -keep, 512).
124 -- Check for updates on those details from command line
125 -- (and and there,
126 -- some shortcuts are available;
127 -- e.g. _k N _&A; 'keep=N';
128 -- and _booleanFlag _&A; 'booleanFlag=not default').
129 -- local the={}
130 -- help:gsub("\n [^%s+](\n)*%s+(\n)*", function(key, x)
131 -- for n, flag in ipairs(arg) do
132 -- if flag:sub(1,1)=="-" and key:find("^%s+(\n)*%s+(\n)*" then
133 -- x = x=="false" and true or x=="true" and "false" or arg[n+1] end end
134 -- if x=="false" then the[key]=false elseif x=="true" then the[key]=true else
135 -- the[key] = tonumber(x) or x end end )

```

```

193 -- CLASSES
194
195
196
197 function new(k,t) k.__index=k; k.__tostring=o; return setmetatable(t,k) end
198
199 -- COLS: turns list of column names into NUMs, SYMs, or SKIPs
200 function COLS.new(k,row, i)
201   i= new(k,{all={},x={},y={},names=row})
202   for at,t in ipairs(row) do push(i.all, i:col(at,txt)) end
203   return i end
204
205 function COLS.add(i,t)
206   for _,col in pairs(i.all) do col:add( t[col.at] ) end
207   return t end
208
209 function COLS.col(i,at,txt, col)
210   if ignorep(txt) then return SKIP:new(at,txt) end
211   col = (nump(txt) and NUM or SYM):new(at,txt)
212   push(goalp(txt) and i.y or i.x, col)
213   if klassp(txt) then i.klass = col end
214   return col end
215
216 -- NUM: summarizes a stream of numbers
217 function NUM.new(k,n,s)
218   return new(k,{n=0,at=n or 0,txt=s or "",has=SOME:new(),ok=false,
219     w=lessp(s or "") and -1 or 1, lo=big, hi=-big}) end
220
221 function NUM.add(i,x)
222   if x == "?" then
223     i.n = i.n + 1
224     if i.has:add(x) then i.ok=false end
225     i.lo,i.hi = min(x,i.lo), max(x,i.hi); end end
226
227 function NUM.dist(i,x,y)
228   if x=="?" and y=="?" then return 1
229   elseif x=="?" then y=i:norm(y); x=y<0.5 and 1 or 0
230   elseif y=="?" then x=i:norm(x); y=x<0.5 and 1 or 0
231   else x,y = i:norm(x), i:norm(y) end
232   return math.abs(x-y) end
233
234 function NUM.mid(i) return per(i:sorted(), .5) end
235
236 function NUM.norm(i,x)
237   return math.abs(i.hi-i.lo)<1E-9 and 0 or (x-i.lo)/(i.hi - i.lo) end
238
239 function NUM.sorted(i)
240   if i.ok==false then table.sort(i.has.all); i.ok=true end
241   return i.has.all end
242
243 -- ROWS: manages 'rows', summarized in 'cols' (columns).
244 function ROWS.new(k,init,s, i)
245   i = new(k,{rows={},cols=nil})
246   if type(init)=="string" then for t in csv(init) do i:add(t) end end
247   if type(init)=="table" then for t in init do i:add(t) end end
248   return i end
249
250 function ROWS.add(i,t)
251   if i.cols then push(i.rows,i.cols:add(t)) else i.cols=COLS:new(t) end end
252
253 function ROWS.clone(i, j) j= ROWS:new(); j:add(i.cols.names);return j end
254
255 function ROWS.dist(i,row1,row2, d,fun)
256   function fun(col) return col:dist(row1[col.at], row2[col.at])^the.p end
257   return (sum(i.cols.x, fun) / #i.cols.x)^(1/the.p) end
258
259 function ROWS.furthest(i,row1,rows, fun)
260   function fun(row2) return (i:dist(row1,row2), row2) end
261   return unpack(per (sort(map(rows,fun),firsts), the.furthest)) end
262
263 function ROWS.half(i, top)
264   local some, top,c,x,y,tmp,mid,lefts,rights,_
265   some= many(i.rows, the.keep)
266   top = top or 1
267   _x = top:furthest(any(some), some)
268   _c,y = top:furthest(x, some)
269   tmp = sort(map(i.rows,function(r) return top:fastmap(r,x,y,c) end),firsts)
270   mid = #i.rows//2
271   lefts, rights = i:clone(), i:clone()
272   for at,row in pairs(tmp) do (at <=mid and lefts or rights):add(row[2]) end
273   return lefts,rights,x,y,c, tmp[mid] end
274
275 function ROWS.mid(i,cols)
276   return map(cols or i.cols.all, function(col) return col:mid() end) end
277
278 function ROWS.fastmap(i, r,x,y,c, a,b)
279   a,b = idist(r,x), idist(r,y); return {(a^2 + c^2 - b^2)/(2*c), r} end
280
281 -- SKIP: summarizes things we want to ignore (so does nothing)
282 function SKIP.new(k,n,s) return new(k,{n=0,at=at or 0,txt=s or ""}) end
283 function SKIP.add(i,x) return x end
284 function SKIP.mid(i) return "?" end
285
286 -- SOME: keeps a random sample on the arriving data
287 function SOME.new(k,keep) return new(k,{n=0,all={}, keep=keep or the.keep}) end
288 function SOME.add(i,x)
289   i.n = i.n+1
290   if #i.all < i.keep then push(i.all,x) ; return i.all
291   elseif r() < i.keep/i.n then i.all[r(#i.all)]=x; return i.all end end
292
293 -- SYM: summarizes a stream of symbols
294 function SYM.new(k,n,s)
295   return new(k,{n=0,at=n or 0,txt=s or "",has={},most=0}) end
296
297 function SYM.add(i,x,inc)
298   if x == "?" then
299     inc = inc or 1
300     i.n = i.n + inc
301     i.has[x] = inc + (i.has[x] or 0)
302     if i.has[x] > i.most then i.most,i.mode=i.has[x],x end end end
303
304 function SYM.dist(i,x,y) return (x=="?" and y=="?" and 1) or (x==y and 0 or 1) end
305 function SYM.mid(i) return i.mode end
306 function SYM.div(i, p)
307   return sum(i.has,function(k) p=-i.has[k]/i.n;return -p*math.log(p,2) end) end
308
309 function SYM.merge(i,j, k)
310   k = SYM:new(i.at,i.txt)
311   for x,n in pairs(i.has) do k:add(x,n) end
312   for x,n in pairs(j.has) do k:add(x,n) end
313   ei, ej, ejk = i:div(), j:div(), k:div()
314   if i.n==0 or j.n==0 or .99*ek <= (i.n*ei + j.n*ej)/k.n then
315     return k end end
316
317 -- CLUSTER
318
319
320 -- CLUSTER: recursively divides data by clustering towards two distant points
321 function CLUSTER.new(k,egs,top)
322   local i,want,left,right
323   i = new(k,{here=egs})
324   top = top or egs
325   want = (#top.rows)^the.want
326   if #egs.rows >= 2*want then
327     left, right, i.x, i.y, i.c, i.mid = egs:half(top)
328     if #left.rows < #egs.rows then
329       i.left = CLUSTER:new(left, top)
330       i.right= CLUSTER:new(right, top) end end
331   return i end
332
333 function CLUSTER.show(i,pre, here)
334   pre = pre or ""
335   here=""
336   if not i.left and not i.right then here= o(i.here:mid(i.here.cols.y)) end
337   print(fmt("%6s: %~30s %s", #i.here.rows, pre, here))
338   for _,kid in pairs(i.left, i.right) do
339     if kid then kid:show(pre .. "|. " ) end end end
340
341 -- EXPLAIN
342
343 -- SPAN: keeps a random sample on the arriving data
344 function SPAN.new(k, col, lo, hi, has)
345   return new(k,{col=col,lo=lo,hi=hi or lo,has=has or SYM:new()}) end
346
347 function SPAN.add(i,x,y,n) i.lo,i.hi=min(x,i.lo),max(x,i.hi); i.has:add(y,n) end
348 function SPAN.merge(i,j)
349   local has = i.has:merge(j.has)
350   if now then return SPAN:new(i.col, i.lo, j.hi, has) end end
351
352 function SPAN.select(i,row, x)
353   x = row[i.col.at]
354   return (x=="") or (i.lo==i.hi and x==i.lo) or (i.lo <= x and x < i.hi) end
355
356 function SPAN.score(i) return i.has.n/i.col.n, i.has:div() end
357
358 function SPAN.scores(i, ss,ds)
359   size,div = i:score()
360   size,div = ss:norm(size), ds:norm(div)
361   return ((1 - size)^2 + (0 - div)^2)^.5 end
362
363 -- EXPLAIN:
364 function EXPLAIN.new(k,egs,top)
365   local i,n,y,ds,ss,top,div,want,size,left,span,right,spans
366   i = new(k,{here = egs})
367   top = top or egs
368   want = (#top.rows)^the.want
369   if #top.rows >= 2*want then
370     left,right = egs:half(top)
371     spans, ds, ss = {}, Num(), Num()
372     for n,col in pairs(i.cols.x) do
373       for _,span in pairs(col:spans(j.cols.x[n])) do
374         push(spans, one)
375         size, div = span:score()
376         ss:add(size)
377         ds:add(div) end end
378     span= sort(spans,function(x,y) return x:scores(ss,ds)<y:scores(ss,ds) end)[1]
379     y, n = egs:clone(), egs:clone()
380     for _,row in pairs(egs.rows) do (span:selects(row) and y or n):add(row) end
381     if #y.rows<#egs.rows and #y.rows>want then i.yes=EXPLAIN:new(y,top) end
382     if #n.rows<#egs.rows and #n.rows>want then i.no =EXPLAIN:new(n,top) end end
383   return i end
384
385 function EXPLAIN.show(i,pre)
386   pre = pre or ""
387   if not pre then
388     tmp = i.here:mid(i.here.y)
389     print(fmt("%6s: %~30s %s", #i.here.rows, pre, o(i.here:mid(i.here.cols.y))))
390
391     for _,pair in pairs({true,i.yes},{false,i.no}) do
392       status,kid = unpack(pair)
393       k:shpw(pre .. "|. " end end
394
395 function SYM.spans(i, j)
396   local xys,all,one,last,xys,x,c n = {},{}
397   for x,n in pairs(i.has) do push(xys, {x,"this",n}) end
398   for x,n in pairs(j.has) do push(xys, {x,"that",n}) end
399   for _,tmp in ipairs(sort(xys,firsts)) do
400     x,c,n = unpack(tmp)
401     if x ~= last then
402       last = x
403       one = push(all, Span(i,x,x)) end
404     one:add(x,y,n) end
405   return all end
406
407 function NUM.spans(i, j)
408   local xys,all,lo,hi,gap,xys,one,x,c,n = {},{}
409   lo,hi = min(i.lo, j.lo), max(i.hi,j.hi)
410   gap = (hi - lo) / (6/the.cohen)
411   for x,n in pairs(i.has) do push(xys, {x,"this",1}) end
412   for x,n in pairs(j.has) do push(xys, {x,"that",1}) end
413   one = Span:new(i,lo,lo)
414   all = {one}
415   for _,tmp in ipairs(sort(xys,first)) do
416     x,c,n = unpack(tmp)
417     if one.hi - one.lo > gap then one = push(all, Span(i, one.hi, x)) end
418     one:add(x,y) end
419   all = merge(all)
420   all[1].lo = -big
421   all[#all].hi = big
422   return all end
423
424 function merge(b4, j,n,now,a,b,merged)
425   j,n,now = 0,#b4,{ }
426   while j < #b4 do
427     j = j+1
428     a, b = b4[j], b4[j+1]
429     if b then
430       merged = a:merge(b)
431       if merged then a,j = merged, j+1 end end
432     push(now,a)
433     j = j+1 end
434   return #now == #b4 and b4 or merge(now) end

```

```

437 -- DEMOS
438 --
439 --
440 --
441 fails=0
442 function asserts(test, msg)
443   print(test and "PASS: " or "FAIL: ", msg or "")
444   if not test then
445     fails=fails+1
446     if the.dump then assert(test, msg) end end end
447
448 function EGS.nothing() return true end
449 function EGS.the() oo(the) end
450 function EGS.rand() print(r()) end
451 function EGS.some(s, t)
452   s=SOME:new(100)
453   for i=1,100000 do s:add(i) end
454   for j,x in pairs(sort(s.all)) do
455     --if (j % 10)==0 then print("") end
456     --io.write(fmt("%6s", x)) end end
457     fmt("%6s", x) end end
458
459 function EGS.clone( r, s)
460   r = ROWS:new(the.data)
461   s = r:clone()
462   for _,row in pairs(r.rows) do s:add(row) end
463   asserts(r.cols.x[1].lo==s.cols.x[1].lo, "clone.lo")
464   asserts(r.cols.x[1].hi==s.cols.x[1].hi, "clone.hi")
465   end
466
467 function EGS.data( r)
468   r = ROWS:new(the.data)
469   asserts(r.cols.x[1].hi == 8, "data.columns") end
470
471 function EGS.dist( r, rows, n)
472   r = ROWS:new(the.data)
473   rows = r.rows
474   n = NUM:new()
475   for _,row in pairs(rows) do n:add(r:dist(row, rows[1])) end
476   --oo(r.cols.x[2]:sorted()) end
477   o(r.cols.x[2]:sorted()) end
478
479 function EGS.many( t)
480   t={}; for j=1,100 do push(t, j) end
481   --print(oo(many(t, 10))) end
482   o(many(t, 10)) end
483
484 function EGS.far( r, c, row1, row2)
485   r = ROWS:new(the.data)
486   row1 = r.rows[1]
487   c, row2 = r:far(r.rows[1], r.rows) end
488   --print(c, "\n", o(row1), "\n", o(row2)) end
489
490 function EGS.half( r, c, row1, row2)
491   local lefts, rights, x, y, x
492   r = ROWS:new(the.data)
493   r:mid(r.cols.y)
494   lefts, rights, x, y, c = r:half()
495   lefts:mid(lefts.cols.y)
496   rights:mid(rights.cols.y)
497   asserts(true, "half") end
498
499 function EGS.cluster(r)
500   r = ROWS:new(the.data)
501   --CLUSTER:new(r):show() end
502   CLUSTER:new(r) end
503
504 -- start-up
505 if arg[0] == "slua" then
506   oo(the)
507   if the.help then print(help:gsub("\nNOTES:*$", "")) else
508     local b4={}; for k,v in pairs(the) do b4[k]=v end
509     for _,todo in pairs(the.todo=="all" and slots(EGS) or {the.todo}) do
510       for k,v in pairs(b4) do the[k]=v end
511       math.randomseed(the.seed)
512       if type(EGS[todo])=="function" then EGS[todo]() end end
513     end
514     for k,v in pairs(_ENV) do if not b4[k] then print("?", k, type(v)) end end
515     os.exit(fails)
516   else
517     return {CLUSTER=CLUSTER, COLS=COLS, NUM=NUM, ROWS=ROWS,
518            SKIP=SKIP, SOME=SOME, SYM=SYM, the=the, oo=oo, o=o}
519   end
520
521 -- git rid of SOME for rows
522 -- nss = NUM | SYM | SKIP
523 -- COLS = all:[nss]t, x:[nss]*, y:[nss]*, klass:col?
524 -- ROWS = cols:COLS, rows:SOME
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