```lua
-- <img align=left width=150 src=head.png>
--
-- **[Repo](https://github.com/timm/lua) âM-^@¢ [Issues](https://github.com/timm/lua/issues) âM-^@¢ [&copy;2022](LICENSE.md)** Tim Menzies
--
-- If we choose our AI tools not on their complexity, but
-- on their understandably, what would they look like?
-- To that end, I've been looking back over
-- common themes seen in my
-- AI graduate students (30+ students, over 20 years). What I was
-- after were the least lines of code that offer the most
-- AI functionality-- and which could be mixed and matched in
-- novel and interesting ways.
--
-- The result is this file. My standard "intro to AI" exercise is six
-- weeks of homeworks where students rebuild the following code,from
-- scratch, in any language they like (except LUA).  After that,
-- students can review all the assumptions of this code, then read the
-- literature looking for other tools that challenge those assumptions.
-- That leads to a second a 4-6 week project using these tools as a baseline aga
inst
-- which they can compare other, more complex, approaches.
--
-- <hr>
--
-- The need for baselines. XXXX
---
-- Standard supervised learners assume that all examples have labels.
-- When this is not true, then we need tools to incrementally
-- (a) summarize what has been seen so far; (b) find and focus
-- on the most interesting part of that summary, (c) collect
-- more data in that region, then (d) repeat.
--
-- <a href="div.png"><img align=right width=225 src="div.png"></a>
-- To make that search manageable, it is useful to exploit a
-- manifold assumption; i.e.
-- higher-dimensional data can be approximated in a lower dimensional
-- manifold without loss of signal [Ch05,Le05].
-- Manifolds lead to _continuity_
-- effects; i.e. if there are fewer dimensions, then there are more
-- similarities between examples.
-- Continuity simplifies _clustering_
-- (and any subsequent reasoning).  More similarities means  easier
-- clustering. And after clustering, reasoning just means reason about
-- a handful of examples (maybe even just one)  from each cluster.
--
-- **ASSIGNMENTS**
-- - **Instance selection**: filter the data down to just a few samples per
-- cluster, the reason using just those.
-- - **Anomaly detection**
-- - **Explanation**
-- Discretize the numeric ranges (\*) at each level of the recursion,
-- then divide the data according what range best selects for one half, or the o
ther
-- at the data at this level of recursion.
-- - **Multi-objective optimization:** This code
-- can apply Zitzler's multi-objective rankining predicate [Zit04] to prune the
worst
-- half of the data, then recurs on the rest [Ch18]. Assuming a large over-gener
ation
-- of the initial population (to say, 10,000, examples), this can be just as eff
ective
-- as genetic optimization [Ch18], but runs much faster.
-- - **Semi-supervised learning**: these applications require only the _2.log(N)
_ labels at
-- of the pair of furthest points seen at each level of recursion.
-- - **Privacy**
-- - **Planning**
-- - **Monitoring**
local help = [[

15 == a little lab of lots of LUA learning algorithms.
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USAGE:
  lua 15.lua [OPTIONS]

OPTIONS:
  -cohen    F   Cohen's delta              = .35
  -data     N   data file                  = etc/data/auto93.csv
  -Dump         stack dump on assert fails = false
  -furthest F   far                        = .9
  -Format   s   format string              = %5.2f
  -keep     P   max kept items             = 512
  -p        P   distance coefficient       = 2
  -seed     P   set seed                   = 10019
  -todo     S   start up action (or 'all') = nothing
  -help         show help                  = false
  -want     F   recurse until rows^want    = .5

KEY: N=fileName F=float P=posint S=string

NOTES: This code uses Aha's distance measure [Aha91] (that can
handle numbers and symbols) to recursively divide data based on two
distant points (these two are found in linear time using the Fastmap
heuristic [Fa95]).

To avoid spurious outliers, this code use the 90% furthest points.

To avoid long runtimes, uses a subset of the data to learn where
to divide data (then all the data gets pushed down first halves).

To support explanation, optionally, at each level of recursion,
this code reports what ranges can best distinguish sibling clusters
C1,C2.  The  discretizer is inspired by the ChiMerge algorithm:
numerics are divided into, say, 16 bins. Then, while we can find
adjacent bins with the similar distributions in C1,C2, then
(a) merge then (b) look for other merges.
]]

-- ## Namespace

-- Cache current globals, use at end to find rogue variables
local b4={}; for k,_ in pairs(_ENV) do b4[k]=k end

-- Defined local names.
local any,asserts,big,cli,csv,fails,firsts,fmt,goalp,ignorep,klassp
local lessp,map,main,many,max,merge,min,morep,new,nump,o,oo,per,pop,push
local r,rows,rnd,rnds,slots,sort,sum,thing,things,unpack

-- Classes have UPPER CASE names.
local CLUSTER, COLS, EGS,  EXPLAIN, NUM, ROWS = {},{},{},{},{},{}
local SKIP,    SOME, SPAN, SYM       = {},{},{},{}

-- ## Settings
-- Parse the help text for flags and defaults (e.g. -keep, 512).
-- Check for updates on those details from command line
-- (and and there,
-- some shortcuts are available;
-- e.g.  _-k N_ &rArr; 'keep=N';
-- and  _-booleanFlag_ &rArr; 'booleanFlag=not default').
local the={}
help:gsub("\n [-][^%s]+[^\n]*%s([^%s]+)",function(key,x)
  for n,flag in ipairs(arg) do
    if flag:sub(1,1)=="-" and key:find("^"..flag:sub(2)..".*") then
      x = x=="false" and true or x=="true" and "false" or arg[n+1] end end
  if x=="false" then the[key]=false elseif x=="true" then the[key]=true else
    the[key] = tonumber(x) or x end end )

-- ------------------------------------------------------------------------
-- this code reads csv files where the words on line1 define column types.
function ignorep(x) return x:find":$" end      -- columns to ignore
function klassp(x)  return x:find"!$" end      -- symbolic goals to achieve
function lessp(x)   return x:find"-$" end      -- number goals to minimize
function morep(x)   return x:find"+$" end      -- numeric goals to maximize
function nump(x)    return x:find"^[A-Z]" end -- numeric columns
function goalp(x)   return morep(x) or lessp(x) or klassp(x) end

-- strings
fmt = string.format

-- maths
big = math.huge
max = math.max
min = math.min
r   = math.random

function rnds(t,f) return map(t, function(x) return rnd(x,f) end) end
function rnd(x,f)
  return fmt(type(x)=="number" and (x~=x//1 and f or the.Format) or "%s",x) end

-- tables
pop = table.remove
unpack = table.unpack
function any(t)         return t[r(#t)] end
function firsts(a,b)    return a[1] < b[1] end
function many(t,n, u)   u={}; for i=1,n do push(u,any(t)) end; return u end
function per(t,p)       return t[ (#t*(p or .5))//1 ] end
function push(t,x)      table.insert(t,x); return x end
function sort(t,f)      table.sort(t,f); return t end

-- meta
function map(t,f, u)  u={};for k,v in pairs(t) do push(u,f(v)) end; return u end
function sum(t,f, n)  n=0; for _,v in pairs(t) do n=n+f(v)     end; return n end
function slots(t, u)
  u={}
  for k,v in pairs(t) do k=tostring(k);if k:sub(1,1)~="_" then push(u,k) end end
  return sort(u) end

-- print tables, recursively
function oo(t) print(o(t)) end
function o(t)
  if type(t)~="table" then return tostring(t) end
  local key=function(k) return fmt(":%s %s",k,o(t[k])) end
  local u = #t>0 and map(t,o) or map(slots(t),key)
  return '{'..table.concat(u," ")..'}' end

-- strings to things
function csv(file,       x)
  file = io.input(file)
  return function()
    x=io.read(); if x then return things(x) else io.close(file) end end end

function thing(x)
  x = x:match"^%s*(.-)%s*$"
  if x=="true" then return true elseif x=="false" then return false end
  return tonumber(x) or x end

function things(x,sep,  t)
  t={}
  for y in x:gmatch(sep or"([^,]+)") do push(t,thing(y)) end
  return t end
```

```lua

-- misc
function distance2Heaven(t,heaven,   num,d)
  for n,txt in pairs(heaven) do
    num = Num(at,txt)
    for _,z in pairs(t) do num:add(z.ys[n]) end
    for _,z in pairs(t) do z.ys[n] = num:distance2heaven(z.ys[n]) end end
  d = function(one) return (sum(one.ys)/#one.ys)^.5 end
  return sort(t, function(a,b) return d(a) < d(b) end) end
--  ____ _     _____ ____  ____  ____  ____
-- |     |     |___| [___  [___  |___  [___
-- |____ |____ |   | ____] ____] |____ ____]
--
function new(k,t) k.__index=k; k.__tostring=o; return setmetatable(t,k) end

-- COLS: turns list of column names into NUMs, SYMs, or SKIPs
function COLS.new(k,row,   i)
  i= new(k,{all={},x={},y={},names=row})
  for at,txt in ipairs(row) do  push(i.all, i:col(at,txt)) end
  return i end

function COLS.add(i,t)
  for _,col in pairs(i.all) do col:add( t[col.at] ) end
  return t end

function COLS.col(i,at,txt,     col)
  if ignorep(txt) then return SKIP:new(at,txt) end
  col = (nump(txt) and NUM or SYM):new(at,txt)
  push(goalp(txt) and i.y or i.x, col)
  if klassp(txt) then i.klass = col end
  return col end

-- NUM: summarizes a stream of numbers
function NUM.new(k,n,s)
  return new(k,{n=0,at=n or 0,txt=s or"",has=SOME:new(),ok=false,
                w=lessp(s or "") and -1 or 1, lo=big, hi=-big}) end

function NUM.add(i,x)
  if x ~= "?" then
    i.n = i.n + 1
    if i.has:add(x) then i.ok=false end
    i.lo,i.hi = min(x,i.lo), max(x,i.hi); end end

function NUM.dist(i,x,y)
  if     x=="?" and y=="?" then return 1
  elseif x=="?" then y=i:norm(y); x=y<0.5 and 1 or 0
  elseif y=="?" then x=i:norm(x); y=x<0.5 and 1 or 0
  else   x,y = i:norm(x), i:norm(y) end
  return math.abs(x-y) end

function NUM.distance2heaven(x, w)
  return ((i.w>0 and 1 or 0) - i:norm(x))^2 end

function NUM.mid(i) return per(i:sorted(), .5) end

function NUM.norm(i,x)
  return math.abs(i.hi-i.lo)<1E-9 and 0 or (x-i.lo)/(i.hi - i.lo) end

function NUM.sorted(i)
  if i.ok==false then table.sort(i.has.all); i.ok=true end
  return i.has.all end

-- ROWS: manages `rows`, summarized in `cols` (columns).
function ROWS.new(k,inits,     i)
  i = new(k,{rows={},cols=nil})
  if type(inits)=="string" then for t in csv(inits) do i:add(t) end end
  if type(inits)=="table"  then for t in inits       do i:add(t) end end
  return i end

function ROWS.add(i,t)
  if i.cols then push(i.rows,i.cols:add(t)) else i.cols=COLS:new(t) end end

function ROWS.clone(i,  j) j= ROWS:new(); j:add(i.cols.names);return j end

function ROWS.dist(i,row1,row2,   d,fun)
  function fun(col) return col:dist(row1[col.at], row2[col.at])^the.p end
  return (sum(i.cols.x, fun)/ #i.cols.x)^(1/the.p) end

function ROWS.furthest(i,row1,rows,     fun)
  function fun(row2) return {i:dist(row1,row2), row2} end
  return unpack(per(sort(map(rows,fun),firsts), the.furthest)) end

function ROWS.half(i, top)
  local some, top,c,x,y,tmp,mid,lefts,rights,_
  some= many(i.rows, the.keep)
  top = top or i
  _,x = top:furthest(any(some), some)
  c,y = top:furthest(x,         some)
  tmp = sort(map(i.rows,function(r) return top:fastmap(r,x,y,c) end),firsts)
  mid = #i.rows//2
  lefts, rights = i:clone(), i:clone()
  for at,row in pairs(tmp) do (at <=mid and lefts or rights):add(row[2]) end
  return lefts,rights,x,y,c, tmp[mid] end

function ROWS.mid(i,cols)
  return map(cols or i.cols.all, function(col) return col:mid() end) end

function ROWS.fastmap(i, r,x,y,c,     a,b)
  a,b = i:dist(r,x), i:dist(r,y); return {(a^2 + c^2 - b^2)/(2*c), r} end

-- SKIP: summarizes things we want to ignore (so does nothing)
function SKIP.new(k,n,s) return new(k,{n=0,at=at or 0,txt=s or""}) end
function SKIP.add(i,x)   return x end
function SKIP.mid(i)     return "?" end

-- SOME: keeps a random sample on the arriving data
function SOME.new(k,keep) return new(k,{n=0,all={}, keep=keep or the.keep}) end
function SOME.add(i,x)
  i.n = i.n+1
  if     #i.all < i.keep then push(i.all,x)          ; return i.all
  elseif r()     < i.keep/i.n then i.all[r(#i.all)]=x; return i.all end end

-- SYM: summarizes a stream of symbols
function SYM.new(k,n,s)
  return new(k,{n=0,at=n or 0,txt=s or"",has={},most=0}) end

function SYM.add(i,x,inc)
  if x ~= "?" then
    inc = inc or 1
    i.n = i.n + inc
    i.has[x] = inc + (i.has[x] or 0)
    if i.has[x] > i.most then i.most,i.mode=i.has[x],x end end end

function SYM.dist(i,x,y) return(x=="?" and y=="?" and 1) or(x==y and 0 or 1) end
function SYM.mid(i)      return i.mode end
function SYM.div(i,   p)
  return sum(i.has,function(k) p=-i.has[k]/i.n;return -p*math.log(p,2) end) end

function SYM.merge(i,j,    k)
  k = SYM:new(i.at,i.txt)
  for x,n in pairs(i.has) do k:add(x,n) end
  for x,n in pairs(j.has) do k:add(x,n) end
  ei, ej, ejk= i:div(), j:div(), k:div()
  if i.n==0 or j.n==0 or .99*ek <= (i.n*ei + j.n*ej)/k.n then
    return k end end
--  ____ _     _   _ ____ _____ ____ ____
-- |     |     |   | [___   |   |___ |___/
-- |____ |____ |___| ____]  |   |___ |   \
--
-- CLUSTER: recursively divides data by clustering towards two distant points
function CLUSTER.new(k,egs,top)
  local i,want,left,right
  i      = new(k, {here=egs})
  top    = top or egs
  want = (#top.rows)^the.want
  if #egs.rows >= 2*want then
    left, right, i.x, i.y, i.c, i.mid = egs:half(top)
    if #left.rows < #egs.rows then
      i.left = CLUSTER:new(left,   top)
      i.right= CLUSTER:new(right, top) end end
  return i end

function CLUSTER.show(i,pre,  here)
  pre = pre or ""
  here=""
  if not i.left and not i.right then here= o(i.here:mid(i.here.cols.y)) end
  print(fmt("%6s : %-30s %s",#i.here.rows, pre, here))
  for _,kid in pairs{i.left, i.right} do
    if kid then kid:show(pre .. "|.. ") end end end

--  ____ _  _ ____ _     _____ _ _  _
-- |___   \/  |___] |     |___| | |\ |
-- |____ _/\_ |     |____ |   | | | \|

-- SPAN: keeps a random sample on the arriving data
function SPAN.new(k, col, lo, hi, has)
  return new(k,{col=col,lo=lo,hi=hi or lo,has=has or SYM:new()}) end

function SPAN.add(i,x,y,n) i.lo,i.hi=min(x,i.lo),max(x,i.hi); i.has:add(y,n) end
function SPAN.merge(i,j)
  local has = i.has:merge(j.has)
  if now then return SPAN:new(i.col, i.lo, j.hi, has) end end

function SPAN.select(i,row,    x)
  x = row[i.col.at]
  return (x=="?") or (i.lo==i.hi and x==i.lo) or (i.lo <= x and x < i.hi) end

function SPAN.score(i) return {i.has.n/i.col.n,  i.has:div()} end


-- EXPLAIN:
function EXPLAIN.new(k,egs,top)
  local i,top,want,left,right,spans,best,yes,no
  i    = new(k,{here = egs})
  top  = top or egs
  want = (#top.rows)^the.want
  if #top.rows >= 2*want then
    left,right = egs:half(top)
    spans  = {}
    for n,col in pairs(i.cols.x) do
      for _,s in pairs(col:spans(j.cols.x[n])) do
        push(spans,{ys=s:score(),it=s}) end end
    best   = distance2heaven(spans,{"+","-"})[1]
    yes,no = egs:clone(), egs:clone()
    for _,row in pairs(egs.rows) do
      (best:selects(row) and yes or no):add(row) end -- divide data in two
    if #yes.rows<#egs.rows then -- make kids if kid size different to parent size
      if #yes.rows>=want then i.yes=EXPLAIN:new(yes,top) end
      if #no.rows >=want then i.no =EXPLAIN:new(no, top)  end end end
  return i end

function EXPLAIN.show(i,pre)
  pre = pre or ""
  if not pre then
    tmp = i.here:mid(i.here.y)
  print(fmt("%6s : %~30s %s", #i.here.rows, pre, o(i.here:mid(i.here.cols.y))))
  for _,pair in pairs{{true,i.yes},{false,i.no}} do
    status,kid = unpack(pair)
    k:shpw(pre .. "|.. ") end end end

function SYM.spans(i, j)
  local xys,all,one,last,xys,x,c n = {},{}
  for x,n in pairs(i.has) do push(xys, {x,"this",n}) end
  for x,n in pairs(j.has) do push(xys, {x,"that",n}) end
  for _,tmp in ipairs(sort(xys,firsts)) do
    x,c,n = unpack(tmp)
    if x ~= last then
      last = x
      one  = push(all, Span(i,x,x)) end
    one:add(x,y,n) end
  return all end

function NUM.spans(i, j)
  local xys,all,lo,hi,gap,xys,one,x,c,n = {},{}
  lo,hi = min(i.lo, j.lo), max(i.hi,j.hi)
  gap   = (hi - lo) / (6/the.cohen)
  for x,n in pairs(i.has) do push(xys, {x,"this",1}) end
  for x,n in pairs(j.has) do push(xys, {x,"that",1}) end
  one = Span:new(i,lo,lo)
  all = {one}
  for _,tmp in ipairs(sort(xys,first)) do
    x,c,n = unpack(tmp)
    if one.hi - one.lo > gap then one = push(all, Span(i, one.hi, x)) end
    one:add(x,y) end
  all          = merge(all)
  all[1   ].lo = -big
  all[#all].hi =  big
  return all end

function merge(b4,       j,n,now,a,b,merged)
  j,n,now = 0,#b4,{}
  while j < #b4 do
    j    = j+1
    a, b = b4[j], b4[j+1]
    if b then
      merged = a:merge(b)
      if merged then a,j = merged, j+1 end end
    push(now,a)
    j = j+1 end
  return #now == #b4 and b4 or merge(now) end
```

```
-- ___ ____ ____ _  _ ____ ____
-- |  \ |___ |__| |\/| |__| [__
-- |__/ |___ |  | |  | |  | ___]
--
fails=0
function asserts(test, msg)
  print(test and "PASS: "or "FAIL: ",msg or "")
  if not test then
    fails=fails+1
    if the.dump then assert(test,msg) end end end

function EGS.nothing() return true end
function EGS.the()     oo(the) end
function EGS.rand()    print(r()) end
function EGS.some(s,t)
  s=SOME:new(100)
  for i=1,100000 do s:add(i) end
  for j,x in pairs(sort(s.all)) do
    --if (j % 10)==0 then print("") end
    --io.write(fmt("%6s",x))  end end
    fmt("%6s",x)  end end

function EGS.clone( r,s)
  r = ROWS:new(the.data)
  s = r:clone()
  for _,row in pairs(r.rows) do s:add(row) end
  asserts(r.cols.x[1].lo==s.cols.x[1].lo,"clone.lo")
  asserts(r.cols.x[1].hi==s.cols.x[1].hi,"clone.hi")
  end

function EGS.data( r)
  r = ROWS:new(the.data)
  asserts(r.cols.x[1].hi == 8, "data.columns") end

function EGS.dist( r,rows,n)
  r = ROWS:new(the.data)
  rows = r.rows
  n = NUM:new()
  for _,row in pairs(rows) do n:add(r:dist(row, rows[1])) end
  --oo(r.cols.x[2]:sorted()) end
  o(r.cols.x[2]:sorted()) end

function EGS.many(   t)
  t={}; for j=1,100 do push(t,j) end
  --print(oo(many(t, 10))) end
  o(many(t, 10)) end

function EGS.far(   r,c,row1,row2)
  r = ROWS:new(the.data)
  row1   = r.rows[1]
  c,row2 = r:far(r.rows[1], r.rows) end
  --print(c,"\n",o(row1),"\n", o(row2)) end

function EGS.half(   r,c,row1,row2)
  local lefts,rights,x,y,x
  r = ROWS:new(the.data)
  r:mid(r.cols.y)
  lefts,rights,x,y,c = r:half()
  lefts:mid(lefts.cols.y )
  rights:mid(rights.cols.y)
  asserts(true,"half") end

function EGS.cluster(r)
  r = ROWS:new(the.data)
  --CLUSTER:new(r):show() end
  CLUSTER:new(r) end

-- start-up
if arg[0] == "sl.lua" then
  if the.help then print(help:gsub("\nNOTES:*$",""")) else
    local b4={}; for k,v in pairs(the) do b4[k]=v end
    for _,todo in pairs(the.todo=="all" and slots(EGS) or {the.todo}) do
      for k,v in pairs(b4) do the[k]=v end
      math.randomseed(the.seed)
      if type(EGS[todo])=="function" then EGS[todo]() end end
  end
  for k,v in pairs(_ENV) do if not b4[k] then print("?",k,type(v)) end end
  os.exit(fails)
else
  return {CLUSTER=CLUSTER, COLS=COLS, NUM=NUM, ROWS=ROWS,
          SKIP=SKIP, SOME=SOME, SYM=SYM,the=the,oo=oo,o=o}
end
-- git rid of SOME for rows
-- nss  = NUM | SYM | SKIP
-- COLS = all:[nss]+, x:[nss]*, y:[nss]*, klass;col?
-- ROWS = cols:COLS, rows:SOME
-- ## References
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