```
b4={}; for k,__in pairs(_ENV) do b4[k]=k end local r,abs,log,ent,min,max local copy,push,fmt fmt2,map,map2,cat,cat2,rnd,rnds local adds,class,thing,things,csv local ok,cli,demos,demo local the,fails,go,no local Nim,Sym.Col 8. Fers
local Num, Sym, Cols, Egs
the={k = 2,
    m = 1,
    seed = 10019,
    rnd = "%5.3f",
    dump = false,
    todo = "the",
    keep = 512}
            math.random
r= math.rand
abs= math.abs
log= math.log
min= math.min
max = math.max
push= function(t,x) t[1 + #t] = x; return x end
 fmt= string.format
fmt2= function(k,v) return fmt(":%s%s",k,v) end
map= function(t,f, u) u={}; for _,v in pairs(t)do u[1+#u]=f(v) end; return u end
map2= function(t,f, u) u={}; for k,v in pairs(t)do u[1+#u]=f(k,v)end; return u end
copy= function(t, u)
   if type(t) ~= "table" then return t end
   u={}; for k, v in pairs(t) do u[copy(k)]=copy(v) end; return u end
cat= function(t) return "{"..table.concat(map(t,tostring), ",").."}" end
cat2= function(t,sep) return "{"..table.concat(map2(t,fmt2),sep or "").."}" end
return fmt(type(x)=="number" and (x~=x//1 and f or the.rnd) or"%s",x) end rnds= function(t,f) return map(t, function(x) return rnd(x,f) end) end
ent= function(t, n,e)
    n=0; for _,v in pairs(t) do n=n+v end
    e=0; for _,v in pairs(t) do e=e-v/n*log(v/n,2) end; return e end
things= function(s,sep, t) t=\{\}; \ for \ y \ in \ s:gmatch("([^{\wedge},]+)") \ do \ t[1+\#t]=coerce(y) \ end \\ return \ t \ end
      re function(src)
    src = io.input(src)
    return function(x) x=io.read()
    if x then return things(x) else io.close(src) end end end
class= function(name, t,new)
  function new(klass,...)
    local obj= setmetatable({},klass)
    local rese klass.new(obj,...)
    if res then obj = setmetatable(res,klass) end
    return obj end
    t=(_tostring=cat2, _is=name or ""}; t.__index=t
    return setmetatable(t, {_call=new}) end
return obj end
cli= function(the, k,v)
    for n,flag in ipairs(arg) do
    k = flag:sub(3)
             v = the(k)
if v -= nil then
v = v==false and"true" or v==true and"false" or arg[n+1]
the(k] = thing(v) end end
return the end
fails=0
         function(test,msg)
  print("", test and "PASS "or "FAIL ",msg or "")
  if not test then
                 fails= fails+1

if the.dump then assert(test,msg) end end end
demos= function(the,go, old)
    old = copy(the)
    if the.todo=="all"
    then for s,f in pairs(go) do demo(s, f, old) end
    else demo(the.todo, go[the.todo], old) end end
```

```
Num=class("Num")

function Num:new(at,name)
self.at, self.name = at or 0, name or ""
self.w = self.name:find"5-" and -1 or 1
self.some, self.ok = (), false
self.n,self.md,self.sd,self.lo,self.hi = 0,0,0,1E32,-1E32 end
function Num:add(x,_, a,d)
if x -="?" then
self.n = self.n + 1
d = x - self.mu + d/self.n
self.m2= self.m2 + d*(x - self.mu)
self.sd (self.m2< or self.x2) and 0 or ((self.m2/(self.n - 1))^0.5)
self.lo= min(x, self.lo)
self.hi= max(x, self.hi)
a = self.some
if # a < the.num.keep then self.ok=false; push(a,x)
elseif r() < the.num.keep/self.n then self.ok=false; a[r(#a)]=x end end
return x end</pre>
   function Num:mid() return self.mu end
function Num:div() return self.sd end
   function Num:like(x, )
        inction Num:like(x,_)
local z, e, pi = 1E-64, math.exp(1), math.pi
if x < self.mu - 4*self.sd then return 0 end
if x > self.mu + 4*self.sd then return 0 end
return e^(-(x - self.mu)^2 / (z + 2*self.sd^2))/(z + (pi*2*self.sd^2)^.5) end
  Sym=class("Sym")
function Sym:new(at,name)
self.at, self.name = at or 0, name or ""
self.has, self.mode, self.most = {},nil,0 end
 function Sym:add(x,inc)
   if x -= "?" then
   inc = inc or 1
   self.n = self.n + inc
   self.has[x] = inc + (self.has[x] or 0)
   if self.has[x] > self.most then
        self.most, self.mode = self.has[x], x end end
   return x end
  function Sym:mid() return self.mode end
function Sym:div() return ent(self.has) end
  function Sym:like(x,prior)
  return ((self.has[x] or 0) + the.m*prior)/(self.n + the.m) end
 Cols=class("Cols")

function Cols:new(names, col)
self.names = names
self.all, self.x, self.y = {}, {}

for at,name in pairs(names) do
col = push(self.all, (name;find"[A-Z]" and Num or Sym) (at,name))
if not name:find"[S" then
if name:find"[S" then
if name:find"[S" then self.klass=col end
col.indep = not name:find"[-+|]S"
push(col.indep and self.x or self.y, col) end end end
  Egs=class("Egs")
function Egs:new() self.rows, self.cols = {},nil end
 function Egs:add(row, add)
  add = function(col) col:add(row[col.at]) end
  if self.cols then push(self.rows, map(self.cols,add)) else
  self.cols = Cols(row) end end
 function Egs:mid(cols)
  return map(cols or self.cols.y, function(col) return col:mid() end) end
 function Egs:div(cols)
       return map(cols or self.cols.y, function(col) return col:mid() end) end
       unction Egs:like(row,egs, n,prior,like,col)
n=0; for _,eg in pairs(egs) do n = n + #eg.rows end
prior = (#self.rows + the.k) / (n + the.k * #egs)
like = log(prior)
for at,x in pairs(row) do
col = self.cols.all(at)
if x = "?" and col.indep then like= like + log(col:like(x,prior)) end end
return like end
  function Eqs:like(row,eqs,
```