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-- ### Maths Tricks
local r,ish,cosine
 -- **r()**: Random number shorthand.
 r=math.random
-- **ish() **: is 'x' is close-ish to 'y'?
-- **cosine() **: for three ABC with sides abc,
-- where does C falls on the line running AB?
function ish(x,y,z) return math.abs(y -x ) < z end
function cosine(a,b,c)
return math.max(0,math.min(1, (a^2+c^2-b^2)/(2*c+1E-32))) end
               ||--|--
  -- ### List Tricks
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local any,many,last,per,pop,push,sort,firsts,stsrif,copy,map,sum
local inc,inc2,inc3, has,has2,has3, powerset, shuffle
-- **any()**: returns any thing from a list
-- **any()**: return multiple **any()** things.
function any(a)
return a[ math.random(#a) ] end
function many(a,n, u) u={}; for j=1,n do u[1+#u] =any(a) end; return u end
 -- **pop() **: dump from end
-- **push() **: add to ed
function pop(a) return table.remove(a) end
function push(t,x) t[1 + #t] = x; return x end
-- **sort()**: return a list, ordered on function `f`.
-- **firsts()**: order on sub-list first items
function sort(t,f) table.sort(t,f); return t end
function firsts(a,b) return a[1] < b[1] end
function stsrif(a,b) return a[1] > b[1] end
 -- **copy()**: deep copy
function copy(t, u)
if type(t)-="lable" then return t end
u={}; for k,v in pairs(t) do u(copy(k)]=copy(v) end
return setmetatable(u, getmetatable(t)) end
 -- **map() **: return a list with 'f' run over all items function map(t,f, u) u={}; for k,v in pairs(t) do u[1+#u]=f(v) end; return u end
 -- **sum()**: sum all list items, filtered through 'f'
-- (which defaults to just use the ran values).
function sum(t,f, n)
n=0; map(t,function(v) n=n+(f and f(v) or v) end)
return n end
 -- **has()** implements a 1,2, or level nested lookup function has(f,a) return f[a] or 0 end function has2(f,a,b) return f[a] and has(f[a],b) or 0 end function has3(f,a,b,c) return f[a] and has2(f[a],b,c) or 0 end
 -- **shuffle()**: randomize order (sorts in place)
function shuffle(t, j)
for i=#t,2,-1 do j=math.random(i); t[i],t[j]=t[j],t[i] end; return t end
     - **pwoerset()**: return all subsets
 -- "pwoerset()": return all subsets
function powerset(s)
local t = {(}}
for i = 1, #s do
    for j = 1, #t do
    t[#t+1] = {s[i],table.unpack(t[j])} end end
    return t end
                 -- ### String -> Things
local words, things, thing, lines
  -- **words()**: split string into list of substrings
 function words (s,sep, t)

sep="([^" .. (sep or ",") .. "]+)"

t={}; for y in s:gmatch(sep) do t[1+#t] = y end; return t end
-- **things()**: convert strings in a list to things
-- **thing()**: convert string to a thing
function things(s) return map(words(s), thing) end
function thing(x)
x = x:match**%**(-)%*s**
if x=="fulse" then return true elseif x=="false" then return false end
return tonumber(x) or x end
 -- **lines()**: (iterator) return lines in a file. Standard usage is
-- 'for cells in file(NAME, things) do ... end'
function lines(file,f, x)
file = io.input(file)
f = f or things
return function() x=io.read(); if x then return f(x) else io.close(file) end end
end end
                  -- ### Things -> Strings
local fmt,o,oo,slots,rnds,rnd
 -- **fmt()**: String format shorthand fmt = string.format
-- **o()**: Print string from nested table.
-- **o()**: Generate string from nested table.
function oo(t) print(o(t)) end
function o(t, seen, u)

if type(t)~="table" then return tostring(t) end
seen = seen or {}

if seen[t] then return "..." end
seen[t] = t

local function show1(x) return o(x, seen) end
local function show2(k) return fmt(":%%%s",k, o(t[k],seen)) end
u = #t>0 and map(t,show1) or map(slots(t),show2)
return (t.s or "")..."{"..table.concat(u,"")..."}" end
  -- **slots() **: return table slots, sorted.
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function slots(t, u) local function public(k) return tostring(k):sub(1,1) \sim= "_" end u={};for k,v in pairs(t) do if public(k) then u[1+#u]=k end end return sort(u) end
  -- **rnds()**: round list of numbers
-- **Ind()**: round one number.

function rnds(t, f) return map(t, function(x) return nd(x, f) end) end

function rnd(x, f)

f = not f and "%s" or number and fmt("%%%sf", f) or f

return fmt(type(x) =="number" and (x~=x//1 and f) or "%s",x) end
                 ### Make settings from help string and CLI (command-line interface)
local cli
  -- **cli()**: In a string, look for lines indented with two spaces, starting wit
       Each such line should have a long and short flag, some help tesx and (at end of line), a default values. e.g.
                 -seed -S set the random number seed = 10019
-|-(7_\(\neg \)|-_\(\neg \)
-- ### Test suites local ok,go
-- **ok()**: maybe, print stack dump on errors.
-- Increment the 'fails' counter on failed 'test'.
function ok(tests,test,msg)
print(test and " PASS:"or " FAIL:",msg or "")
if not test then
tests.ails = tests.ails+1
if the and the.dump then assert(test,msg) end end end
if the and the dump then assert(test,msg) end end end
-- **go()**: run some 'tests', controlled by 'settings'.
-- Maybe update the 'ails' counter.
-- Return the total fails to the operating system.
function go(settings,tests,b4, defaults)
tests.ails = 0
defaults={}; for k,v in pairs(settings) do defaults[k]=v end
local todo = settings.todo or "all"
for k,one in pairs(todo=w"all" and slots(tests) or {todo}) do
if k ~= "main" and type(tests[one]) == "function" then
for k,v in pairs(defaults) do settings[k]=v end
math.randomseed(settings.seed or 1)
print(fmt("#%s",one))
tests[one](tests) end end
if b4 then
      if b4 then
     if b4 then
  for k,v in pairs(_ENV) do
    if not b4[k] then print("??",k,type(v)) end end end
os.exit(tests.ails) end
                  -- ### Objects
local as, is
-- **new() **: make a new instance.
-- **class() **: define a new class of instances
as = setnetatable
function is(s, t
    t={tostringo,s=s or ""}; t.index=t
    return as(t, (call=function(...) return t.new(...) end}) end
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local nbl, trainl,testl,classifyl,scorel

function nbl(file)
local i = (h={}), nh=0,e={}), names=nil, n=0, wait=the.wait, log={}}

for row in lines(file) do
    if not i.names then i.names=row else testl(i,row); trainl(i,row) end end
    return scorel(i.log) end

function trainl(i,t)
    i.n = i.n + 1
    if not i.h[t[#t]] then i.nh = i.nh + 1 end
    inc(i.h, t[#t])
    for col,x in pairs(t) do if x~="?" then inc3(i.e,col,x,t[#t]) end end end

function testl(i,t)
    if i.n > i.wait then push(i.log, {want=t[#t], got=classifyl(i,t)}) end end

function classifyl(i,t)
local hi,out = -1
    for h,_ in pairs(i.h) do
    local prior = ((i.h[h] or 0) + the.K)/(i.n + the.K*i.nh)
    local l = prior
    for col,x in pairs(t) do
    if x ~= "?" and col ~= #t then
        l=1*(has3(i.e,col,x,h) + the.M*prior)/((i.h[h] or 0) + the.M) end end
    if l>hi then hi,out=1,h end end
    return out end

function scorel(log, n)
    n=0; for _r,x in pairs(log) do if x.want==x.got then n=n+1 end end
    return n/#log end
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                       -- ## Egs
local Egs,Cols,Ratio,Nominal=is"Egs",is"Cols",is"Ratio", is"Nominal"
      -- Egs store examples (in 'rows'), summarized in columns (in 'cols') function Egs:new(names) return as({rows={}}, cols=Cols(names)}, Egs) end
      function Egs:new4file(file, i)
  for _,row in lines(file) do if i then i:add(row) else i=Egs(row) end end
  return i end
      function Egs.add(i,t)
          t = t.cells or t -- detail (for future extension)
push(i.rows, map(i.cols.all, function(col) return col:add(t[col.at]) end)) end
       function Egs.mid(i,cols) return map(cols or i.cols.all, function(col) return col
:mid() end) end
      function Eqs.clone(i) return Eqs(i.cols.names) end
      function Egs.klass(i,row) return row[i,cols.klass.at] end
     -- ## Col
-- Convert names into various Column types.
local ako={}
ako.ratio = function(x) return x:find"^[A-Z]" end
ako.goal = function(x) return x:find"[-+]" end
ako.klass = function(x) return x:find"[$" end
ako.ignore = function(x) return x:find"[$" end
ako.less = function(x) return x:find"-$" end
       -- ## Col
       -- Every new column goes into 'all'. Also, for any column that we we
             are not ignoring, then that also gets added to (a) either the list of 'x' independent columns or 'y' dependent columns; and (b) maybe, the 'klass' slot.
      -- the 'klass' slot.

function Cols:new(names)

local i = as((names-names, klass=nil,all={}, x={}, y={}}, Cols)

for at,name in pairs(names) do

local col = (ako.ratio(name) and Ratio or Nominal) (at,name)

col.is.goal = ako.goal(name)

push(i.all, col)

if not ako.ignore(name) then

if ako.klass(name) then i.klass = col end

push(ako.goal(name) and i.y or i.x, col) end end

return i end
       -- ## Nominal
-- Summarize symbols in 'Nominal's
function Nominal:new(at,name)
at,name = at or 0, name or ""
return as({at=at, name=name, n=0, has={}, mode=nil, most=0}, Nominal) end
       function Nominal.add(i,x)
if x ~= "?" then
i.n = i.n+i
i.has[x] = 1 + (i.has[x] or 0)
if i.has[x] > i.most then i.most, i.mode = i.has[x], x end end
return x end
      function Nominal.mid(i) return i.mode end
      -- ## Ratio
-- Summarize numbers in 'Ratio's
function Ratio:new(at,name)
at,name = at or 0, name or ""
return as({at=at, name=name, n=0, mu=0, m2=0, sd=0, w=ako.less(name) and -1 or
1}, Ratio) end
       function Ratio.add(i,x)
if v ~= "?" then
          inf x -= """ then
i.n = i.n+1
local d= x - i.mu
i.mu = i.mu + d/i.n
i.m2 = i.m2 + d*(x - i.mu)
i.m2 = i.m2 + d*(x - i.mu)
i.sd = ((i.m2<0 or i.n<2) and 0) or ((i.m2/(i.n - 1))^0.5)
i.lo = i.lo and math.min(x, i.lo) or x
i.hi = i.hi and math.max(x, i.hi) or x end</pre>
       function Ratio.mid(i) return i.mu end
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                       NENLIM
       local Nb = is"Nb"
      -- ## Add likelihood calculators
function Egs.like(i,t,prior)
local like = prior
for at,x in pairs(t) do
local col = i.cols.all[at]
if not col.is_goal then
like = like * (x=="?" and 1 or i.cols.all[at]:like(x,prior)) end end
return like end
 410
### function Ratio.like(i,x,prior)
### if x < i.mu - 3*i.sd then return 0 end
### if x > i.mu + 3*i.sd then return 0 end
### local denom = (math.pi*2*i.sd*2)^.5
### local nom = math.exp(1)^(-(x-mu)^2/(2*i.sd^2+1E-32))
### return nom/(denom + 1E-32) end
       function Nominal.like(i,x,prior)
  return ((i.has[x] or 0) + the.M*prior)/(i.n + the.M) end
              ## Create and update
        function Nb:new()
  return as({h={}, all=nil, nh=0, n=0, wait=the.wait, log={}},Nb) end
       function Nb:new4file(file.
                                                                      i)
            i = Nb()
for row in lines(file) do i:add(row) end end
      function Nb.add(i,row)
  if not i.all then print(1); i.all = Nb(row) else i:test(row); i:train(row) end
       -- ## Train, test, classify
function Nb.train(i,t)
i.n = i.n + 1
print(2,o(i.all))
local h = i.all:klass(t)
print(3)
if not i.h[h] then i.nh = i.nh + 1; i.h[h] = i.all:clone() end
i.h[h].add(row)
            if not i.h[h] then
i.h[h]:add(row)
i.all:add(row) end
         \begin{array}{ll} \textbf{function} \text{ Nb.test(i,t)} \\ \textbf{if i.n} > \textbf{i.wait then} \text{ push(i.log, } \{ want=\textbf{i.all:klass(t), got=classify(i,t)} \}) \\ \textbf{end} \\ \textbf{end} \end{array} 
        function Nb.classify(i,t)
local hi,out = -1
for klass,h in pairs(i.h) do
local prior = (h.n + the.K) / (i.n + the.K*i.nh)
local like = h:like(t,prior)
if like > hi then hi,out=like,klass end end
return out end
        -- ## Score
function Nb.score(i, n)
n=0; for _,x in pairs(i.log) do if x.want==x.got then n=n+1 end end
return n/#i.log end
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