```
-- maths
r= math.random
abs= math.abs
log= math.log
min= math.min
max= math.max
function ent(t, n,e)
n=0; for _,v in pairs(t) do n=n+v end
e=0; for _,v in pairs(t) do e=e-v/n*log(v/n,2) end; return e end
 -- 15ts
function push(t,x) t[1 + #t] = x; return x end
function sort(t,f) table.sort(t,f); return t end
function map(t,f, u) u={}; for _v in pairs(t)do u[1+#u]=f(v) end; return u end
function map2(t,f, u) u={}; for k,v in pairs(t)do u[k] = f(k,v) end; return u end
 function copy(t, u)
  if type(t) ~= "table" then return t end
  u={};for k,v in pairs(t) do u[copy(k)]=copy(v) end; return u end
  function slots(t, u,public)
function public(k) return tostring(k):sub(1,1) ~= "_" end
u={};for k,v in pairs(t) do if public(k) then u[1+#u]=k end end
return sort(u) end
  -- things to strings
fmt= string.format
fmt2= function(k, v) return fmt(":%s %s",k,v) end
  function ooo(t) print( ft>1 and o(t) or oo(t)) end
function o(t,s) return "{"..table.concat(map(t,tostring),s or",").."}" end
function oo(t,sep, slot)
function slot(k) return fmt2(k, t[k]) end
return (t.is or"")..o(map(slots(t),slot),sep or" ") end
  function \operatorname{rnds}(t,f) return \operatorname{map}(t,\operatorname{function}(x)\operatorname{return}\operatorname{rnd}(x,f) end) end function \operatorname{rnd}(x,f) return \operatorname{fmt}(\operatorname{type}(x) = \operatorname{"number"}\operatorname{and}(x \sim x / 1) and f or the rnd) or "%s",x) end
  -- strings to things
function coerce(x)
x = x:match**%s*(-)%s*$"
if x=="false" then return true elseif x=="false" then return false end
return math.tointeger(x) or tonumber(x) or x end
  function csv(src, things) function things(s, t) t=(s, \text{ for } y \text{ in } s \text{ :gmatch}, t) \\ t=(s, \text{ for } y \text{ in } s \text{ :gmatch}, (([\land,]+)^*) \text{ do } t[1+\#t]=\text{coerce}(y) \text{ end; return } t \text{ end } src = io.input(src) \\ src = io.input(src) \\ return function(x) x=io.read() \\ if x then return things(x) else io.close(src) end end end
 -- misc
function class(name, t,new)
function new(klass,...)
  local obj = setmetatable({},klass)
  local res = klass.new(obj,...)
  if res then obj = setmetatable(res,klass) end
  return obj
end ------
t={_tostring=oo, is=name or ""}; t.__index=t
  return setmetatable(t, {_call=new}) end
 function adds(obj,data)

if type(data) == "string"

then for row in csv(data) do obj:add(row) end
else for _,row in pairs(data or {}) do obj:add(row) end end
return obj end
  -- startup, execution, unit tests function settings (t,help) help:gsub ("n [-]([^*s]+)[*s]+[^n]*%s([^*s]+)",function(k,x) t[k]=coerce(x) end) return t end
function cli(the, flag)
for k,v in pairs(the) do
flag="-".k
for n, flag1 in ipairs(arg) do
   if flag1 == flag then
    v = v==false and"fune" or v==true and"false" or arg[n+1]
    the[k] = coerce(v) end end end
   if the.h then os.exit(print(help)) else return the end end
 function ok(test,msg)
  print("", test and "PASS "or "FAIL ", msg or "")
  if not test then
              fails= fails+1

if the.dump then assert(test,msg) end end end
 function demos(the,go, demo1,defaults)
function demo1(txt,fun)
assert(tun, fmt ("unknown start-up action: %s",txt))
the = copy(defaults)
math.randomseed(the.seed or 10019)
print(txt)
fun()
```

```
local Some=class("Some")
function Some:new()
  self.kept, self.ok, self.n = {}, false,0 end
     self.n = 1 + self.n

a = self.kept

if #a < the.keep then self.ok=false; push(a,x)

elseif r() < the.keep/self.n then self.ok=false; a[r(#a)]=x end end
function Some:has()
  if not self.ok then table.sort(self.kept) end
  self.ok = true
  return self.kept end
local Num=class("Num")
function Num:new(at,name)
    self.at, self.name = at or 0, name or "
    self.w = self.name:find"$-" and -1 or 1
     self.some=Some()
self.n,self.mu,self.m2,self.sd,self.lo,self.hi = 0,0,0,0,1E32,-1E32 end
 function Num:add(x,_, a,d)
if x ~="?" then
    if x ~="?" then
self.some:add(x)
self.n = self.n + 1
self.lo = min(x, self.lo)
self.hi = max(x, self.hi)
d = x - self.mu + d/self.n
self.m2 = self.m2 + d*(x - self.mu)
self.m2 = self.m2 + d*(x - self.mu)
self.sd = (self.m2<0 or self.n<2) and 0 or ((self.m2/(self.n - 1))^0.5) end
return x end</pre>
function Num:mid() return self.mu end
function Num:div() return self.sd end
function Num:norm(x, lo,hi)
lo,hi= self.lo, self.hi
return x=="?" and x or hi-lo < 1E-9 and 0 or (x - lo)/(hi - lo) end</pre>
 local Sym=class("Sym")
function Sym:new(at,name)
self.at, self.name = at or 0, name or ""
self.n, self.has, self.mode, self.most = 0,{},nil,0 end
function Sym:add(x,inc)
  if x ~= "?" then
  inc = inc or 1
  self.n = self.n + inc
  self.has[x] = inc + (self.has[x] or 0)
  if self.has[x] > self.most then self.most,self.mode = self.has[x],x end end
  return x end
 function Sym:mid() return self.mode end
function Sym:div() return ent(self.has) end
function Sym:like(x,prior)
  return ((self.has[x] or 0) + the.m*prior)/(self.n + the.m) end
local Cols=class("Cols")
function Cols:new(names, col)
self.names = names
self.names = names
self.all, self.x, self.y = {}, {}, {}
for at.name in pairs(names) do
    col = push(self.all, (name:find"[A-Z]" and Num or Sym)(at.name))
    if not name:find"[s" then
        if name:find"[s" then
    col.indep = not name:find"[-+!]$"
    push(col.indep and self.x or self.y, col) end end end
 local Eqs=class("Egs")
 function Egs:new() self.rows, self.cols = {},nil end
function Egs:add(row, add)
  add = function(col) col:add(row[col.at]) end
  if self.cols then push(self.rows, map(self.cols,add)) else
    self.cols = Cols(row) end end
function Egs:mid(cols)
  return map(cols or self.cols.y, function(col) return col:mid() end) end
function Egs:div(cols)
   return map(cols or self.cols.y, function(col) return col:div() end) end
function Egs:better(row1,row2)
local s1, s2, n, e = 0, 0, #self.cols.y, math.exp(1)
for _,col in pairs(self.cols.y) do
  local a = col:norm(row1[col.at])
  local b = col:norm(row2[col.at])
  s1 = s1 - e^c(col.w * (a - b) / n)
  s2 = s2 - e^c(col.w * (b - a) / n) end
  return s1 / n < s2 / n end</pre>
 function Egs:betters()
  return sort(self.rows, function(a,b) return self:better(a,b) end) end
```