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1  #!/usr/bin/env python3 --B
2  """
3  xai4.py: explainable multi-objective optimization
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5
6  Input is CSV. Header (row 1) defines column roles as follows:
7  [A-Z]* : Numeric (e.g. "Age"), [a-z]* : Symbolic (e.g. "job").
8  *+ : Maximize (e.g. "Pay+"), *- : Minimize (e.g. "Cost-").
9  *X : Ignored (e.g. "idx*"). ? : Missing value (not in header)
10
11 To download example data:
12 mkdir -p $HOME/gits
13 git clone http://github.com/timm/moot $HOME/gits/moot
14
15 To download code, install it, then test it, download this file then:
16 chmod +x xai.py
17 ./xai.py --xai -gits/moot/optimize/misc/auto93.csv"""
18 import ast,sys,random
19 from math import sqrt,exp,floor
20 from types import SimpleNamespace as obj
21 from pathlib import Path
22
23 ATOM = str | int | float
24 ROW = list[ATOM]
25 ROWS = list[ROW]
26 NUM,SYM,DATA = obj,obj,obj
27 COL = NUM | SYM
28 THING = COL | DATA
29
30 BIG=1e32
31 the=obj(bins=7, budget=30, seed=1)
32
33 ### Constructors -----
34 def Sym(): return obj(it=Sym, n=0, has={})
35 def Num(): return obj(it=Num, n=0, mu=0, m2=0)
36
37 def Col(at=0, txt=""):
38     col = (Num if txt[0].isupper() else Sym)()
39     col.at, col.txt, col.best = at, txt, 0 if txt[-1]=="-" else 1
40     return col
41
42 def Cols(names: # (list[str]) -> Cols
43 cols = [Col(n,s) for n,s in enumerate(names)]
44 return obj(it=cols, names=names, all=cols,
45 x=[col for col in cols if col.txt[-1] not in "+-X"],
46 y=[col for col in cols if col.txt[-1] in "+-"])
47
48 def Data(rows=None):
49     return adds(rows, obj(it=Data, rows=[], n=0, cols=None, _centroid=None))
50
51 def clone(data, rows=None): return adds(rows, Data([data.cols.names]))
52
53 ### Functions -----
54 def adds(src, i=None): # (src:Iterable, ?i) -> i
55     i = i or Num(); [add(i,v) for v in src]; return i
56
57 def sub(i, v): return add(i, v, inc=False)
58
59 def add(i, v, inc=True):
60     if v=="":
61         if Data is i.it and not i.cols: i.cols = Cols(v) # initializing, not adding
62     else:
63         i.n += 1 # adding
64         if Sym is i.it: i.has[v] = inc + i.has.get(v,0)
65         elif Num is i.it: d = v-i.mu; i.mu += inc*d/i.n; i.m2 += inc*d*(v-i.mu)
66         else:
67             i._centroid = None # old centroid now out of date
68             [add(col,v[col.at],inc) for col in i.cols.all] # recursive add to cols
69             i.rows.append if inc else i.rows.remove(v) # handle row storage
70     return v # convention: always return the thing being added
71
72 def norm(num,n):
73     z = (n - num.mu) / sd(num); return 1 / (1 + exp(-1.7 * max(-3, min(3, z))))
74
75 def sd(num):
76     return 1/BIG + (0 if num.n < 2 else sqrt(max(0,num.m2)/(num.n - 1)))
77
78 def mid(col): return col.mu if Num is col.it else max(col.has, key=col.has.get)
79
80 def mids(data):
81     data._centroid = data._centroid or [mid(col) for col in data.cols.all]
82     return data._centroid
83
84 def disty(data, row):
85     ys = data.cols.y
86     return sqrt(sum(abs(norm(y, row[y.at]) - y.best)**2 for y in ys) / len(ys))
87
88 def distx(data, row1, row2):
89     xs = data.cols.x
90     return sqrt(sum(_aha(x, row1[x.at], row2[x.at])**2 for x in xs) / len(xs))
91
92 def _aha(col, u, v):
93     if u==v=="": return 1
94     if Sym is col.it : return u != v
95     u, v = norm(col,u), norm(col,v)
96     u = u if u != "?" else (0 if v>0.5 else 1)
97     v = v if v != "?" else (0 if u>0.5 else 1)
98     return abs(u - v)
99
100 def peeking(data,rows): # best if rows arrived shuffled
101     d = clone(data, rows[:the.warm]) # all rows labelled by this function
102     a,z = clone(data),clone(data) # best, rest labelled rows
103     x = lambda r: distx(d,r,mids(a)) - distx(d,r,mids(z)) # <0 if closest to best
104     y = lambda r: disty(d,r) # distanace of goals to "heaven" (best values)
105     d.rows.sorted(key=y)
106     adds(d.rows[:the.warm//2], a)
107     adds(d.rows[the.warm//2:], z)
108     for r in rows[the.warm:]:
109         if d.n >= the.budget: break
110         elif x(r) < 0:
111             add(d, add(a,r))
112             if a.n > sqrt(d.n): # too many best things
113                 a.rows.sorted(key=y)
114             add(z, sub(a, a.rows[-1])) # demote worse row in best to rest
115     d.rows.sorted(key=x)
116     return obj(sorter=x, labelled=d)
117
118 ## Cutting -----
119 def score(num): return num.mu + sd(num) / (sqrt(num.n) + 1/BIG)
120
121 def cut(data, rows):
122     all_bins = (b for col in data.cols.x for b in cuts(col, rows, data))
123     return min(all_bins, key=lambda b: score(b.y), default=None)
124
125 def cuts(col, rows, data):
126     d, xys = {}, [(r[col.at], disty(data, r)) for r in rows if r[col.at]!="?"]
127     for x, y in sorted(xys):
128         k = x if Sym is col.it else floor(the.bins * norm(col, x))
129         if k not in d: d[k] = obj(it=col.at, txt=col.txt, xlo=x, xhi=x, y=Num())
130         add(d[k].y, y)

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131     d[k].xhi = x
132     return _complete(col, sorted(d.values(), key=lambda b: b.xlo))
133
134 def _complete(col, lst):
135     if Num is col.it:
136         for n, b in enumerate(lst):
137             b.xlo = lst[n-1].xhi if n > 0 else -BIG
138             b.xhi = lst[n+1].xlo if n < len(lst)-1 else BIG
139     return lst
140
141 ### Main -----
142 def gauss(mid,div):
143     return mid + 2 * div * (sum(random.random() for _ in range(3)) - 1.5)
144
145 def select(rule, row):
146     if (x:=row[rule.at]) == "?": return rule.xlo == rule.xhi == x
147     return rule.xlo <= x < rule.xhi
148
149 def xai(data):
150     print(o(the))
151     print(*data.cols.names)
152     print(o(mid=mids(data)))
153     def show(n): return f"^{dM}^{hM}^{mM}" if n==BIG else "AM-HM-MM" if n==BIG else
154     o(n)
155     go(rows, lvl=0, prefix=""):
156     ys = Num(); rows.sort(key=lambda row: add(ys, disty(data, row)))
157     print(f"{{rows[{len(rows)//2}]}} {{o(mu=ys.mu, n=ys.n, sd=sd(ys))}} {prefix}")
158     if rule := cut(data, rows):
159         now = [row for row in rows if select(rule, row)]
160         if 4 < len(now) < len(rows):
161             go(now, lvl + 1, f"{{rule.txt}} {{show(rule.xlo)}} {{show(rule.xhi)}}")
162     go(data.rows, 0)
163
164 def six(data):
165     seen = clone(data)
166     unique=set()
167     def go(rows, lvl=0, prefix=""):
168         ys = Num(); rows.sort(key=lambda row: add(ys, disty(data, row)))
169         some = shuffle(rows)[:the.budget]
170         for row in some:
171             add(seen, row)
172             unique.add(tuple(row))
173         if rule := cut(seen, some):
174             now = [row for row in rows if select(rule, row)]
175             if 4 < len(now) < len(rows):
176                 return go(now, lvl + 1, f"{{rule.txt}} {{o(rule.xlo)}} {{o(rule.xhi)}}")
177             return int(100*ys.mu)
178     return go(data.rows, 0)
179
180 ## Lib -----
181 def o(v=None, dec=2, **d):
182     isa = isinstance
183     if d: v=d
184     if isa(v, (int, float)): return f"{{round({v},dec)}}"
185     if isa(v, list): return f"{{'.join(o(k,dec) for k in v)}}"
186     if isa(v, tuple): return f"{{'.join(o(k,dec) for k in v)}}"
187     if callable(v): return v.__name__
188     if hasattr(v, "__dict__"): v = vars(v)
189     if isa(v, dict): return f"{{'.'.join(f'{{k}} {{o(v[k],dec)}}' for k in v)}}"
190     return str(v)
191
192 def coerce(s):
193     try: return int(s)
194     except Exception as _: pass
195     try: return float(s)
196     except Exception as _: pass
197     s=s.strip()
198     return {"true":True, "false":False}.get(s,s)
199
200 def csv(fileName):
201     with open(fileName,encoding="utf-8") as f:
202         for l in f:
203             if (l:=l.split("%")[0].strip()):
204                 yield [coerce(x) for x in l.split(",")]
205
206 def shuffle(lst): random.shuffle(lst); return lst
207
208

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208 #-----#
209 File=str(Path.home()) + "/gits/moot/optimize/misc/auto93.csv"
210
211 def go_h(_=None):
212     "show help"
213     print(_doc_, "\n\nOptions\n")
214     for k,f in globals().items():
215         if k.startswith("go_") and f.__doc__:
216             left, right = f.__doc__.split(":")
217             left = k[2:].replace("_", "-") + " " + left.strip()
218             d = f.__defaults__
219             default = f"(default:{[d[0]})" if d else ""
220             print(f" {left:15} {right.strip()} {default}")
221
222 def go_s(s=1):
223     "INT: set random SEED"
224     the.seed = coerce(s); random.seed(the.seed)
225
226 def go_b(s=5):
227     "INT: set number of BINS used on discretization"
228     the.bins = coerce(s)
229
230 def go_B(s):
231     "INT: set BUDGET for rows labelled each round"
232     the.budget = coerce(s)
233
234 def go_all(file=File):
235     "FILE: run all actions that use a FILE"
236     for k,fun in globals().items():
237         if k.startswith("go_") and k != "go_all":
238             print("\n",k,"-----"); fun(file)
239
240 def go_num(_=None):
241     "test Num"
242     num = adds(gauss(10, 2) for _ in range(1000))
243     print(o(mu=num.mu, sd=sd(num)))
244     assert 9.9 <= num.mu <=10.1 and 1.9 <= sd(num) <= 2.1
245
246 def go_sym(_=None):
247     "test Sym"
248     sym = adds('Previously, we have defined an iterative data mining', Sym())
249     print(sym.has)
250     assert sym.has["a"]==5
251
252 def go_csv(file=File):
253     "FILE: test csv loading"
254     total=0
255     for n, row in enumerate(csv(file)):
256         if n > 0: total += len(row)
257         if n > 0: assert isinstance(row[1], (float,int))
258         if n % 40==0: print(row)
259     assert 3184 == total
260
261 def go_data(file=File):
262     "FILE: test adding columns from file"
263     data = Data(csv(file))
264     total = sum(len(row) for row in data.rows)
265     print(*data.cols.names)
266     assert Num.is data.cols.all[0].it
267     assert 3184 == total
268     for col in data.cols.x: print(o(col))
269
270 def go_clone(file=File):
271     "FILE: test echoing structure of a table to a new table"
272     data1 = Data(csv(file))
273     data2 = clone(data1,data1.rows)
274     assert data1.cols.x[1].mu == data2.cols.x[1].mu
275
276 def go_distx(file=File):
277     "FILE: can we sort rows by their distance to one row?"
278     data=Data(csv(file))
279     print(*data.cols.names, "distx", sep=",")
280     r1 = data.rows[0]
281     data.rows.sort(key=lambda r2: distx(data, r1,r2))
282     for n,r2 in enumerate(data.rows[1:]):
283         assert o < distx(data, r1,r2) <= 1
284         if n%40==0: print(r2,o(distx(data, r1,r2)),sep=".")
285
286 def go_disty(file=File):
287     "FILE: can we sort rows by their distance to heaven?"
288     data=Data(csv(file))
289     print(*data.cols.names, "disty", sep=",")
290     data.rows.sort(key=lambda r: disty(data,r))
291     for n,r1 in enumerate(data.rows):
292         if n>0:
293             r2=data.rows[n-1]
294             assert disty(data, r1) >= disty(data,r2)
295             if n%40==0: print(r1,o(disty(data, r1)),sep=".")
296
297 def go_bins(file=File):
298     data = Data(csv(file))
299     all_bins = (b for col in data.cols.x for b in cuts(col, data.rows, data))
300     for b in sorted(all_bins, key=lambda b: score(b,y)):
301         print(b.txt,b.xlo,b.xhi, o(mu=b.y.mu, sd=sd(b.y), n=b.y.n,
302                                     scored= score(b.y)),sep="\t")
303
304 def go_xai(file=File):
305     "FILE: can we succinctly list main effects in a table?"
306     print("\n"+file)
307     xai(Data(csv(file)))
308
309 def go_six(file="data.csv"):
310     "FILE: redo xai, but in each loop, just read BUDGET rows"
311     xai(Data(csv(file))); print(" ")
312     go_s(the.seed)
313     for b in [5,10,20,30]:
314         go_B(the.budget)
315         print(b,sorted(six(Data(csv(file)))) for _ in range(20)))
316
317 def go_lurch(file=File):
318     data = Data(csv(file))
319     nlen(data.rows)//2
320     train,test = shuffle(data.rows[:n]) (the.Budget], data.rows[m:]
321     labelled = clone(data,train)
322     m= int(sqrt(the.Budget))
323     bmid,rmid = mid(clone(data,train[:m])), mid(clone(data,train[m:]))
324     xai(labelled)
325     sorter=lambda r: distx(labelled, bmid,r) - distx(labelled, rmid,r)
326     row = min(test.sort(key=sorter)[:5],
327               key=lambda r:dist(data.r))
328     print(row,ydist(data, row))
329
330 def go_peeking(file=File):
331     data = Data(csv(file))
332     nlen(data.rows)//2
333     train,test = shuffle(data.rows[:n]). data.rows[n:]
334     model=peeking(data, train)
335     xai(model,labelled)
336     row = min(test.sort(key=model.sorter)[:5],
337               key=lambda r:dist(data.r))

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338     print(row,ydist(data, row))
339
340     if __name__ == "__main__":
341         go_s(1)
342         for n, s in enumerate(sys.argv):
343             if fn := vars().get(f"go{s.replace('-', '_')}"):
344                 fn(sys.argv[n+1]) if n < len(sys.argv) - 1 else fn()

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