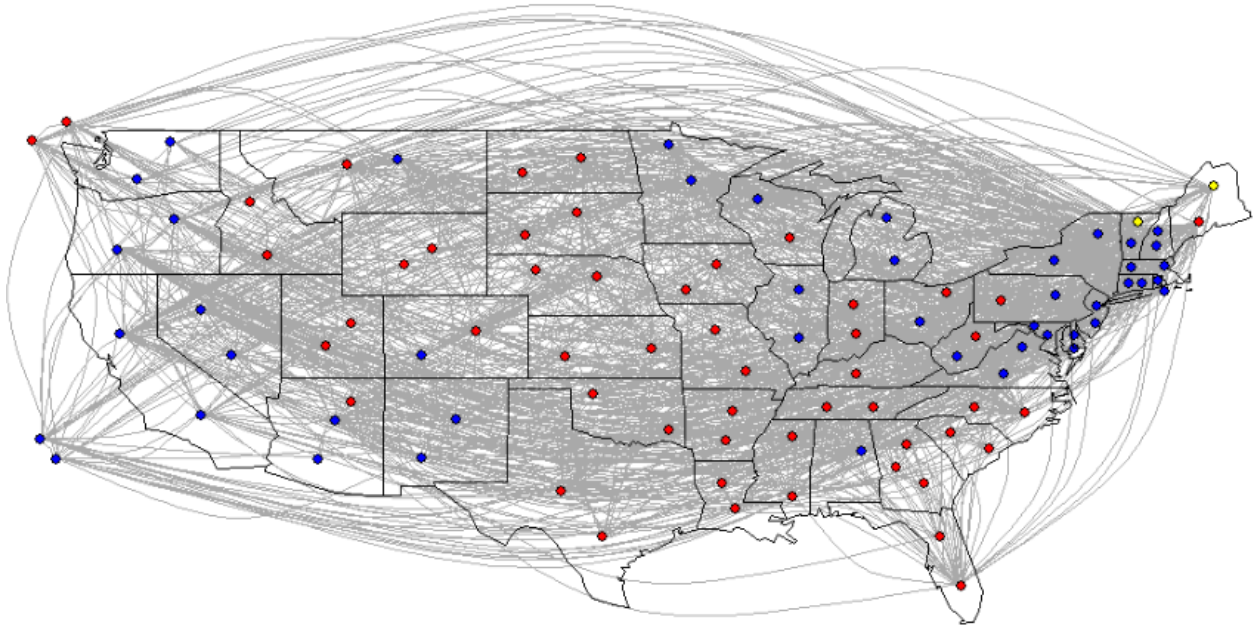


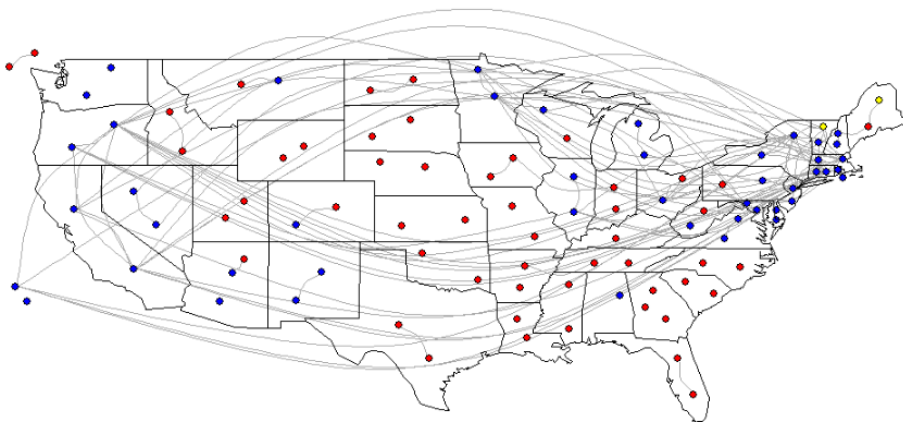
Tim Miller
15.071
HW #7

PROBLEM 1A



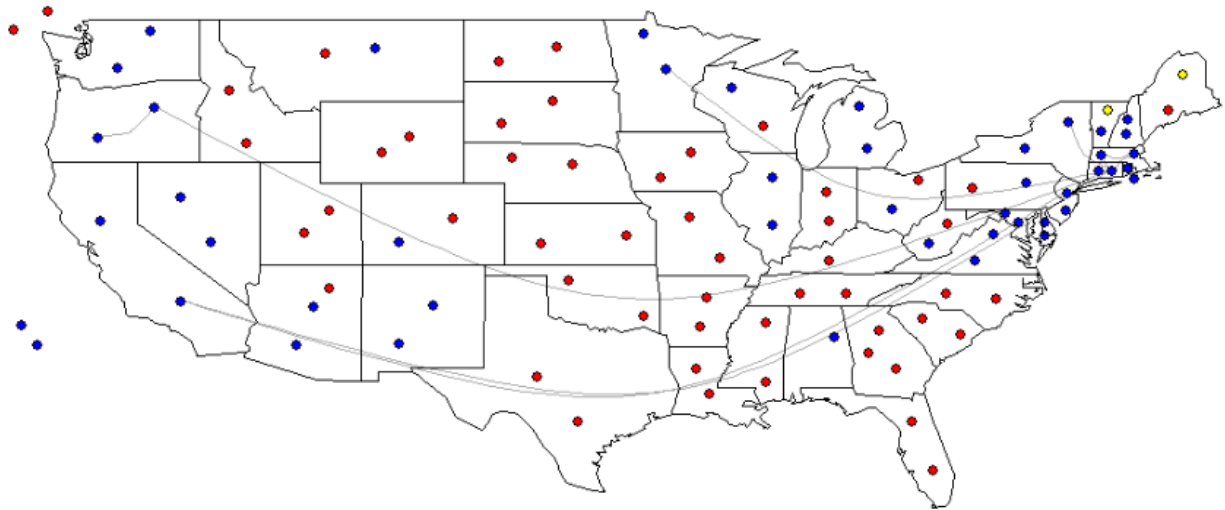
As expected, Democratic senators typically come from the west coast and northeast while Republican senators typically come from the south / southeast and Midwest of the country. This is because you typically find Democratic voters in the large coastal cities like L.A., SF, NYC, and Boston while Republican voters tend to be found in less densely populated areas across the south and Midwest.

PROBLEM 1B



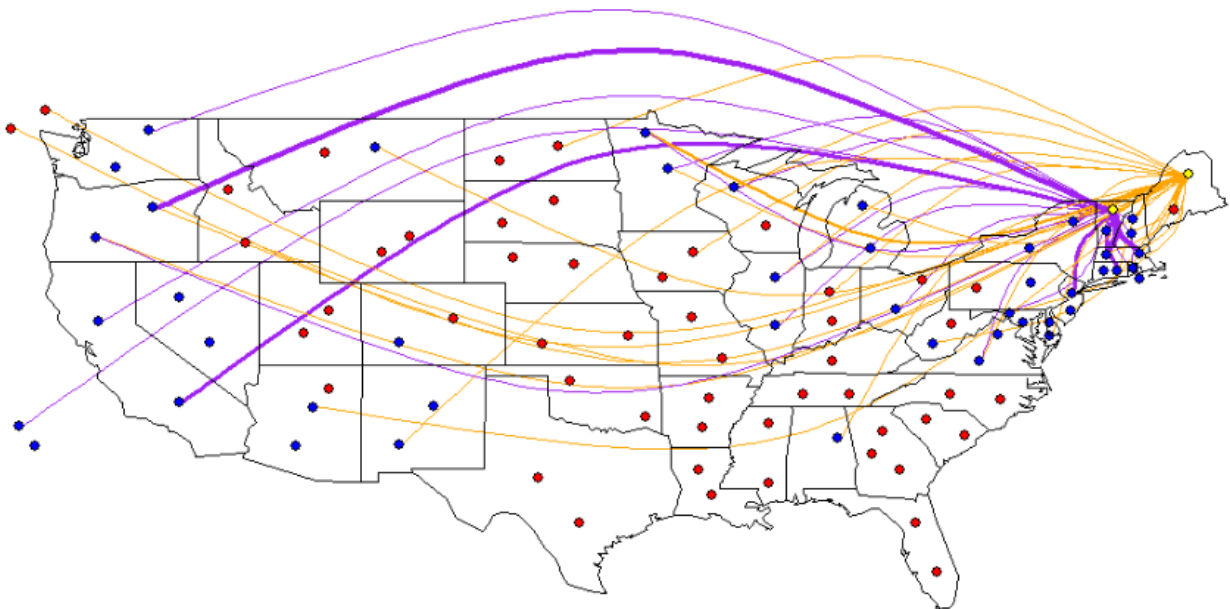
The above graph has a threshold of $n = 30$. One of the first interesting observations is that senators from blue states are more likely to co-sponsor bills with other senators than red states. You can see the

number of connections between blue dots in this chart, but very few between red dots. The reason for this might be that the Republicans had a majority in the senate for this dataset. Therefore, the Democrats might have felt the need to co-sponsor bills as a way to show unity and push their ideas through the Republican majority.



This chart was set at a threshold of $n = 70$. Another interesting observation is that there are a number of co-sponsorships across states e.g., west coast states with east coast states, but fewer co-sponsorships within a state. Interestingly, the senators from Oregon were on the same page frequently – one of the few (maybe only) states with this high of a co-sponsorship rate between senators from the same state.

PROBLEM 1C



There are a few interesting observations from this chart.

First, we see that the independent senator from Maine mostly has connections with Republican senators from other states. This is no surprise given the other senator in Maine is a Republican. This tells us that although the senator is Independent, they likely have a Republican leaning in their politics and policies they back.

Similarly, we see that the independent senator from Vermont mostly has connections with Democratic senators from other states. This is no surprise given the other senator in Vermont is a Democrat. This tells us that although the senator is Independent, they likely have a Democratic leaning in their politics and policies they back.

PROBLEM 1D

Calculating centrality figures

```
# Calculate degree centrality
dg = degree(sg)
sg.Senators$degree <- dg

# Calculate closeness centrality
cl = closeness(sg)
sg.Senators$closeness <- cl

# Calculate betweenness
bn = betweenness(sg)
sg.Senators$betweenness <- bn
```

Senators with top 10 degree of centrality

```
> head(sg.Senators[order(sg.Senators$degree, decreasing = TRUE),], 10)
```

	id	name	state	party	x	y	degree	closeness	betweenness	quotient	clust
53	53	Amy Klobuchar	MN	D	-94.17185	46.52615	56	0.006756757	228.46469	4.079727	2
88	88	Tina Smith	MN	D	-95.26519	48.27262	52	0.006666667	162.18280	3.118900	2
19	19	Susan Collins	ME	R	-69.57167	44.51100	51	0.006666667	132.81845	2.604283	3
6	6	Richard Blumenthal	CT	D	-72.34624	41.55773	50	0.006535948	123.27626	2.465525	2
39	39	Margaret Hassan	NH	D	-71.53721	44.09488	49	0.006578947	102.88327	2.099659	3
98	98	Elizabeth Warren	MA	D	-72.83165	42.32477	47	0.006369427	62.05448	1.320308	2
20	20	Christopher Coons	DE	D	-75.60370	38.39383	46	0.006451613	124.92085	2.715671	3
96	96	Chris Van Hollen	MD	D	-77.52402	39.49261	45	0.006289308	47.78719	1.061938	2
101	101	Ron Wyden	OR	D	-121.97770	43.19769	45	0.006024096	91.53141	2.034031	2
32	32	Dianne Feinstein	CA	D	-121.81547	39.14369	44	0.006172840	60.71637	1.379918	2

Senators with top 10 closeness centrality

```
> head(sg.Senators[order(sg.Senators$closeness, decreasing = TRUE),], 10)
```

id	name	state	party	x	y	degree	closeness	betweenness	quotient	clust
53 53	Amy Klobuchar	MN	D	-94.17185	46.52615	56	0.006756757	228.46469	4.079727	2
19 19	Susan Collins	ME	R	-69.57167	44.51100	51	0.006666667	132.81845	2.604283	3
88 88	Tina Smith	MN	D	-95.26519	48.27262	52	0.006666667	162.18280	3.118900	2
39 39	Margaret Hassan	NH	D	-71.53721	44.09488	49	0.006578947	102.88327	2.099659	3
6 6	Richard Blumenthal	CT	D	-72.34624	41.55773	50	0.006535948	123.27626	2.465525	2
20 20	Christopher Coons	DE	D	-75.60370	38.39383	46	0.006451613	124.92085	2.715671	3
48 48	Doug Jones	AL	D	-85.88179	33.44027	42	0.006410256	103.28284	2.459115	1
98 98	Elizabeth Warren	MA	D	-72.83165	42.32477	47	0.006369427	62.05448	1.320308	2
78 78	Marco Rubio	FL	R	-81.10930	26.98167	41	0.006329114	325.48986	7.938777	1
96 96	Chris Van hollen	MD	D	-77.52402	39.49261	45	0.006289308	47.78719	1.061938	2

```
> |
```

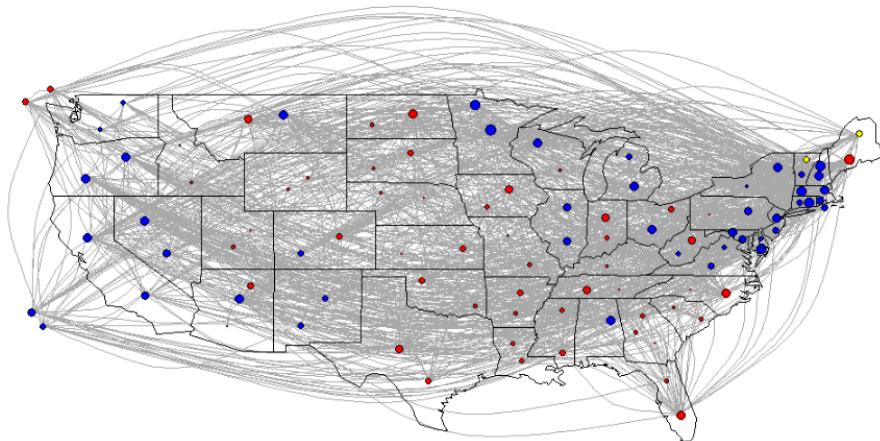
Senators with top 10 betweenness

```
> head(sg.Senators[order(sg.Senators$betweenness, decreasing = TRUE),], 10)
```

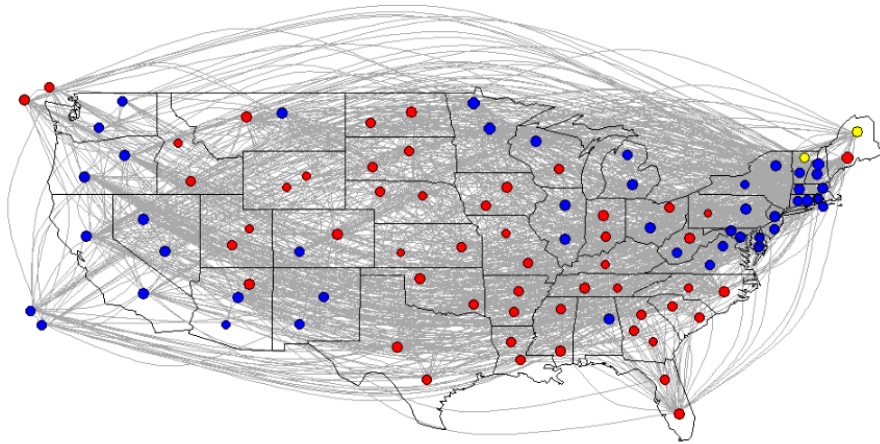
id	name	state	party	x	y	degree	closeness	betweenness	quotient	clust
78 78	Marco Rubio	FL	R	-81.10930	26.98167	41	0.006329114	325.4899	7.938777	1
53 53	Amy Klobuchar	MN	D	-94.17185	46.52615	56	0.006756757	228.4647	4.079727	2
5 5	Marsha Blackburn	TN	R	-87.60523	35.56603	34	0.006097561	225.7828	6.640671	1
24 24	Kevin Cramer	ND	R	-99.51486	47.63509	39	0.006250000	194.0737	4.976248	1
10 10	Mike Braun	IN	R	-86.30604	40.52763	33	0.005988024	169.7993	5.145432	1
88 88	Tina Smith	MN	D	-95.26519	48.27262	52	0.006666667	162.1828	3.118900	2
27 27	Steve Daines	MT	R	-110.84405	47.28107	36	0.006134969	157.3378	4.370494	1
31 31	Joni Ernst	IA	R	-92.92207	42.46009	37	0.006172840	156.4261	4.227732	1
93 93	Thomas Tillis	NC	R	-77.98822	35.32976	38	0.006250000	145.6314	3.832404	1
87 87	Kyrsten Sinema	AZ	D	-111.41824	34.94484	39	0.006250000	143.5341	3.680361	1

```
.. |
```

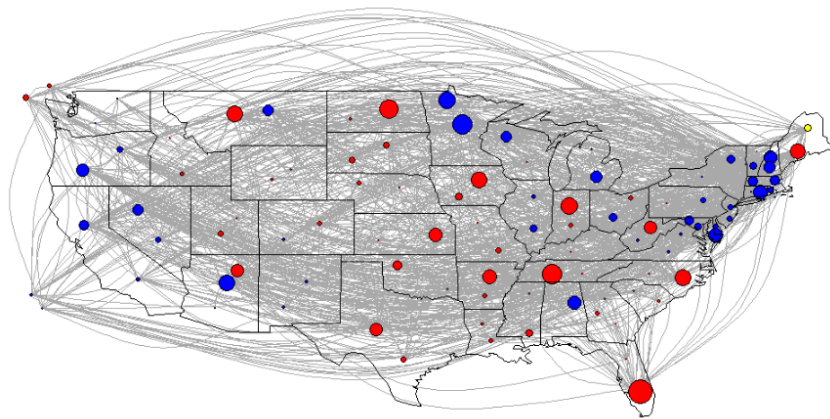
Map of degree of centrality (larger circle = higher degree of centrality)



Map of closeness centrality (larger circle = larger closeness centrality)



Map of betweenness (larger circle = higher betweenness)



Takeaways:

- Amy Klobuchar is either #1 or #2 in all the centrality measures. She is often seen as a moderate Democrat. Given the Democrats had the minority, adding Sen. Klobuchar to many of these bills might have been a political strategy to get the Republicans to the bargaining table. My guess is they are more apt to listen to her vs. someone who is more liberal.
- For degree of centrality and closeness, most of the top senators in the list are Democratic. Not unexpected given what we said earlier about Democrats likely needing to band together for support given they had a minority senate position.
- However, for betweenness we see many more Republicans show up on the list. And surprisingly the senator with the highest betweenness score is Marco Rubio – a Republican. Much like Sen. Klobuchar, Sen. Rubio is seen more as a centrist and likely worked more closely with Democrats than his Republican colleagues were willing to do.
- Lastly, the betweenness chart shows how betweenness differs between senators in a specific state. States typically have a senior and junior senator. So likely the more senior senator - who has been in the senate longer – has a higher betweenness score.

PROBLEM 1E

```
# calculate quotient of betweenness centrality divided by degree of centrality
sg.Senators$quotient <- sg.Senators$betweenness / sg.Senators$degree

# Senators with top 10 betweenness divided by closeness
head(sg.Senators[order(sg.Senators$quotient, decreasing = TRUE),], 10)
```

```
> head(sg.Senators[order(sg.Senators$quotient, decreasing = TRUE),], 10)
  id      name state party      x      y degree  closeness betweenness quotient
78 78   Marco Rubio  FL    R -81.10930 26.98167   41 0.006329114   325.4899  7.938777
5  5  Marsha Blackburn TN    R -87.60523 35.56603   34 0.006097561   225.7828  6.640671
64 64   Jerry Moran  KS    R -96.05998 38.44235   18 0.005434783   101.6930  5.649612
23 23   Tom Cotton  AR    R -92.14113 35.42359   21 0.005263158   116.5119  5.548184
10 10   Mike Braun  IN    R -86.30604 40.52763   33 0.005988024   169.7993  5.145432
24 24   Kevin Cramer ND    R -99.51486 47.63509   39 0.006250000   194.0737  4.976248
27 27   Steve Daines MT    R -110.84405 47.28107   36 0.006134969   157.3378  4.370494
31 31    Joni Ernst  IA    R -92.92207 42.46009   37 0.006172840   156.4261  4.227732
53 53   Amy Klobuchar MN    D -94.17185 46.52615   56 0.006756757   228.4647  4.079727
93 93   Thomas Tillis NC    R -77.98822 35.32976   38 0.006250000   145.6314  3.832404
> |
```

This metric normalizes the betweenness centrality by the number of people the senator is connected with (e.g., the degree of centrality). Someone might have a high betweenness simply because they are connected to a lot of people – perhaps because they have been in the senate a long time. However, we want to identify the right balance of betweenness and degree of centrality. In other words, we want to identify the people that still have a high betweenness i.e., a lot of shortest paths flow through them, but don't rely on just knowing a lot of people. We might use this metric to identify the “arbitrators” in Congress i.e., the people that are being put to work to try to work across the aisle to get things accomplished. Or perhaps the “power brokers” because info flows through them and they are heavily connected to others.

PROBLEM 1F

```
# create communities
set.seed(173)
community = cluster_spinglass(sg, spins = 100, weights = E(sg)$n)
head(community)

# get community information
clust = community$membership #extract community assignments
table(clust)
> table(clust)
clust
 1  2  3  4  5
48 31 18  1  2
```

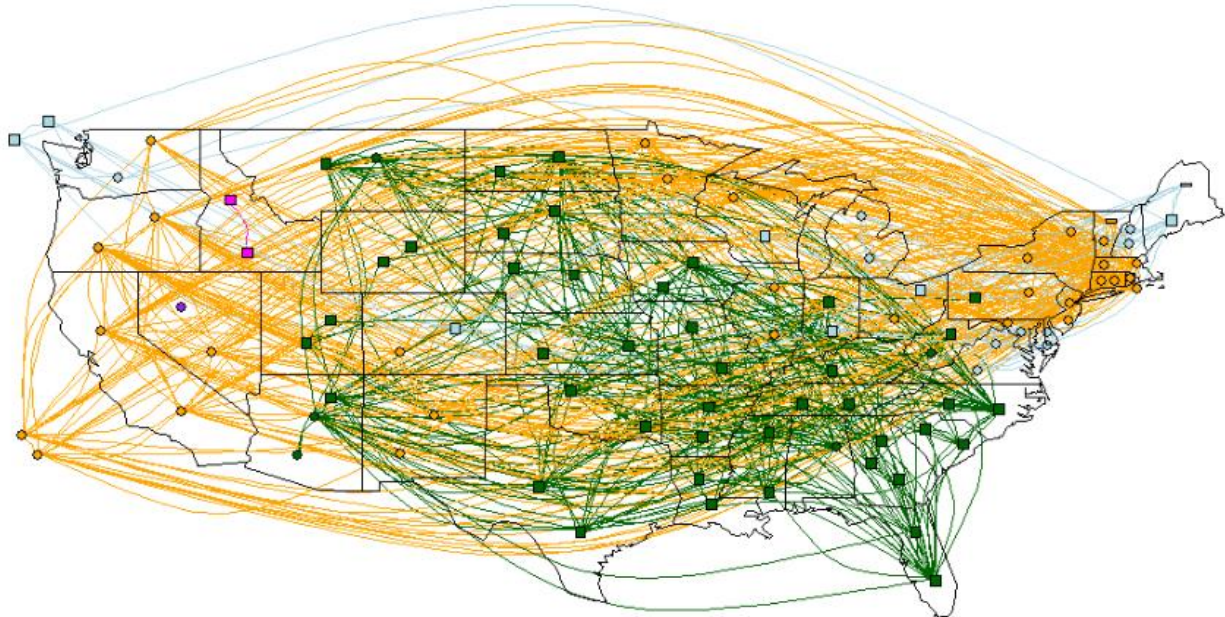
We find a total of 5 communities. In community 1 there are 48 members, in community 2 there are 31 members, in community 3 there are 18 members, in community 4 there is 1 members, and community 5 has 2 members.

```
> community$modularity
[1] 0.03623698
```

Calculating the community modularity, we get a value of 0.03623698.

PROBLEM 1G

```
# Plot
plot(sg,
  vertex.size = 50, # you can modify this so that the points are visible
  vertex.label=NA, # don't plot the Senator's names next to each vertex
  vertex.shape=recode(V(sg)$party,"R"="square","D"="circle", "I"="rectangle"), # assign vertex shapes by party
  vertex.color=clrs[sg.Senators$clust], # assign vertex color by community
  edge.lty = ifelse(E(sg)$c1 == E(sg)$c2, "solid", "blank"), # only show edges within the same community
  edge.color = clrs[E(sg)$c1], # edge color by community
  edge.curved = TRUE, # make the edges curved
  layout = cbind(V(sg)$x,V(sg)$y), # plot each Senator in their state
  rescale=FALSE, # fix the plot axes to the co-ordinate scale
  xlim = range(senators$x), ylim = range(senators$y) # fix the upper/lower bounds of the plot
)
maps::map("state", add=TRUE, col="black") # add a map of the US states
```



PROBLEM 1H

The below table shows the number from each party in each community:

```
> table(sg.Senators$party, clust)
      clust
      1  2  3  4  5
D  5 30 10  1  0
I  0  1  1  0  0
R 43  0  7  0  2
```

PROBLEM 1I

Looking at the below table, we find the following states have senators in different communities:

- Colorado
- Indiana
- Maryland
- Nevada
- Ohio
- Pennsylvania
- Washington
- Wisconsin

So in total, there are 8 out of 50 states with senators in different communities.

```
> table(sg.Senators$state, clust)
      clust
      1 2 3 4 5
AK 0 0 2 0 0
AL 1 0 0 0 0
AR 2 0 0 0 0
AZ 3 0 0 0 0
CA 0 2 0 0 0
CO 0 1 1 0 0
CT 0 2 0 0 0
DE 0 0 2 0 0
FL 2 0 0 0 0
GA 3 0 0 0 0
HI 0 2 0 0 0
IA 2 0 0 0 0
ID 0 0 0 0 2
IL 0 2 0 0 0
IN 1 0 1 0 0
KS 2 0 0 0 0
KY 1 0 0 0 0
LA 2 0 0 0 0
MA 0 2 0 0 0
MD 0 1 1 0 0
ME 0 0 2 0 0
MI 0 0 2 0 0
MN 0 2 0 0 0
MO 2 0 0 0 0
MS 2 0 0 0 0
MT 2 0 0 0 0
NC 2 0 0 0 0
ND 2 0 0 0 0
NE 2 0 0 0 0
NH 0 0 2 0 0
NJ 0 2 0 0 0
NM 0 2 0 0 0
NV 0 1 0 1 0
NY 0 2 0 0 0
OH 0 1 1 0 0
OK 2 0 0 0 0
OR 0 2 0 0 0
PA 1 1 0 0 0
RI 0 2 0 0 0
SC 2 0 0 0 0
SD 2 0 0 0 0
TN 2 0 0 0 0
TX 2 0 0 0 0
UT 2 0 0 0 0
VA 0 0 2 0 0
VT 0 2 0 0 0
WA 0 1 1 0 0
WI 0 1 1 0 0
WV 2 0 0 0 0
WY 2 0 0 0 0
```


PROBLEM 1J

Cluster 1 is largely Republican. Based on the chart from problem 1G we find that most of the cluster 1 senators are located in the central and southern parts of the country. This is no surprise given this is where most of the Republican senators are coming from anyway. In cluster 1 we see that the 5 Democrats come from states that have a Republican senator including Arizona, West Virginia, Alabama, and Wyoming. This might suggest that although the senator might have a different party affiliation (Democrat), in practice they might be more likely to co-sponsor bills coming from the Republican party given pressure from either their fellow senator or from the will of the people of their state.

Cluster 2 falls along similar party lines. We see cluster 2 pops up in the northeast and west coast, areas that are Democrat strongholds. Unsurprisingly there are no Republicans in this cluster, suggesting this group might be a strongly Democratic agenda which is unlikely to attract co-sponsorship from Republicans.

Interestingly, of the 8 states that have senators in different clusters there is only 1 state – Pennsylvania – where one senator is in cluster 1 and the other in cluster 2. This again suggests strong policy differences between cluster 1 and 2 (driven by specific policy support by voters).

Cluster 3 is interesting because it has a more equal split between Democrats and Republicans. This is interesting because these clusters appear in some of the typical presidential election swing states e.g., Ohio, Michigan, and Virginia. What this might suggest is the ideology of cluster 3 is more moderate or centrist and includes senators that are more likely to work with and consider the other side.

Cluster 4 is one Democrat in Nevada. Perhaps this person is very new or they have very unique politics that they are unlikely to be similar to any other senator clusters.

Lastly Cluster 5 includes the 2 Republican senators from Idaho. Similar to cluster 4, these senators might have a lot in common with each other, but less with the broader Republican party. Some of this might be due to geography and them being disconnected from the core of the Republican base in midwestern and southern America.