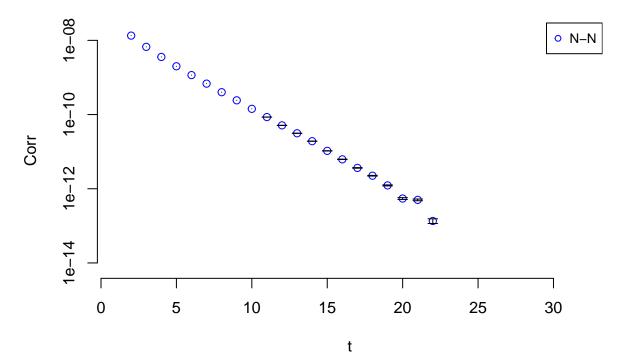
# NJN-Korrelatoren

## Timo Beilschmidt November 15, 2019

#### **NN-Correlator**

```
## [1] "N-N, T=64, n_src=16, n_conf=52, Gi = Gi_Cg5gt, Gf = Gf_Cg5gt"
  [1] "Symmetrized:"
   [1] -5.263089e-09 1.342494e-08 6.680684e-09 3.574597e-09
                                                               2.002010e-09
   [6]
        1.157457e-09 6.816264e-10 4.004103e-10
                                                  2.418247e-10
                                                               1.425746e-10
        8.548801e-11 5.111694e-11 3.129150e-11
                                                  1.914125e-11
                                                                1.050606e-11
##
  [11]
        6.204907e-12 3.646169e-12 2.245112e-12 1.230222e-12
##
  [16]
                                                               5.450018e-13
  [21]
        5.014849e-13 1.352102e-13 -3.329118e-16 -8.137589e-14 -1.173848e-13
  [26] -9.507969e-14 -2.576958e-14 -1.025189e-13 -8.087892e-14 -4.376005e-14
  [31] -5.800247e-14 -9.127010e-15 -1.293427e-14 -1.555794e-14 -3.269643e-14
  [36] -6.208327e-14 -4.456083e-14 6.916324e-15 3.105809e-14 -2.326185e-14
## [41]
        2.065029e-14 3.709208e-14 3.454967e-14 -2.500308e-14 -7.657407e-14
## [46] -1.471450e-13 -1.812902e-13 -1.841362e-13 -8.442682e-14 -3.191316e-13
  [51] -1.709732e-13 3.922412e-13
                                   4.970998e-13
                                                  1.484360e-12
##
  [56]
        6.871682e-12 1.475798e-11 2.921650e-11
                                                  6.409887e-11
                                                               1.428875e-10
## [61]
        3.422838e-10 8.992334e-10 2.557055e-09 1.634944e-08
```

### **N-N Correlator**

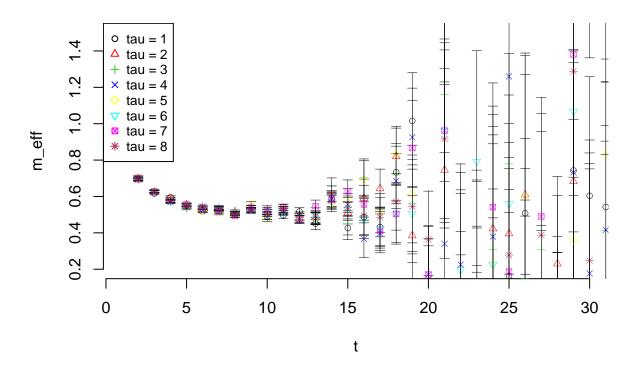


### Effective Mass

We calculate the effective mass following https://arxiv.org/abs/1612.06963.

$$m^{eff}(t,\tau) = \frac{1}{\tau} ln\left(\frac{C(t)}{C(t+\tau)}\right) \rightarrow_{t\to\infty} \frac{1}{\tau} ln(e^{E_0\tau}) = E_0$$

# N-N Correlator effective mass

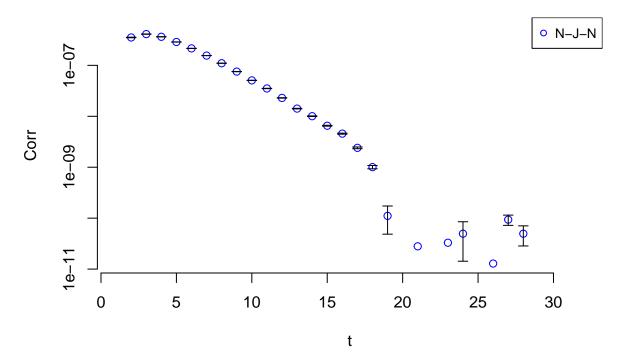


#### **NJN-Correlator**

First the 3pt-function correlator:

```
## [1] "N-J-N, T=64, n_src=16, n_conf=52, Gi = Gi_Cg5gt, Gf = Gf_Cg5gt"
## [1] "Symmetrized:"
   [1] -1.878429e-07 3.527035e-07 4.105506e-07 3.634870e-07 2.875087e-07
        2.152937e-07 1.555487e-07
                                    1.100326e-07
                                                  7.542379e-08 5.068947e-08
   [6]
## [11]
        3.514744e-08
                     2.293536e-08
                                    1.415576e-08
                                                  1.003578e-08
                                                                6.525015e-09
## [16]
        4.562794e-09 2.402439e-09 1.005561e-09
                                                 1.108351e-10 -3.512737e-11
## [21]
        2.797372 e-11 \ -2.930776 e-10 \ \ 3.292029 e-11 \ \ 4.961927 e-11 \ \ -5.054414 e-11
        1.285237e-11 9.344241e-11 4.954832e-11 -2.731457e-11 -6.977694e-11
## [26]
## [31] -1.114514e-10 -1.367227e-10 -9.908533e-11 -1.173011e-10 -1.574097e-10
## [36] -4.459261e-11 3.899846e-11 -1.630353e-10 -1.652079e-10 -6.671210e-11
## [41] -6.780158e-11 -1.524821e-10 2.969911e-10 3.853345e-10
                                                                4.140481e-10
        4.073492e-10 1.069840e-10 7.835085e-10
                                                  4.305285e-10
## [46]
                                                                5.941536e-10
## [51]
        3.654188e-10 7.466623e-10 8.873875e-10
                                                  2.209112e-09
                                                                2.990080e-09
## [56]
        5.460322e-09 1.097093e-08 1.836923e-08 3.199812e-08
                                                                5.958482e-08
## [61]
        1.080306e-07 1.975960e-07 3.818178e-07 5.637172e-07
```

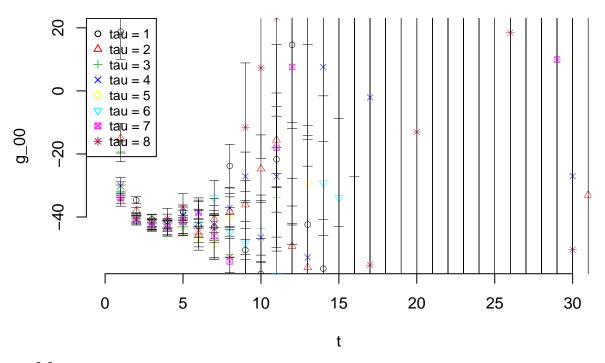
# 3pt-function Correlator



#### Ratio-Plot

$$\left. \frac{\partial m_{\lambda}^{eff}(t,\tau)}{\partial \lambda} \right|_{\lambda=0} = \frac{1}{\tau} \left( \frac{\partial_{\lambda} C_{\lambda}(t)}{C(t)} - \frac{\partial_{\lambda} C_{\lambda}(t+\tau)}{C(t+\tau)} \right)_{\lambda=0}$$

### N-J-N linear response of effective mass to external bilinear current



```
[1] "tau = 1"
##
##
    [1]
              18.80974
                            -34.65756
                                           -40.76115
                                                          -41.21405
                                                                         -38.42931
    [6]
            -42.92478
                                           -23.78204
                                                          -50.46930
                                                                         -58.06235
##
                            -43.12660
   [11]
            -21.69523
                             14.63249
                                           -42.38689
                                                          -56.38159
                                                                        -157.62016
##
                                           240.29800
##
   [16]
           -192.69994
                            370.37823
                                                          311.28926
                                                                       -1126.76216
##
   [21]
            231.96654
                       -352805.34934
                                       363550.75463
                                                        -9524.63212
                                                                        5340.13207
         -11431.48250
   [26]
                         13205.05278
                                         -7634.02347
                                                         7075.69906
                                                                      -13290.52968
          62343.20413
                        -46277.88803
                                                     -105783.39341
##
   [31]
                                         81785.10144
                                                                       11408.57520
                                                                       11322.56078
   [36]
           1448.90143
                         16681.82212
                                       -11373.83695
                                                        -9638.59473
##
  [41]
          77618.99002
                        -75704.79971
                                         -2698.29355
                                                        -1107.40099
                                                                        4683.07539
                                                                      -18793.40924
          -7938.09858
                          3572.23405
## [46]
                                           562.33139
                                                        -2164.03272
##
  [51]
          15230.80233
                            527.09394
                                          -592.66149
                                                          310.42571
                                                                          23.63231
   [56]
              41.22222
                            217.22439
                                            80.53689
                                                          119.90330
                                                                         103.43813
##
   [61]
              99.37799
                            81.29831
                                           116.17381
##
   [1] "tau = 2"
##
           -15.00614
    [1]
                         -38.03306
                                       -42.84110
                                                     -43.28637
                                                                   -41.34914
##
##
    [6]
           -45.49935
                         -40.63432
                                       -38.26841
                                                     -36.10133
                                                                   -24.68327
## [11]
           -15.54973
                         -49.31300
                                       -55.98732
                                                     -123.04259
                                                                   -78.39246
  [16]
                          44.62178
            180.68343
                                       -66.66956
                                                      35.80034
                                                                  -371.17219
##
   [21]
         -5823.59851
                        -896.82960
##
                                      3336.63172
                                                     1586.76097
                                                                  4063.14514
                                                    -389.45216
   [26]
            55.73850
                       -1430.09117
                                      -985.83329
                                                                   -88.32955
##
##
   [31]
           -33.05842
                         833.38629
                                       463.84785
                                                     179.15588
                                                                 -5174.97284
   [36]
          4719.04341
                        9721.27984 -20179.85663
                                                   -3357.19290
                                                                 16147.95944
##
   [41]
         -1818.96363
                       25252.27520
                                      3099.65774 -24434.72957
                                                                 -1359.52359
## [46]
          -583.35017
                        -602.97902
                                      2455.89365
                                                   -8093.51694
                                                                 -4127.80097
```

```
## [51]
          7015.03122
                       -151.72202
                                      208.59591
                                                    464.57574
                                                                  33.45331
##
   Г56]
            68.24953
                        182.68442
                                      125.29665
                                                     64.85764
                                                                  83.77362
            79.26487
  [61]
                         90.01813
                                             NΑ
  [1] "tau = 3"
##
##
    [1] -1.917709e+01 -3.956935e+01 -4.193581e+01 -4.238954e+01 -4.315320e+01
    [6] -3.768820e+01 -4.382127e+01 -5.186506e+01 -6.119044e+01 -4.354238e+01
##
  [11] -3.382166e+01 -6.592442e+01 -1.496321e+02 -9.144351e+01 2.813730e+01
         9.729135e+01 3.661069e+02 3.734224e+02 8.539743e+02 -1.042469e+03
  [16]
##
  [21]
         1.787680e+06 -8.797288e+02 7.615548e+02 -1.787857e+06
                                                                   7.753959e+01
  [26] -1.507150e+02 -7.275708e+02 -6.043354e+02 -1.199145e+03
                                                                  1.236397e+04
  [31]
        4.419629e+04 -3.854730e+02 -1.250759e+04 -4.329259e+04 2.331382e+03
         1.810647e+00 2.283178e+03 -9.074021e+02 -3.455240e+02 -2.765148e+04
  [36]
  [41] -3.932747e+03 3.876759e+03 2.686051e+04 5.772883e+03 3.782773e+03
## [46] -6.270332e+02 -5.831184e+02 -5.011664e+03 -1.609937e+03 -1.459922e+03
## [51] -1.818705e+03 2.943801e+02 4.529363e+02 1.074589e+02 9.526434e+01
   [56]
         7.319487e+01
                       1.464081e+02 1.115453e+02 9.815914e+01 8.425169e+01
##
  [61]
        9.551793e+01
                                  NA
  [1] "tau = 4"
                                     -41.952610
##
    [1]
          -30.069425
                        -40.790959
                                                  -42.553890
                                                                -39.274074
##
    [6]
          -38.358154
                        -42.412326
                                     -37.074398
                                                   -27.064134
                                                                -46.475653
## [11]
          -27.198723
                       -68.792722
                                     -52.826259
                                                    7.595774
                                                                152.948642
## [16]
          196.785248
                        -2.070160
                                     372.323281 -4481.234004
                                                               -933.453026
                      -455.083008
                                                 1209.071748
## [21]
         -415.020310
                                    4260.445016
                                                                479.881656
##
  [26]
         -218.216405
                       124.368149
                                    -941.279730
                                                 2010.448623
                                                                -27.026438
##
  [31] -1011.142734
                       1216.174491 -1389.340444 -2405.872280
                                                               4461.597711
  [36] -6329.481443
                        327.298128
                                    3304.553353 -3257.378788
                                                               5589.445493
        -347.416976
                                    -224.113195
                                                  800.689714
                                                               -218.510648
##
  [41]
                       835.654364
##
  [46] -1233.720207
                       -118.845383
                                    -872.166748
                                                  -75.325067
                                                               -168.846142
## [51]
           60.735909
                                                  -29.800026
                        61.958005
                                    -405.478758
                                                                 37.021076
## [56]
           72.181079
                        112.802331
                                      93.869910
                                                    84.877338
                                                                 97.257675
## [61]
##
  [1] "tau = 5"
##
    [1]
           -30.97276
                        -40.42899
                                      -42.11239
                                                    -43.43241
                                                                 -42.99048
                        -48.34375
##
    [6]
           -46.82849
                                      -40.18162
                                                    -61.24645
                                                                 -70.31021
##
   [11]
           -87.27715
                         -68.37181
                                      -29.27630
                                                     61.87347
                                                                 213.78650
                      -1931.50159
  Γ167
##
           384.47312
                                    -1216.42889
                                                  -148.69078
                                                                 562.25530
## [21]
          1450.73917
                       -7611.08579
                                     1459.38690
                                                    569.21201
                                                                  29.42525
## [26]
         -1171.81749
                       8582.86188
                                      294.81979
                                                   -325.09485
                                                                -852.17042
  [31]
          -530.63893
                        1366.22129
                                     -739.45967
                                                   -148.71824 -48935.90044
##
## [36]
          1365.55588
                        902.88844
                                    -1454.02326
                                                  -687.96765
                                                               56096.77455
##
  [41]
          -886.15434
                        -567.78347
                                     2047.85581
                                                   1783.61518
                                                               -6407.68472
  [46]
                        -916.38477
                                    -1607.30675
                                                  -1449.42673
##
           955.46954
                                                                -765.15370
##
  ſ51]
         -1578.01871
                        184.89438
                                     1210.21723
                                                    375.12631
                                                                 118.39769
##
  [56]
           118.31892
                        109.79236
                                      100.06805
                                                    88.52137
                                                                        NA
## [1] "tau = 6"
                                      -42.44337
                                                                 -42.77935
##
    [1]
           -31.83053
                        -40.82455
                                                    -43.62864
           -42.19431
##
   [6]
                        -33.92960
                                      -44.95731
                                                    -48.29969
                                                                 -79.35579
## [11]
           -58.55973
                          25.32961
                                       50.36697
                                                    -29.22481
                                                                 -33.94547
## [16]
           118.67399
                        -357.93481
                                     -677.62771
                                                    68.58495
                                                               16593.69738
## [21]
           928.30957
                        1566.25198
                                      302.45434
                                                    138.00198
                                                                -832.00204
## [26]
        -15703.76046
                       17221.19966
                                       86.88903
                                                 -1009.08853
                                                                 537.39376
## [31]
           881.09814
                       -4738.25530
                                     4107.00734
                                                   1544.54822
                                                                 982.67562
                       -252.31022
## [36]
           175.48718
                                     4555.13325 -22053.80141
                                                               -3004.86437
## [41]
           133.48905
                          66.86378
                                     -279.47036
                                                  -541.55482
                                                                -153.05948
```

```
## [46]
           271.20853
                        156.55724
                                     -409.28028
                                                   282.62596
                                                                -225.06781
                       -545.91422
## [51]
           -72.05068
                                     -163.42761
                                                   151.92405
                                                                 103.47143
           143.68601
## [56]
                        132.51609
                                      96.49702
                                                           NA
## [1] "tau = 7"
##
    [1]
          -33.933118
                       -41.019212
                                     -42.432698
                                                  -43.239281
                                                                -41.559387
##
   [6]
          -38.746146
                       -45.985632
                                     -54.115440
                                                  -62.554538
                                                                -75.496853
## [11]
          -18.071123
                         7.575153
                                     24.495145
                                                   30.646830
                                                                187.030088
         -301.323371
## [16]
                      1053.876505
                                      52.137852
                                                  278.451767 -1070.528744
                                                 -947.669384 -1186.237383
## [21]
          308.421813
                       -76.100388
                                    -157.423109
## [26]
                                    -653.401006
         -839.898419
                       602.380476
                                                    9.935791
                                                                833.535303
## [31]
          741.384979
                      1840.809010 -1181.832910
                                                  758.856936
                                                                550.911697
## [36]
         -365.892378 -4701.043858
                                    -419.052147
                                                 -431.934687
                                                               1787.848460
## [41]
          198.046774
                      1010.243065
                                     641.973516
                                                5095.447810
                                                               -551.448631
                      -202.014380
## [46]
         -340.689231
                                    -572.991317 -1272.040649
                                                               -407.984398
## [51]
         -748.045020
                       178.425274
                                      83.410473
                                                  167.167624
                                                                 93.041784
## [56]
           81.987360
                        99.745815
                                             NA
## [1] "tau = 8"
   [1]
          -34.588282
                       -40.665552
                                     -41.493998
                                                  -40.467393
                                                                -36.819929
          -43.587638
                       -43.758462
                                     -52.677043
                                                  -11.542140
                                                                 7.288447
##
   [6]
## [11]
           23.284274
                        43.483145
                                      71.205772
                                                  213.282801
                                                                135.389731
## [16]
        9320.282634
                       -55.231285
                                     -65.746065
                                                  201.809654
                                                                -13.036351
## [21]
         -473.290263
                      -404.765880
                                    -256.150697 -9580.259496 -3418.478446
                                                                -50.340198
## [26]
           18.459492
                      -251.504327
                                     781.630542
                                                  848.546422
## [31]
         1488.677397
                       128.367751
                                    3370.611391
                                                 -545.640874
                                                               3054.635784
                                                                809.476423
## [36]
         -273.152490 -1240.919639
                                    -540.270120 -1360.477268
## [41]
          290.385524 -5824.365890 -3117.991981
                                                 -598.857002
                                                                715.743570
## [46]
          709.926451
                       -74.433835
                                    -689.860290
                                                 -250.362949
                                                               6353.137943
## [51]
           71.340868
                        59.662926
                                      92.369692
                                                  110.546804
                                                                119.991352
## [56]
           95.260590
                                NA
```