

# NJN-Korrelatoren

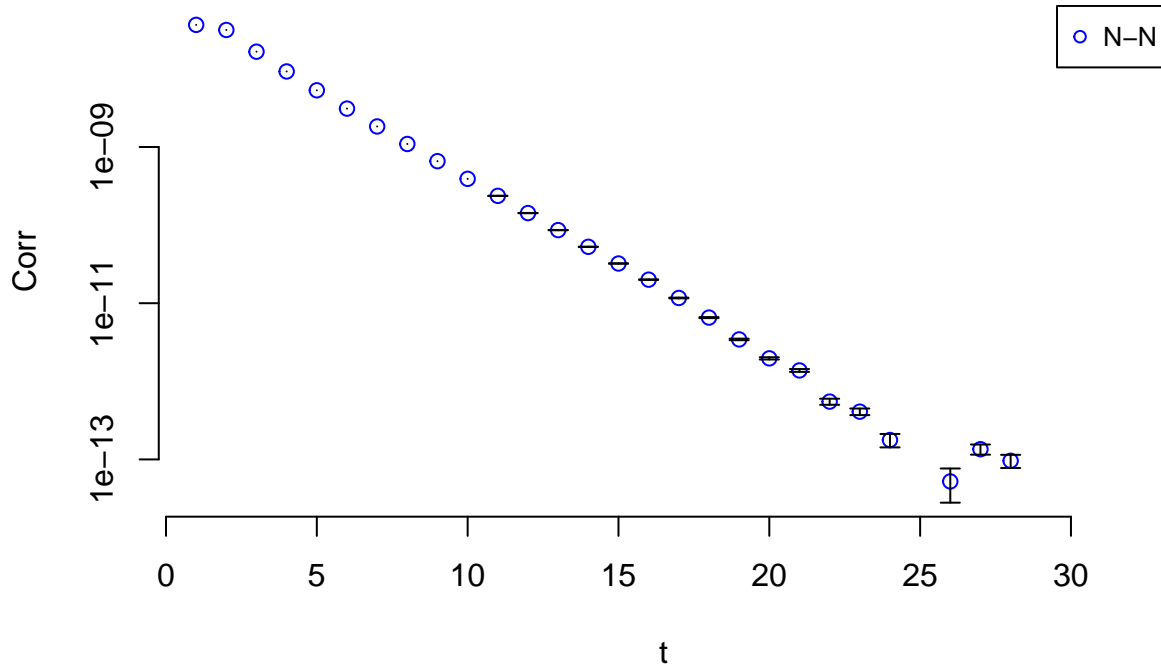
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*November 15, 2019*

## NN-Correlator

```
## [1] "N-N, T=64, n_src=16, n_conf=52, Gi = Gi_Cg5, Gf = Gf_Cg5"
## [1] "Symmetrized:"
## [1] 3.659473e-08 3.149733e-08 1.660153e-08 9.268001e-09 5.316160e-09
## [6] 3.101836e-09 1.831759e-09 1.092908e-09 6.583152e-10 3.909847e-10
## [11] 2.369275e-10 1.425725e-10 8.624975e-11 5.272966e-11 3.223009e-11
## [16] 2.002283e-11 1.167318e-11 6.543200e-12 3.439132e-12 1.966912e-12
## [21] 1.378407e-12 5.498324e-13 4.088967e-13 1.771753e-13 -1.892277e-14
## [26] 5.223083e-14 1.351647e-13 9.605017e-14 -1.377050e-14 -6.748304e-14
## [31] -7.954334e-14 -8.761381e-14 -4.839580e-14 -5.226023e-14 -9.212550e-14
## [36] -1.329026e-14 4.382036e-14 -1.137539e-13 -1.194977e-13 -4.793475e-14
## [41] -6.502525e-14 -1.700127e-13 1.841084e-13 3.144864e-13 4.419252e-13
## [46] 4.730956e-13 3.230008e-14 8.966850e-13 9.333902e-13 1.226868e-12
## [51] 1.482529e-12 2.868467e-12 4.655678e-12 8.402386e-12 1.545104e-11
## [56] 3.099444e-11 6.509481e-11 1.302679e-10 2.704009e-10 5.785913e-10
## [61] 1.275388e-09 2.959821e-09 7.371161e-09 -1.046501e-08
```

## N-N Correlator

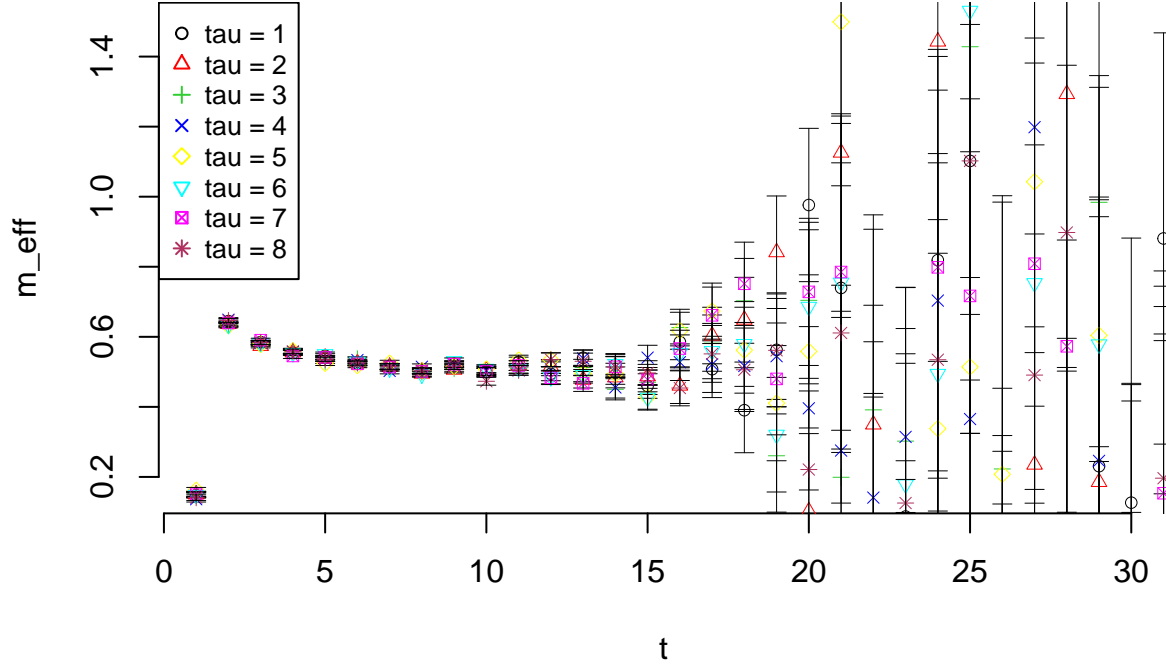


## Effective Mass

We calculate the effective mass following <https://arxiv.org/abs/1612.06963>.

$$m^{eff}(t, \tau) = \frac{1}{\tau} \ln \left( \frac{C(t)}{C(t+\tau)} \right) \rightarrow_{t \rightarrow \infty} \frac{1}{\tau} \ln(e^{E_0 \tau}) = E_0$$

### N-N Correlator effective mass

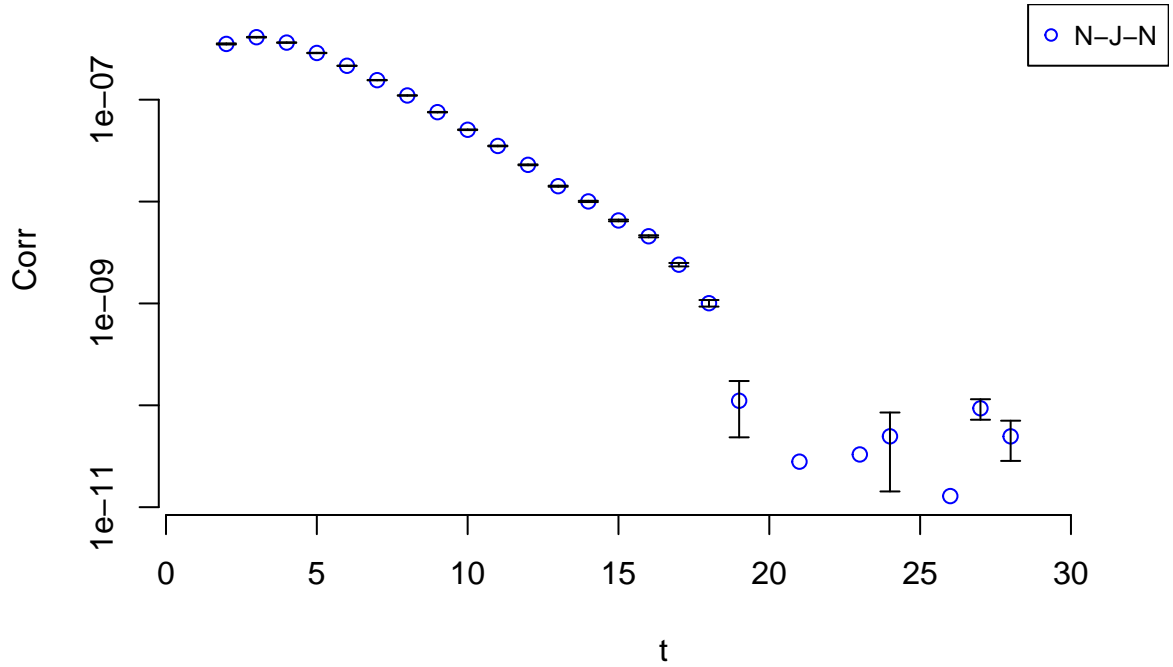


## NJN-Correlator

First the 3pt-function correlator:

```
## [1] "N-J-N, T=64, n_src=16, n_conf=52, Gi = Gi_Cg5, Gf = Gf_Cg5"
## [1] "Symmetrized:"
## [1] -1.878429e-07  3.527035e-07  4.105506e-07  3.634870e-07  2.875087e-07
## [6]  2.152937e-07  1.555487e-07  1.100326e-07  7.542379e-08  5.068947e-08
## [11]  3.514744e-08  2.293536e-08  1.415576e-08  1.003578e-08  6.525015e-09
## [16]  4.562794e-09  2.402439e-09  1.005561e-09  1.108351e-10 -3.512737e-11
## [21]  2.797372e-11 -2.930776e-10  3.292029e-11  4.961927e-11 -5.054414e-11
## [26]  1.285237e-11  9.344241e-11  4.954832e-11 -2.731457e-11 -6.977694e-11
## [31] -1.114514e-10 -1.367227e-10 -9.908533e-11 -1.173011e-10 -1.574097e-10
## [36] -4.459261e-11  3.899846e-11 -1.630353e-10 -1.652079e-10 -6.671210e-11
## [41] -6.780158e-11 -1.524821e-10  2.969911e-10  3.853345e-10  4.140481e-10
## [46]  4.073492e-10  1.069840e-10  7.835085e-10  4.305285e-10  5.941536e-10
## [51]  3.654188e-10  7.466623e-10  8.873875e-10  2.209112e-09  2.990080e-09
## [56]  5.460322e-09  1.097093e-08  1.836923e-08  3.199812e-08  5.958482e-08
## [61]  1.080306e-07  1.975960e-07  3.818178e-07  5.637172e-07
```

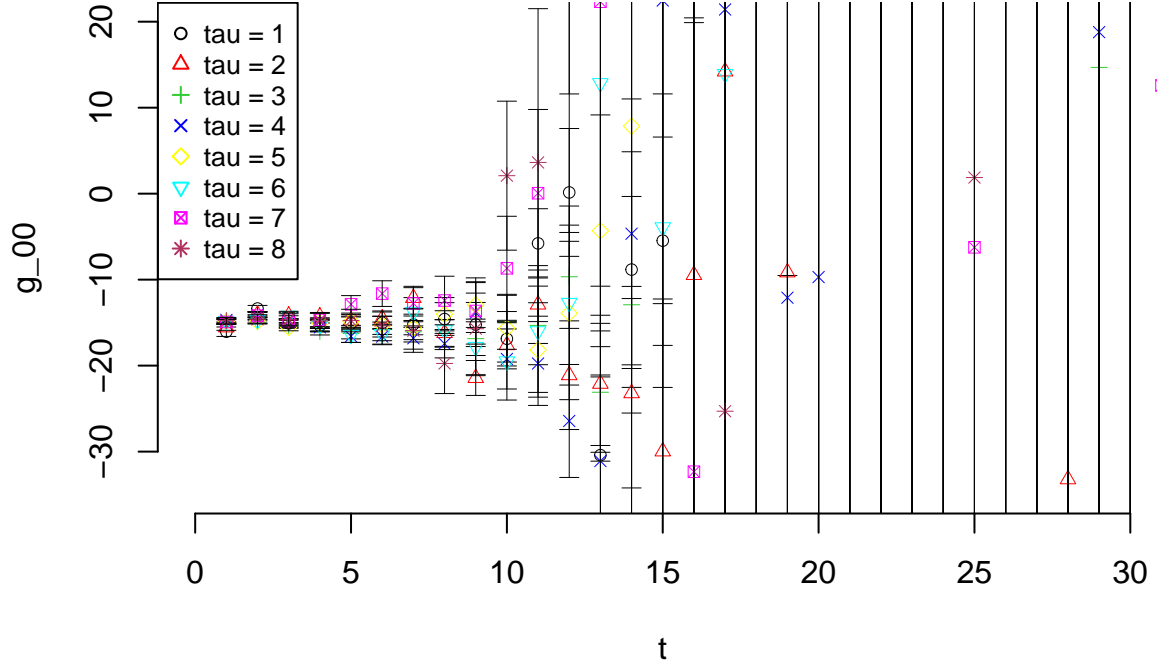
### 3pt-function Correlator



## Ratio-Plot

$$\left. \frac{\partial m_{\lambda}^{eff}(t, \tau)}{\partial \lambda} \right|_{\lambda=0} = \frac{1}{\tau} \left( \frac{\partial_{\lambda} C_{\lambda}(t)}{C(t)} - \frac{\partial_{\lambda} C_{\lambda}(t+\tau)}{C(t+\tau)} \right)_{\lambda=0}$$

## N-J-N linear response of effective mass to external bilinear current



##	[1]	"tau = 1"			
##	[1]	-16.056576	-13.358650	-15.089688	-15.346603
##	[6]	-15.025688	-15.214502	-14.582470	-15.218748
##	[11]	-5.780408	0.141904	-30.410069	-8.829371
##	[16]	72.554325	74.250295	257.219322	201.816875
##	[21]	2572.314932	-2703.342701	-593.038493	-239.040762
##	[26]	-1465.329591	1713.675808	2959.224367	-431.693537
##	[31]	-658.962272	-303.175429	316.492952	-59.245807
##	[36]	-1845.019902	2063.232904	166.823864	-1087.801410
##	[41]	-231.847449	-1048.023195	243.350970	1098.138457
##	[46]	618.687494	-633.860354	416.475439	98.500576
##	[51]	-731.095177	19.736188	-138.216913	40.109305
##	[56]	14.854835	44.503824	21.880236	19.923981
##	[61]	18.001724	15.119542	107.073724	NA
##	[1]	"tau = 2"			
##	[1]	-15.553879	-14.072614	-14.186314	-14.291932
##	[6]	-14.529106	-12.133155	-16.211363	-21.435518
##	[11]	-12.895486	-21.114824	-22.110608	-23.213416
##	[16]	-9.461799	14.209576	41.706934	-9.157596
##	[21]	-179.659419	-141.731833	-44.997005	-92.461442
##	[26]	-83.120884	-102.347354	-33.220733	170.098184
##	[31]	-4843.068493	-382.057780	4339.420672	504.326141
##	[36]	630.399067	871.156291	-1613.384567	-2915.130327
##	[41]	-301.082432	-321.845389	395.589022	412.401644
##	[46]	29.225738	541.478195	151.659161	40.430885

```

## [51] 54.213838 34.762027 39.113184 49.748800 13.436000
## [56] 21.899615 20.657584 20.724088 17.426476 16.613729
## [61] 15.554026 61.274529 NA
## [1] "tau = 3"
## [1] -14.795830 -14.498205 -15.318769 -16.012603 -16.254587
## [6] -15.802222 -16.073093 -16.253201 -16.863188 -14.962111
## [11] -15.322694 -9.664639 -23.097214 -12.922705 27.487565
## [16] 65.937016 212.382933 439.117575 391.530850 179.610981
## [21] -1011.329522 -697.655118 -667.911281 352.287125 -657.078616
## [26] -134.878987 -105.086694 389.200801 14.681714 -166.404472
## [31] -98.117119 2.478085 -358.059793 1242.309619 -19.927445
## [36] -238.782943 -881.521555 113.946957 680.412962 -98.916991
## [41] 15.421020 126.249414 132.137894 41.233709 6.636497
## [46] 111.043963 112.766137 236.509220 66.630028 150.708686
## [51] -38.618379 46.828469 -10.507986 53.573893 25.097404
## [56] 31.234346 29.072714 17.981283 16.228809 16.065619
## [61] 45.638364 NA
## [1] "tau = 4"
## [1] -14.689684 -14.101185 -14.861884 -15.545364 -16.586031
## [6] -16.622839 -16.821176 -17.452448 -13.856118 -19.226127
## [11] -19.755414 -26.436842 -31.095085 -4.658673 22.464025
## [16] 24.106528 21.418393 183.307782 -12.099401 -9.703311
## [21] -163.943294 -96.415003 -146.944464 45.334932 62.128138
## [26] -243.934347 -78.637638 -172.534447 18.784325 34.482287
## [31] 132.699256 -36.039394 -133.145163 -193.237456 245.885615
## [36] 81.128753 85.220126 178.357697 473.436324 307.890748
## [41] -488.889332 292.677791 -597.004196 -485.240361 527.386408
## [46] -233.098472 -69.401997 261.109675 85.533704 56.260285
## [51] 33.231793 19.031800 27.172131 45.431408 26.982186
## [56] 9.660724 13.003155 17.668081 14.480847 38.357149
## [61] NA
## [1] "tau = 5"
## [1] -14.890694 -14.854606 -15.544802 -15.048970 -14.844311
## [6] -15.305520 -15.604964 -14.020734 -12.950837 -15.647129
## [11] -18.176712 -13.901829 -4.318902 7.847296 42.697691
## [16] 32.540540 50.068591 -54.841894 -120.653047 -184.618557
## [21] -132.892802 -137.800121 49.467113 -198.867781 -86.864850
## [26] -185.862181 -592.053885 -73.592972 238.473118 -221.040598
## [31] -144.797701 554.020367 -76.267520 -83.500258 302.949829
## [36] 387.447843 174.590353 -50.361380 -3.645275 -7.982934
## [41] -65.538610 -142.825844 86.282415 78.226614 90.765234
## [46] 57.324963 57.567235 97.474533 61.886589 62.543857
## [51] 56.985037 43.826026 29.617557 31.671566 21.625783
## [56] 24.427927 25.655036 20.542711 34.725623 NA
## [1] "tau = 6"
## [1] -14.787221 -14.686631 -14.205881 -15.260224 -16.416988
## [6] -16.344193 -13.738389 -15.876547 -17.822272 -19.506665
## [11] -15.997455 -12.699789 12.857113 33.611018 -3.904951
## [16] 74.157157 13.925343 -46.198763 -15404.067783 -55.506721
## [21] -103.279241 -139.909666 -101.683332 -131.583188 15176.654879
## [26] -168.470474 -213.753266 -153.006304 -126.210802 -51.408254
## [31] -81.695349 -50.251636 13.804417 -127.008238 51.351562
## [36] -105.598986 154.952235 153.158180 289.395408 285.020293
## [41] -376.363925 291.617357 245.177375 132.316457 233.383829

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## [46] 116.685252 575.958507 59.779731 -101.228300 -42.693549
## [51] -209.543968 -40.135497 -16.861602 5.662128 10.331602
## [56] 18.896603 21.119391 34.297977 NA
## [1] "tau = 7"
## [1] -14.92383502 -14.18559540 -14.80294667 -14.68591240 -12.87581553
## [6] -11.62388294 -12.76465069 -12.42710923 -13.64683598 -8.68042793
## [11] 0.05236747 31.27921712 22.32247602 29.74602243 87.24956971
## [16] -32.34007912 -80.54020108 -181.25591575 -136.00805661 -138.13694093
## [21] -137.28187394 -194.11042575 148.26951691 -74.98958441 -6.24004105
## [26] -197.53427178 756.90853021 -231.29532223 -241.90727108 -243.72418672
## [31] 12.58605784 15.28577505 59.72775681 -834.37517712 114.22647294
## [36] 214.22976823 13.08726591 47.54613733 76.20502611 160.24226153
## [41] 117.97185267 179.37700134 72.82813596 97.35099183 76.67295474
## [46] 92.08876042 76.96067025 70.94255619 43.62890373 65.86045165
## [51] 25.93777122 28.79698576 9.68780619 14.39034151 16.57054025
## [56] 19.17975699 30.46006249 NA
## [1] "tau = 8"
## [1] -14.773723 -14.610876 -14.665820 -14.783752 -14.757857
## [6] -15.374473 -15.930440 -19.748567 -15.707208 2.091131
## [11] 3.630497 30.476977 45.654273 79.678897 -2620.310598
## [16] 2297.022111 -25.303704 -150.591412 -62.505438 -1114.141406
## [21] -259.529089 -242.549446 2449.708860 -2304.853335 1.877252
## [26] 89.591274 -425.013906 988.297857 88.983149 118.777559
## [31] 86.337074 -96.649870 -205.039349 102.093577 184.862409
## [36] -45.162255 15.727025 -28.672792 85.099813 14.177703
## [41] 203.275321 -91.341377 258.892029 115.212836 104.220584
## [46] 64.647279 2.054148 96.784400 31.170686 45.489268
## [51] 42.512069 31.856350 15.416019 23.676719 17.279461
## [56] 32.042773 NA

```