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In[212]:= Vac = Flatten[{Solve[THiggs1Mod == 0, mH1][[1]],
    Solve[THiggs2Mod == 0, mH2][[1]],
    Solve[TSingletMod == 0, MS][[1]],
    Solve[TRight3Mod == 0, MN[3, 3]][[1]],
    Solve[TLeft1Mod == 0, ML[1, 1]][[1]],
    Solve[TLeft2Mod == 0, ML[2, 2]][[1]],
    Solve[TLeft3Mod == 0, ML[3, 3]][[1]]}];

In[213]:= TE = Mneut[[Range[1, 7], Range[1, 7]]] /. Vac // Simplify;
TO = Mneut[[Range[8, 14], Range[8, 14]]] /. Vac // Simplify;
TC = Mchar /. Vac // Simplify;

In[216]:= prec = 50;
$MinPrecision = prec;
TeV = 10^12; GeV = 10^9; MeV = 10^6;
vSq = SetPrecision[(174 GeV)^2, prec];
vSqHiggs = vSq -  $\sigma_V[1]^2 - \sigma_V[2]^2 - \sigma_V[3]^2$ ;
mW = SetPrecision[80.403 GeV, prec];
mZ = SetPrecision[91.1876 GeV, prec];
 $\alpha_{ew}$  = SetPrecision[1/127.908957, prec];
 $\theta_w$  = SetPrecision[ArcSin[Sqrt[0.23124]], prec]; mtPole = SetPrecision[180 GeV, prec];
 $\alpha_{strong}$  = SetPrecision[0.102, prec];
mup = SetPrecision[1.5 MeV, prec];
mcharm = SetPrecision[1.1 GeV, prec];
mtop = SetPrecision[mtPole / (1 + 4 *  $\alpha_{strong}$  / (3 Pi)), prec];
mdown = SetPrecision[3 MeV, prec];
mstrange = SetPrecision[60 MeV, prec];
mbottom = SetPrecision[4.1 GeV, prec];
melectron = SetPrecision[0.511 MeV, prec];
mmuon = SetPrecision[105.66 MeV, prec];
mtau = SetPrecision[1.777 GeV, prec];
(*Yup=SetPrecision[mup / v2, prec];
Ycrm=SetPrecision[mcharm / v2, prec];*)
Ytop = SetPrecision[mtop / v2, prec];
(*Ydwn=SetPrecision[mdown / v1, prec];
Ystg=SetPrecision[mstrange / v1, prec];*)
Ybtm = SetPrecision[mbottom / v1, prec];
(*Ye=SetPrecision[melectron / v1, prec];
Y $\mu$ =SetPrecision[mmuon / v1, prec];*)
Y $\tau$  = SetPrecision[mtau / v1, prec];

In[236]:=  $\beta$  = SetPrecision[ArcTan[30], prec];
g1 := SetPrecision[Sqrt[(2 * Tan[ $\theta_w$ ])^2 * mW^2] / vSq], prec];
g2 := SetPrecision[mW * Sqrt[2 / vSq], prec];
v1 = Sqrt[vSqHiggs / (1 + Tan[ $\beta$ ]^2)];
v2 = v1 * Tan[ $\beta$ ];

In[240]:= varA = Union[Variables[TE], Variables[TO]]

Out[240]= {A0, A2, A3,  $\kappa_0$ ,  $\kappa_2$ ,  $\kappa_3$ ,  $\sigma_S$ , A1[1], A1[2], A1[3], ML[1, 2],
    ML[1, 3], ML[2, 3],  $\kappa_1[1]$ ,  $\kappa_1[2]$ ,  $\kappa_1[3]$ ,  $\sigma_n[3]$ ,  $\sigma_V[1]$ ,  $\sigma_V[2]$ ,  $\sigma_V[3]$ }

In[241]:= varB = Complement[Variables[TC], Union[Variables[TE], Variables[TO]]]

Out[241]= {A $\tau$ , ME[3, 3]}

In[242]:= varC = Union[Variables[Mch $\chi$ ], Variables[Mnex]]

Out[242]= {M1, M2,  $\kappa_0$ ,  $\kappa_2$ ,  $\kappa_3$ ,  $\sigma_S$ ,  $\kappa_1[1]$ ,  $\kappa_1[2]$ ,  $\kappa_1[3]$ ,  $\sigma_n[3]$ ,  $\sigma_V[1]$ ,  $\sigma_V[2]$ ,  $\sigma_V[3]$ }

In[243]:= Union[varA, varB, varC]

Out[243]= {A0, A2, A3, A $\tau$ , M1, M2,  $\kappa_0$ ,  $\kappa_2$ ,  $\kappa_3$ ,  $\sigma_S$ , A1[1], A1[2], A1[3], ME[3, 3],
    ML[1, 2], ML[1, 3], ML[2, 3],  $\kappa_1[1]$ ,  $\kappa_1[2]$ ,  $\kappa_1[3]$ ,  $\sigma_n[3]$ ,  $\sigma_V[1]$ ,  $\sigma_V[2]$ ,  $\sigma_V[3]$ }

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In[244]:= Block[{A0, A1, A2, A3, Aτ, κ0, κ1, κ2, κ3, M1, M2, ME, ML, σS, σn, σν},
  $MinPrecision = prec;
  A0 = SetPrecision[TeV, prec];
  A2 = -SetPrecision[TeV, prec];
  A3 = -SetPrecision[TeV, prec];
  Aτ = SetPrecision[TeV, prec];
  A1[i_] := -SetPrecision[TeV, prec];
  κ0 = SetPrecision[0.4, prec];
  κ1[i_] := SetPrecision[10^-5, prec];
  κ2 = SetPrecision[0.5, prec];
  κ3 = SetPrecision[0.6, prec];
  M1 = SetPrecision[350 GeV, prec];
  M2 = SetPrecision[500 GeV, prec];
  σS = SetPrecision[TeV, prec];
  σn[3] = SetPrecision[TeV, prec];
  σν[1] = SetPrecision[0.19 MeV, prec];
  σν[2] = SetPrecision[0.14 MeV, prec];
  σν[3] = SetPrecision[0.15 MeV, prec];
  ME[3, 3] = ML[1, 2] = ML[1, 3] = ML[2, 3] = SetPrecision[TeV, prec];
  {valsNe, vecSNe} = Eigensystem[TE];
  {valsNo, vecSNo} = Eigensystem[TO];
  {valSC, vecSC} = Eigensystem[TC];
  valFN = Sqrt[Eigenvalues[Mnex.Transpose[Conjugate[Mnex]]]];
  vecFN = Inverse[Transpose[Eigenvectors[Mnex.Transpose[Conjugate[Mnex]]]]];
  valFC = Sqrt[Eigenvalues[Conjugate[MchχT].Mchχ]];
  vecFCu = Conjugate[Inverse[Transpose[Eigenvectors[Mchχ.Conjugate[MchχT]]]]];
  vecFCv = Inverse[Transpose[Eigenvectors[Conjugate[MchχT].Mchχ]]];
  $MinPrecision = 0;
  Im[{N[Sqrt[valsNe] * 10^-9, 4], N[Sqrt[valsNo] * 10^-9, 4]}] // Chop
]

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Out[244]= {{0, 0, 0, 0, 0, 0, 0}, {0, 0, 0, 0, 0, 0, 0}}

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In[245]:= Chop[N[vecSNe^2, 2], 0.01] // MatrixForm

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Out[245]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 1.0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1.0 & 0 \\ 0 & 0 & 0 & 1.0 & 0 & 0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.63 & 0 & 0 & 0 & 0.36 \\ 0 & 0.054 & 0.33 & 0 & 0 & 0 & 0.62 \\ 0 & 0.94 & 0.037 & 0 & 0 & 0 & 0.021 \end{pmatrix}$$


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In[246]:= N[Sqrt[valsNe] * 10^-9, 4] // Chop

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Out[246]= {1.115 × 10^6, 1.077 × 10^6, 9.567 × 10^5, 6053., 717.5, 320.6, 23.08}

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In[247]:= Chop[N[vecSNo^2, 2], 0.01] // MatrixForm

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Out[247]//MatrixForm=

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 1.0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1.0 & 0 \\ 0 & 0 & 0 & 1.0 & 0 & 0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0.50 & 0 & 0 & 0 & 0.50 \\ 0 & 0 & 0.50 & 0 & 0 & 0 & 0.50 \\ 0 & 1.0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$


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In[248]:= N[Sqrt[valsNo] * 10^-9, 4] // Chop

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Out[248]= {1.115 × 10^6, 1.077 × 10^6, 9.567 × 10^5, 6053., 1732., 632.9, 0}

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In[249]:= Chop[N[vecSC^2, 2], 0.01] // MatrixForm
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Out[249]//MatrixForm=
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$$\begin{pmatrix} 0 & 0 & 0 & 1.0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1.0 & 0 \\ 0 & 0 & 1.0 & 0 & 0 & 0 \\ 1.0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1. \\ 0 & 1.0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

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In[250]:= N[Sqrt[valSC] * 10^-9, 4] // Chop
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Out[250]= {1.115 × 106, 1.077 × 106, 9.567 × 105, 6053., 1001., 0}
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In[251]:= N[valFC * 10^-9, 4] // Chop
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Out[251]= {530.5, 376.2, 1.777, 0, 0}
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In[252]:= N[valFN * 10^-9, 4] // Chop
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Out[252]= {1055., 531.0, 408.0, 393.0, 331.7, 46.93, 1.726 × 10-10, 0, 0}
```