```
ln[211]:= TH1M = THiggs1Mod /. \{\sigma n[3] \rightarrow 0, \sigma v[i_] \rightarrow 0\};
                   TH2M = THiggs2Mod /. \{\sigma n[3] \rightarrow 0, \ \sigma v[i_] \rightarrow 0\};
                   TSM = TSingletMod /. \{\sigma n[3] \rightarrow 0, \sigma v[i] \rightarrow 0\};
                   TL1M = TLeft1Mod /. \{\sigma n[3] \rightarrow 0, \sigma v[i_] \rightarrow 0\};
                   TL2M = TLeft2Mod /. \{\sigma n[3] \rightarrow 0, \sigma v[i_] \rightarrow 0\};
                   In[217]:= Vac3 = Flatten[{Solve[TH1M == 0, mH1][[1]],
                                Solve[TH2M == 0, mH2][[1]],
                                \texttt{Solve}[\texttt{TSM} = \texttt{0, MS}][[\texttt{1}]], \{\sigma n[\texttt{3}] \rightarrow \texttt{0, } \sigma v[\texttt{i}] \rightarrow \texttt{0}\}\}];
In[219]:= TE3 = Mneut[[Range[1, 7], Range[1, 7]]] /. Vac3 // Simplify;
                   TO3 = Mneut[[Range[8, 14], Range[8, 14]]] /. Vac3 // Simplify;
                   TC3 = Mchar /. Vac3 // Simplify;
                   Mc\chi = Mch\chi /. Vac3 // Simplify;
                   Mc\chi T = Mch\chi T /. Vac3 // Simplify;
                   Mn\chi = Mne\chi /. Vac3 // Simplify;
In[226]:= prec = 50;
                   $MinPrecision = prec;
                   TeV = 10^12; GeV = 10^9; MeV = 10^6;
                   vSq = SetPrecision[(174 GeV)^2, prec];
                   vSqHiggs = (vSq - \sigma v[1]^2 - \sigma v[2]^2 - \sigma v[3]^2) /. \{\sigma n[3] \rightarrow 0, \sigma v[i_] \rightarrow 0\};
                   mW = SetPrecision[80.403 GeV, prec];
                   mZ = SetPrecision[91.1876 GeV, prec];
                   \alphaew = SetPrecision[1/127.908957, prec];
                   Ow = SetPrecision[ArcSin[Sqrt[0.23124]], prec]; mtPole = SetPrecision[180 GeV, prec];
                   astrong = SetPrecision[0.102, prec];
                   mup = SetPrecision[1.5 MeV, prec];
                   mcharm = SetPrecision[1.1 GeV, prec];
                   mtop = SetPrecision[mtPole / (1 + 4 * αstrong / (3 Pi)), prec];
                   mdown = SetPrecision[3 MeV, prec];
                   mstrange = SetPrecision[60 MeV, prec];
                   mbottom = SetPrecision[4.1 GeV, prec];
                   melectron = SetPrecision[0.511 MeV, prec];
                   mmuon = SetPrecision[105.66 MeV, prec];
                   mtau = SetPrecision[1.777 GeV, prec];
                    (*Yup=SetPrecision[mup /v2,prec];
                   Ycrm=SetPrecision[mcharm /v2,prec];*)
                   Ytop = SetPrecision[mtop / v2, prec];
                    (*Ydwn=SetPrecision[mdown /v1,prec];
                   Ystg=SetPrecision[mstrange /v1,prec];*)
                   Ybtm = SetPrecision[mbottom / v1, prec];
                    (*Ye=SetPrecision[melectron /v1,prec];
                   Yμ=SetPrecision[mmuon /v1,prec];*)
                   Yt = SetPrecision[mtau / v1, prec];
ln[248] = \beta = SetPrecision[ArcTan[30], prec];
                   g1 := SetPrecision[Sqrt[(2*Tan[\theta w]^2*mW^2)/vSq], prec];
                   g2 := SetPrecision[mW * Sqrt[2 / vSq], prec];
                   v1 = Sqrt[vSqHiggs / (1 + Tan[\beta]^2)];
                   v2 = v1 * Tan[\beta];
In[252]:= varA = Union[Variables[TE3], Variables[TO3]]
 \text{Out}[252] = \{ \texttt{A0, A2, A3, } \\ \texttt{\kappa0, } \\ \texttt{\kappa2, } \\ \texttt{\kappa3, } \\ \texttt{\sigmaS, A1[1], A1[2], A1[3], } \\ \texttt{ML[1, 1], } \\ \texttt{ML[1, 2], 
                        \mathtt{ML}[1,\,3]\,,\,\mathtt{ML}[2,\,2]\,,\,\mathtt{ML}[2,\,3]\,,\,\mathtt{ML}[3,\,3]\,,\,\mathtt{MN}[3,\,3]\,,\,\kappa\mathbf{1}[1]\,,\,\kappa\mathbf{1}[2]\,,\,\kappa\mathbf{1}[3]\,\}
|n|253|:= varB = Complement[Variables[TC3], Union[Variables[TE3], Variables[TO3]]]
Out[253]= \{A\tau, ME[3, 3]\}
ln[255]:= varC = Union[Variables[Mc\chi], Variables[Mn\chi]]
Out[255]= {M1, M2, \kappa0, \kappa2, \kappa3, \sigma5, \kappa1[1], \kappa1[2], \kappa1[3]}
In[256]:= Union[varA, varB, varC]
Out[256] = \{A0, A2, A3, A\tau, M1, M2, \kappa0, \kappa2, \kappa3, \sigmaS, A1[1], A1[2], A1[3], ME[3, 3], ML[1, 1], MI[1, 1], M
                        \mathtt{ML}[1, 2], \mathtt{ML}[1, 3], \mathtt{ML}[2, 2], \mathtt{ML}[2, 3], \mathtt{ML}[3, 3], \mathtt{MN}[3, 3], \kappa 1[1], \kappa 1[2], \kappa 1[3]}
```

```
ln[384]:= Block[{A0, A1, A2, A3, At, M1, M2, \kappa0, \kappa1, \kappa2, \kappa3, \sigma5, ME, ML, MN},
        $MinPrecision = prec;
        A0 = SetPrecision[TeV, prec];
       A1[i ] := SetPrecision[TeV, prec];
        A2 = SetPrecision[TeV, prec];
       A3 = -SetPrecision[300 GeV, prec];
       Aτ = SetPrecision[TeV, prec];
        κ0 = SetPrecision[0.4, prec];
       k1[i_] := SetPrecision[10^-5, prec];
        κ2 = SetPrecision[0.5, prec];
        κ3 = SetPrecision[0.6, prec];
       M1 = SetPrecision[350 GeV, prec];
       M2 = SetPrecision[500 GeV, prec];
        \sigma S = SetPrecision[TeV, prec];
       ME[3, 3] = SetPrecision[TeV, prec];
       MN[3, 3] = SetPrecision[TeV, prec];
       ML[1, 1] = ML[2, 2] = ML[3, 3] = SetPrecision[TeV, prec];
       ML[1, 2] = ML[1, 3] = ML[2, 3] = SetPrecision[500 GeV, prec];
        {valSNe, vecSNe} = Eigensystem[TE3];
        {valSNo, vecSNo} = Eigensystem[TO3];
        {valSC, vecSC} = Eigensystem[TC3];
        valFN = Sqrt[Eigenvalues[Mn\chi.Transpose[Conjugate[Mn\chi]]]];
        vecFN = Inverse[Transpose[Eigenvectors[Mn\chi.Transpose[Conjugate[Mn\chi]]]]]];
        {\tt valFC = Sqrt[Eigenvalues[Conjugate[Mc$\chi$T].Mc$\chi]];}
        vecFCu = Conjugate[Inverse[Transpose[Eigenvectors[Mcχ.Conjugate[McχT]]]]];
        vecFCv = Inverse[Transpose[Eigenvectors[Conjugate[Mc\chiT].Mc\chi]]];
        $MinPrecision = 0;
        Im[{N[Sqrt[valSNe] * 10^-9, 4], N[Sqrt[valSNo] * 10^-9, 4]}] // Chop
Out[384]= \{\{0, 0, 0, 0, 0, 0, 0, 0\}, \{0, 0, 0, 0, 0, 0, 0\}\}
In[385]:= Chop[N[vecSNe^2, 2], 0.01] // MatrixForm
Out[385]//MatrixForm=
                     0
                            0
                                    0
        1.0
                            0.028 0.028 0.028 0.92
        0
             0
                     0
        0
                            0.31
                                    0.31
                                           0.31
                                                   0.084
        0
                            0
                                    0.50
                                           0.50
                                                   0
        0
                     0
                            0.67
                                    0.17
                                           0.17
                                                   0
             0.037 0.96
        0
                            0
                                    0
        0
             0.96
                    0.037 0
                                    0
                                           0
                                                   0
ln[386]:= N[Sqrt[valSNe] *10^-9, 4] // Chop
Out[386]= {5800., 1578., 1185., 863.6, 863.6, 466.7, 15.59}
In[387]:= Chop[N[vecSNo^2, 2], 0.01] // MatrixForm
Out[387]//MatrixForm=
        1.0 0
                                              0
                                              0.041
        0
             0
                        0.32
                               0.32
                                       0.32
        0
                        0
                               0.50
                                       0.50
                                              0
        0
             0
                  0
                        0.67
                               0.17
                                       0.17
                                              0
        0
                  1.0 0
             0
                               0
                                       0
                                              0
        0
             0
                  0
                        0.014 0.014 0.014 0.96
        0
             1.0
                 0
                        0
                               0
                                              0
In[388]:= N[Sqrt[valSNo] * 10^-9, 4] // Chop
Out[388]= \{5800., 1248., 863.6, 863.6, 671.5, 194.9, 0\}
```

```
In[389]:= Chop[N[vecSC^2, 2], 0.01] // MatrixForm
```

Out[389]//MatrixForm=

```
 \begin{pmatrix} \textbf{1.0} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} \\ \textbf{0} & \textbf{0} & \textbf{0.33} & \textbf{0.33} & \textbf{0.33} & \textbf{0} \\ \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{1.0} \\ \textbf{0} & \textbf{0} & \textbf{0.50} & \textbf{0.50} & \textbf{0} & \textbf{0} \\ \textbf{0} & \textbf{0} & \textbf{0.17} & \textbf{0.17} & \textbf{0.67} & \textbf{0} \\ \textbf{0} & \textbf{1.0} & \textbf{0} & \textbf{0} & \textbf{0} & \textbf{0} \end{pmatrix}
```

In[390]:= N [Sqrt[valSC] * 10 ^ -9, 4] // Chop

Out[390]= $\{5800., 1226., 1001., 867.3, 867.0, 0\}$

 $ln[392]:= N[valFC * 10^-9, 4] // Chop$

Out[392]= $\{530.5, 376.2, 1.777, 0, 0\}$

 $ln[393] := N[valFN * 10^-9, 4] // Chop$

Out[393]= $\left\{614.4, 527.7, 500.0, 407.1, 387.0, 328.1, 1.815 \times 10^{-8}, 0, 0\right\}$