

In[229]:= **Mchar[[Range[1, 6], 1]] // Simplify // MatrixForm**

Out[229]//MatrixForm=

$$\begin{pmatrix} \frac{1}{4} \left( 4 \text{mH}^2 + g^2 v_1^2 + g^2 v_2^2 + 4 \kappa_0^2 \sigma S^2 - g^2 \sigma_V [1]^2 - g^2 \sigma_V [2]^2 - g^2 \sigma_V [3]^2 + 4 Y \tau^2 \sigma_V [3]^2 + g^2 (v_1^2 - v_2^2 + \sigma_V [1]^2 + \sigma_V [2]^2 + \sigma_V [3]^2) \right) \\ \frac{1}{2} \left( g^2 v_1 v_2 - 2 v_1 v_2 \kappa_0^2 + 2 A_0 \sigma S + \kappa_0 \kappa_3 \sigma S^2 + \kappa_0 \kappa_2 \sigma n [3]^2 \right) \\ -\kappa_0 \sigma S \kappa_1 [1] \sigma n [3] + \frac{1}{2} g^2 v_1 \sigma_V [1] \\ -\kappa_0 \sigma S \kappa_1 [2] \sigma n [3] + \frac{1}{2} g^2 v_1 \sigma_V [2] \\ -\kappa_0 \sigma S \kappa_1 [3] \sigma n [3] + \frac{1}{2} v_1 \left( g^2 - 2 Y \tau^2 \right) \sigma_V [3] \\ -v_2 Y \tau \kappa_1 [3] \sigma n [3] - A \tau \sigma_V [3] \end{pmatrix}$$

In[230]:= **Mchar[[Range[1, 6], 2]] // Simplify // MatrixForm**

Out[230]//MatrixForm=

$$\begin{pmatrix} \frac{1}{2} \left( g^2 v_1 v_2 - 2 v_1 v_2 \kappa_0^2 + 2 A_0 \sigma S + \kappa_0 \kappa_3 \sigma S^2 + \kappa_0 \kappa_2 \sigma n [3]^2 \right) \\ \frac{1}{4} \left( 4 \text{mH}^2 + g^2 v_1^2 + g^2 v_2^2 + 4 \kappa_0^2 \sigma S^2 + 4 \kappa_1 [1]^2 \sigma n [3]^2 + 4 \kappa_1 [2]^2 \sigma n [3]^2 + 4 \kappa_1 [3]^2 \sigma n [3]^2 + g^2 \sigma_V [1]^2 + g^2 \sigma_V [2]^2 + g^2 \sigma_V [3]^2 - g^2 (v_1^2 - v_2^2 + \sigma_V [1]^2 + \sigma_V [2]^2 + \sigma_V [3]^2) \right) \\ -A_1 [1] \sigma n [3] + \frac{1}{2} g^2 v_2 \sigma_V [1] - \kappa_1 [1] \left( \kappa_2 \sigma S \sigma n [3] + v_2 \left( \kappa_1 [1] \sigma_V [1] + \kappa_1 [2] \sigma_V [2] + \kappa_1 [3] \sigma_V [3] \right) \right) \\ -A_1 [2] \sigma n [3] + \frac{1}{2} g^2 v_2 \sigma_V [2] - \kappa_1 [2] \left( \kappa_2 \sigma S \sigma n [3] + v_2 \left( \kappa_1 [1] \sigma_V [1] + \kappa_1 [2] \sigma_V [2] + \kappa_1 [3] \sigma_V [3] \right) \right) \\ -A_1 [3] \sigma n [3] + \frac{1}{2} g^2 v_2 \sigma_V [3] - \kappa_1 [3] \left( \kappa_2 \sigma S \sigma n [3] + v_2 \left( \kappa_1 [1] \sigma_V [1] + \kappa_1 [2] \sigma_V [2] + \kappa_1 [3] \sigma_V [3] \right) \right) \\ -Y \tau \left( v_1 \kappa_1 [3] \sigma n [3] + \kappa_0 \sigma S \sigma_V [3] \right) \end{pmatrix}$$

In[231]:= **Mchar[[Range[1, 6], 3]] // Simplify // MatrixForm**

Out[231]//MatrixForm=

$$\begin{pmatrix} -\kappa_0 \sigma S \kappa_1 [1] \sigma n [3] + \frac{1}{2} g^2 v_1 \sigma_V [1] \\ -A_1 [1] \sigma n [3] + \frac{1}{2} g^2 v_2 \sigma_V [1] - \kappa_1 [1] \left( \kappa_2 \sigma S \sigma n [3] + v_2 \left( \kappa_1 [1] \sigma_V [1] + \kappa_1 [2] \sigma_V [2] + \kappa_1 [3] \sigma_V [3] \right) \right) \\ \frac{1}{4} \left( 4 \left( \text{ML} [1, 1]^2 + \kappa_1 [1]^2 \sigma n [3]^2 \right) - g^2 \left( v_1^2 - v_2^2 - \sigma_V [1]^2 + \sigma_V [2]^2 + \sigma_V [3]^2 \right) + g^2 \left( v_1^2 - v_2^2 + \sigma_V [1]^2 + \sigma_V [2]^2 + \sigma_V [3]^2 \right) \right) \\ \text{ML} [1, 2]^2 + \kappa_1 [1] \kappa_1 [2] \sigma n [3]^2 + \frac{1}{2} g^2 \sigma_V [1] \sigma_V [2] \\ \text{ML} [1, 3]^2 + \kappa_1 [1] \kappa_1 [3] \sigma n [3]^2 + \frac{1}{2} g^2 \sigma_V [1] \sigma_V [3] \\ 0 \end{pmatrix}$$

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In[232]:= Mchar[[Range[1, 6], 4]] // Simplify // MatrixForm
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Out[232]//MatrixForm=
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$$\begin{pmatrix} -\kappa_0 \sigma_S \kappa_1[2] \sigma_n[3] + \frac{1}{2} g_2^2 \mathbf{v}_1 \sigma_V[2] \\ -\mathbf{A}_1[2] \sigma_n[3] + \frac{1}{2} g_2^2 \mathbf{v}_2 \sigma_V[2] - \kappa_1[2] (\kappa_2 \sigma_S \sigma_n[3] + \mathbf{v}_2 (\kappa_1[1] \sigma_V[1] + \kappa_1[2] \sigma_V[2] + \kappa_1[3] \sigma_V[3])) \\ \mathbf{M}_L[1, 2]^2 + \kappa_1[1] \kappa_1[2] \sigma_n[3]^2 + \frac{1}{2} g_2^2 \sigma_V[1] \sigma_V[2] \\ \frac{1}{4} (4 (\mathbf{M}_L[2, 2]^2 + \kappa_1[2]^2 \sigma_n[3]^2) - g_2^2 (\mathbf{v}_1^2 - \mathbf{v}_2^2 + \sigma_V[1]^2 - \sigma_V[2]^2 + \sigma_V[3]^2) + g_1^2 (\mathbf{v}_1^2 - \mathbf{v}_2^2 + \sigma_V[1]^2 + \sigma_V[2]^2 + \sigma_V[3]^2)) \\ \mathbf{M}_L[2, 3]^2 + \kappa_1[2] \kappa_1[3] \sigma_n[3]^2 + \frac{1}{2} g_2^2 \sigma_V[2] \sigma_V[3] \\ 0 \end{pmatrix}$$

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In[233]:= Mchar[[Range[1, 6], 5]] // Simplify // MatrixForm
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Out[233]//MatrixForm=
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$$\begin{pmatrix} -\kappa_0 \sigma_S \kappa_1[3] \sigma_n[3] + \frac{1}{2} \mathbf{v}_1 (g_2^2 - 2 Y_\tau^2) \sigma_V[3] \\ -\mathbf{A}_1[3] \sigma_n[3] + \frac{1}{2} g_2^2 \mathbf{v}_2 \sigma_V[3] - \kappa_1[3] (\kappa_2 \sigma_S \sigma_n[3] + \mathbf{v}_2 (\kappa_1[1] \sigma_V[1] + \kappa_1[2] \sigma_V[2] + \kappa_1[3] \sigma_V[3])) \\ \mathbf{M}_L[1, 3]^2 + \kappa_1[1] \kappa_1[3] \sigma_n[3]^2 + \frac{1}{2} g_2^2 \sigma_V[1] \sigma_V[3] \\ \mathbf{M}_L[2, 3]^2 + \kappa_1[2] \kappa_1[3] \sigma_n[3]^2 + \frac{1}{2} g_2^2 \sigma_V[2] \sigma_V[3] \\ \frac{1}{4} (4 (\mathbf{v}_1^2 Y_\tau^2 + \mathbf{M}_L[3, 3]^2 + \kappa_1[3]^2 \sigma_n[3]^2) - g_2^2 (\mathbf{v}_1^2 - \mathbf{v}_2^2 + \sigma_V[1]^2 + \sigma_V[2]^2 - \sigma_V[3]^2) + g_1^2 (\mathbf{v}_1^2 - \mathbf{v}_2^2 + \sigma_V[1]^2 + \sigma_V[2]^2 + \sigma_V[3]^2)) \\ \mathbf{A}_\tau \mathbf{v}_1 - \mathbf{v}_2 Y_\tau \kappa_0 \sigma_S \end{pmatrix}$$

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In[234]:= Mchar[[Range[1, 6], 6]] // Simplify // MatrixForm
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Out[234]//MatrixForm=
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$$\begin{pmatrix} -\mathbf{v}_2 Y_\tau \kappa_1[3] \sigma_n[3] - \mathbf{A}_\tau \sigma_V[3] \\ -Y_\tau (\mathbf{v}_1 \kappa_1[3] \sigma_n[3] + \kappa_0 \sigma_S \sigma_V[3]) \\ 0 \\ 0 \\ \mathbf{A}_\tau \mathbf{v}_1 - \mathbf{v}_2 Y_\tau \kappa_0 \sigma_S \\ \mathbf{v}_1^2 Y_\tau^2 + \mathbf{M}_E[3, 3]^2 + Y_\tau^2 \sigma_V[3]^2 - \frac{1}{2} g_1^2 (\mathbf{v}_1^2 - \mathbf{v}_2^2 + \sigma_V[1]^2 + \sigma_V[2]^2 + \sigma_V[3]^2) \end{pmatrix}$$