

**Directions:** Read all the questions carefully and answer them completely. No credit will be given for undocumented responses. **Show all your work to get full credit.**

Use Matlab to complete the following questions.

1. A population  $P$  (unit: million) obeys the logistic model. It satisfies the equation

$$\frac{dP}{dt} = 0.000167716P(188.121 - P).$$

Assume when  $t = 0$  (unit: year),  $P_0 = 5.308$ . Let  $h = 0.05$ .

- (a) Use Euler's method to compute  $P(300)$ .
- (b) Use Improved Euler's method to compute  $P(300)$ .
- (c) Use Runge-Kutta method to compute  $P(300)$ .
- (d) Plot all three solutions (domain:  $[0, 300]$ ) in a same figure.