

## Waves

Basic:  $y = A \sin(kx - \omega t)$  where  $k = \frac{2\pi}{\lambda}$  and  $\omega = \frac{2\pi}{T}$ . We also have  $f = \frac{1}{T}$ ,  $c = \frac{\omega}{k} = \lambda f$

Velocity of wave in string:  $c = \sqrt{\frac{T}{\mu}}$

Power transmitted in string with sinusoidal waves:  $P = \frac{1}{2} \mu \omega^2 A^2 c$

Trig. Identity:  $\sin(\alpha + \beta) = 2 \sin\left(\frac{\alpha + \beta}{2}\right) \cos\left(\frac{\alpha - \beta}{2}\right)$

Standing waves is the sum of two waves  $y = y_1 + y_2$ , where  $y_1 = A \sin(kx - \omega t + \phi)$  and  $y_2 = A \sin(kx + \omega t)$

Interference. Given:  $y_1 = A \sin(kr - \omega t)$  and  $y_2 = A \sin(k(r + \Delta r) - \omega t)$  adding them we have  $y = y_1 + y_2 = 2A \sin(kr - \omega t + k\Delta r/2) \cos(k\Delta r/2)$ ; thus, the effective amplitude that determines constructive and destructive interference is:  $A_{eff} = 2A \cos(k\Delta r/2)$

Intensity:  $I = \frac{P}{4\pi r^2}$  in 3D;  $I = \frac{P}{2\pi r}$  in 2D; constant in 1D.

Sound intensity level (Volume)  $\beta = 10 \log(I/I_0)$

Beats:  $f_{beat} = f_a - f_b$

Doppler effect:  $f_o = \frac{c \pm v_o}{c \pm v_s} f_s$ ; for light:  $f_o = \sqrt{\frac{c-v}{c+v}} f_s$  where  $v$  is the relative velocity ( $\pm$ )

Angle of a shock wave:  $\sin \alpha = \frac{c}{v_s}$