(1) Two different wave functions, $\psi_1(x)$ and $\psi_2(x)$, are shown below. Consider the following four combinations of states:

(a)
$$\psi_1(x)$$

(b)
$$\psi_2(x)$$

(c)
$$\psi_1(x) + \psi_2(x)$$

(b)
$$\psi_2(x)$$
 (c) $\psi_1(x) + \psi_2(x)$ (d) $\psi_1(x) + i\psi_2(x)$

Assume each state (or combination of states) is properly normalized.

(a) Rank the states, from lowest to highest, based on the expectation value of x for each state.

Smallest value of
$$\langle x \rangle$$

Smallest value of
$$\langle x \rangle$$
 C C

Largest value of $\langle x \rangle$

(b) Rank the states, from lowest to highest, based on the uncertainty in *x* for each state.

Smallest value of
$$\Delta x$$
 C $\Delta = b = d$

Largest value of Δx

