Show that the shortest path between two points on the surface of a cylinder of radius ${\it R}$ is

$$\theta(z) = \alpha z + \beta$$