

Two beads of mass m are connected by a spring with zero rest length and spring constant k . The beads are also confined to move around a circular, frictionless hoop of radius R . The beads can freely pass through each other.

Write down the total energy of the system in terms of

- Cartesian coordinates $(x_1, y_1, \dot{x}_1, \dot{y}_1, x_2, y_2, \dot{x}_2, \dot{y}_2)$
- Polar coordinates $(r_1, \phi_1, \dot{r}_1, \dot{\phi}_1, r_2, \phi_2, \dot{r}_2, \dot{\phi}_2)$

Solve this problem for both vertically and a horizontally oriented hoops.

