

## Homework 2 - Readings Ch3 (91-113) & Ch4

- Given a point  $p(x, y, z)$  and the point  $p'(x', y', z')$  where  $p'(x', y', z')$  is the point  $p(x, y, z)$  translated by  $T_x, T_y, T_z$ :

- Show the **equations** to compute  $p'$  from  $p$ .

$$p'(x', y', z') = [T_x, T_y, T_z] * p(x, y, z)$$

- Show the 4x4 **transformation matrix** to compute  $p'$  from  $p$ .

$$\begin{bmatrix} 1 & 0 & 0 & T_x \\ 0 & 1 & 0 & T_y \\ 0 & 0 & 1 & T_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \\ 1 \end{bmatrix} = \begin{bmatrix} p'_x \\ p'_y \\ p'_z \\ 1 \end{bmatrix}$$

- Given a point  $p(x, y, z)$  and the point  $p'(x', y', z')$ , where  $p'(x', y', z')$  is the  $\beta$  degree rotated point of  $p(x, y, z)$  around the z-axis:

- Show the **equations** to compute  $p'$  from  $p$ .

$$p'(x', y', z') = R_z(\beta) * p(x, y, z)$$

- Show the 4x4 **transformation matrix** to compute  $p'$  from  $p$ .

$$\begin{bmatrix} \cos(\beta) & -\sin(\beta) & 0 & 0 \\ \sin(\beta) & \cos(\beta) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \\ 1 \end{bmatrix} = \begin{bmatrix} p'_x \\ p'_y \\ p'_z \\ 1 \end{bmatrix}$$

- Given a point  $p(x, y, z)$  and the point  $p'(x', y', z')$ , where  $p'(x', y', z')$  is the point  $p(x, y, z)$  scaled by  $S_x, S_y, S_z$ :

- Show the **equations** to compute  $p'$  from  $p$ .

$$p'(x', y', z') = S_{x,y,z} * p(x, y, z)$$

- Show the 4x4 **transformation matrix** to compute  $p'$  from  $p$ .

$$\begin{bmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} p_x \\ p_y \\ p_z \\ 1 \end{bmatrix} = \begin{bmatrix} p'_x \\ p'_y \\ p'_z \\ 1 \end{bmatrix}$$

- What is a model matrix? Write a simple vertex shader that uses a model matrix. Explain your shader.

A model matrix is a matrix that can calculate the Translation, Rotation, and Scale to all the vertices in our world.

```
var VSHADER_SOURCE =  
'attribute vec4 a_Position;  
uniform mat4 u_ModelMatrix;  
void main() {  
    gl_Position = u_ModelMatrix * a_Position;  
}';
```

The shader above takes a position out of a vertex and will translate, rotate, and scale when called in js program