

Accounting for temporal variation in morbidity measurement and projections

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Abstract

This is important stuff!

G is a bad health condition that varies as a function of time to death, y and not as a function of chronological age, a . However, there will still be an apparent age function, $g'(a)$, given that $g(y)$ is regular and mortality is sort of stable, but not really. $g'(a)$, in this case, is an aggregate based on both mortality and the real underlying time-to-death process:

$$g'(a) = \frac{\int_0^\omega g(y)N(a, y) \, dy}{N(a)} \quad (1)$$

$$= \frac{\int_0^\omega g(y)N(a)\mu(a+y)\frac{\ell(a+y)}{\ell(a)} \, dy}{N(a)} \quad (2)$$

$$= \int_0^\omega g(y)f(y|a) \, dy \quad (3)$$

a little exercise we still need to do: find the $g'(a)$ that belongs to $g(y)$ in our canned example. It will be different for males and females because they have different mortality schedules. In this case, we can make the healthy life expectancy function be based on mortality and $g'(a)$ and see what would be the prediction if $g'(a)$ is held constant and we induce mortality improvement. The answer is that mortality improvement will appear to increase the proportion of remaining life expectancy that is unhealthy: also the absolute years spent unhealthy, but the change in sex gap is maybe ambiguous (gotta check, maybe not), depending on the changes induced.

brief interlude This is a simple case of $g(y)$, but in reality morbidity often varies as a function of both chronological and thanatological age, and we ought to have a function $g(a, y)$.

If

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