Ba**R**celona Summer School for Demography Module 2: Demography in R

Projection

11 July, 2025

Instructor: Tim Riffe







Workshop plan, July 1-5, 2024

1: Monday Intro concepts, and R setup

2: Tuesday Mortality and fertility

3: Wednesday standardization and decomposition

4: Thursday Growth

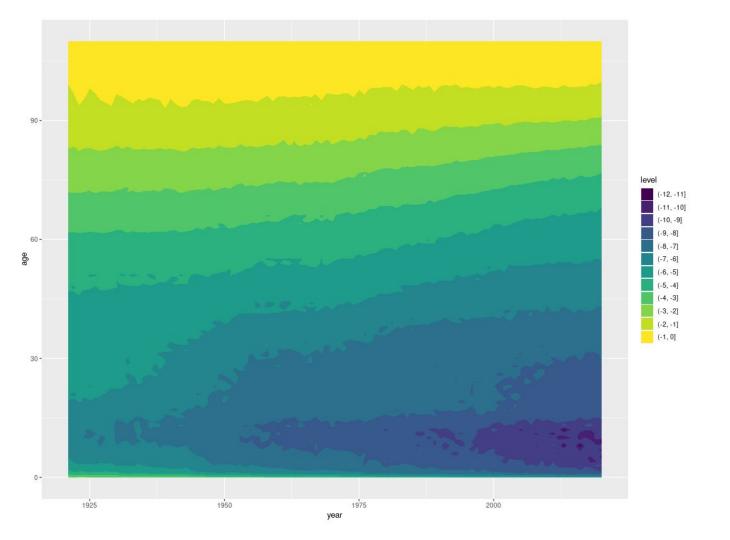
5: Friday Projection

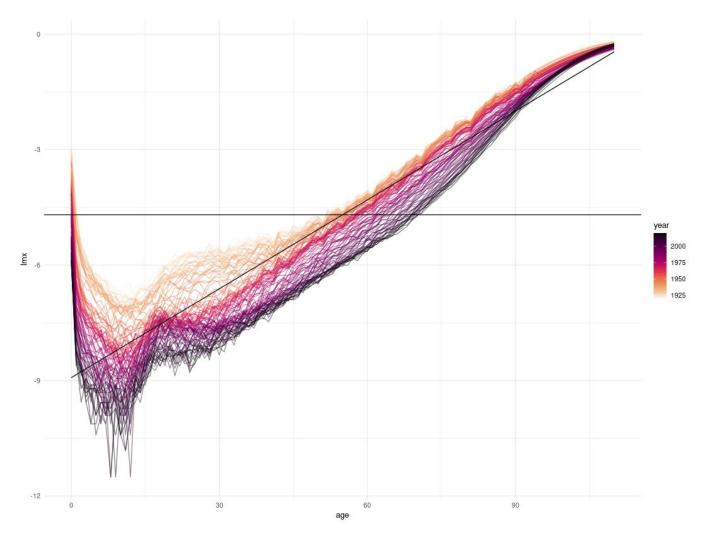
Review of session 4

- Geometric and exponential growth
- Stationary and stable structure
- Stable structure in periods; stationary structure in cohorts
- Stable populations don't happen they are always in the distance;
 change is constant
- colorspace for good palettes.

Projection

- Predict the past/present to predict the future
- Simplify
- Extrapolate





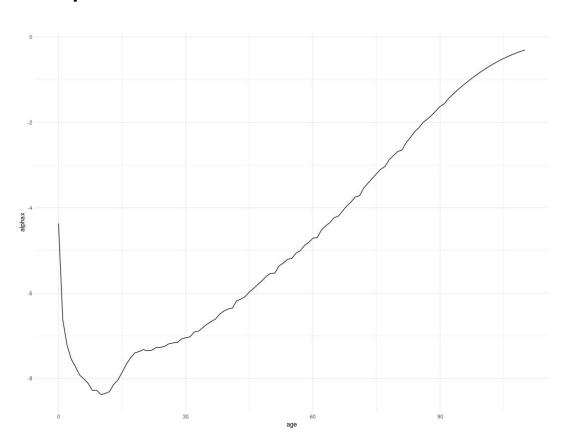
% Variance (of log rates) explained

Parameters	
1 (simple intercept)	Total var = 276
2 (line)	66.4 %
3 (simple plane)	72.9 %
4 (plane with tilt)	75.0 %
200 (each year has own line)	75.2 %
111 (age intercepts)	76.5 %
222 (each age has own line)	93.9 %

Lee Carter method

$$ln(m_x(t)) = \alpha_x + \beta_x \kappa(t) + \epsilon_x(t)$$

Alpha



Calculating beta and kappa

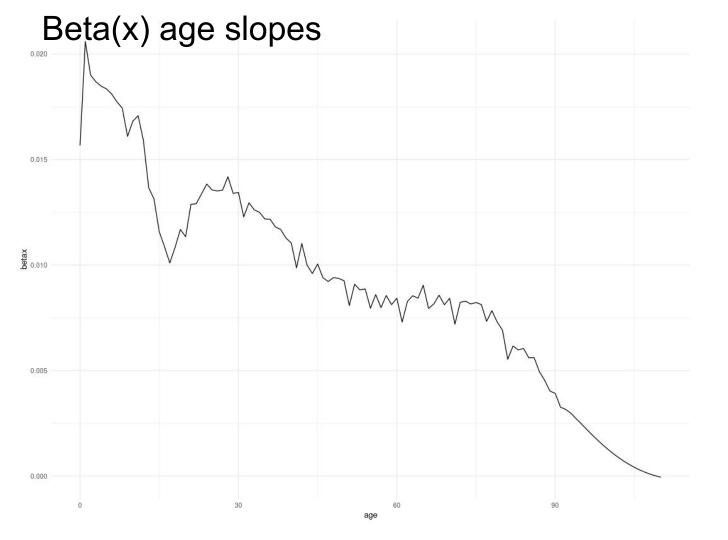
SVD - singular value decomposition

Factorize a matrix **M** into pieces **d**, **U**, **V**, such that:

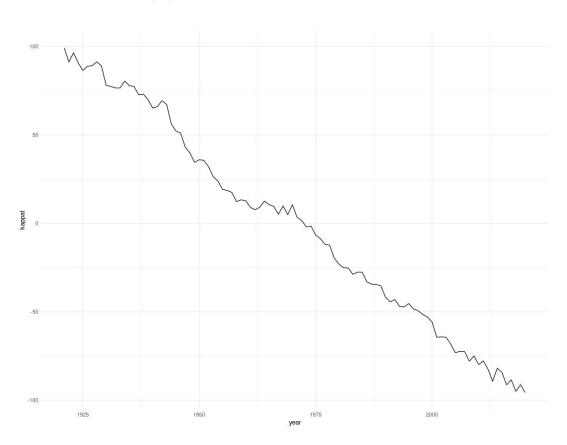
 $M = U \operatorname{diag}(d) V^{T}$

 $\beta(x)$ (age slopes) derived from **U** (scale first column to 1)

 $\kappa(t)$ (secular change) derived from ${\bf V}$ (scale first column of ${\bf V}$ to sum to first element of ${\bf d}$



Kappa(t) the trend to extrapolate



% Variance (of log rates) explained

Parameters	
1 (simple intercept)	Total var = 276
4 (plane with tilt)	75.0 %
200 (each year has own line)	75.2 %
111 (age intercepts)	76.5 %
222 (each age has own line)	93.9 %
224 (LC, simple)	94.2 %



Modeling and Forecasting U. S. Mortality

Ronald D. Lee; Lawrence R. Carter

Journal of the American Statistical Association, Vol. 87, No. 419 (Sep., 1992), 659-671.

Stable URL:

http://links.jstor.org/sici?sici=0162-1459%28199209%2987%3A419%3C659%3AMAFUSM%3E2.0.CO%3B2-T

Journal of the American Statistical Association is currently published by American Statistical Association.

$$ln(m_x(t)) = \alpha_x + \beta_x \kappa(t) + \epsilon_x(t)$$