

# Temporal proportionality in the graphical representation of age-period-cohort classified demographic rates: (Re)introducing the equilateral Lexis surface

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December 21, 2011

## Abstract

The use of demographic surfaces composed of equilateral APC triangles is encouraged over standard 'Lexis' proportions in order to eliminate distortion of the cohort perspective. This transform procedure yields age, period and cohort dimensions of comparable scales. Resulting images are highly legible and interpretable in a similar way to more commonly used standard demographic surfaces. While 'Lexis' diagrams and 'Lexis' surfaces are now known to be misnomers, intellectual parentage for the equilateral Lexis surface most likely is owed to Lexis (1875).

## 1 The standard demographic surface

Any demographic data classified by age, period and cohort are candidate to be plotted as surfaces, with color gradients or contours specifying value intervals for the rate in question. Such surfaces allow for the meaningful summary of large amounts of data and are useful as both diagnostics and didactic tools. Software has been developed in order to convert tables of demographic data into surface figures [Vaupel et al., 1987, Andreev, 1999], as well as a variety of general surface functions from statistical programming languages coercible to 'Lexis' surfaces<sup>1</sup>. Demographic surfaces follow a strict set of guidelines on proportionality, with a unity aspect ratio between age on the y-axis and period on the x-axis<sup>2</sup>. A ninety degree angle between age and period directions forces a 45 degree angle along the cohort dimension, matching each year of cohort time to a length equal to  $\sqrt{2}$  in euclidean space.

Standard demographic surfaces respecting these conventions of proportions are most commonly referred to as 'Lexis' surfaces. We know this name to be a misnomer due to the investigative work of Vandeschrick [2001] and Keiding [2011].

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<sup>1</sup>such as `levelplot()` in the `lattice` package[Sarkar, 2008] in the R language[Ihaka and Gentleman, 1996], among others.

<sup>2</sup>rearranging the data, a less common rendering of age in the y-axis and cohort in the x-axis with a unity aspect ratio has also been done.

## 2 transforming the Lexis diagram

### References

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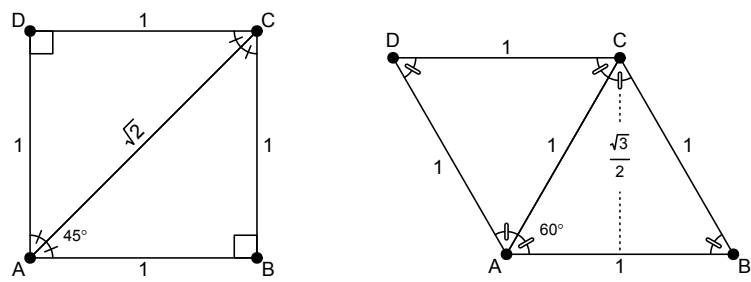


Figure 1: A deceptive scatterplot