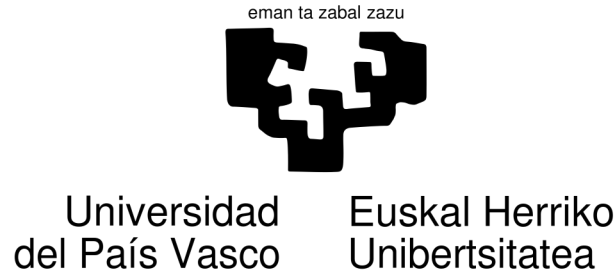


# decomposing multistate models

Tim Riffe

28 May, 2021

REVES annual meeting



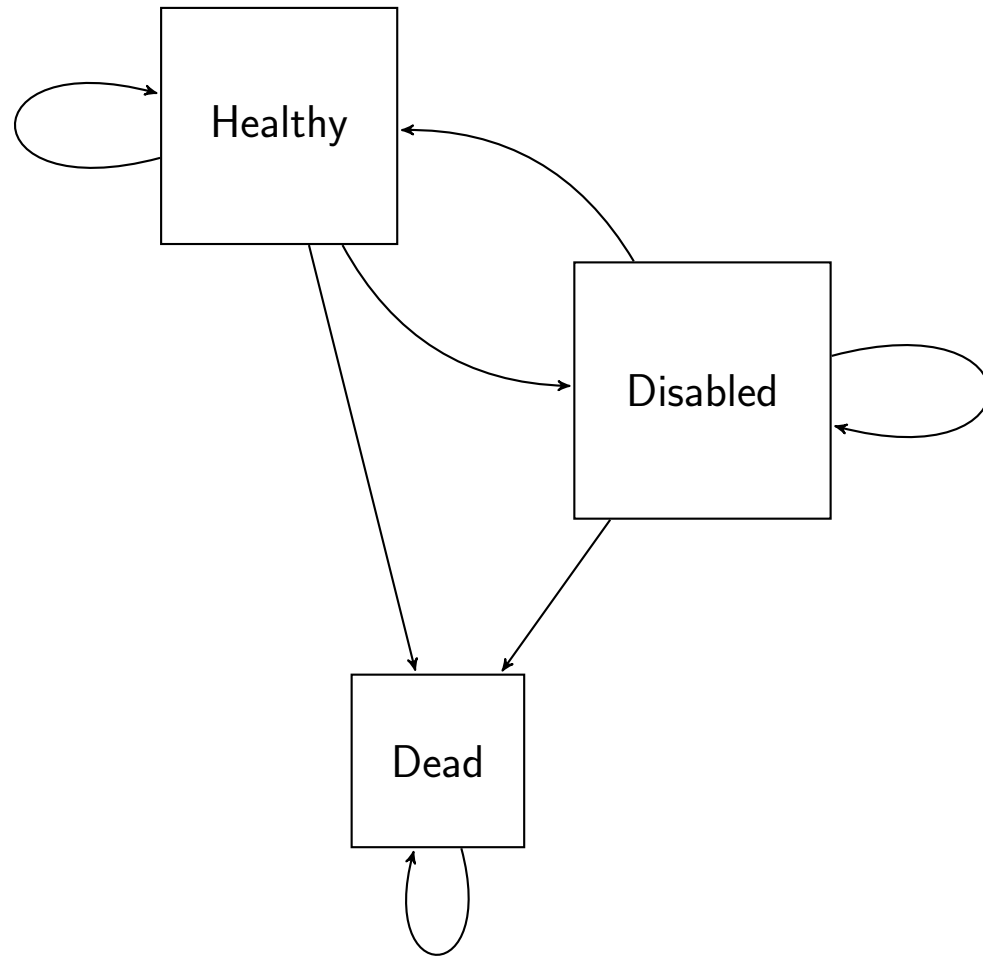
# Consider parameterizing in terms of **conditional probabilities** when decomposing discrete time multistate models

Tim Riffe

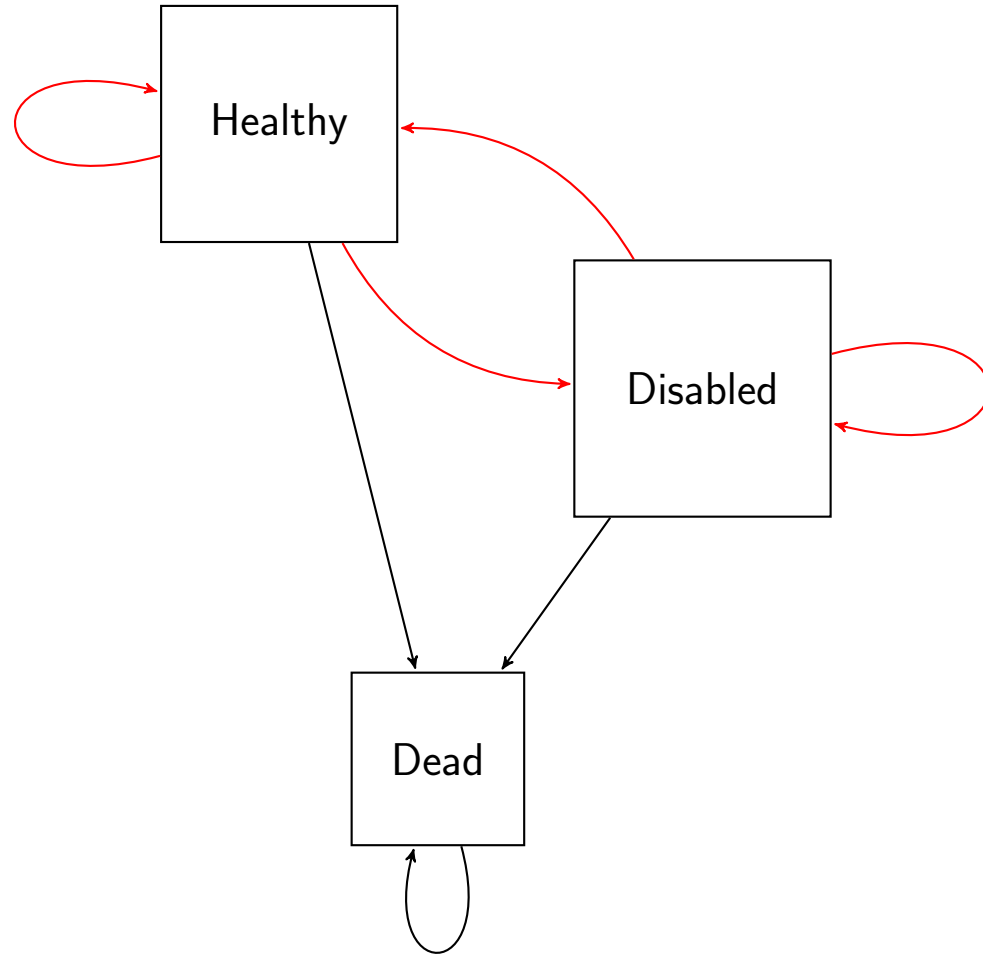
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# A typical multistate model



# A typical multistate model



$$\text{🎁} = f(\theta)$$

🎁 is any synthetic index calculated from  $\theta$

# setup

$$\Delta \text{🎁} = \text{🎁}^2 - \text{🎁}^1$$

$$= f(\theta^2) - f(\theta^1)$$

$$\Delta \text{🎁} = \sum \mathbf{c}_i$$

$$\mathbf{c} = \mathcal{D}(f, \theta^2, \theta^1)$$

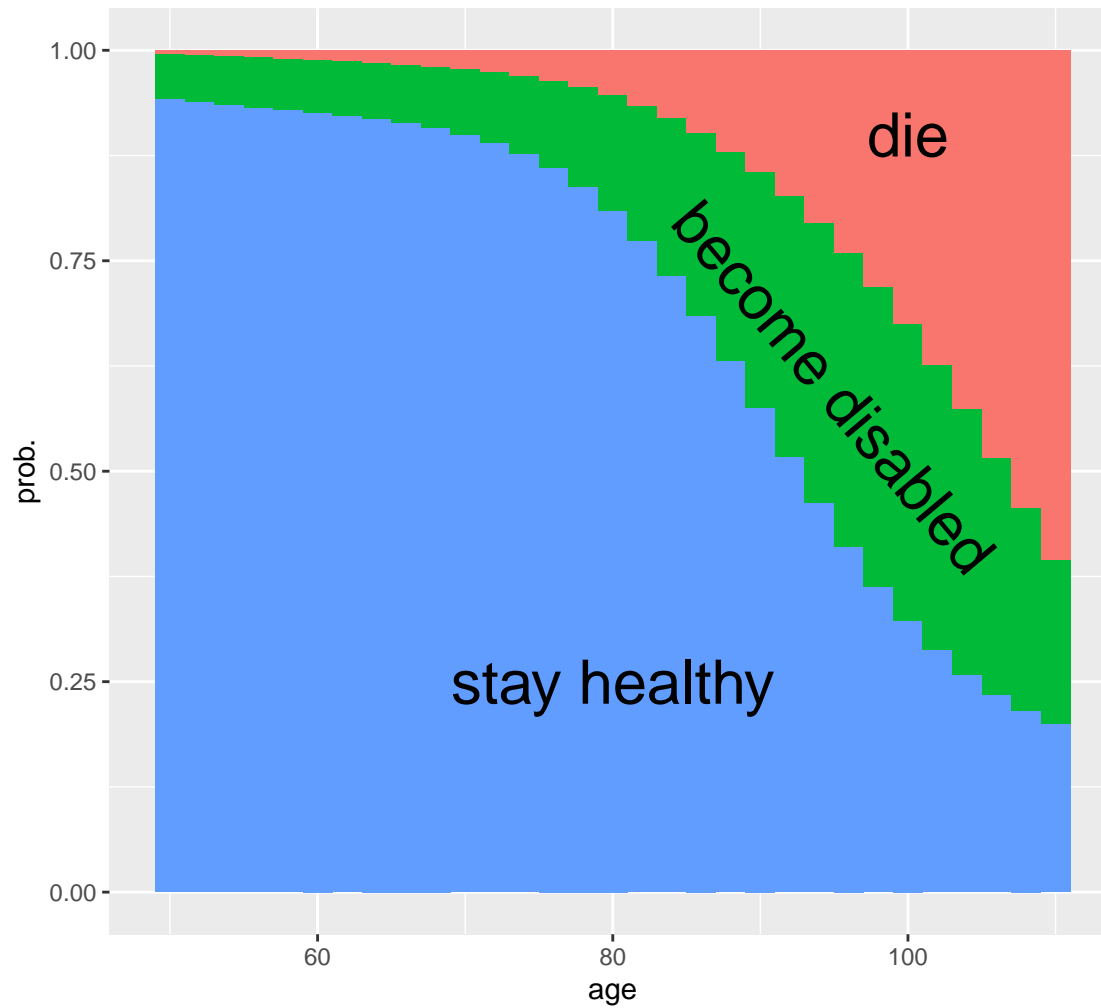
# Decomposition, $\mathcal{D}()$

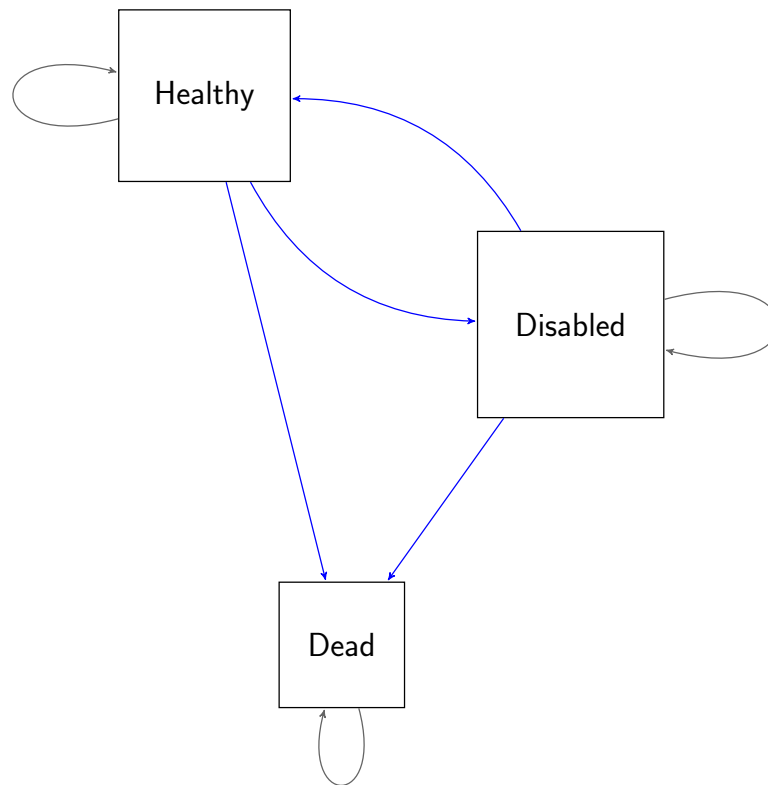
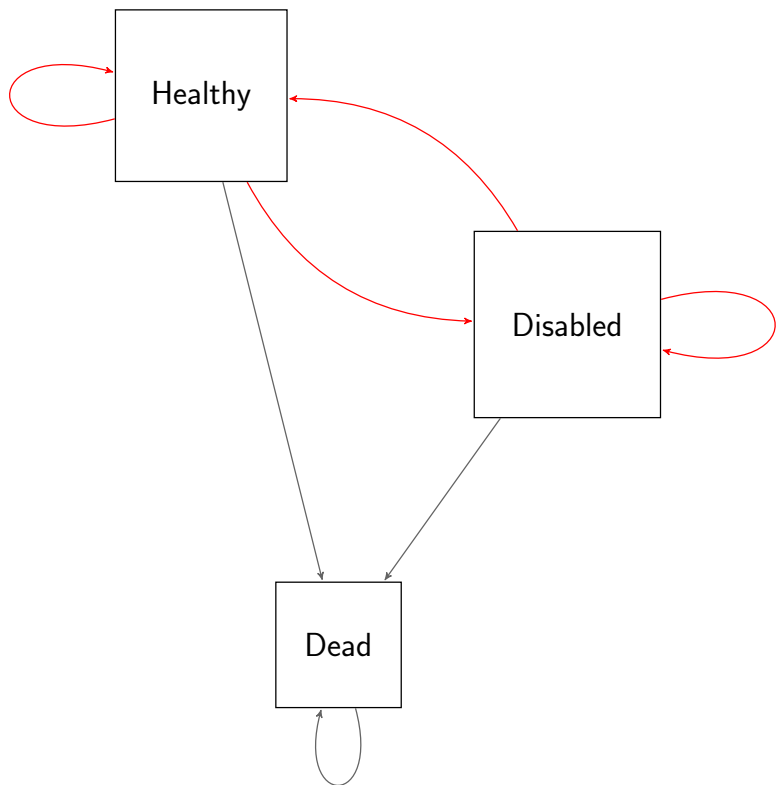
- ▶ LTRE (Caswell 1989)
- ▶ Stepwise (Andreev et al 2002)
- ▶ Pseudo continuous (Horiuchi et al 2008)

Let's talk about  $\theta$



Pick two colors to make  $\theta$





# Example

DFLE increased from 30.75 in 2006 to 32.33 in 2014.  
That's  $\Delta \text{🎁} = 1.58$  years

(HRS, age 50 women with secondary education)

# Example

Same result,  whether we omit:

- ▶ self-transitions
- ▶ mortality transitions
- ▶ health transitions

But **very different stories** if we decompose:

$\theta$ omits	DF $\rightarrow$ DF	DF $\rightarrow$ Dis	DF mort	Dis $\rightarrow$ DF	Dis $\rightarrow$ Dis	Dis mort
self		-0.01	1.32	-0.28		0.54
mort	1.28	0.04		-1.86	2.13	
health	0.21		1.10		-0.41	0.67

# "Thank you" intermission



We would like a solution that gives consistent interpretable results

## Solution

Make  $\theta$  consist in conditional probabilities

For standard calcs compose  $\theta$  from (two of)

$$[p^{stay}, p^{switch}, p^{die}]$$

Transform this into two multiplicative probabilities

$$[p^{stay} | survive, p^{survive}]$$

# Complementarity

DF mort	Dis. mort	DF→ <i>Dis</i>	Dis→ <i>Df</i>
1.29	0.58	0.02	-0.31

Transitions can be framed in terms of mortality or survival, in terms of staying in the state of transferring out of it. Results *identical*



# Complementarity

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# Really, IDENTICAL

# Complementarity

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Transitions can be framed in terms of mortality or survival, in terms of staying in the state of transferring out of it. Results *identical*

## Really, IDENTICAL

## Thanks