

Lecture 2: Byzantine Broadcast in the Synchronous Model via the Dolev-Strong Protocol

(Lecture Series on Foundations of Blockchains)

Recap of the SMR Problem

- clients submit transactions to one or more nodes
 - (users of blockchain)
- each node maintains local history (append-only data structure)
 - (machines running the blockchain protocol)

Goal: a protocol (event-driven code) that satisfies:

- ① consistency: all nodes agree on the same history
- ② liveness: every submitted tx eventually added to all nodes' histories

Plan: solve first under a bunch of assumptions, relax assumptions one-by-one.

Assumptions (to be relaxed)

- ① permissioned. a priori known set of nodes $\{1, 2, \dots, n\}$ (known IP addresses).
- ② PKI ("public key infrastructure"). each node i has a pk_i/ski_i pair, pk_i known to all nodes up front.
- ③ synchronous. (i) all nodes share a global clock, time steps $0, 1, 2, 3, \dots$.
(ii) all msgs sent at time t arrive by time $t+1$ (in some arbitrary order)
- ④ all honest nodes: all nodes run intended protocol, no (intended or unintended) deviations.

Solution via Round-Robin Leaders

Idea: nodes take turns as "leaders." (e.g., round-robin, or choose randomly)

- leader sends ordered list of txs it knows about to all other nodes (plays the role of a "block")
- when node receives most recent leader's ordered list, appends it to local history

Note: satisfies consistency + liveness.

↓
nodes operate
in lockstep

↓
every node eventually
becomes leader, adds all
txs it knows about

Faulty/Byzantine Nodes

Definition: a node that is not honest is called **faulty**.

Types of faulty nodes:

- ① **crash fault.** (run honestly until some failure time, then stop entirely - no more messages sent)
- ② **omission fault.** (can selectively withhold messages it's supposed to send)
- ③ **Byzantine fault.** (can behave arbitrarily) (though still can't break cryptography)

Canonical poly: send conflicting messages to different nodes.

New assumption: For known parameter f , $\leq f$ nodes are Byzantine,
 $n-f$ nodes are honest.

The Byzantine Broadcast Problem

Idea: stick with the rotating leaders approach.

Subroutine: Byzantine broadcast. (BB)

- one node is the **sender** (known to all up front)
- Sender has a private input $r^* \in V$

'is guess of
what it is'

Goals

- ① termination. each honest node eventually halts w/ some value $v_i \in V$
- ② agreement. all honest nodes choose the same value v_i .
- ③ validity. if sender is honest, all honest v_i 's equal r^* .

SMR Reduces to BB

SMR Protocol: [given a Byzantine broadcast subroutine]

- ① take turns as leader (e.g., round-robin)
- ② run BB protocol (with sender = current leader), agree on a tx list L .
- ③ each node appends L to its local history

Why is the reduction correct?

- BB agreement \Rightarrow SMR consistency (every time step, all honest nodes add the same tx list)
- BB validity \Rightarrow SMR liveness
 - (if honest node knows about a tx, eventually will become the leader (sender \Rightarrow since honest, validity \Rightarrow all other honest nodes add that tx))

Intuition: The $f = 1$ Case ($n \geq 4$)

Proposed protocol: (to be run by honest nodes)

$t=0$: sender sends its value v^* to all other nodes (signed, as always)

$t=1$: nodes echo msg from sender to all other nodes (signed again)

$t=2$: each node i chooses output v_i by majority vote (≤ 1 vote from sender, $\leq n-2$ from other non-senders)
(if leader, output v^*) break ties consistently (e.g., lexicographically)

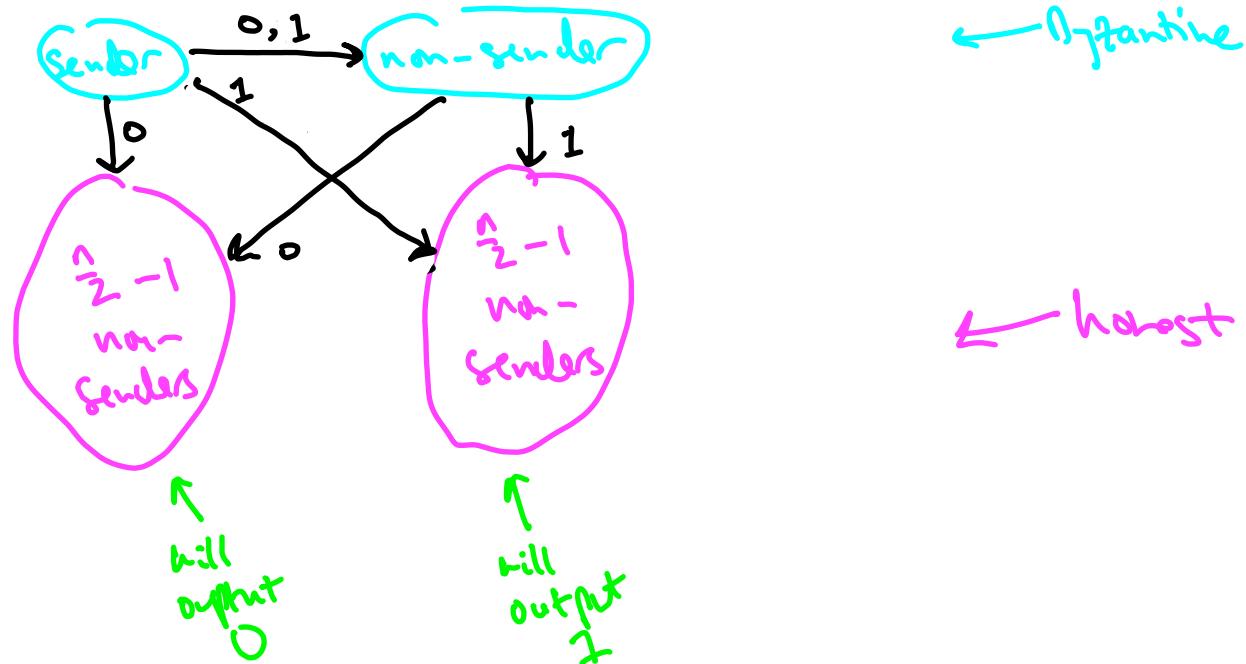
Note: validity + agreement (= termination) hold.

- honest leader \Rightarrow honest non-sender receives $> n-2$ votes for v^*

- Byzantine leader \Rightarrow all (honest) non-senders collect exact same set of votes, all output the same value ($\overset{\text{chosen by}}{\text{majority vote}}$)

Counterexample for $f = 2$

Claim: previous protocol does not satisfy agreement when $f = 2$.



The Dolev-Strong Protocol (I) (1983)

Definition: node i is convinced of value v at time t
if it receives a message such that:

- references the value v
- signed first by the sender
- signed also by $\geq t - 1$ other distinct nodes, none of which are i

The Dolev-Strong Protocol (II)

Protocol: (to be run by honest nodes)

t=0: Sender (with private input v^*) sends v^* (with its signature) to all other nodes

$t=1, 2, 3, \dots, f+1$: if node i convinced of value v at this time step by a message m , add i 's signature and echo to all other nodes

Final output: if node i convinced of exactly one value v , output v ; otherwise, output \perp .

(convinced of
0 or ≥ 2
values)

default value, e.g. empty list of txs

Theorem: under current assumptions (permissioned, PKI, synchronous), the Dolev-Strong protocol satisfies Validity + agreement.

Dolev-Strong Protocol: Validity

Claim: The Dolev-Strong protocol satisfies validity.

Proof: Assume sender is honest.

- \Rightarrow at $t=0$, will send v^* (with its signature) to all other nodes (received by time $t=1$)
- \Rightarrow all honest nodes convinced of v^* already at the $t=1$

Ideal signatures assumption \Rightarrow can't forge messages from the sender

- \Rightarrow no way to convince an honest node of any value $v \neq v^*$
- \Rightarrow all honest nodes output v^*

QED

Dolev-Strong Protocol: Agreement

Claim: the Dolev-Strong protocol satisfies agreement.

Sufficient: if an honest node i ever gets convinced of a value v

\Rightarrow all honest nodes convinced of v by end of protocol.

(\Rightarrow all ^{honest} nodes convinced of same set of values \Rightarrow all output the same thing)

Case 1: node i gets convinced of value v by message m at time $t < f+1$

\Rightarrow will add its signature to m + send to all other nodes

\Rightarrow all honest nodes convinced of v by the step $t+1 \leq f+1$.

Case 2: Convinced at time $f+1$.

\Rightarrow convinced by a message with $f+1$ distinct signatures

\Rightarrow one of those must have been provided by an honest node, ^{at some} _{earlier time step} $\leq f$ non-honest nodes

\Rightarrow all honest nodes by now convinced of v

QED

Dolev-Strong: How Big Can f Be?

Question: how does value of f affect the DS protocol + its analysis?

- protocol's duration scales linearly with f
- validity, agreement hold no matter what f is (very unusual)

Note: but in SM_L context, only useful if $f < n/2$.

- if $f \leq n/2$, can resolve conflicts through majority vote