

Part01:

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import rospy
from geometry_msgs.msg import Twist
import heapq as hq
import copy
import numpy as np
import math
from matplotlib import pyplot as plt
import cv2 as cv
from numpy import tan, deg2rad, rad2deg

SCALE_FACTOR = 2

BLUE = (255, 0, 0)
DARK_GREEN = (15, 168, 33)
GREEN = (0, 255, 0)
RED = (0, 0, 255)
YELLOW = (9, 227, 212)
BLACK = (0, 0, 0)
GRAY = (199, 198, 195)

# for coordinates
X = 0
Y = 1
THETA = 2

# map dimensions
X_MAX = 600
Y_MAX = 200
X_MAX_SCALED = X_MAX * SCALE_FACTOR
Y_MAX_SCALED = Y_MAX * SCALE_FACTOR

# used accessing node information
PARENT_COORDINATES = 4
COORDINATES = 5

# the turtlebot is 10.5 cm.
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# in an unscaled simulation, 1 pixel represents a 1cm x 1cm square
# multiply ROBOT_SIZE by SCALE_FACTOR to determine pixel representation of
robot
ROBOT_SIZE = 10
ROBOT_SIZE_SCALED = ROBOT_SIZE * SCALE_FACTOR
ROBOT_SIZE_SCALED = math.ceil(ROBOT_SIZE)

Open_List = []      # used to track all the open nodes
Closed_List = []    # {"C2G", "C2C", "TC", "node_index", "parent_coor",
"node_coor"} # used to track the closed node
Closed_Coor = set()  # closed coordinates. Used to quickly check if a
coordinate is closed
threshold_coor = set()
obstacle_points = set() # used to quickly look up if a point is in an
obstacle
map_points = set()      # used to quickly look up if a point is in the
map

node_index = 0

"""
draw_map()
creates a (200 * SCALE_FACTOR) * (600 * SCALE_FACTOR) numpy array that
represents the world map
the map represents a 2 meter by 6 meter world
using a SCALE_FACTOR of 2, each pixel represents a 50mm x 50mm square in
the world
"""
def draw_map():
    # Background
    background_color = BLACK
    map = np.zeros((Y_MAX_SCALED, X_MAX_SCALED, 3), np.uint8)
    map[:] = background_color

    # Map boarder
    map[0:ROBOT_SIZE_SCALED, 0:ROBOT_SIZE_SCALED, 0:3] = YELLOW # north edge

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    map[(Y_MAX_SCALED - ROBOT_SIZE_SCALED) : Y_MAX_SCALED , :
] = YELLOW      # south edge

    map[:,
0:ROBOT_SIZE_SCALED , ] = YELLOW      # east
edge

    map[:, (X_MAX_SCALED -
ROBOT_SIZE_SCALED) : X_MAX_SCALED ] = YELLOW      # west edge

    # box 1 boundary
    pts = np.array([[150 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 0 *
SCALE_FACTOR],
                    [150 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 125 *
SCALE_FACTOR + ROBOT_SIZE_SCALED],
                    [165 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 125 *
SCALE_FACTOR + ROBOT_SIZE_SCALED],
                    [165 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 0 *
SCALE_FACTOR]]),
                np.int32)
    cv.fillPoly(map, [pts], YELLOW)

    # box 1
    pts = np.array([[150 * SCALE_FACTOR, 0 * SCALE_FACTOR],
                    [150 * SCALE_FACTOR, 125 * SCALE_FACTOR],
                    [165 * SCALE_FACTOR, 125 * SCALE_FACTOR],
                    [165 * SCALE_FACTOR, 0 * SCALE_FACTOR]]),
                np.int32)
    cv.fillPoly(map, [pts], BLUE)

    # box 2 boundary
    pts = np.array([[250 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 200 *
SCALE_FACTOR],
                    [250 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 75 *
SCALE_FACTOR - ROBOT_SIZE_SCALED],
                    [265 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 75 *
SCALE_FACTOR - ROBOT_SIZE_SCALED],
                    [265 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 200 *
SCALE_FACTOR]]),
                np.int32)
    cv.fillPoly(map, [pts], YELLOW)

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    # box 2
    pts = np.array([[250 * SCALE_FACTOR, 200 * SCALE_FACTOR],
                    [250 * SCALE_FACTOR, 75 * SCALE_FACTOR],
                    [265 * SCALE_FACTOR, 75 * SCALE_FACTOR],
                    [265 * SCALE_FACTOR, 200 * SCALE_FACTOR]],
                    np.int32)
    cv.fillPoly(map, [pts], BLUE)

    # circle boundry
    cv.circle(map, (400 * SCALE_FACTOR, 90 * SCALE_FACTOR), 50 *
SCALE_FACTOR + ROBOT_SIZE_SCALED, YELLOW, -1)

    # circle
    cv.circle(map, (400 * SCALE_FACTOR, 90 * SCALE_FACTOR), 50 *
SCALE_FACTOR, BLUE, -1)

    return map

"""
get_valid_point_map()
input: np array representing the world map.  array values are the colors
on the map
output: np array of 1s and 0s representing if a point is valid to be
traveled in.
Function works by checking the color of pixel and determinining if that
color is valid or invalid
"""
def get_valid_point_map(color_map):
    valid_point_map = np.ones((Y_MAX_SCALED, X_MAX_SCALED), np.uint8)
    for x in range(0, X_MAX_SCALED):
        for y in range(0, Y_MAX_SCALED):
            pixel_color = tuple(color_map[y, x])
            if pixel_color == YELLOW or pixel_color == BLUE:
                valid_point_map[y, x] = 0
    return valid_point_map

def determine_valid_point(valid_point_map, coordinates):
    if not __point_is_inside_map(coordinates[X], coordinates[Y]):

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        return False
    if valid_point_map[coordinates[Y], coordinates[X]] == 1:
        return True
    else:
        return False

def __point_is_inside_map(x, y):
    if (x > X_MAX) or (x < 0):
        return False
    elif (y > Y_MAX) or (y < 0):
        return False
    else:
        return True

def __add_point(x, y, map, color):
    map[y, x] = color
    return map

def __draw_line(p1, p2, map, color):
    pts = np.array([[p1[0], p1[1]], [p2[0], p2[1]]],
                    dtype=np.int32)
    cv.fillPoly(map, [pts], color)

def draw_node(child_coordinates, parent_coordinates, map, color):
    child_coordinates = tuple(int(SCALE_FACTOR * _) for _ in
child_coordinates)
    cv.circle(map, child_coordinates, radius=3, color=color, thickness=-1)

    if (parent_coordinates is not None):
        parent_coordinates = tuple(int(SCALE_FACTOR * _) for _ in
parent_coordinates)
        cv.circle(map, parent_coordinates, radius=3, color=color,
thickness=-1)
        __draw_line(child_coordinates, parent_coordinates, map, color)

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#function that defines the goal position as a circle with a threshold.
# takes in the size of the robot as the threshold for the target
def point_in_goal(x, y):
    distance = math.sqrt((x-goal_position[0])**2 + (y-goal_position[1])**2)
    if distance <= ROBOT_SIZE_SCALED:
        return True
    else:
        return False

#function to calculate the cost to go to from the point to the goal in a
straight line
def C2G_func (n_position, g_position):
    C2G = round(((g_position[0]-n_position[0])**2 +
(g_position[1]-n_position[1])**2)**0.5, 1)
    return C2G

def explore(n,UL,UR):
    t = 0
    D=0
    Xn=n[5][X]
    Yn=n[5][Y]
    Thetan = deg2rad(n[5][THETA])

    # Xi, Yi,Thetai: Input point's coordinates
    # Xn, Yn, Thetan: End point coordintes
    while t<1:
        Thetan += (r / L) * (UR - UL) * dt * 2 * math.pi/60
        Xn += round((0.5*r * (UL + UR) * math.cos(Thetan) * dt)*2)/20
        Yn += round((0.5*r * (UL + UR) * math.sin(Thetan) * dt)*2)/20
        t = t + dt
        temp_point = (Xn, Yn)
        if temp_point in obstacle_points:
            return None

    # print("temp_point:", temp_point)
    Theta_n = round(rad2deg(Thetan), 2)
    theta_dot = (r / L) * (UR - UL) * 2*math.pi/60
    x_dot = 0.5*(r/100) * (UL + UR) * math.cos(Thetan)*2*math.pi/60
    y_dot = 0.5*(r/100) * (UL + UR) * math.sin(Thetan)*2*math.pi/60

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    new_position = round(Xn), round(Yn), round(Theta_n)
    D=round(D+ math.sqrt(math.pow((0.5*r * (UL + UR) * math.cos(Thetan) *
dt),2)+math.pow((0.5*r * (UL + UR) * math.sin(Thetan) * dt),2)), 2)
    new_C2C = round((n[1]+D),2)
    new_C2G = round((C2G_func(new_position, goal_position)),2)
    new_TC = round((new_C2C + new_C2G),2)

    point_vel = (float(x_dot), float(y_dot), float(theta_dot))
    new_node = (new_TC, new_C2C, new_C2G, node_index, n[5], new_position,
point_vel)

    return new_node

# main exploration function. starts by popping a node out of the open list
and checking the status of the
# popped node prior to expanding the search using the exploration
functions defined above.
# node: (C2G, C2C, TC, point_index, (x,y,theta)parent_coordinates,
(x,y,theta)coordinates)
def exploreNodes():
    global goal_found
    hq.heapify(Open_List)
    # print("OpenListLen:", len(Open_List))
    while Open_List:
        if goal_found:
            break
        popped_node = hq.heappop(Open_List)
        Closed_Coor.add((popped_node[5][0], popped_node[5][1]))

        #popped node is checked and added to the closed list as a dic
        check_popped_status(popped_node)
        popped_node_dic = {"TC": popped_node[0], "C2C": popped_node[1],
"C2G": popped_node[2], "node_index": popped_node[3], "parent_coor":
popped_node[4], "node_coor": popped_node[5], "vel": popped_node[6]}
        Closed_List.append(popped_node_dic)

        # checks if the newly created node falls within the defined map
points, outside the obstacles,
        # has not been closed already and its not within the threshold of
other points

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        # when all pass, it adds it to the open list

        #[RPM_1, RPM_1]
        new_node = explore(copy.deepcopy(popped_node), actions[0][0],
actions[0][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)

        #[RPM_1, 0]
        new_node = explore(copy.deepcopy(popped_node), actions[1][0],
actions[1][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)

        #[0, RPM_1]
        new_node = explore(copy.deepcopy(popped_node), actions[2][0],
actions[2][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)

        #[RPM_2, RPM_2]
        new_node = explore(copy.deepcopy(popped_node), actions[3][0],
actions[3][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:

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        if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
            if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                if threshold(new_node[5][0], new_node[5][1]):
                    checkTC(copy.deepcopy(popped_node), new_node)

#[RPM_2, 0]
new_node = explore(copy.deepcopy(popped_node), actions[4][0],
actions[4][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:
            if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                    if threshold(new_node[5][0], new_node[5][1]):
                        checkTC(copy.deepcopy(popped_node), new_node)

#[0, RPM_2]
new_node = explore(copy.deepcopy(popped_node), actions[5][0],
actions[5][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:
            if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                    if threshold(new_node[5][0], new_node[5][1]):
                        checkTC(copy.deepcopy(popped_node), new_node)

#[RPM_1, RPM_2]
new_node = explore(copy.deepcopy(popped_node), actions[6][0],
actions[6][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:
            if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                    if threshold(new_node[5][0], new_node[5][1]):
                        checkTC(copy.deepcopy(popped_node), new_node)

#[RPM_2, RPM_1]

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        new_node = explore(copy.deepcopy(popped_node), actions[7][0],
actions[7][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)
# print("OpenList:", Open_List)
return Open_List, Closed_Coor, Closed_List

#threshold function that checks if the newly created point falls within
the already explored points,
# angle must be the same. point can have multiple different angle
def threshold(nx, ny):
    if (nx, ny) in threshold_coor:
        return True
    else:
        threshold_coor.add((nx+0.5, ny))
        threshold_coor.add((nx+0.5, ny+0.5))
        threshold_coor.add((nx, ny+0.5))
        threshold_coor.add((nx-0.5, ny+0.5))
        threshold_coor.add((nx-0.5, ny))
        threshold_coor.add((nx-0.5, ny-0.5))
        threshold_coor.add((nx, ny-0.5))
        threshold_coor.add((nx, ny+0.5))
        return threshold_coor, False

#check if newly explored point has been explored previously, if so compare
C2C and update if the new C2C is
# lower than the one originally stored
def checkTC (on, n):
    global node_index
    for i, nodes in enumerate(Open_List):
        if (nodes[5][0],nodes[5][1]) == (n[5][0],n[5][1]):
            if n[0] < nodes[0]:
                new_node = (n[0], n[1], n[2], nodes[1], n[4], n[5], n[6])
                Open_List[i] = new_node

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        hq.heapify(Open_List)
        return Open_List
    else:
        node_index += 1
        new = (n[0], n[1], n[2], node_index, on[5], n[5], n[6])
        hq.heappush(Open_List, new)
    return Open_List

#function to check the status of the popped node, if it matches the goal
coordinates it starts the backtracking function
def check_popped_status (n):
    global goal_found
    if point_in_goal(n[5][0], n[5][1]):
        goal_node = {"TC": n[0], "C2C": n[1], "C2G": n[2], "node_index":
n[3], "parent_coor": n[4], "node_coor": n[5], "vel": n[6]}
        Closed_List.append(goal_node)
        print("goal node position:", n[5])
        print("target position:", goal_position)
        print("Goal found")
        print("destination info:", n)
        goal_found = True
        start_backtrack ()
    else:
        return(n)

#backtracking function that takes in the last closed node from the closed
list and runs a loop using
# the node coordinates and the parent coordinate to trace back the steps
leading to the start position
def start_backtrack ():
    print("Backtracking...")
    path_nodes = []
    path_coor = []
    path_vel = []
    current_node = Closed_List[-1]
    path_nodes.append(current_node)
    path_coor.append((current_node['node_coor'][X],
current_node['node_coor'][Y], current_node['node_coor'][THETA]))

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    path_vel.append((current_node['vel'][X], current_node['vel'][Y],
current_node['vel'][THETA]))
    print("First node used:", current_node)

# (TC, C2C, C2G, point_index, (x,y,theta)parent_coordinates,
(x,y,theta)coordinates, vel(x,y,theta))
    while current_node["parent_coor"] is not None:
        search_value = current_node["parent_coor"]
        for node in Closed_List:
            if node["node_coor"] == search_value:
                # If a matching value is found, assign the entire
dictionary as the new current_node
                current_node = node
                break

        path_nodes.append(current_node)
        path_coor.append((current_node['node_coor'][X],
current_node['node_coor'][Y], current_node['node_coor'][THETA]))
        path_vel.append((current_node['vel'][X], current_node['vel'][Y],
current_node['vel'][THETA]))

    path_nodes.reverse()
    path_coor.reverse()
    path_vel.reverse()
    # move(path_vel)
    run_visualization(path_coor)

def move(path_vel):

    vel_msg = Twist()
    if ROS == True:
        rospy.init_node('turtlebot3_control')
        vel_pub = rospy.Publisher('cmd_vel', Twist, queue_size=10)
        print('starting movement!')

    rate = rospy.Rate(.7825)

    counter = 0
    for i in path_vel:

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    vel_msg.linear.x = math.sqrt(i[0]**2 + i[1]**2)
    vel_msg.angular.z = (-1*i[2])

    print("[",counter,"]")
    counter+=1
    print(vel_msg)
    print()
    if ROS == True:
        vel_pub.publish(vel_msg)
        rate.sleep()

vel_msg.linear.x = 0
vel_msg.angular.z = 0
if ROS == True:
    vel_pub.publish(vel_msg)

# runs visulization of path plan using OpenCV.
# path shown is the solution path, with the connected nodes from the open
list
def run_visualization(path_coordinates):
    for node in path_coordinates:
        if not point_in_goal(node[X], node[Y]):
            draw_node((node[X], node[Y]), None, color_map, GREEN)
            for action in actions:
                plot_curve(node, action[0], action[1], color_map, GRAY)
            cv.imshow('A* Algorithm', color_map)
            cv.waitKey(200)
        else:
            #color goal node red
            node = path_coordinates[-1]
            draw_node((node[X], node[Y]), None, color_map, RED)

    cv.imshow('A* Algorithm', color_map)
    cv.waitKey(0)
    cv.destroyAllWindows()
    return

def plot_curve(node, UL,UR, map, color):
    t = 0

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D=0
Xn=node[X]
Yn=node[Y]
Thetan = deg2rad(node[THETA])

# Xi, Yi,Thetai: Input point's coordinates
# Xs, Ys: Start point coordinates for plot function
# Xn, Yn, Thetan: End point coordintes
while t<1:
    Xs = Xn
    Ys = Yn
    Thetan += (r / L) * (UR - UL) * dt * 2 * math.pi/60
    Xn += round((0.5*r * (UL + UR) * math.cos(Thetan) * dt)*2)/20
    Yn += round((0.5*r * (UL + UR) * math.sin(Thetan) * dt)*2)/20
    t = t + dt
    __draw_line((Xs*SCALE_FACTOR, Ys*SCALE_FACTOR), (Xn*SCALE_FACTOR,
Yn*SCALE_FACTOR), map, color)
    Xn = Xn
    Yn = Yn

if __name__ == '__main__':

    DEBUG = False
    ROS = False

    # user input required to fill out the following
    if DEBUG == False:
        start_x_position = int(input("enter start X position(20-580): "))
        start_y_position = int(input("enter start Y position(20-180): "))
        start_theta_position = int(input("enter start theta
position(0-360): "))
        print()
        goal_x_position = int(input("enter goal X position(20-580): "))
        goal_y_position = int(input("enter goal y position(20-180): "))
        RPM_1 = 10          # (rot/s)
        RPM_2 = 20          # (rot/s)
        r = 3.3             # (cm)
        L = 12              # (cm)
        dt = 0.1

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    clearance = 10
    ROBOT_SIZE_SCALED = ROBOT_SIZE + clearance * SCALE_FACTOR
else:
    start_x_position = 50
    start_y_position = 100
    start_theta_position = 0
    goal_x_position = 530
    goal_y_position = 180
    RPM_1 = 10          # (rot/s)
    RPM_2 = 20          # (rot/s)
    r = 3.3             # (cm)
    L = 12              # (cm)
    dt = 0.1
    # step_size = 1
    # ROBOT_SIZE = 5    # (mm) 105 is the size if the robot in mm. Will
not work for this simulation
    clearance = 10
    ROBOT_SIZE_SCALED = ROBOT_SIZE_SCALED + clearance * SCALE_FACTOR

    # 0 = left    1 = right
    actions = [[RPM_1, RPM_1], [RPM_1, 0], [0, RPM_1], [RPM_2, RPM_2],
[RPM_2, 0], [0, RPM_2], [RPM_1, RPM_2], [RPM_2, RPM_1]]

    start_position = (start_x_position, start_y_position,
start_theta_position)
    goal_position = (goal_x_position, goal_y_position)

    # initial values for the start node
    vel1 = (0, 0, 0)
    C2G1 = C2G_func(start_position, goal_position)
    C2C1 = 0
    TC1 = C2G1 + C2C1
    # (C2G, C2C, TC, point_index, (x,y,theta)parent_coordinates,
(x,y,theta)coordinates, velocity)
    start_node = (TC1, C2C1, C2G1, node_index, None, start_position, vel1)
    hq.heappush(Open_List, start_node)
    print("initial_Open_list:", Open_List)

    print("Drawing map...")
    color_map = draw_map()

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print("Determining open points and obstacle points...")
valid_point_map = get_valid_point_map(color_map)
# creat 2 sets, 1 containing all the possible points within map, 1
# containing all possible points within the obstacle spaces
# this will be used later to check the created points to see if they
# can be used
x_range = np.arange(0, 600, 0.5)
y_range = np.arange(0, 200, 0.5)
for x in np.arange(0, 600, 0.5):
    for y in np.arange(0, 200, 0.5):
        if valid_point_map[int(y * SCALE_FACTOR), int(x *
SCALE_FACTOR)] == 1:
            map_points.add((x, y))
        else:
            obstacle_points.add((x, y))

if (start_position[0], start_position[1]) in obstacle_points:
    print("start point selected is in obstacle space, try again")
    exit()

if (start_position[0], start_position[1]) not in map_points:
    print("start point selected is outside the map, try again")
    exit()

if (goal_position[0], goal_position[1]) in obstacle_points:
    print(goal_position)
    print("goal point selected is in obstacle space, try again")
    exit()

if (goal_position[0], goal_position[1]) not in map_points:
    print("goal point selected is outside the map, try again")
    exit()

goal_found = False
print("start node:", start_node)
print("starting exploration")
while not goal_found:
    exploreNodes()

```


Part02:

```
#!/usr/bin/env python

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# ARISING IN ANY WAY OUT OF THE USE OF THIS SOFTWARE, EVEN IF ADVISED OF
THE
# POSSIBILITY OF SUCH DAMAGE.

import rospy
from geometry_msgs.msg import Twist
import heapq as hq
```

```
import copy
import numpy as np
import math
from matplotlib import pyplot as plt
import cv2 as cv
from numpy import tan, deg2rad, rad2deg

SCALE_FACTOR = 2

BLUE = (255, 0, 0)
DARK_GREEN = (15, 168, 33)
GREEN = (0, 255, 0)
RED = (0, 0, 255)
YELLOW = (9, 227, 212)
BLACK = (0, 0, 0)
GRAY = (199, 198, 195)

# for coordinates
X = 0
Y = 1
THETA = 2

# map dimensions
X_MAX = 600
Y_MAX = 200
X_MAX_SCALED = X_MAX * SCALE_FACTOR
Y_MAX_SCALED = Y_MAX * SCALE_FACTOR

# used accessing node information
PARENT_COORDINATES = 4
COORDINATES = 5

# the turtlebot is 10.5 cm.
# in an unscaled simulation, 1 pixel represents a 1cm x 1cm square
# multiply ROBOT_SIZE by SCALE_FACTOR to determine pixel representation of
robot
ROBOT_SIZE = 10.5
ROBOT_SIZE_SCALED = ROBOT_SIZE * SCALE_FACTOR
```

```

ROBOT_SIZE_SCALED = math.ceil(ROBOT_SIZE)

Open_List = []      # used to track all the open nodes
Closed_List = []    # {"C2G", "C2C", "TC", "node_index", "parent_coor",
"node_coor"} # used to track the closed node
Closed_Coor = set() # closed coordinates. Used to quickly check if a
coordinate is closed
threshold_coor = set()
obstacle_points = set() # used to quickly look up if a point is in an
obstacle
map_points = set()      # used to quickly look up if a point is in the
map

node_index = 0

"""
draw_map()
creates a (200 * SCALE_FACTOR) * (600 * SCALE_FACTOR) numpy array that
represents the world map
the map represents a 2 meter by 6 meter world
using a SCALE_FACTOR of 2, each pixel represents a 50mm x 50mm square in
the world
"""
def draw_map():
    # Background
    background_color = BLACK
    map = np.zeros((Y_MAX_SCALED, X_MAX_SCALED, 3), np.uint8)
    map[:] = background_color

    # Map boarder
    map[0:ROBOT_SIZE_SCALED, :, :] = YELLOW # north edge
    map[(Y_MAX_SCALED - ROBOT_SIZE_SCALED) : Y_MAX_SCALED, :, :] = YELLOW # south edge
    map[:, 0:ROBOT_SIZE_SCALED, :] = YELLOW # west edge
    map[:, Y_MAX_SCALED - ROBOT_SIZE_SCALED : Y_MAX_SCALED, :] = YELLOW # east edge

```

```

        map[:, (X_MAX_SCALED -
ROBOT_SIZE_SCALED) : X_MAX_SCALED ] = YELLOW      # west edge

    # box 1 boundary
    pts = np.array([[150 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 0 *
SCALE_FACTOR],
                    [150 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 125 *
SCALE_FACTOR + ROBOT_SIZE_SCALED],
                    [165 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 125 *
SCALE_FACTOR + ROBOT_SIZE_SCALED],
                    [165 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 0 *
SCALE_FACTOR]]),
                  np.int32)
    cv.fillPoly(map, [pts], YELLOW)

    # box 1
    pts = np.array([[150 * SCALE_FACTOR, 0 * SCALE_FACTOR],
                    [150 * SCALE_FACTOR, 125 * SCALE_FACTOR],
                    [165 * SCALE_FACTOR, 125 * SCALE_FACTOR],
                    [165 * SCALE_FACTOR, 0 * SCALE_FACTOR]]),
                  np.int32)
    cv.fillPoly(map, [pts], BLUE)

    # box 2 boundary
    pts = np.array([[250 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 200 *
SCALE_FACTOR],
                    [250 * SCALE_FACTOR - ROBOT_SIZE_SCALED, 75 *
SCALE_FACTOR - ROBOT_SIZE_SCALED],
                    [265 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 75 *
SCALE_FACTOR - ROBOT_SIZE_SCALED],
                    [265 * SCALE_FACTOR + ROBOT_SIZE_SCALED, 200 *
SCALE_FACTOR]]),
                  np.int32)
    cv.fillPoly(map, [pts], YELLOW)

    # box 2
    pts = np.array([[250 * SCALE_FACTOR, 200 * SCALE_FACTOR],
                    [250 * SCALE_FACTOR, 75 * SCALE_FACTOR],
                    [265 * SCALE_FACTOR, 75 * SCALE_FACTOR],
                    [265 * SCALE_FACTOR, 200 * SCALE_FACTOR]]),

```

```

        np.int32)
    cv.fillPoly(map, [pts], BLUE)

    # circle boundry
    cv.circle(map, (400 * SCALE_FACTOR, 90 * SCALE_FACTOR), 50 *
SCALE_FACTOR + ROBOT_SIZE_SCALED, YELLOW, -1)

    # circle
    cv.circle(map, (400 * SCALE_FACTOR, 90 * SCALE_FACTOR), 50 *
SCALE_FACTOR, BLUE, -1)

    return map

"""
get_valid_point_map()
input: np array representing the world map.  array values are the colors
on the map
output: np array of 1s and 0s representing if a point is valid to be
traveled in.
Function works by checking the color of pixel and determinining if that
color is valid or invalid
"""
def get_valid_point_map(color_map):
    valid_point_map = np.ones((Y_MAX_SCALED, X_MAX_SCALED), np.uint8)
    for x in range(0, X_MAX_SCALED):
        for y in range(0, Y_MAX_SCALED):
            pixel_color = tuple(color_map[y, x])
            if pixel_color == YELLOW or pixel_color == BLUE:
                valid_point_map[y, x] = 0
    return valid_point_map

def determine_valid_point(valid_point_map, coordinates):
    if not __point_is_inside_map(coordinates[X], coordinates[Y]):
        return False
    if valid_point_map[coordinates[Y], coordinates[X]] == 1:
        return True
    else:
        return False

```

```

def __point_is_inside_map(x, y):
    if (x > X_MAX) or (x < 0):
        return False
    elif (y > Y_MAX) or (y < 0):
        return False
    else:
        return True

def __add_point(x, y, map, color):
    map[y, x] = color
    return map

def __draw_line(p1, p2, map, color):
    pts = np.array([[p1[0], p1[1]], [p2[0], p2[1]]],
                    np.int32)
    cv.fillPoly(map, [pts], color)

def draw_node(child_coordinates, parent_coordinates, map, color):

    child_coordinates = tuple(int(SCALE_FACTOR * _) for _ in
child_coordinates)
    cv.circle(map, child_coordinates, radius=3, color=color, thickness=-1)

    if (parent_coordinates is not None):
        parent_coordinates = tuple(int(SCALE_FACTOR * _) for _ in
parent_coordinates)
        cv.circle(map, parent_coordinates, radius=3, color=color,
thickness=-1)
        __draw_line(child_coordinates, parent_coordinates, map, color)

#function that defines the goal position as a circle with a threshold.
# takes in the size of the robot as the threshold for the target
def point_in_goal(x, y):
    distance = math.sqrt((x-goal_position[0])**2 + (y-goal_position[1])**2)
    if distance <= ROBOT_SIZE_SCALED:

```

```

        return True
    else:
        return False

#function to calculate the cost to go to from the point to the goal in a
straight line
def C2G_func (n_position, g_position):
    C2G = round(((g_position[0]-n_position[0])**2 +
(g_position[1]-n_position[1])**2)**0.5, 1)
    return C2G

def explore(n,UL,UR):
    t = 0
    D=0
    Xn=n[5][X]
    Yn=n[5][Y]
    Thetan = deg2rad(n[5][THETA])

    # Xi, Yi,Thetai: Input point's coordinates
    # Xn, Yn, Thetan: End point coordintes
    while t<1:
        Thetan += (r / L) * (UR - UL) * dt * 2 * math.pi/60
        Xn += round((0.5*r * (UL + UR) * math.cos(Thetan) * dt)*2)/20
        Yn += round((0.5*r * (UL + UR) * math.sin(Thetan) * dt)*2)/20
        t = t + dt
        temp_point = (Xn, Yn)
        if temp_point in obstacle_points:
            return None

    # print("temp_point:", temp_point)
    Theta_n = round(rad2deg(Thetan), 2)
    theta_dot = (r / L) * (UR - UL) * 2*math.pi/60
    x_dot = 0.5*(r/100) * (UL + UR) * math.cos(Thetan)*2*math.pi/60
    y_dot = 0.5*(r/100) * (UL + UR) * math.sin(Thetan)*2*math.pi/60
    new_position = round(Xn), round(Yn), round(Theta_n)
    D=round(D+ math.sqrt(math.pow((0.5*r * (UL + UR) * math.cos(Thetan) *
dt),2)+math.pow((0.5*r * (UL + UR) * math.sin(Thetan) * dt),2)), 2)
    new_C2C = round((n[1]+D),2)
    new_C2G = round((C2G_func(new_position, goal_position)),2)

```

```

new_TC = round((new_C2C + new_C2G),2)

point_vel = (float(x_dot), float(y_dot), float(theta_dot))
new_node = (new_TC, new_C2C, new_C2G, node_index, n[5], new_position,
point_vel)

return new_node

# main exploration function. starts by popping a node out of the open list
and checking the status of the
# popped node prior to expanding the search using the exploration
functions defined above.
# node: (C2G, C2C, TC, point_index, (x,y,theta)parent_coordinates,
(x,y,theta)coordinates)
def exploreNodes():
    global goal_found
    hq.heapify(Open_List)
    # print("OpenListLen:", len(Open_List))
    while Open_List:
        if goal_found:
            break
        popped_node = hq.heappop(Open_List)
        Closed_Coor.add((popped_node[5][0], popped_node[5][1]))

        #popped node is checked and added to the closed list as a dic
        check_popped_status(popped_node)
        popped_node_dic = {"TC": popped_node[0], "C2C": popped_node[1],
"C2G": popped_node[2], "node_index": popped_node[3], "parent_coor":
popped_node[4], "node_coor": popped_node[5], "vel": popped_node[6]}
        Closed_List.append(popped_node_dic)

        # checks if the newly created node falls within the defined map
points, outside the obstacles,
        # has not been closed already and its not within the threshold of
other points
        # when all pass, it adds it to the open list

        #[RPM_1, RPM_1]
        new_node = explore(copy.deepcopy(popped_node), actions[0][0],
actions[0][1])

```



```

        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)

# [RPM_1, 0]
new_node = explore(copy.deepcopy(popped_node), actions[1][0],
actions[1][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)

# [0, RPM_1]
new_node = explore(copy.deepcopy(popped_node), actions[2][0],
actions[2][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):
                            checkTC(copy.deepcopy(popped_node), new_node)

# [RPM_2, RPM_2]
new_node = explore(copy.deepcopy(popped_node), actions[3][0],
actions[3][1])
        if new_node is not None:
            if ((new_node[5][0], new_node[5][1])) in map_points:
                if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                    if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                        if threshold(new_node[5][0], new_node[5][1]):

```

```

        checkTC(copy.deepcopy(popped_node), new_node)

    #[RPM_2, 0]
    new_node = explore(copy.deepcopy(popped_node), actions[4][0],
actions[4][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:
            if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                    if threshold(new_node[5][0], new_node[5][1]):
                        checkTC(copy.deepcopy(popped_node), new_node)

    #[0, RPM_2]
    new_node = explore(copy.deepcopy(popped_node), actions[5][0],
actions[5][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:
            if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                    if threshold(new_node[5][0], new_node[5][1]):
                        checkTC(copy.deepcopy(popped_node), new_node)

    #[RPM_1, RPM_2]
    new_node = explore(copy.deepcopy(popped_node), actions[6][0],
actions[6][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:
            if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
                if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
                    if threshold(new_node[5][0], new_node[5][1]):
                        checkTC(copy.deepcopy(popped_node), new_node)

    #[RPM_2, RPM_1]
    new_node = explore(copy.deepcopy(popped_node), actions[7][0],
actions[7][1])
    if new_node is not None:
        if ((new_node[5][0], new_node[5][1])) in map_points:

```

```

        if ((new_node[5][0], new_node[5][1])) not in
obstacle_points:
        if ((new_node[5][0], new_node[5][1])) not in
Closed_Coor:
        if threshold(new_node[5][0], new_node[5][1]):
            checkTC(copy.deepcopy(popped_node), new_node)
        # print("OpenList:", Open_List)
        return Open_List, Closed_Coor, Closed_List

#threshold function that checks if the newly created point falls within
the already explored points,
# angle must be the same. point can have multiple different angle
def threshold(nx, ny):
    if (nx, ny) in threshold_coor:
        return True
    else:
        threshold_coor.add((nx+0.5, ny))
        threshold_coor.add((nx+0.5, ny+0.5))
        threshold_coor.add((nx, ny+0.5))
        threshold_coor.add((nx-0.5, ny+0.5))
        threshold_coor.add((nx-0.5, ny))
        threshold_coor.add((nx-0.5, ny-0.5))
        threshold_coor.add((nx, ny-0.5))
        threshold_coor.add((nx, ny+0.5))
        return threshold_coor, False

#check if newly explored point has been explored previously, if so compare
C2C and update if the new C2C is
# lower than the one originally stored
def checkTC (on, n):
    global node_index
    for i, nodes in enumerate(Open_List):
        if (nodes[5][0],nodes[5][1]) == (n[5][0],n[5][1]):
            if n[0] < nodes[0]:
                new_node = (n[0], n[1], n[2], nodes[1], n[4], n[5], n[6])
                Open_List[i] = new_node
                heapq.heapify(Open_List)
            return Open_List
    else:
        node_index += 1

```

```

        new = (n[0], n[1], n[2], node_index, on[5], n[5], n[6])
        hq.heappush(Open_List, new)
    return Open_List

#function to check the status of the popped node, if it matches the goal
coordinates it starts the backtracking function
def check_popped_status (n):
    global goal_found
    if point_in_goal(n[5][0], n[5][1]):
        goal_node = {"TC": n[0], "C2C": n[1], "C2G": n[2], "node_index":
n[3], "parent_coor": n[4], "node_coor": n[5], "vel": n[6]}
        Closed_List.append(goal_node)
        print("goal node position:", n[5])
        print("target position:", goal_position)
        print("Goal found")
        print("destination info:", n)
        goal_found = True
        start_backtrack ()
    else:
        return(n)

#backtracking function that takes in the last closed node from the closed
list and runs a loop using
# the node coordinates and the parent coordinate to trace back the steps
leading to the start position
def start_backtrack ():
    print("Backtracking...")
    path_nodes = []
    path_coor = []
    path_vel = []
    current_node = Closed_List[-1]
    path_nodes.append(current_node)
    path_coor.append((current_node['node_coor'][X],
current_node['node_coor'][Y], current_node['node_coor'][THETA]))
    path_vel.append((current_node['vel'][X], current_node['vel'][Y],
current_node['vel'][THETA]))
    print("First node used:", current_node)

```

```

# (TC, C2C, C2G, point_index, (x,y,theta)parent_coordinates,
(x,y,theta)coordinates, vel(x,y,theta))
    while current_node["parent_coor"] is not None:
        search_value = current_node["parent_coor"]
        for node in Closed_List:
            if node["node_coor"] == search_value:
                # If a matching value is found, assign the entire
dictionary as the new current_node
                current_node = node
                break
        path_nodes.append(current_node)
        path_coor.append((current_node['node_coor'][X],
current_node['node_coor'][Y], current_node['node_coor'][THETA]))
        path_vel.append((current_node['vel'][X], current_node['vel'][Y],
current_node['vel'][THETA]))

    path_nodes.reverse()
    path_coor.reverse()
    path_vel.reverse()
    move(path_vel)
    run_visualization(path_coor)

def move(path_vel):

    vel_msg = Twist()
    if ROS == True:
        rospy.init_node('turtlebot3_control')
        vel_pub = rospy.Publisher('cmd_vel', Twist, queue_size=10)
        print('starting movement!')

    rate = rospy.Rate(.775)

    counter = 0
    for i in path_vel:
        vel_msg.linear.x = math.sqrt(i[0]**2 + i[1]**2)
        vel_msg.angular.z = (-1*i[2])

        print("[",counter,"]")

```

```

        counter+=1
        print(vel_msg)
        print()
        if ROS == True:
            vel_pub.publish(vel_msg)
            rate.sleep()

vel_msg.linear.x = 0
vel_msg.angular.z = 0
if ROS == True:
    vel_pub.publish(vel_msg)

# runs visulization of path plan using OpenCV.
# path shown is the solution path, with the connected nodes from the open
list
def run_visualization(path_coordinates):
    for node in path_coordinates:
        if not point_in_goal(node[X], node[Y]):
            draw_node((node[X], node[Y]), None, color_map, GREEN)
            for action in actions:
                plot_curve(node, action[0], action[1], color_map, GRAY)
            cv.imshow('A* Algorithm', color_map)
            cv.waitKey(200)
        else:
            #color goal node red
            node = path_coordinates[-1]
            draw_node((node[X], node[Y]), None, color_map, RED)

    cv.imshow('A* Algorithm', color_map)
    cv.waitKey(0)
    cv.destroyAllWindows()
    return

def plot_curve(node, UL, UR, map, color):
    t = 0
    D=0
    Xn=node[X]
    Yn=node[Y]
    Thetan = deg2rad(node[THETA])

```

```

# Xi, Yi, Thetai: Input point's coordinates
# Xs, Ys: Start point coordinates for plot function
# Xn, Yn, Thetan: End point coordintes
while t<1:
    Xs = Xn
    Ys = Yn
    Thetan += (r / L) * (UR - UL) * dt * 2 * math.pi/60
    Xn += round((0.5*r * (UL + UR) * math.cos(Thetan) * dt)*2)/20
    Yn += round((0.5*r * (UL + UR) * math.sin(Thetan) * dt)*2)/20
    t = t + dt
    __draw_line((Xs*SCALE_FACTOR, Ys*SCALE_FACTOR), (Xn*SCALE_FACTOR,
Yn*SCALE_FACTOR), map, color)
    Xn = Xn
    Yn = Yn

if __name__ == '__main__':

    DEBUG = True
    ROS = True

    # user input required to fill out the following
    if DEBUG == False:
        start_x_position = int(input("enter start X position(0-600): "))
        start_y_position = int(input("enter start Y position(0-250): "))
        start_theta_position = int(input("enter start theta
position(0-360): "))
        print()
        goal_x_position = int(input("enter goal X position(0-600): "))
        goal_y_position = int(input("enter goal y position(0-250): "))
        print()
        RPM_1 = int(input("enter RPM for wheel rotation speed 1 (0-100):
"))
        RPM_2 = int(input("enter RPM for wheel rotation speed 2 (0-100):
"))
        print()
        step_size = int(input("enter step size (0-10): "))
        clearance = int(input("enter the clearance used for navigation (in
mm): "))

```

```

    ROBOT_SIZE_SCALED = ROBOT_SIZE + clearance * SCALE_FACTOR
else:
    start_x_position = 50
    start_y_position = 100
    start_theta_position = 0
    goal_x_position = 530
    goal_y_position = 180
    RPM_1 = 10          # (rot/s)
    RPM_2 = 20          # (rot/s)
    r = 3.3             # (cm)
    L = 12              # (cm)
    dt = 0.1
    # step_size = 1
    # ROBOT_SIZE = 5    # (mm) 105 is the size if the robot in mm. Will
not work for this simulation
    clearance = 10
    ROBOT_SIZE_SCALED = ROBOT_SIZE_SCALED + clearance * SCALE_FACTOR

    # 0 = left    1 = right
    actions = [[RPM_1, RPM_1], [RPM_1, 0], [0, RPM_1], [RPM_2, RPM_2],
[RPM_2, 0], [0, RPM_2], [RPM_1, RPM_2], [RPM_2, RPM_1]]

    start_position = (start_x_position, start_y_position,
start_theta_position)
    goal_position = (goal_x_position, goal_y_position)

    # initial values for the start node
    vel1 = (0, 0, 0)
    C2G1 = C2G_func(start_position, goal_position)
    C2C1 = 0
    TC1 = C2G1 + C2C1
    # (C2G, C2C, TC, point_index, (x,y,theta)parent_coordinates,
(x,y,theta)coordinates, velocity)
    start_node = (TC1, C2C1, C2G1, node_index, None, start_position, vel1)
    hq.heappush(Open_List, start_node)
    print("initial_Open_list:", Open_List)

    print("Drawing map...")
    color_map = draw_map()

```



```

print("Determining open points and obstacle points...")
valid_point_map = get_valid_point_map(color_map)
# creat 2 sets, 1 containing all the possible points within map, 1
# containing all possible points within the obstacle spaces
# this will be used later to check the created points to see if they
# can be used
x_range = np.arange(0, 600, 0.5)
y_range = np.arange(0, 200, 0.5)
for x in np.arange(0, 600, 0.5):
    for y in np.arange(0, 200, 0.5):
        if valid_point_map[int(y * SCALE_FACTOR), int(x *
SCALE_FACTOR)] == 1:
            map_points.add((x, y))
        else:
            obstacle_points.add((x, y))

if (start_position[0], start_position[1]) in obstacle_points:
    print("start point selected is in obstacle space, try again")
    exit()

if (start_position[0], start_position[1]) not in map_points:
    print("start point selected is outside the map, try again")
    exit()

if (goal_position[0], goal_position[1]) in obstacle_points:
    print(goal_position)
    print("goal point selected is in obstacle space, try again")
    exit()

if (goal_position[0], goal_position[1]) not in map_points:
    print("goal point selected is outside the map, try again")
    exit()

goal_found = False
print("start node:", start_node)
print("starting exploration")
while not goal_found:
    exploreNodes()

```