

# *ISB 2025 Tutorial*

## Musculoskeletal simulations with biophysical muscle models

Lena Ting, Surabhi Simha, Hansol Ryu,  
Tim van der Zee, Friedl De Groote



*Funded by NIH HD HD90642 + NIH software supplement*



**Surabhi Simha**  
ISB talk (T 10am)  
Tuning muscle spindle  
signals for locomotion

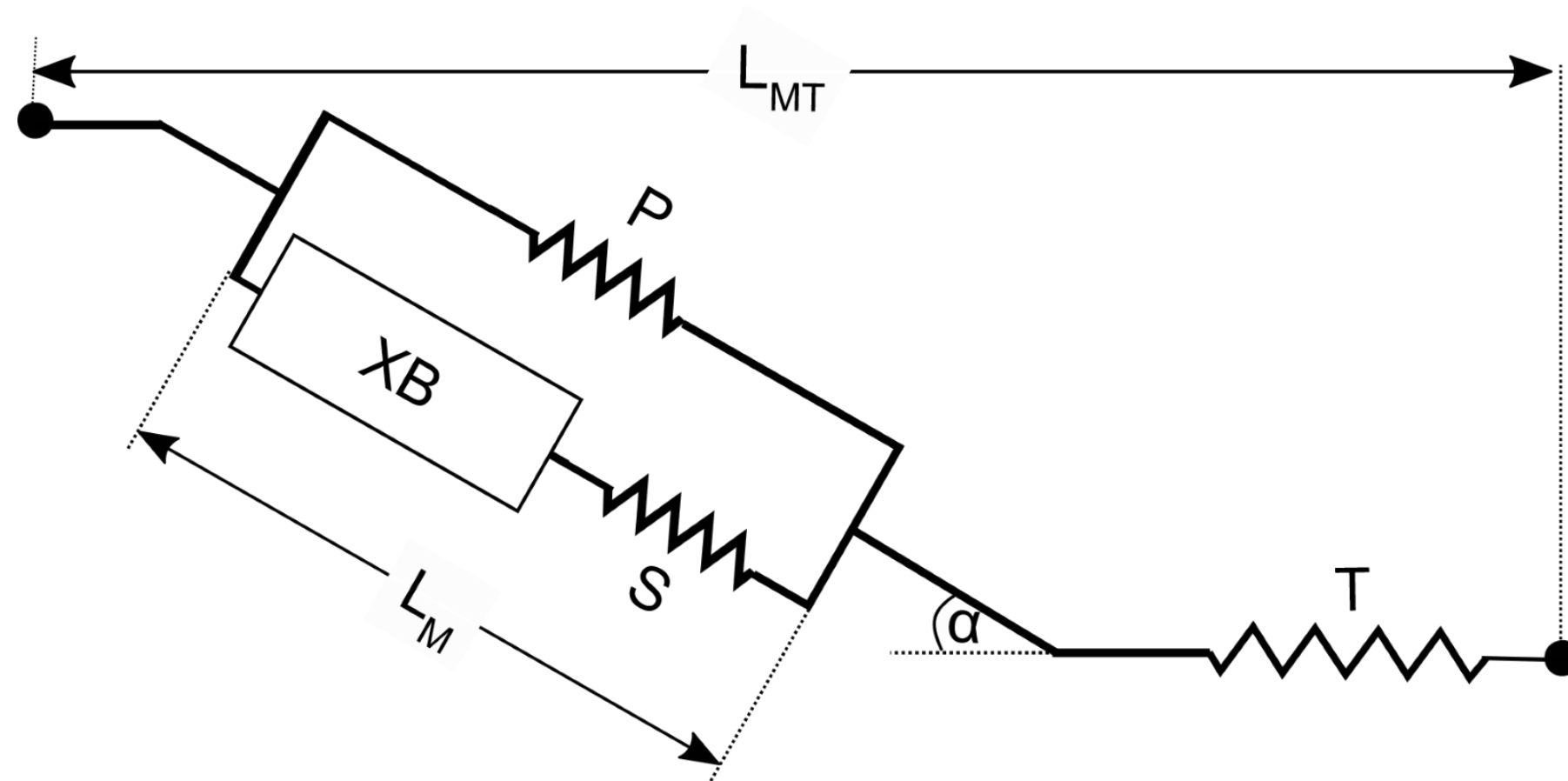


**Tim van der Zee**  
ISB talk (M 2:50), poster (W 5pm)  
Biophysical muscle models  
for musculoskeletal simulation

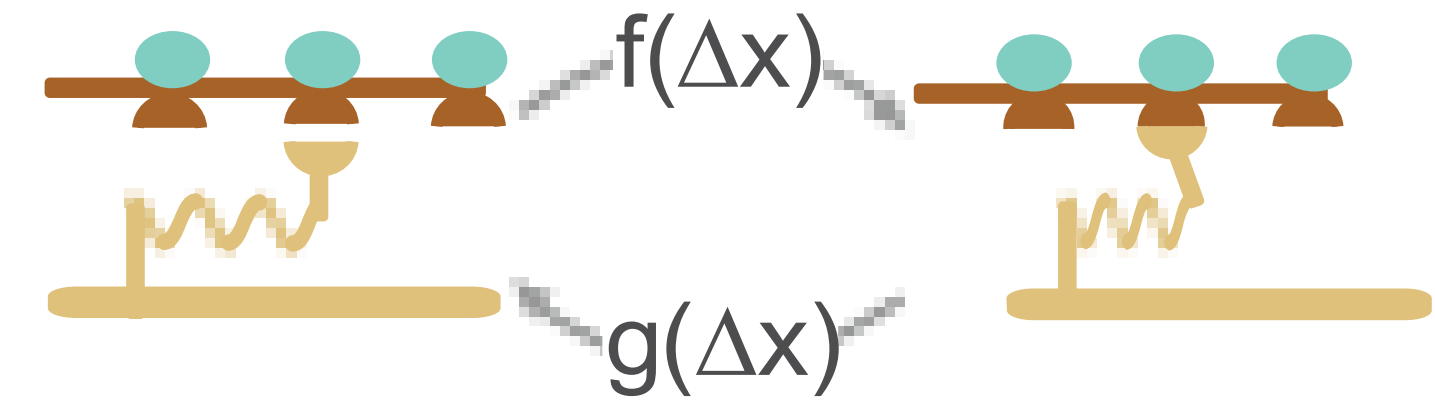


**Hansol Ryu**  
ISB talk (M 3:20pm)  
Biophysical model for  
postural control

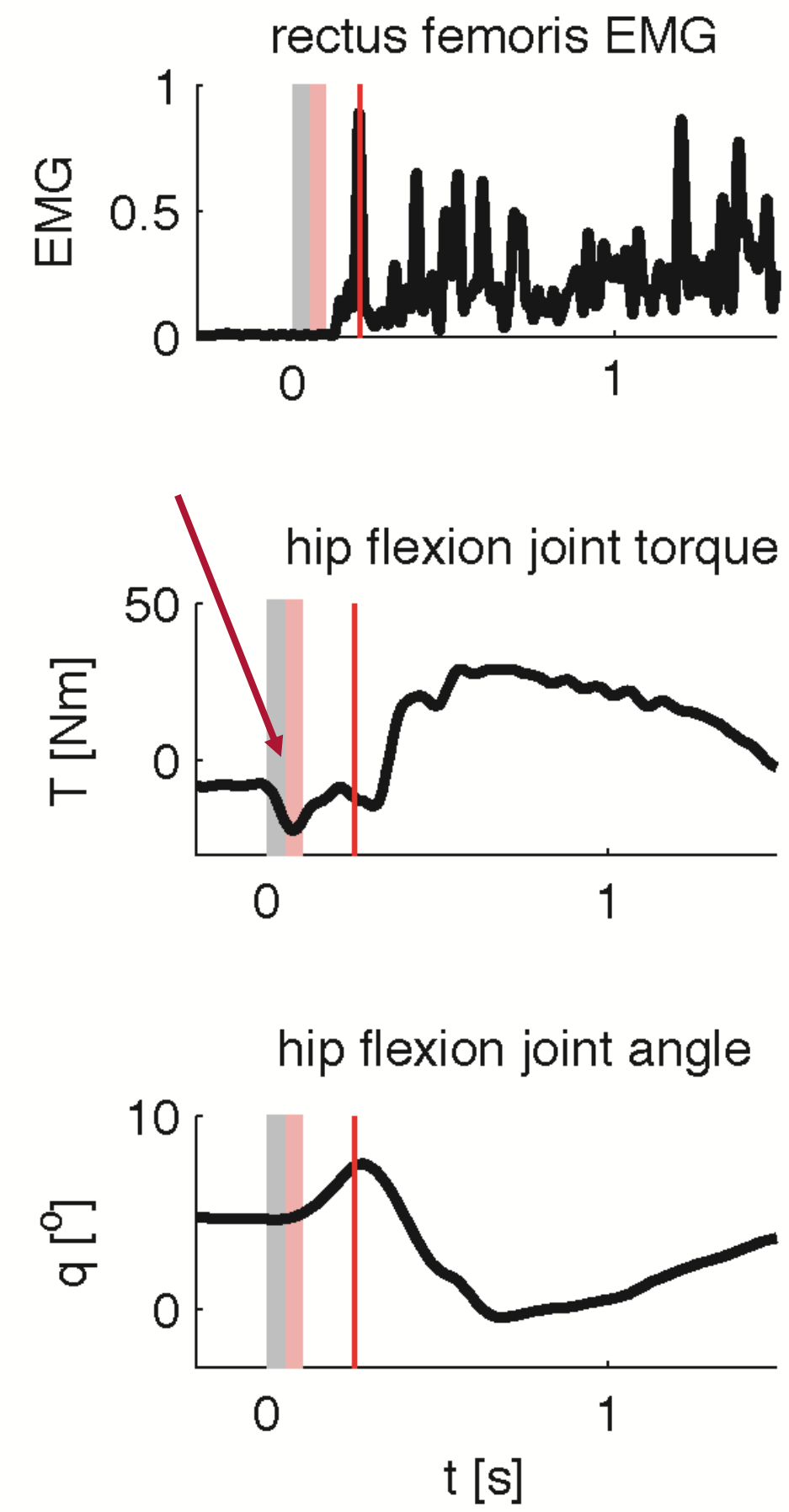
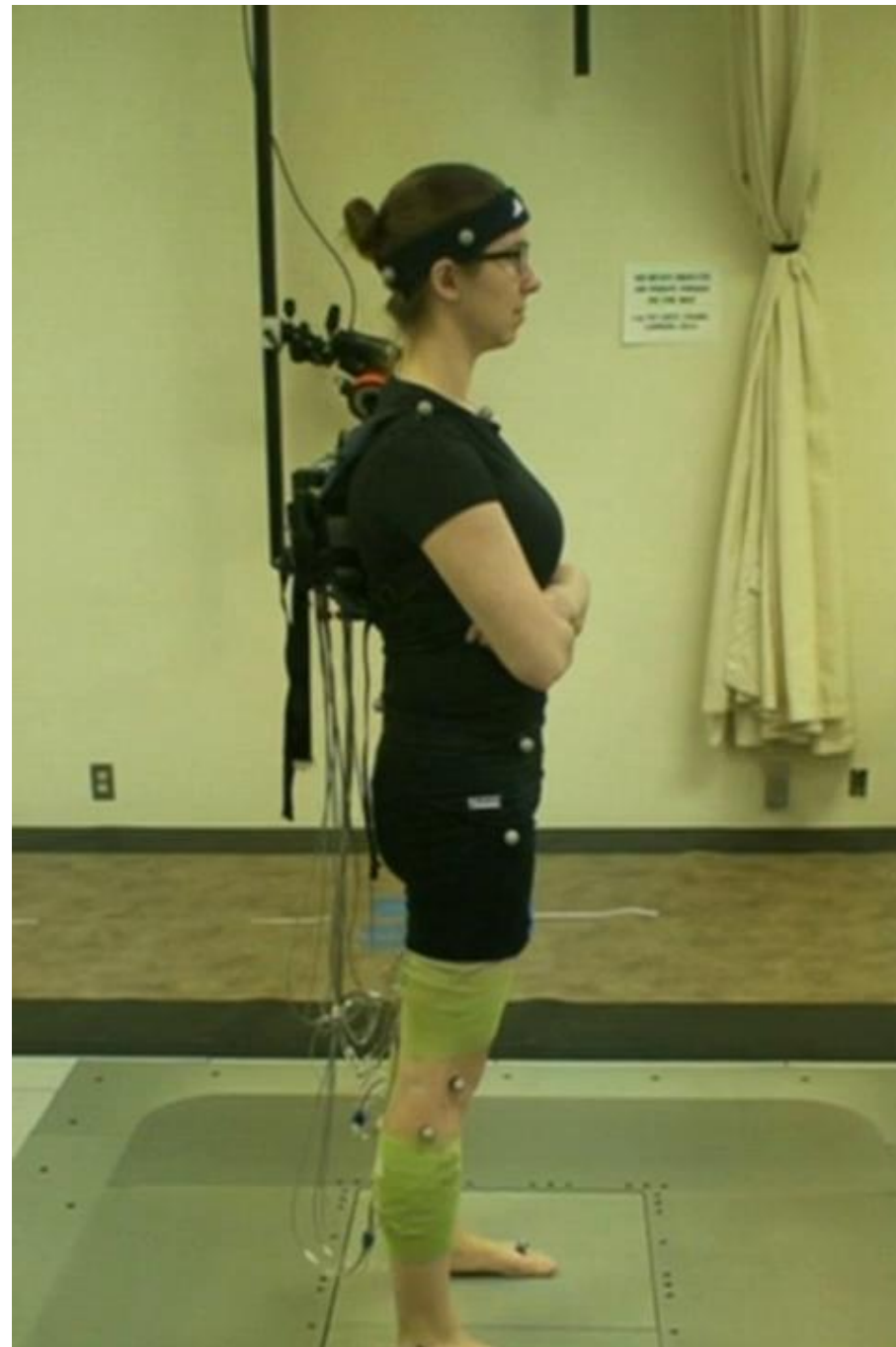
Transient force properties of muscle are needed to use musculoskeletal modeling to understand unsteady movement



Zajac 1989

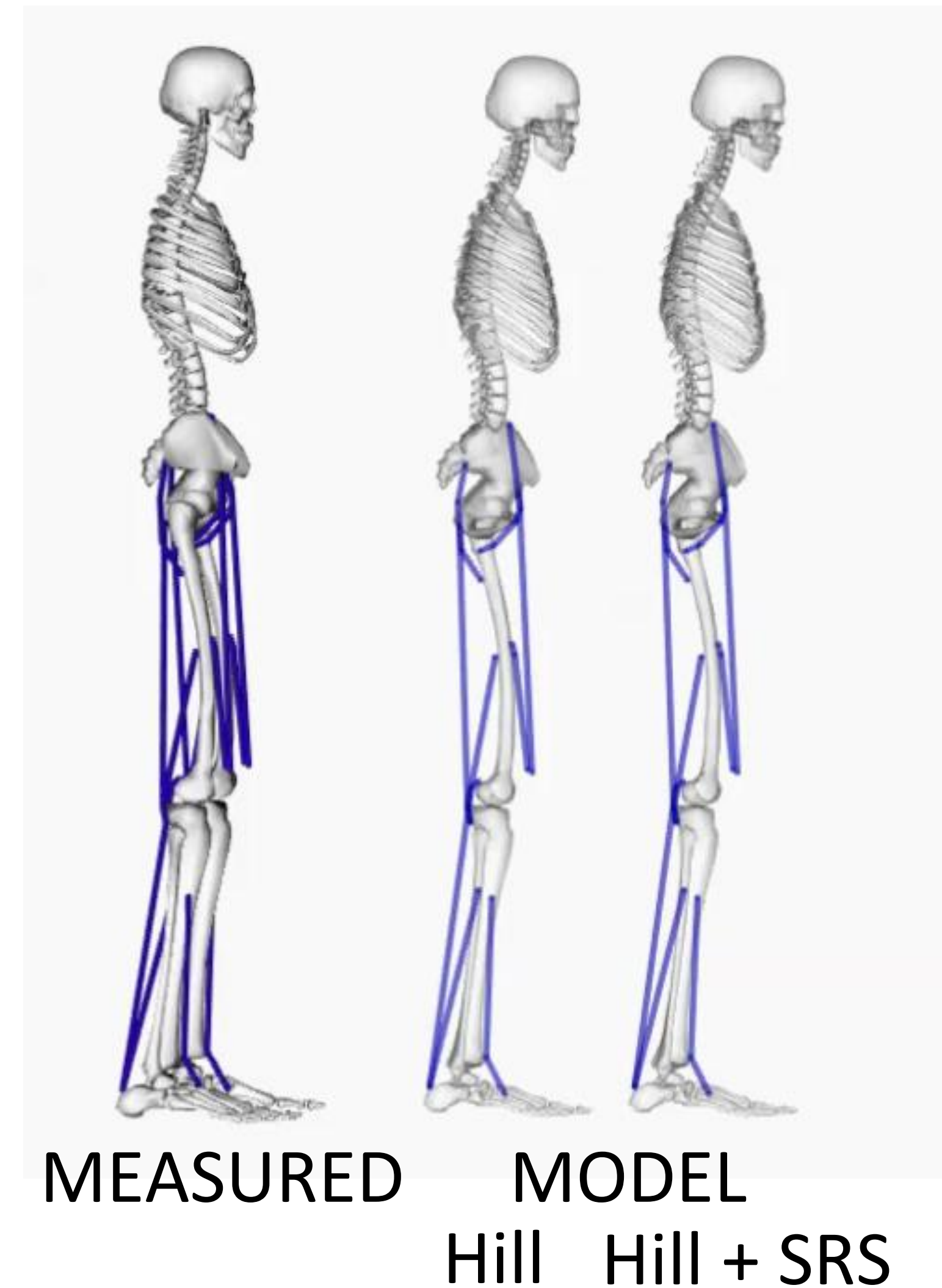
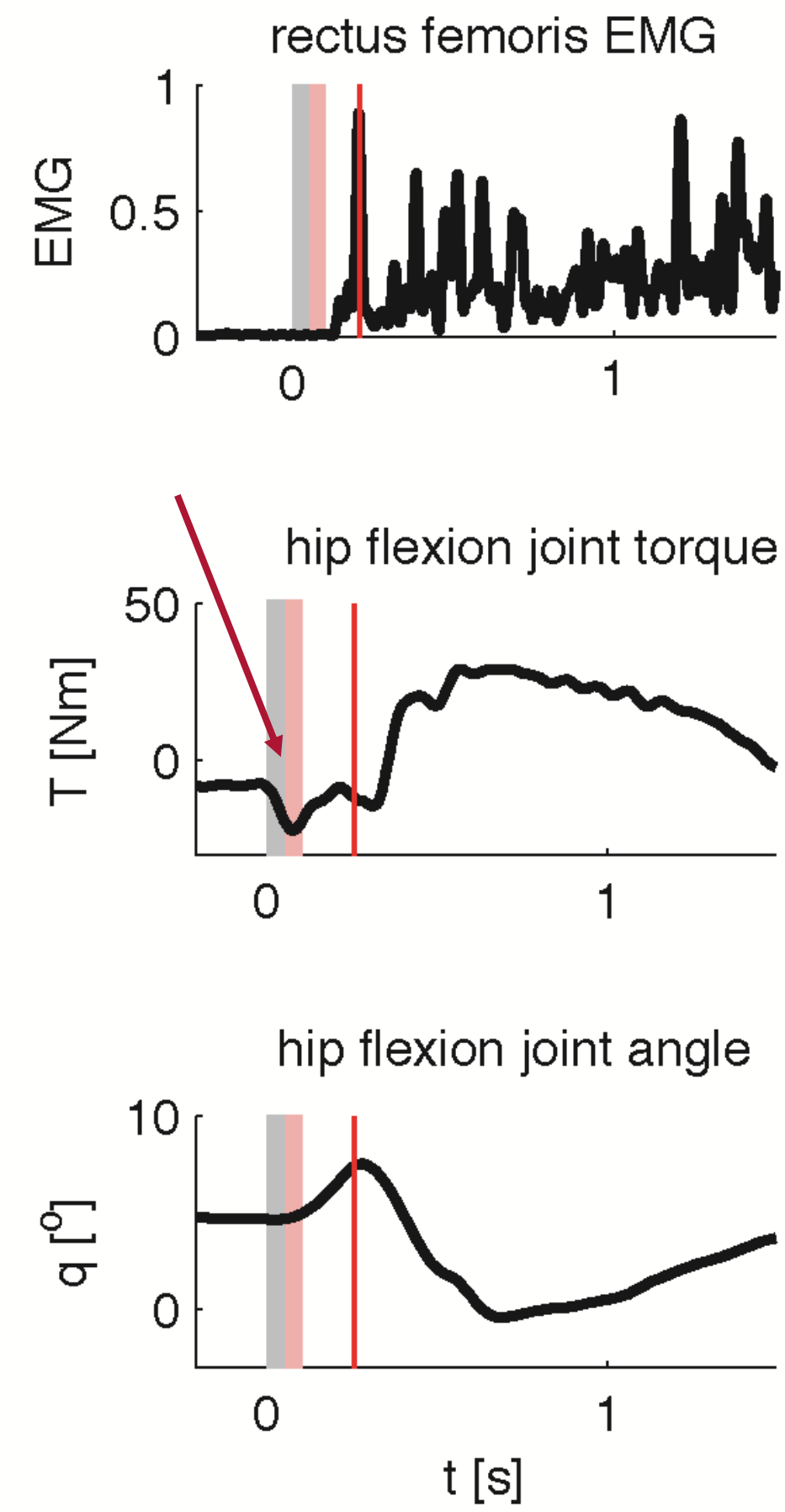
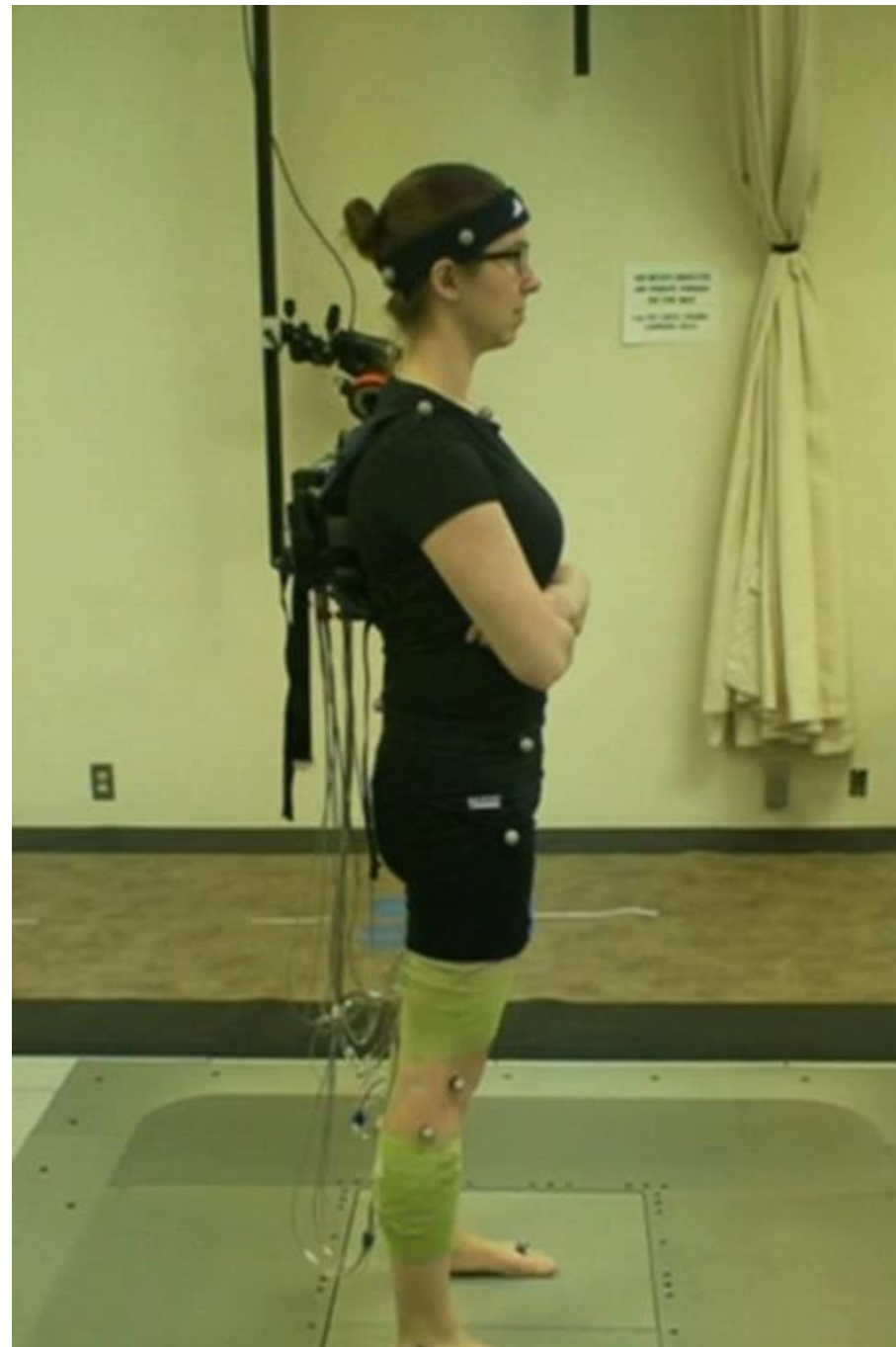


# Initial 'stiff' response to perturbations of standing balance cannot be captured by Hill muscle model





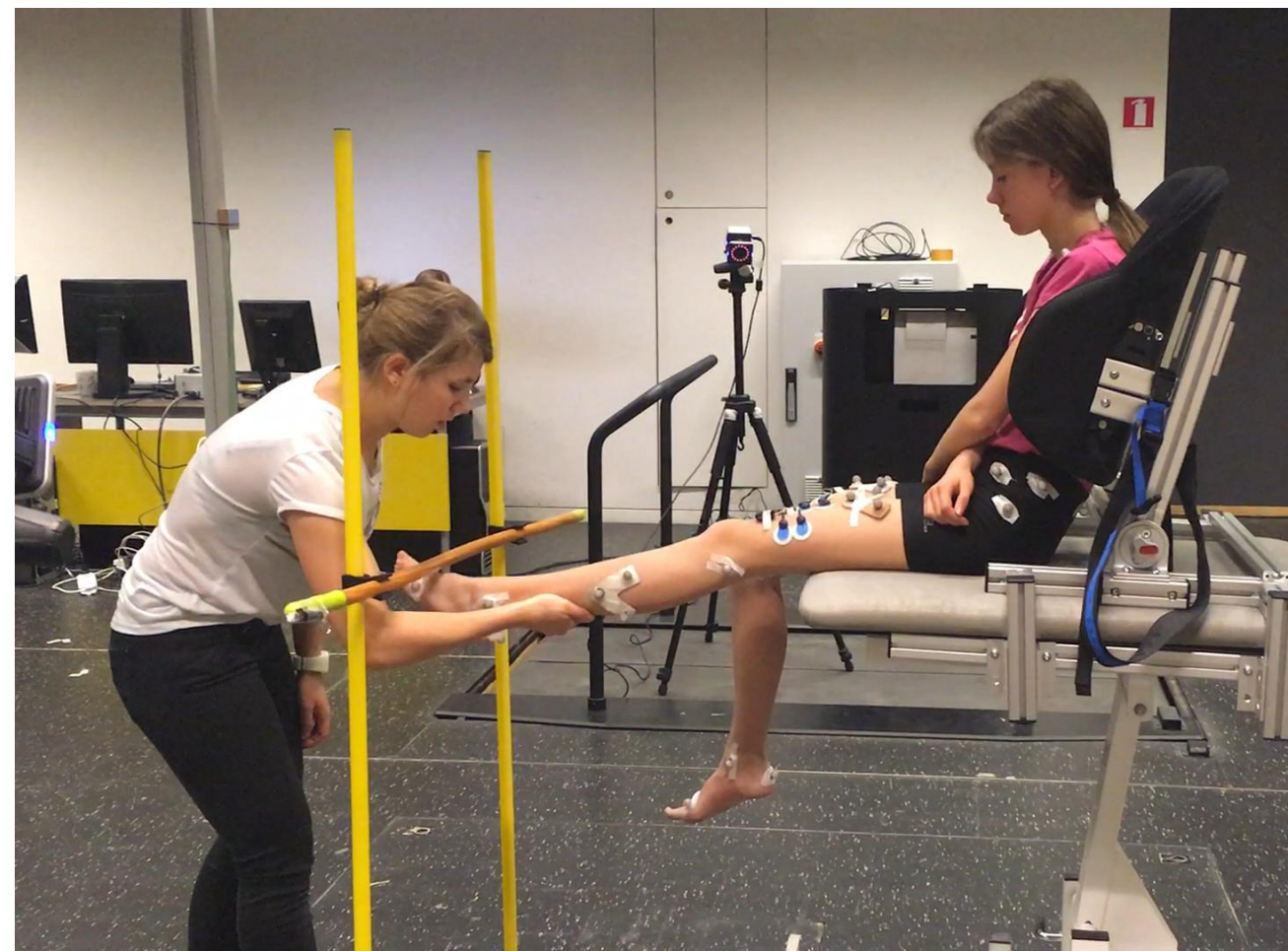
# Initial 'stiff' response to perturbations of standing balance cannot be captured by Hill muscle model



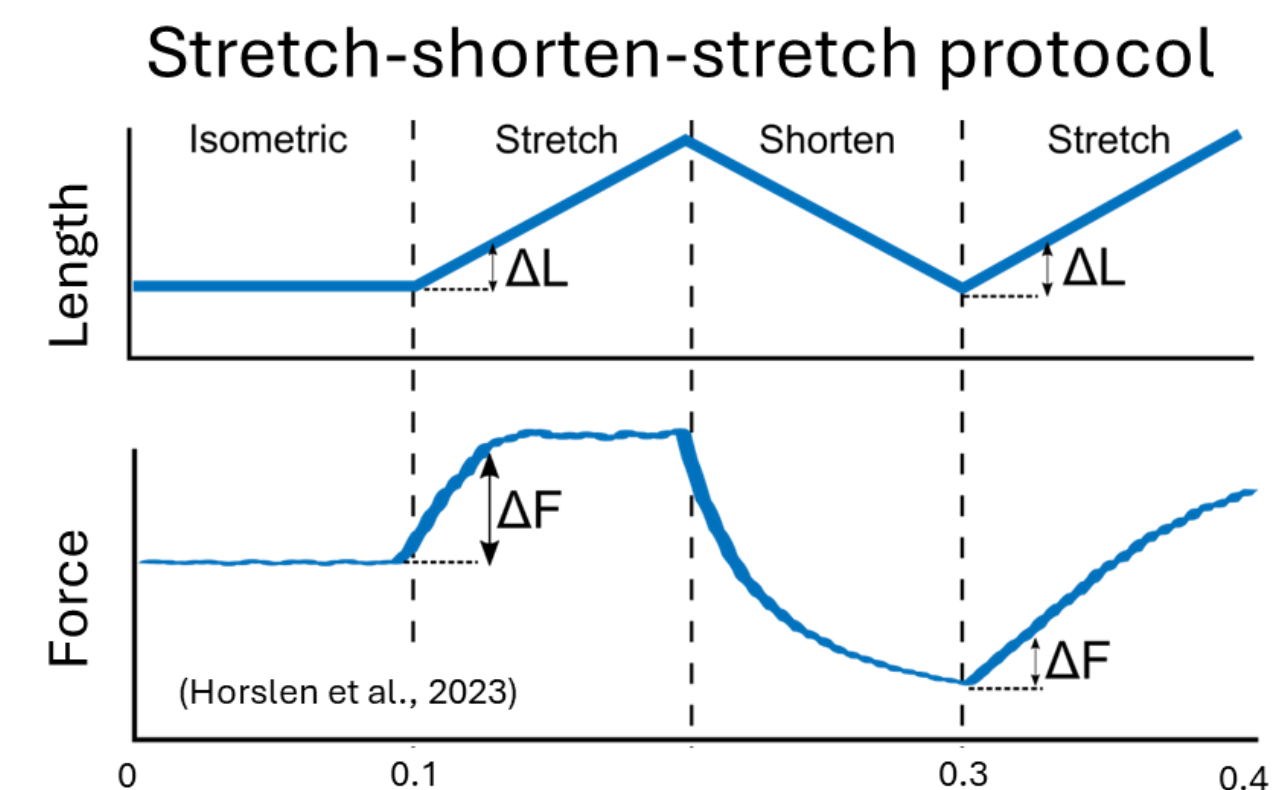
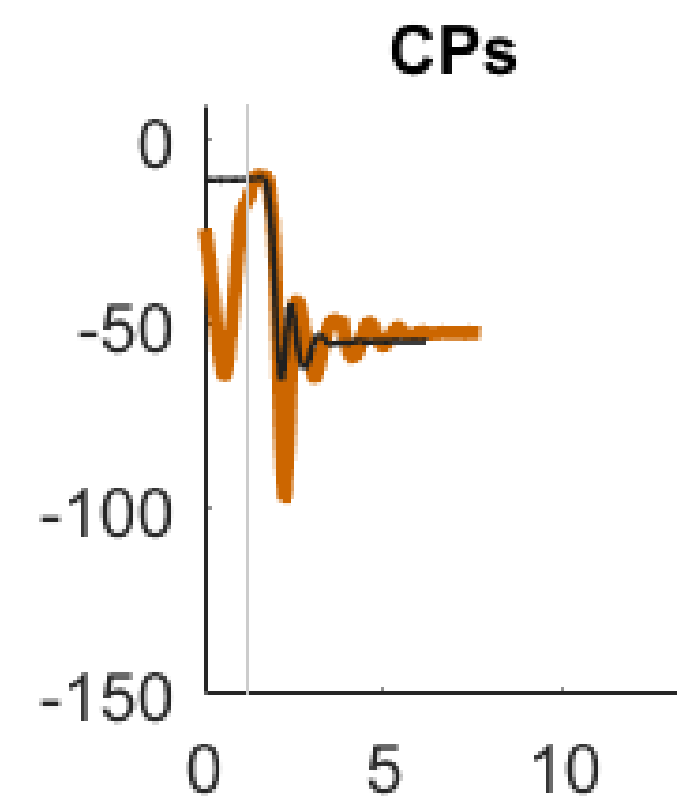
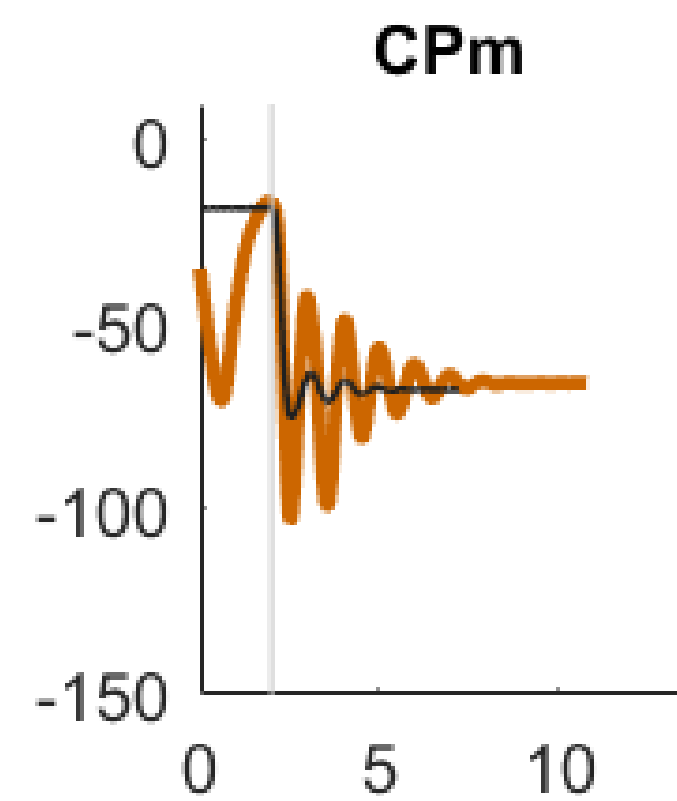
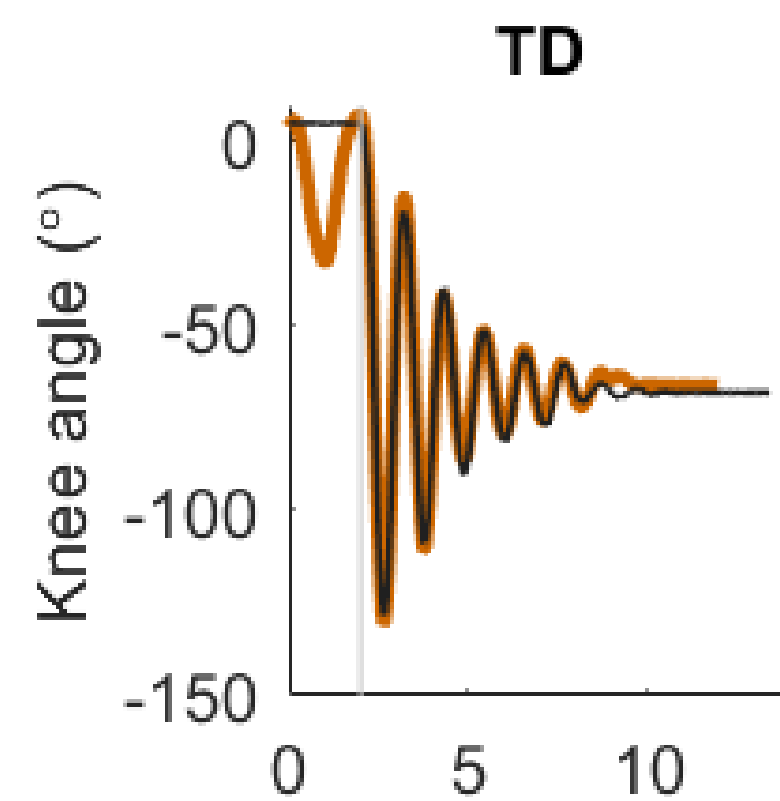
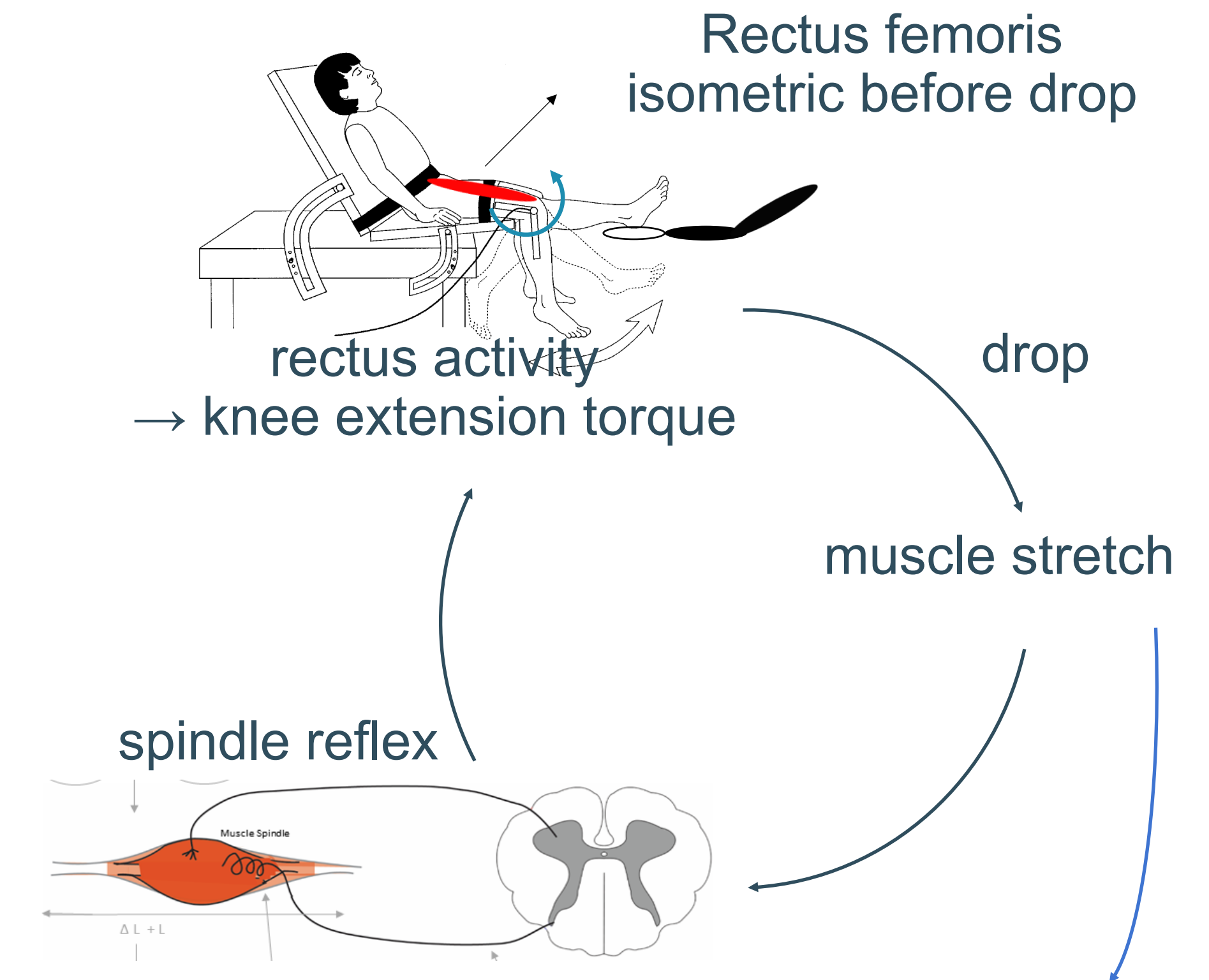


# Pendulum test of spasticity is movement history dependent

Typically developing child



Child with cerebral palsy (CP)





# Simulating muscle force using a biophysical model

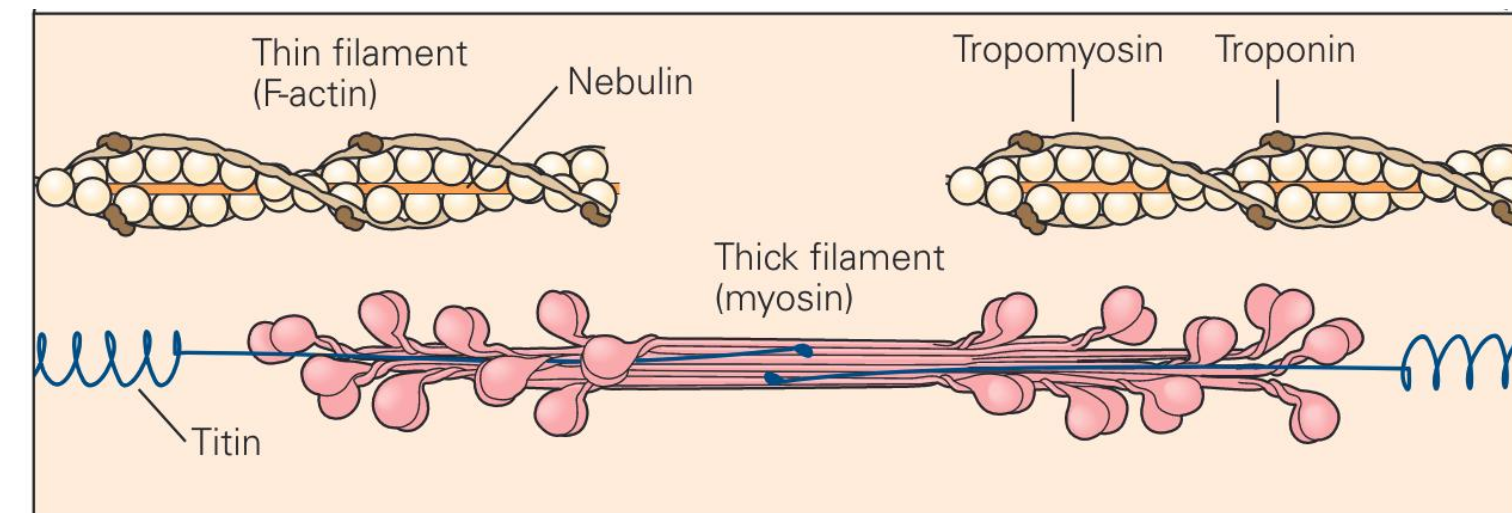
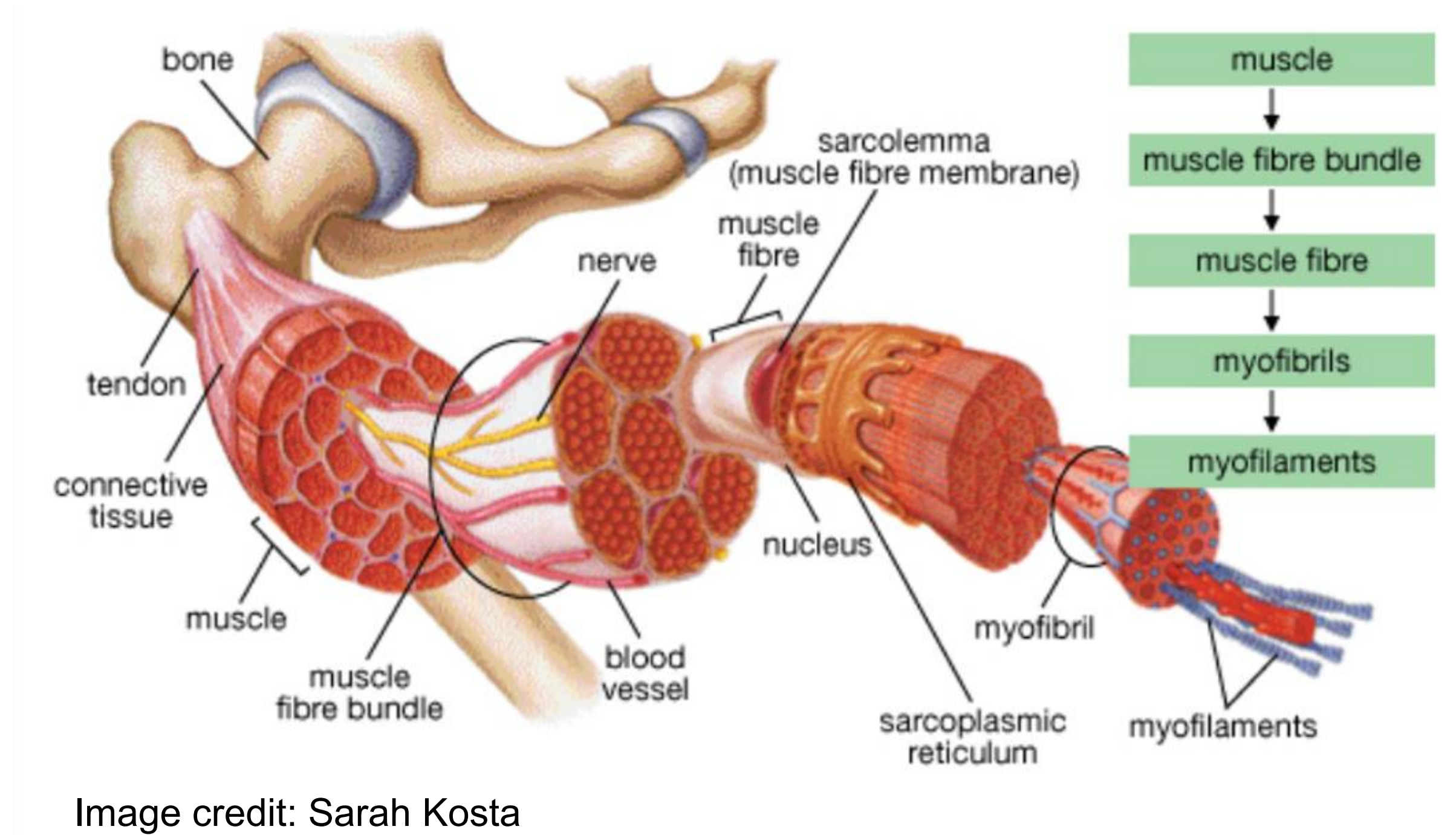
Lena Ting, Surabhi Simha, Hansol Ryu, Tim van der Zee, Friedl De Groote

July 27<sup>th</sup> 2025





# Physiology: muscle active force comes from crossbridge binding



Kandell, Schwartz, Jessell 2013

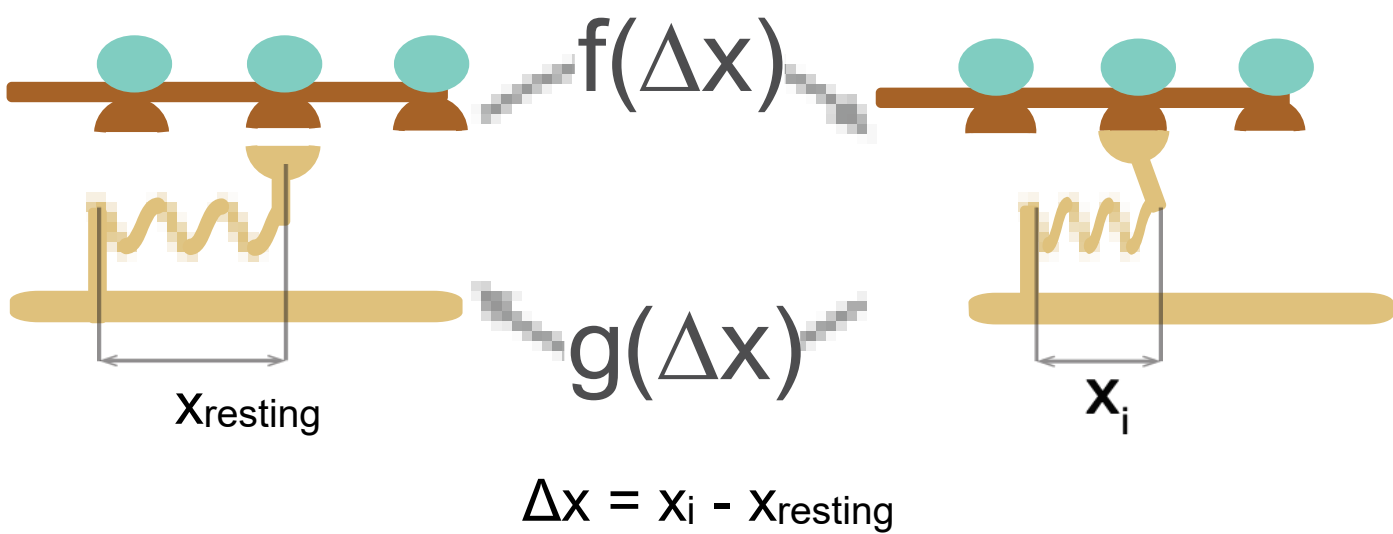
Image credit: Sarah Kosta

# Crossbridge model: spring that continuously transitions b/w attached and detached



## Simplify the crossbridge

- 1 dimensional spring
- 2 states (detached or attached)

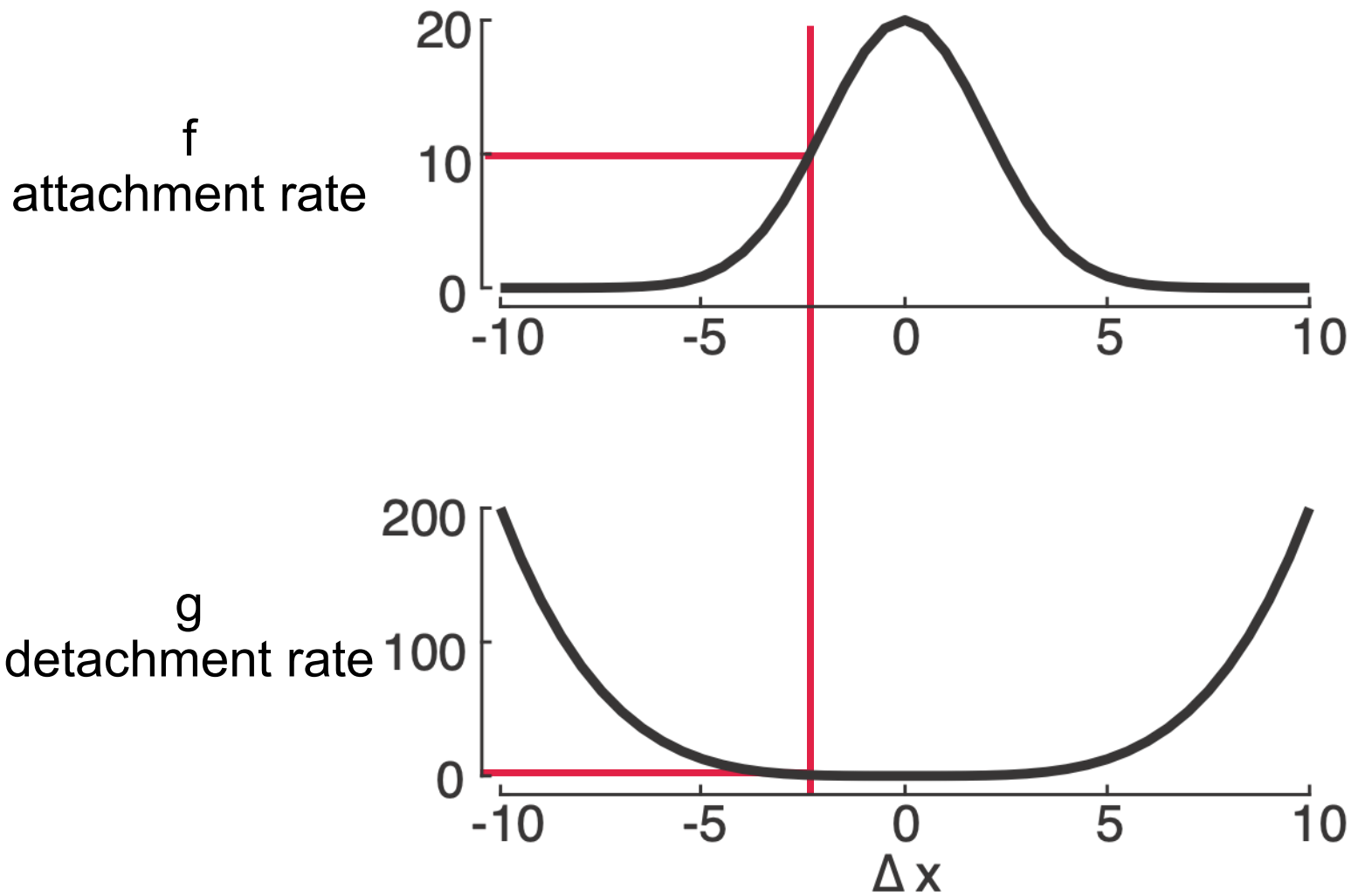


## Count number of attached crossbridges

states continuously transition

$$\frac{dn_{attached}}{dt} = \overset{90}{f(x)} \cdot \overset{10}{n_{detached}} - \overset{1000}{g(x)} \cdot \overset{2}{n_{attached}}$$

attachment rate                      detachment rate

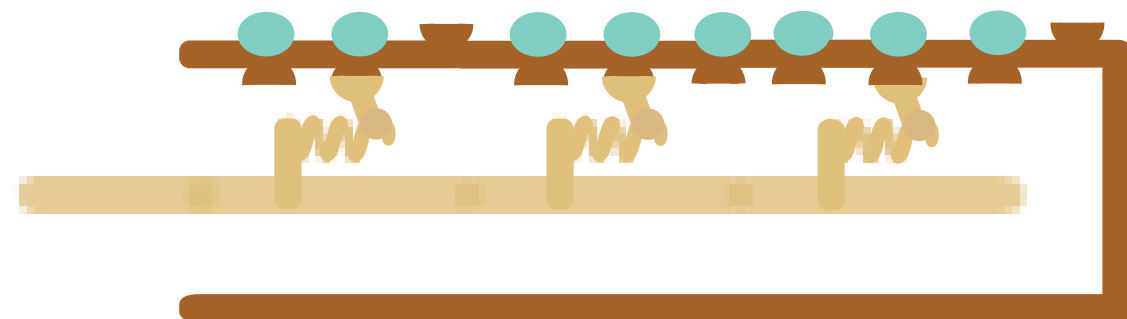


count attached crossbridges at single time point (numerical integrator)





# Muscle model: distribution of “cross-bridge springs”

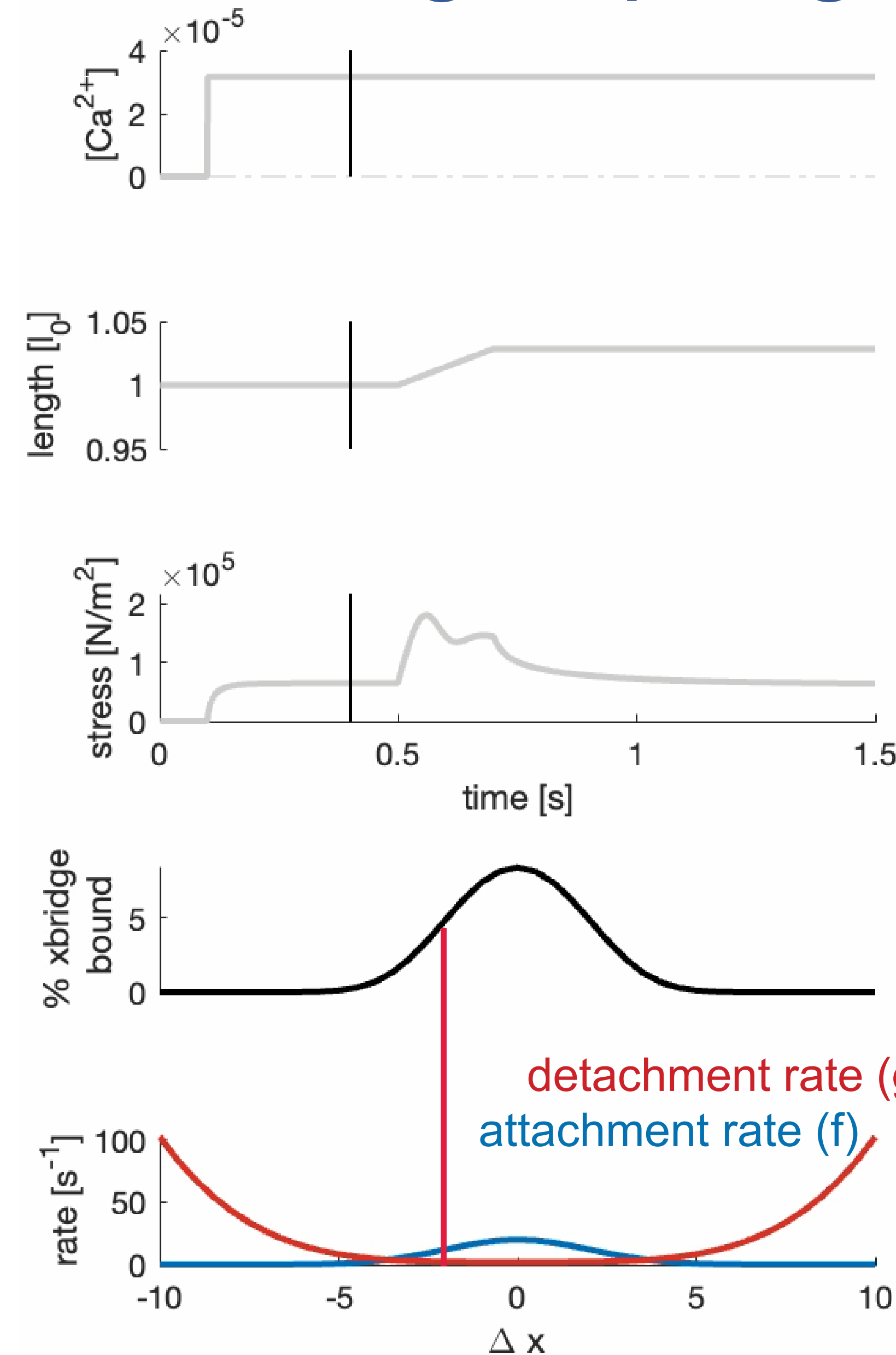


Calculate force from one attached crossbridge

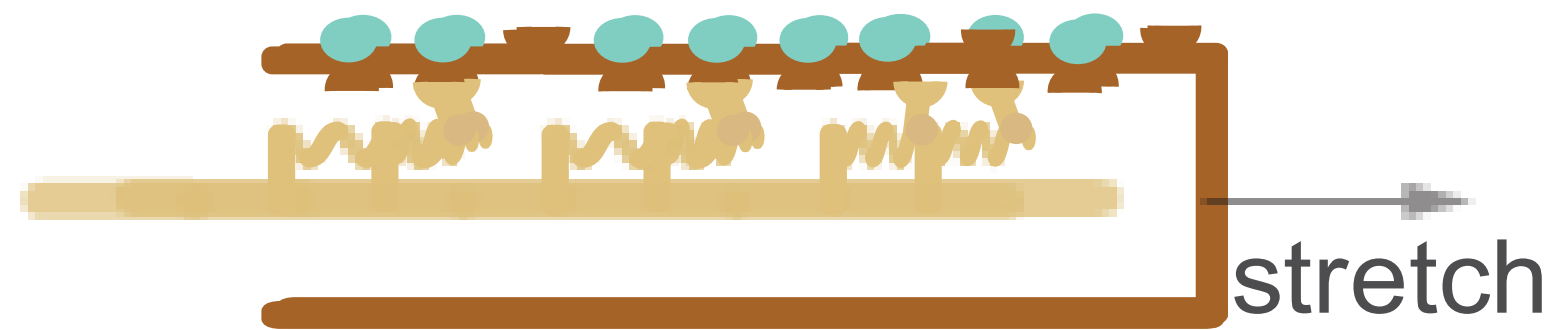
spring force  $F = k_{cb} \cdot \Delta x$

Add forces from all attached crossbridges

$$F_{total} = \sum_{i=0}^{i=n_{bound}} F_i$$



# Muscle model: distribution of “cross-bridge springs”

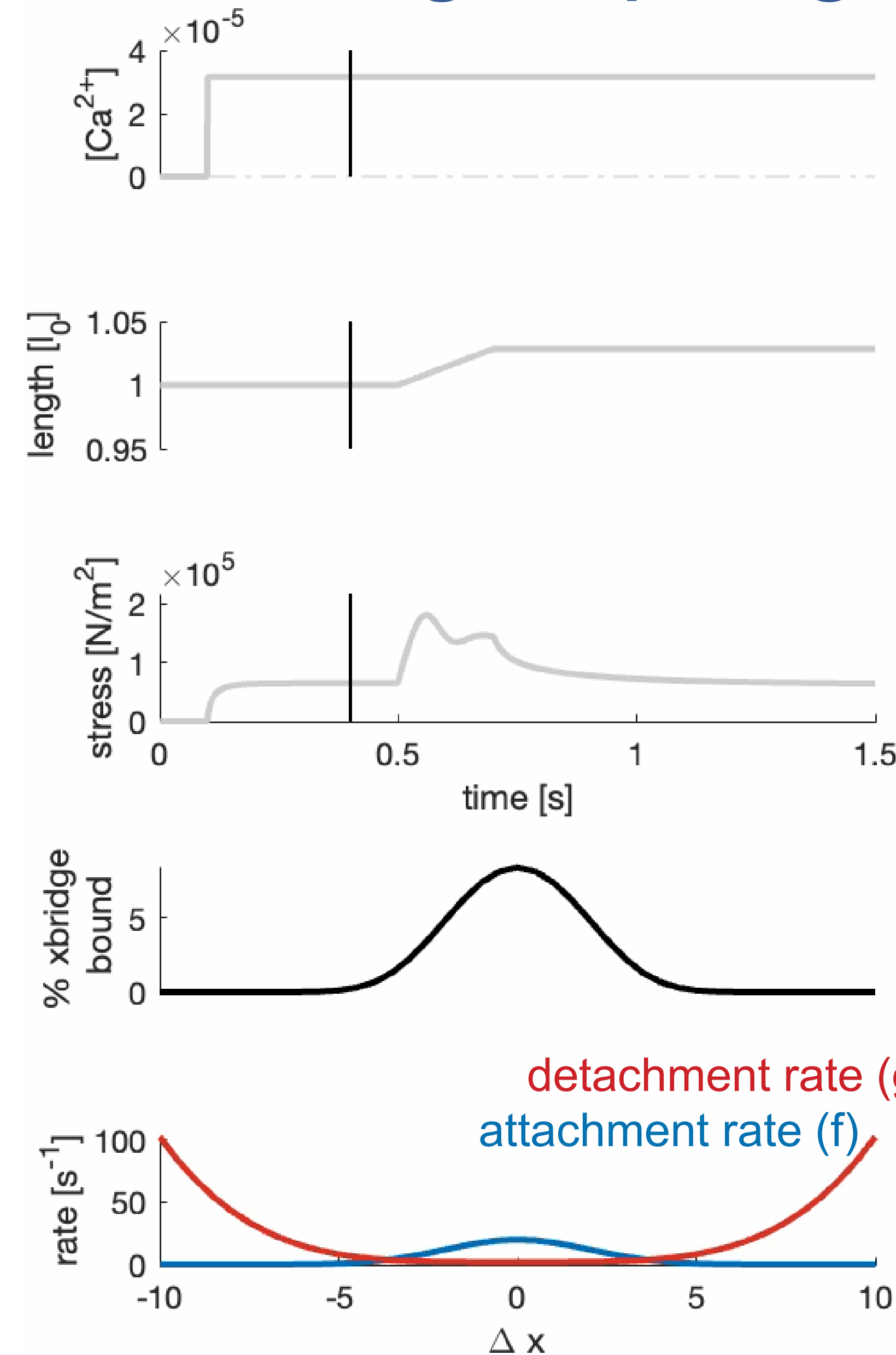


Calculate force from one attached crossbridge

spring force  $F = k_{cb} \cdot \Delta x$

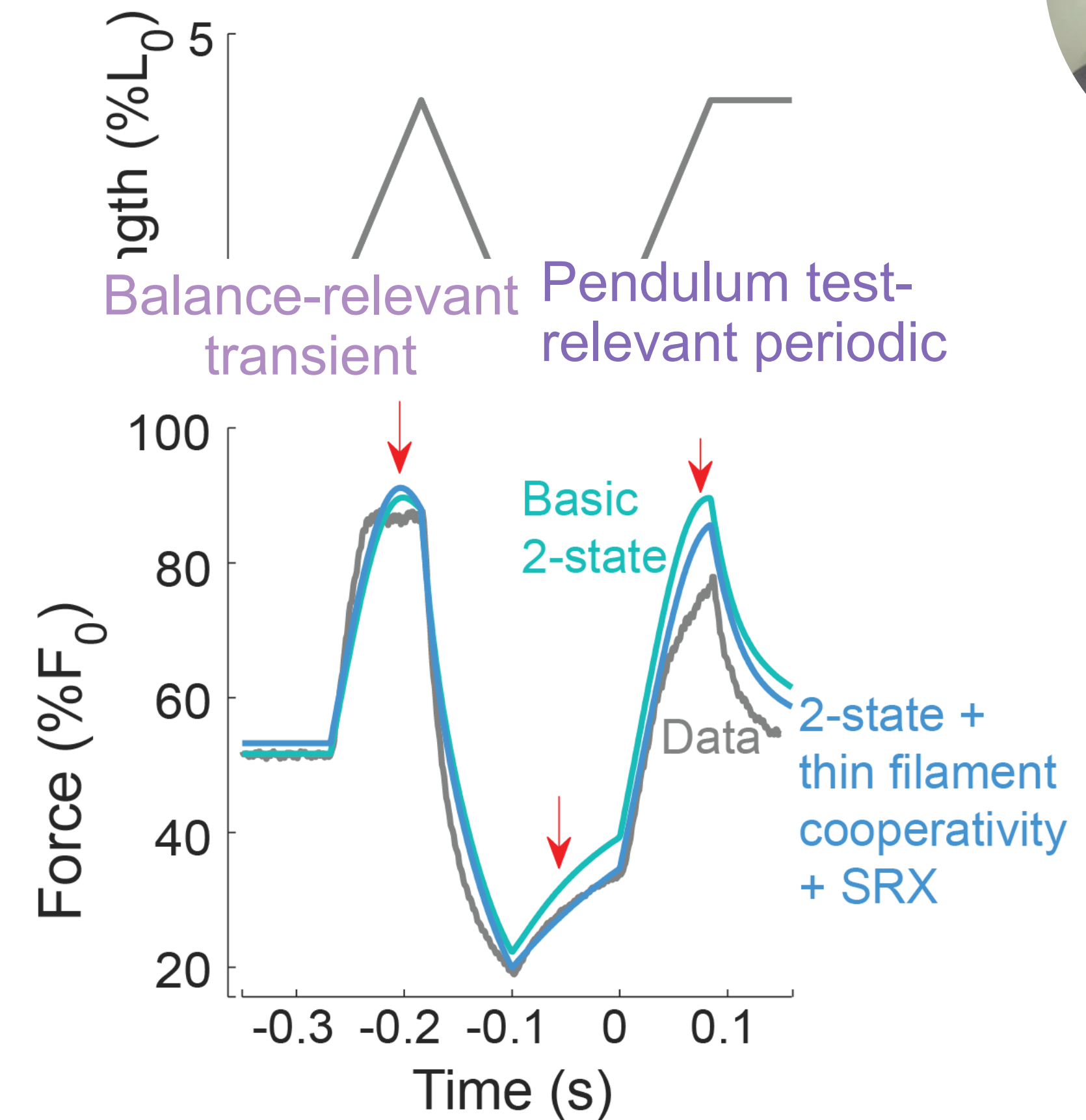
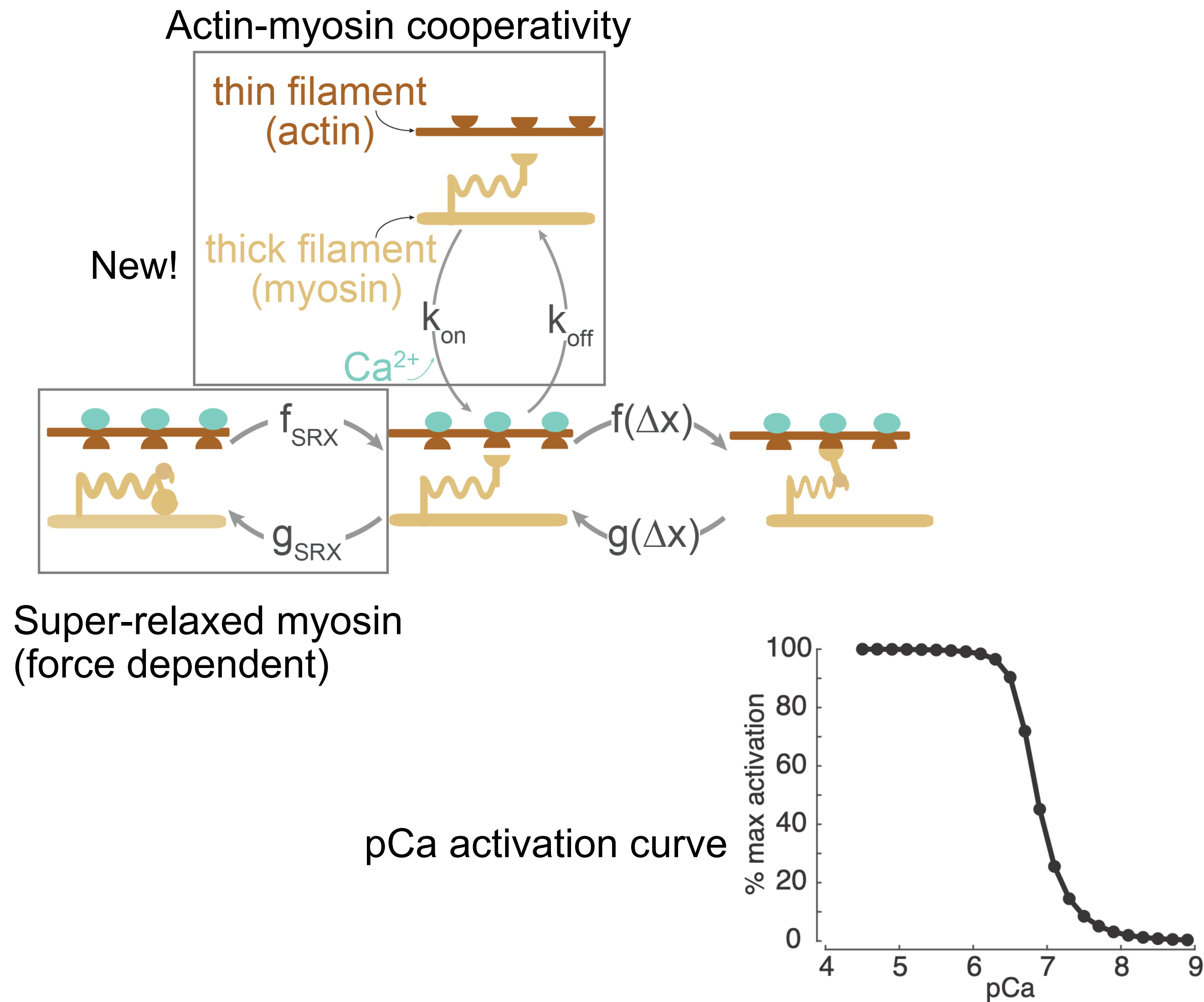
Add forces from all attached crossbridges

$$F_{total} = \sum_{i=0}^{i=n_{bound}} F_i$$



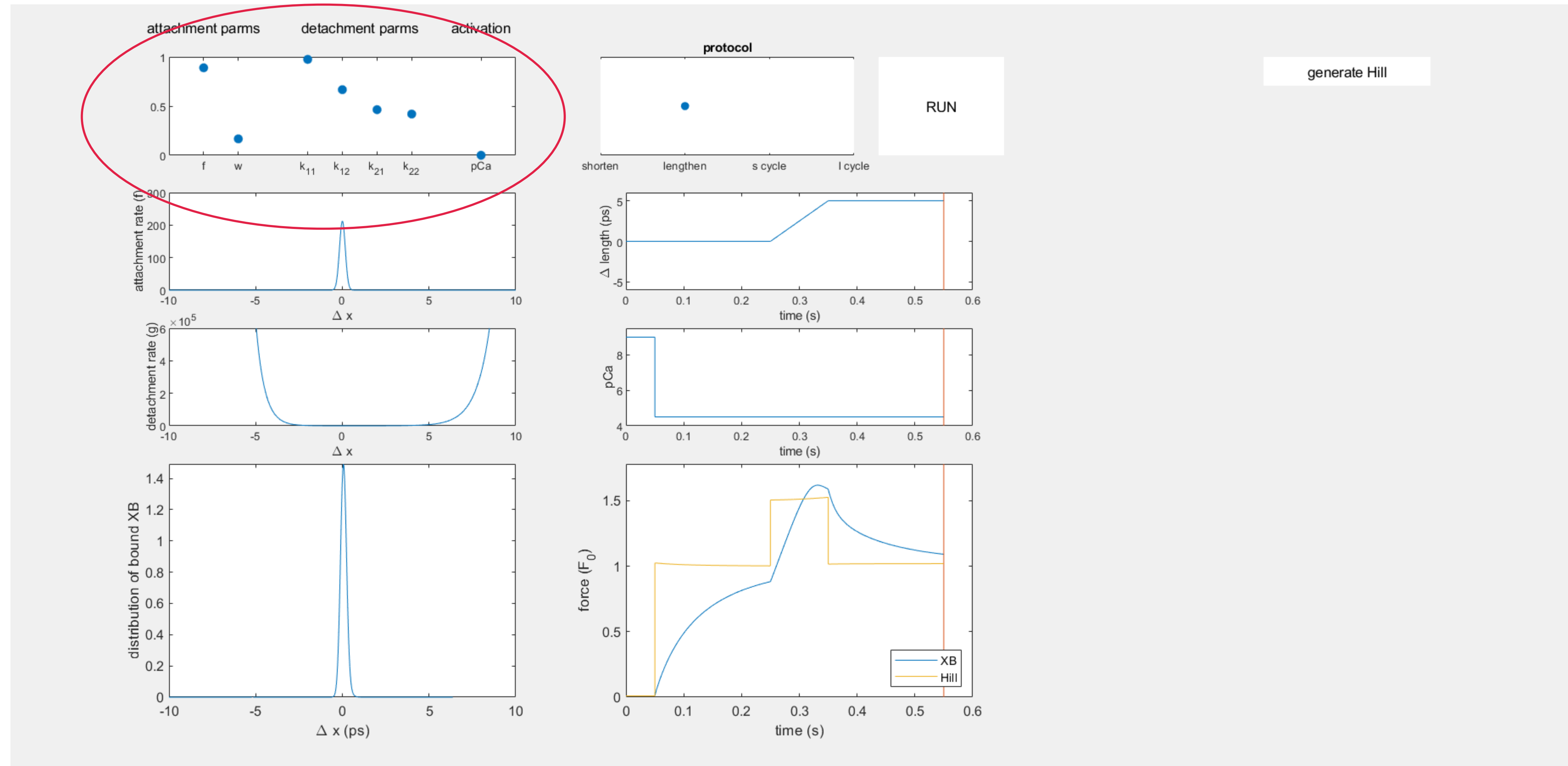


# Add 2 more states for good force response to cyclic stretches



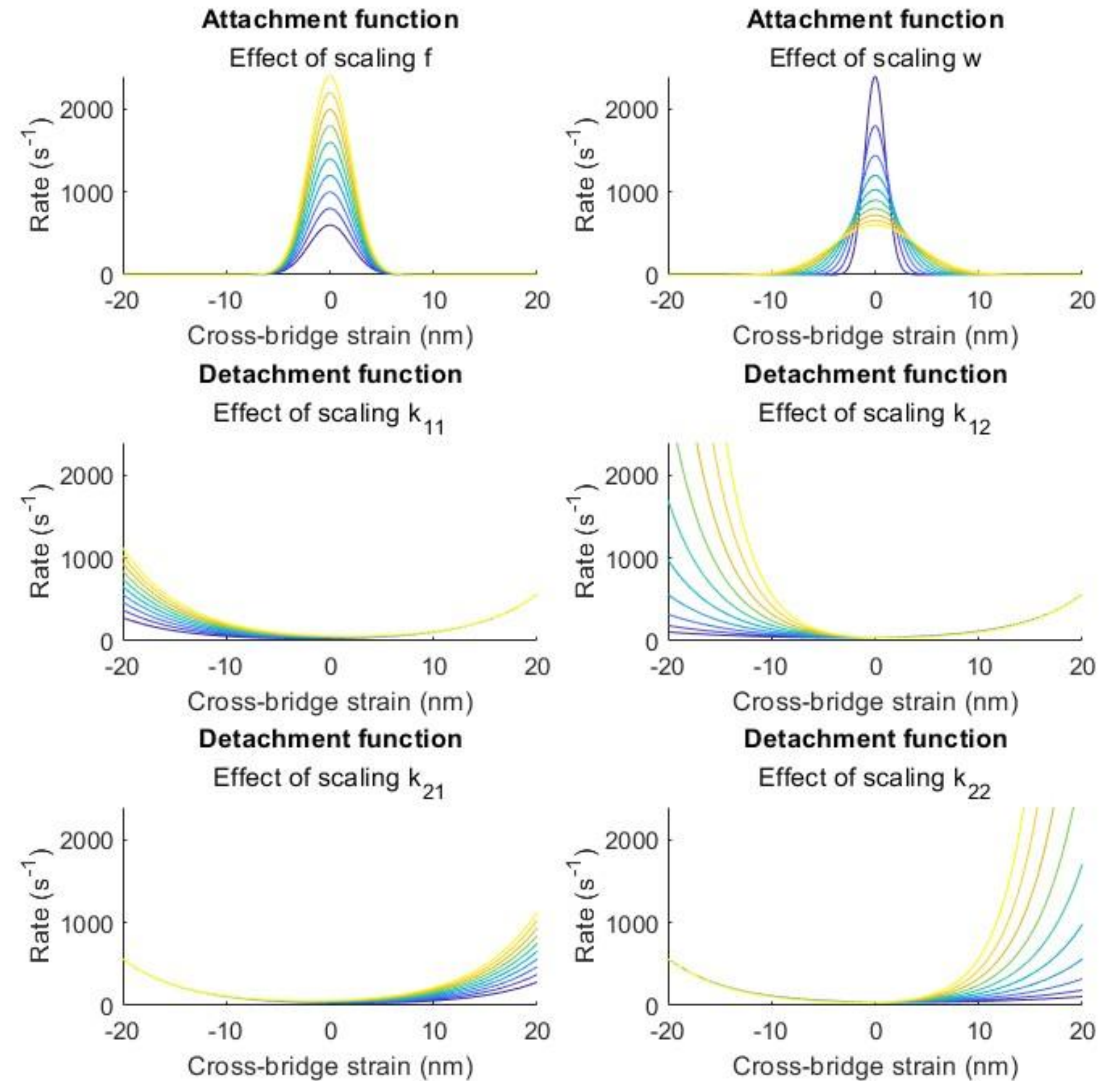
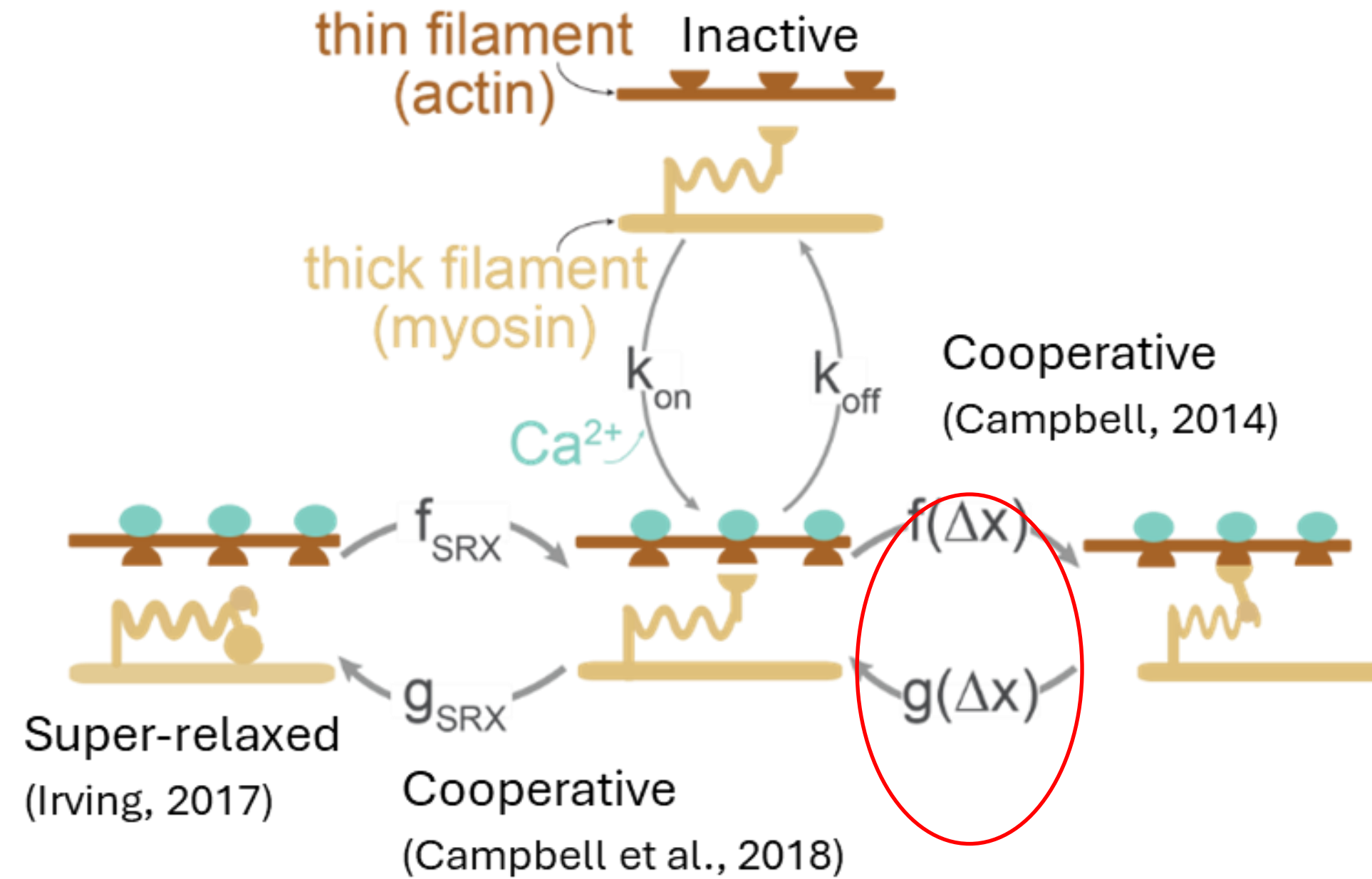
van der Zee et. al. 2025, *in prep*  
 Simha & Ting, *J. Expt. Phys.*, 2023

# Tutorial Part 1: simulating a biophysical muscle model





# Attachment and detachment rate functions



- Attachment rate  $f(\Delta x) = f(f, w)$

- Detachment  $k_{21}, k_{22}$

The cross-bridge attachment functions  $f(x)$  and  $\phi(x)$  are gaussians:

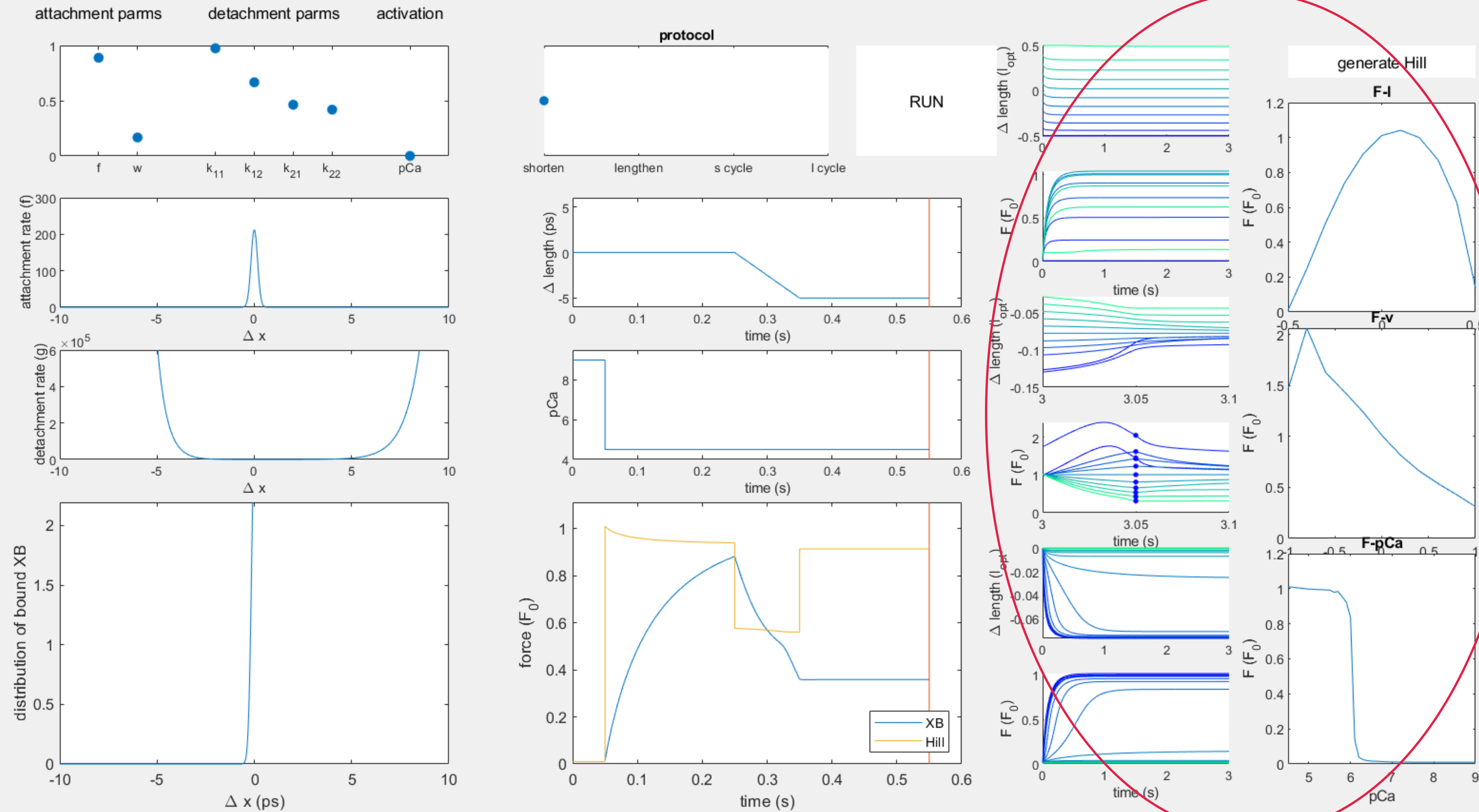
$$f(x) = \frac{f_1}{\sqrt{2\pi \cdot w^2}} \cdot e^{-\frac{x^2}{2 \cdot w^2}}$$

$$\phi(x) = \frac{\phi_1}{\sqrt{2\pi \cdot w^2}} \cdot e^{-\frac{x^2}{2 \cdot w^2}}$$

The cross-bridge detachment function  $g(x)$  is the sum of two exponentials:

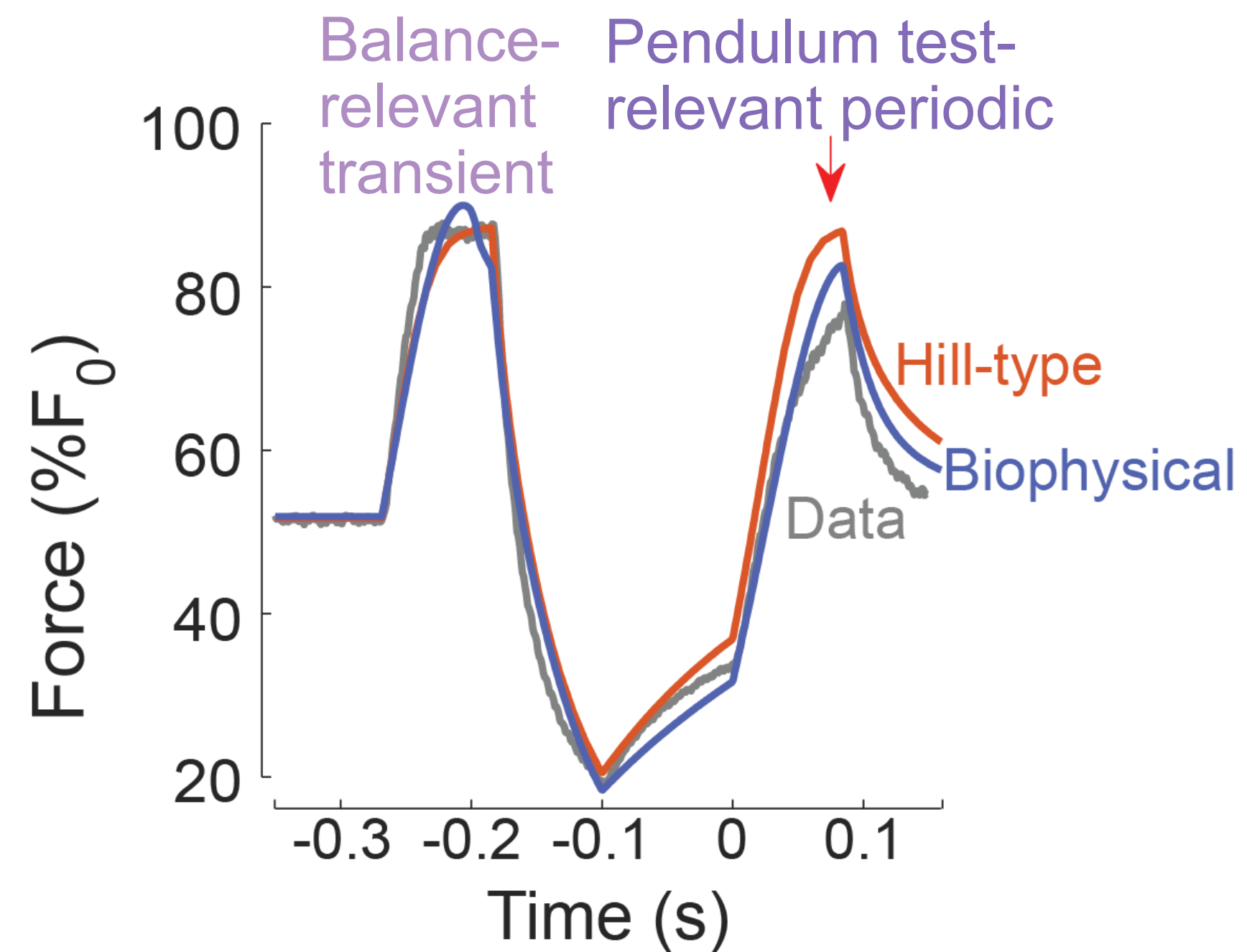
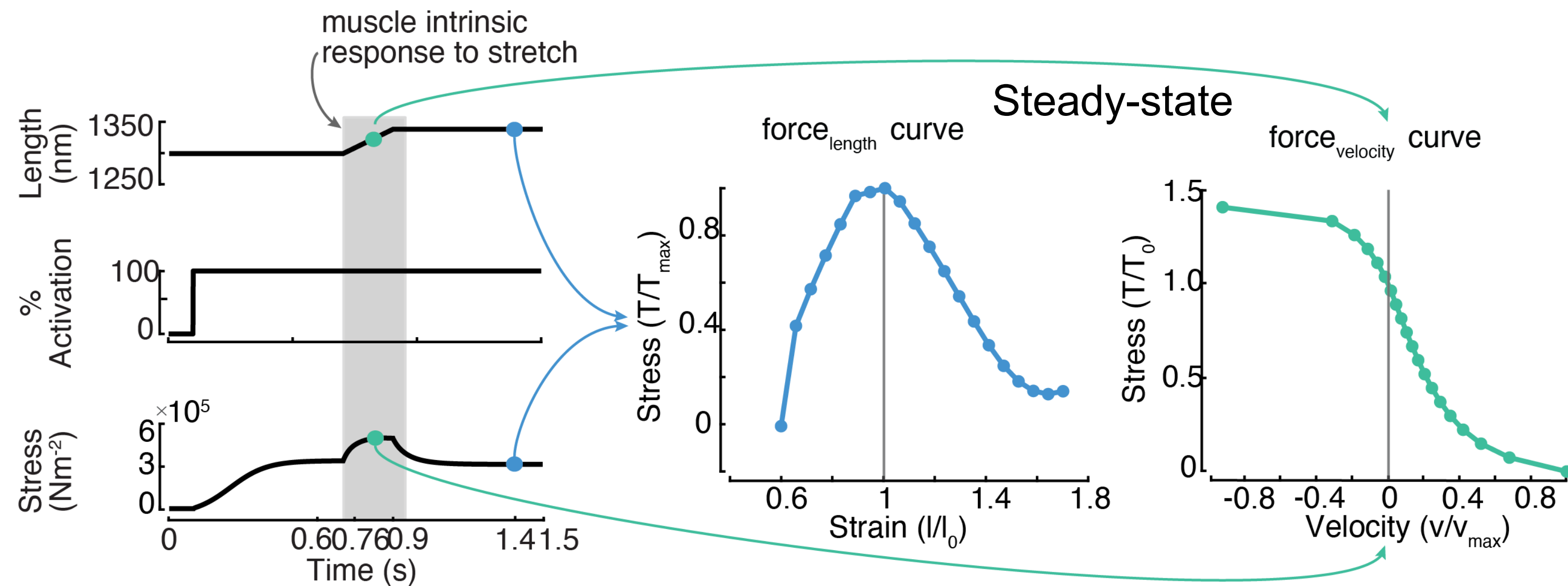
$$g(x) = \sum_{i=1}^2 q_i \cdot e^{x \cdot E_i}$$

# Tutorial Part 1: generating an equivalent Hill model





# Hill-type force-velocity emerges from biophysical model



# *ISB 2025 Tutorial*

## Musculoskeletal simulations with biophysical muscle models

Lena Ting, Surabhi Simha, Hansol Ryu,  
Tim van der Zee, Friedl De Groote



*Funded by NIH HD HD90642 + NIH software supplement*



**Surabhi Simha**  
ISB talk (T 10am)  
Tuning muscle spindle  
signals for locomotion



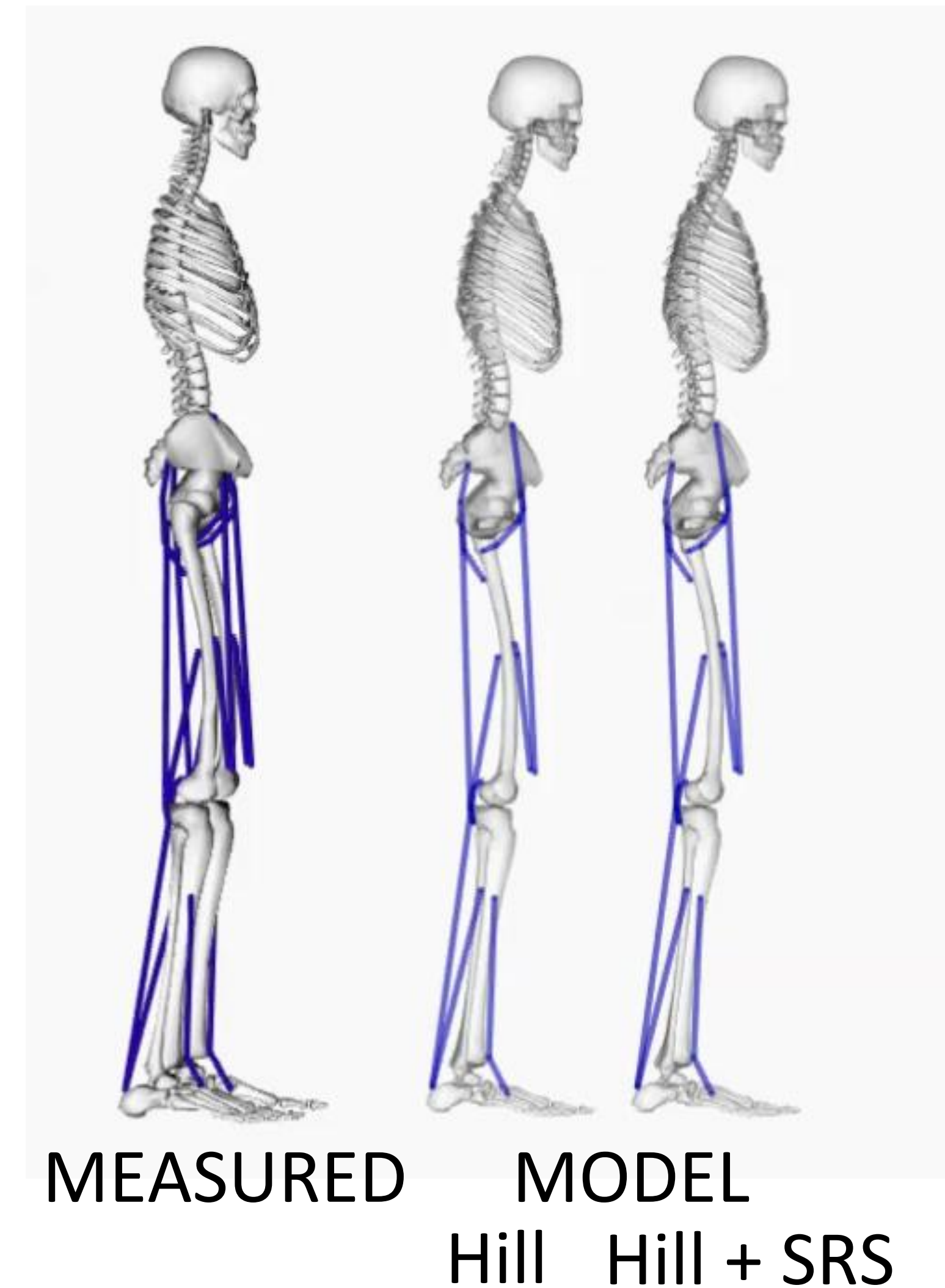
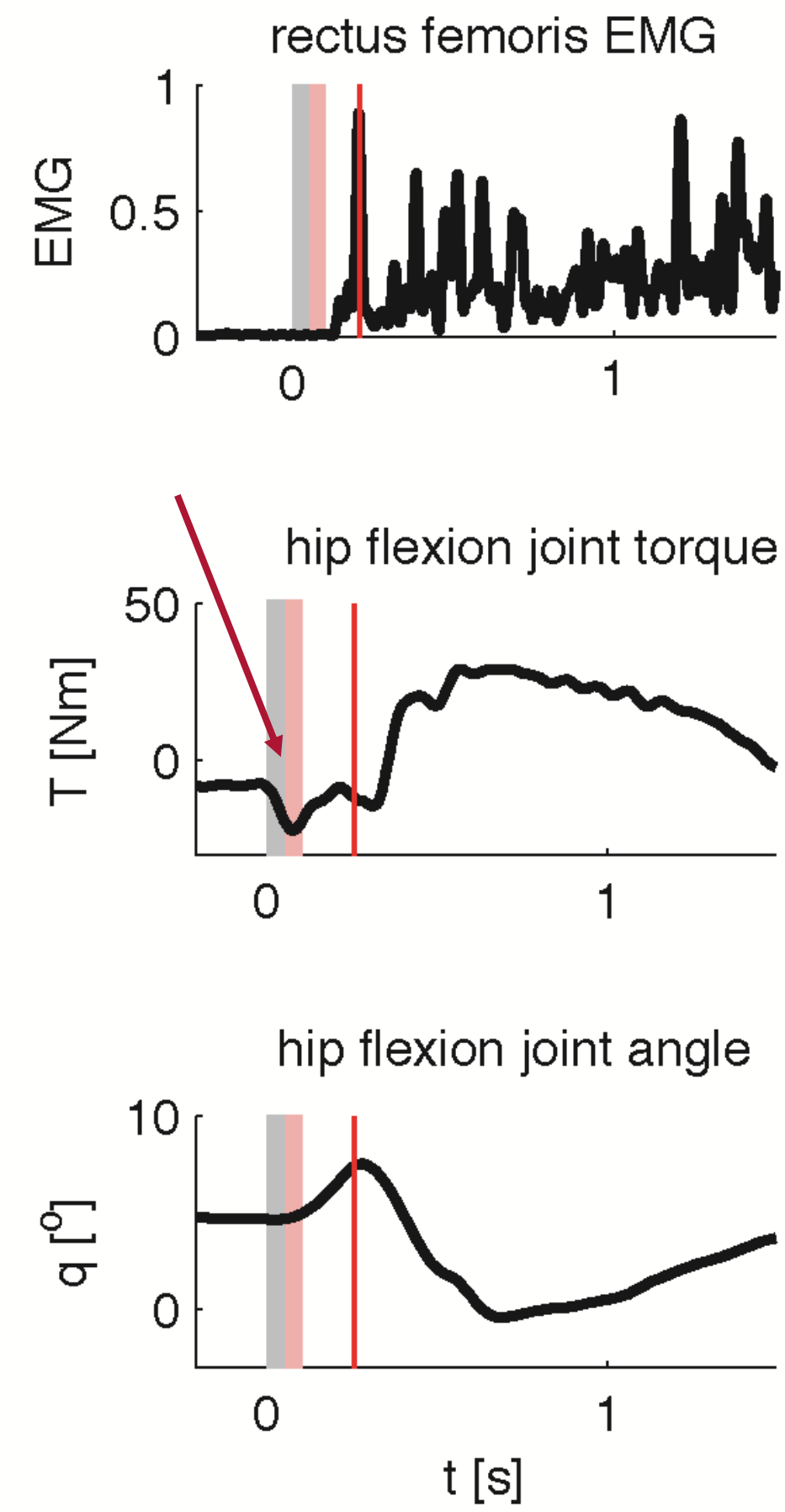
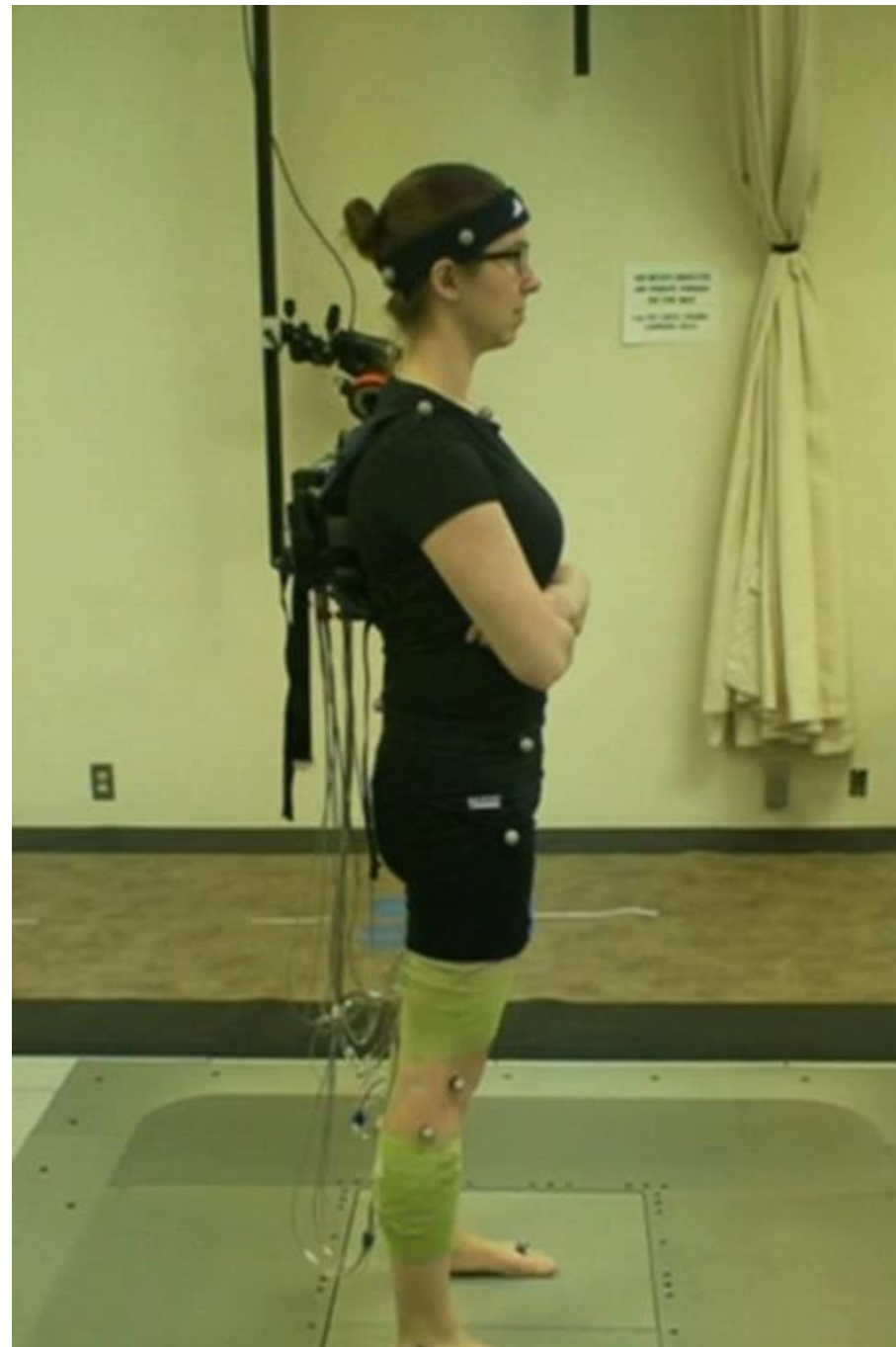
**Tim van der Zee**  
ISB talk (M 2:50), poster (W 5pm)  
Biophysical muscle models  
for musculoskeletal simulation



**Hansol Ryu**  
ISB talk (M 3:20pm)  
Biophysical model for  
postural control



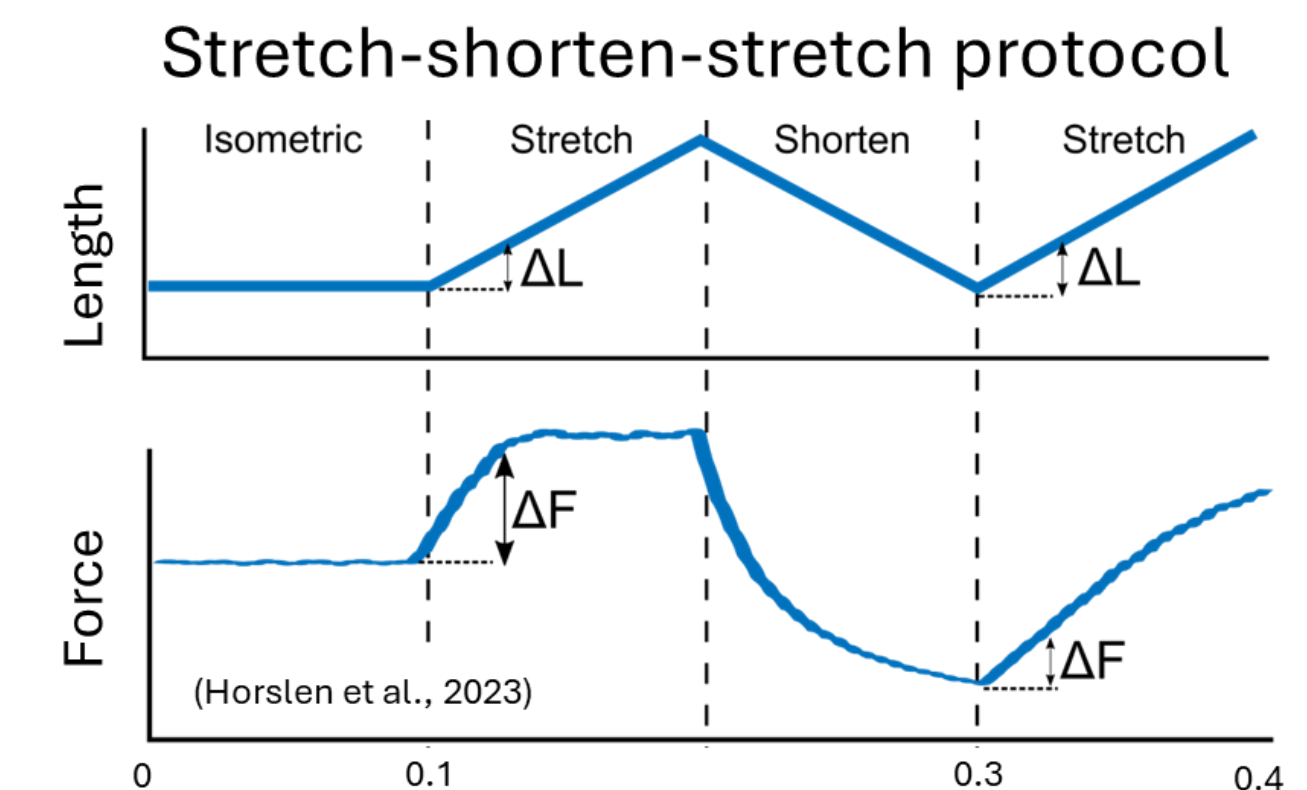
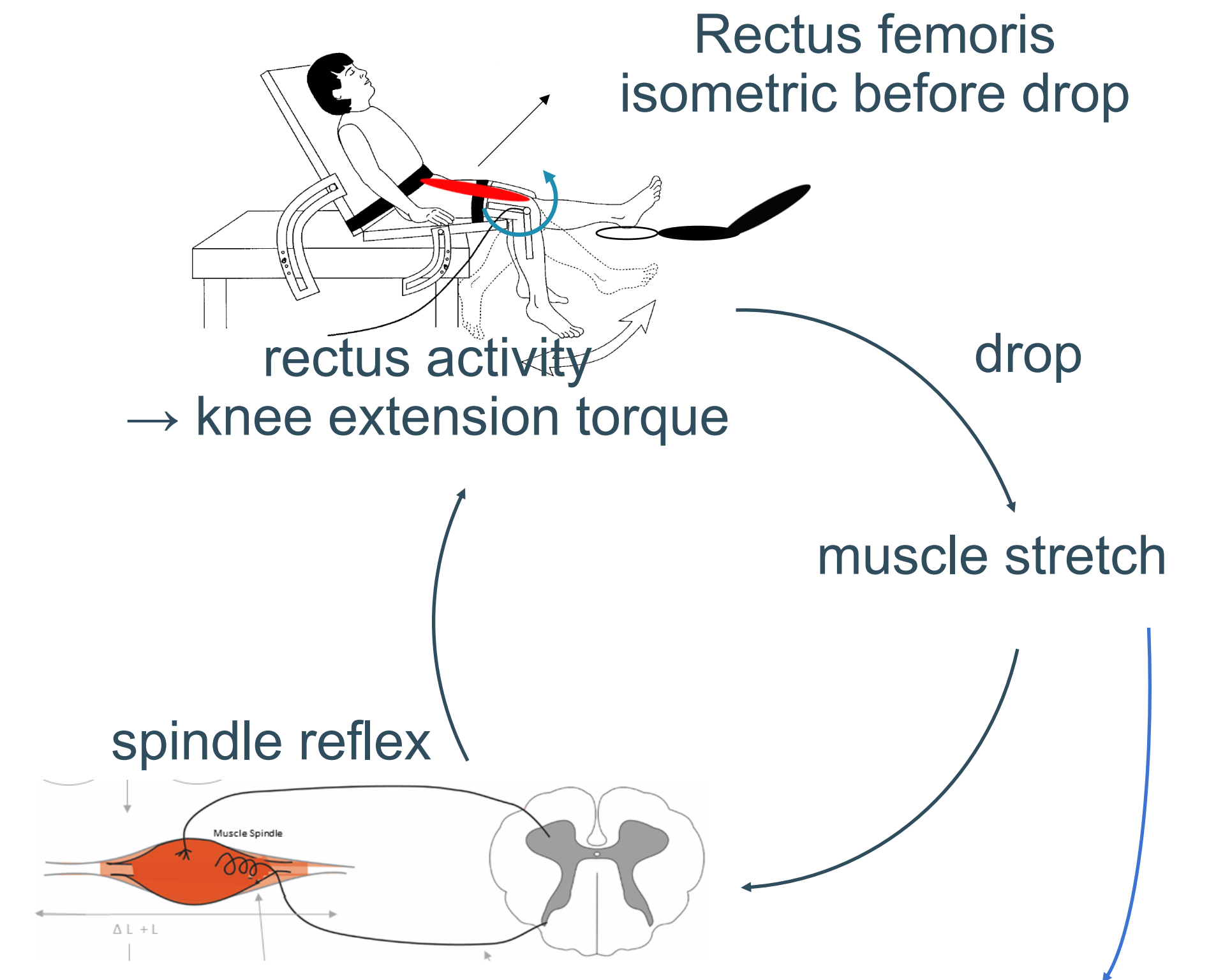
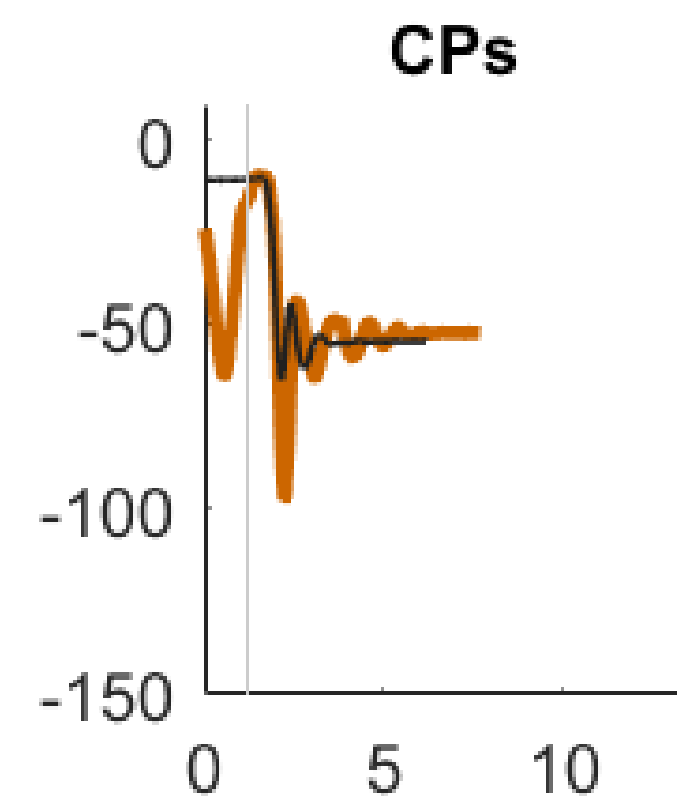
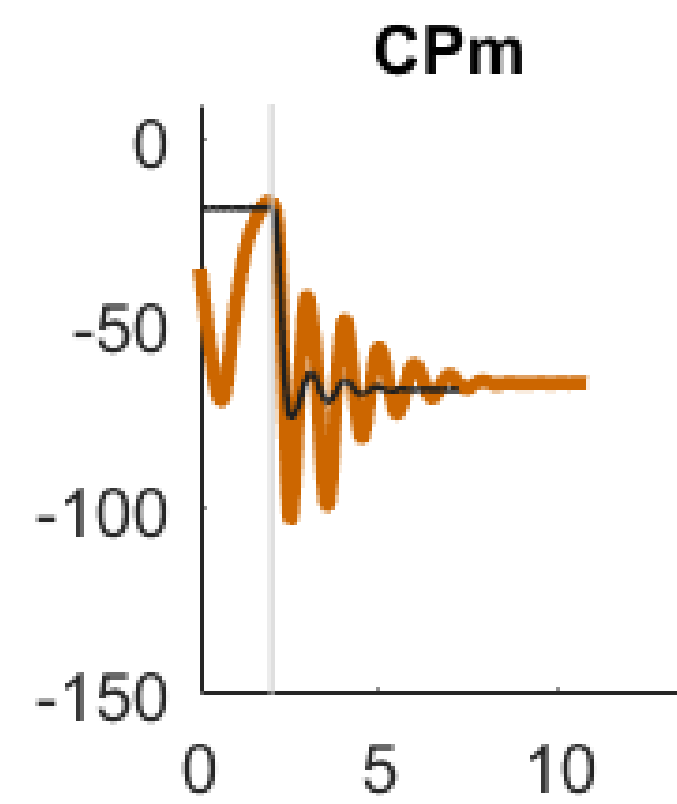
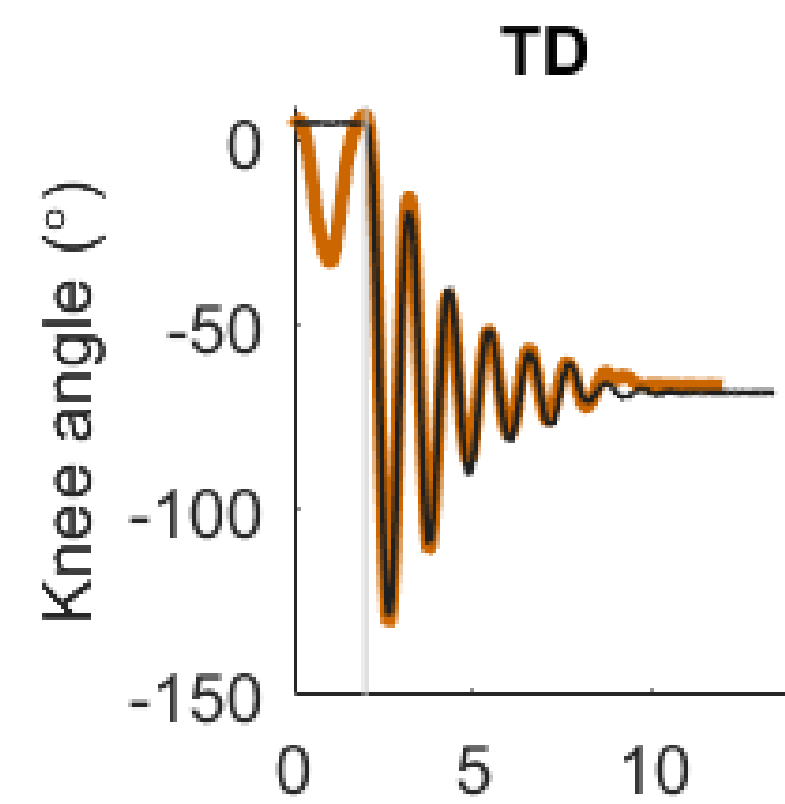
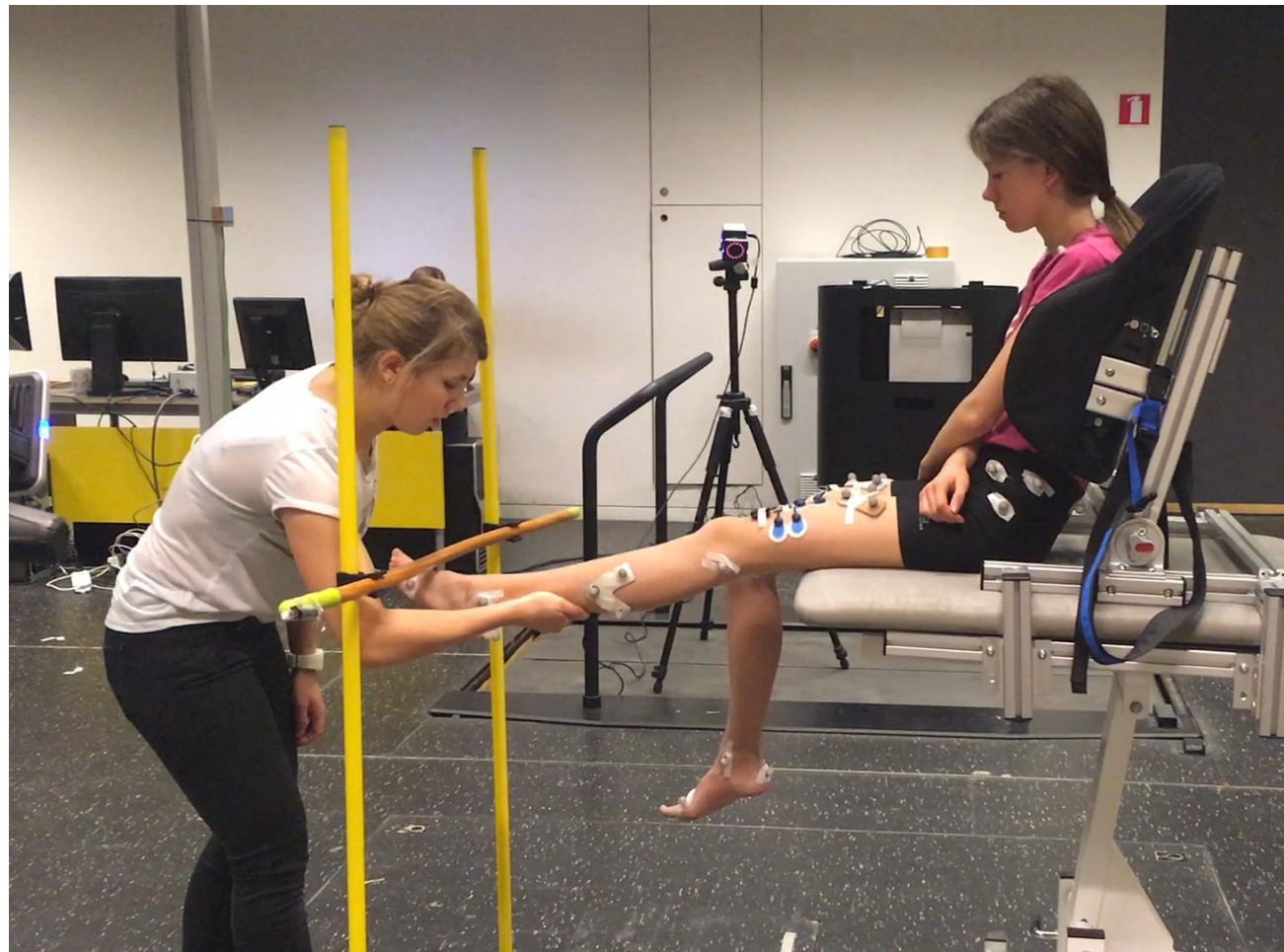
# Initial 'stiff' response to perturbations of standing balance cannot be captured by Hill muscle model





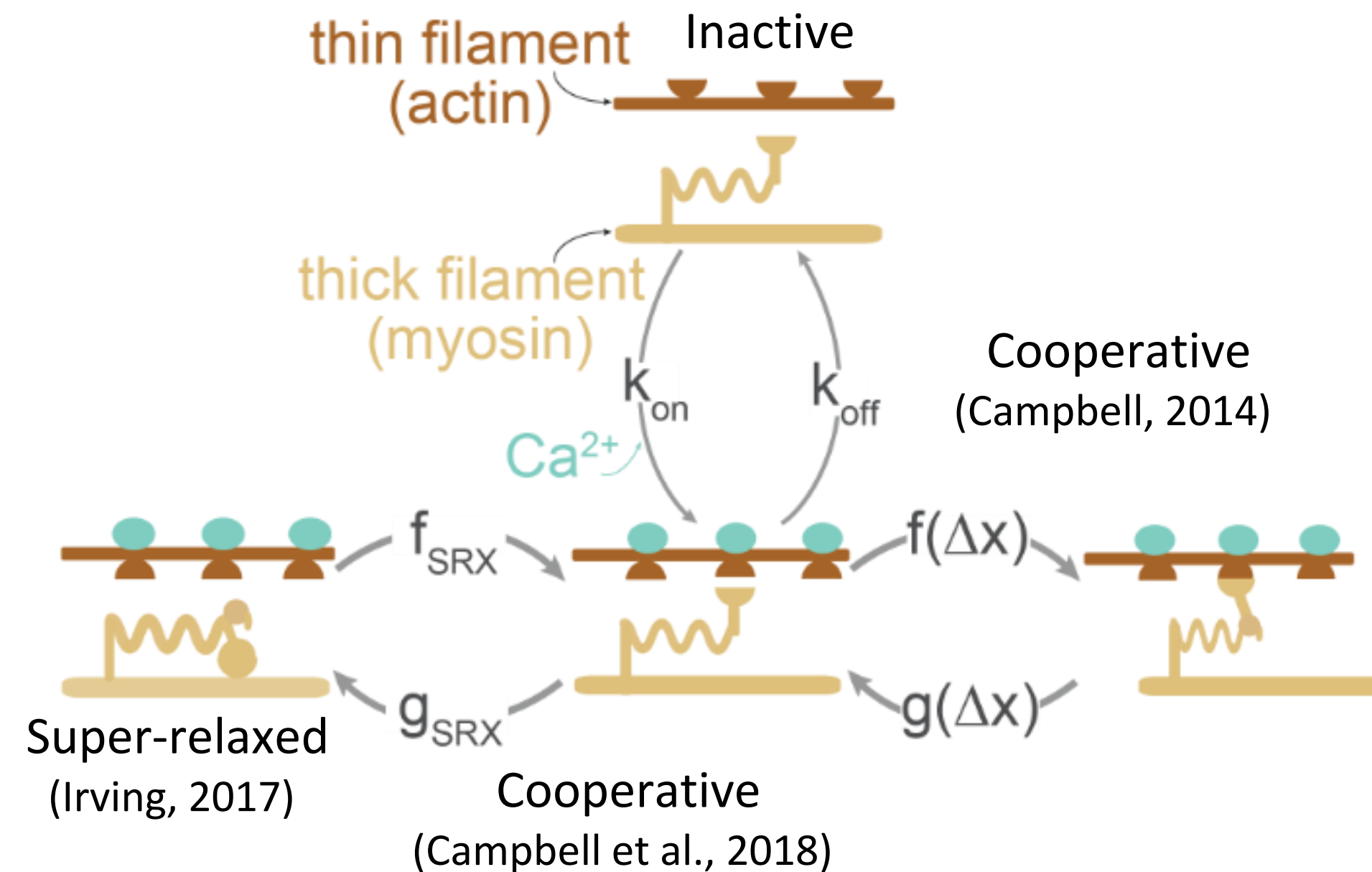
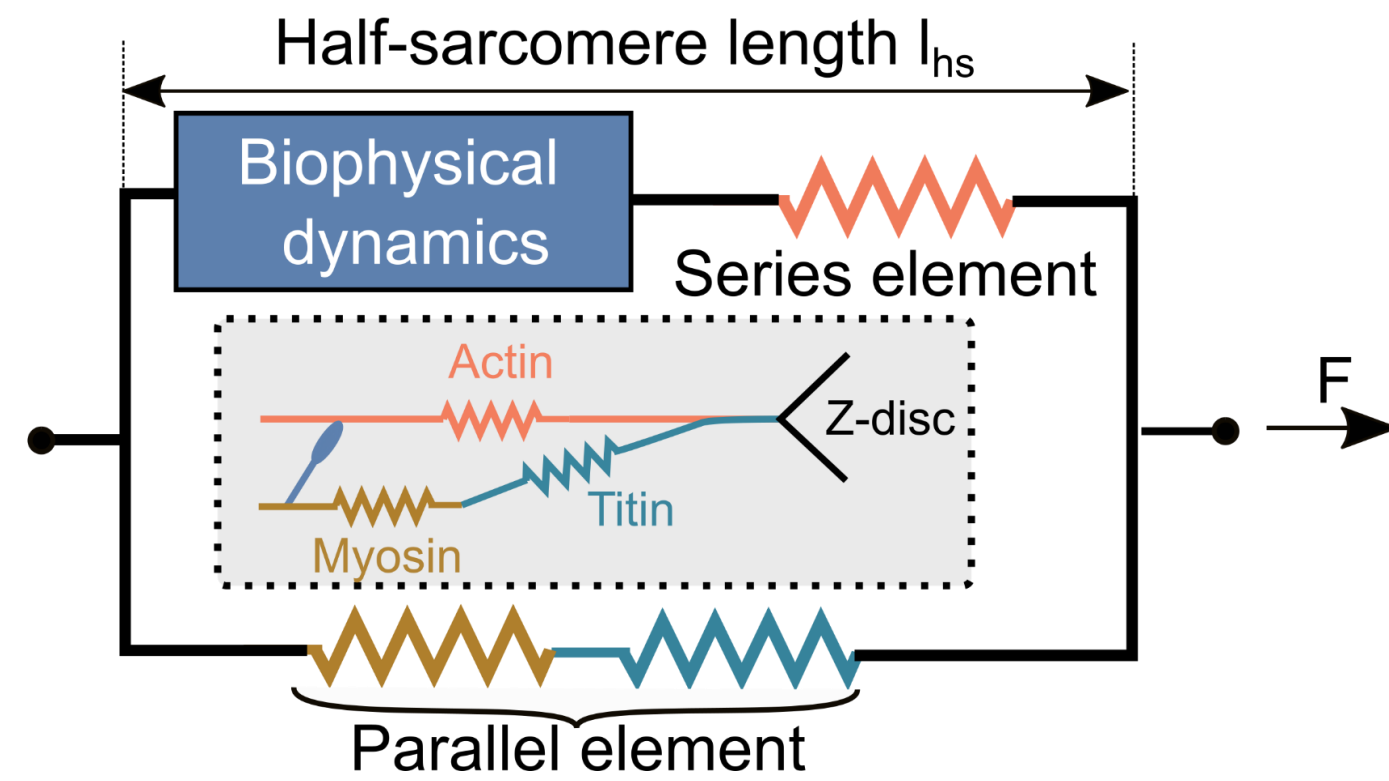
# Pendulum test of spasticity is movement history dependent

Typically developing child Child with cerebral palsy (CP)

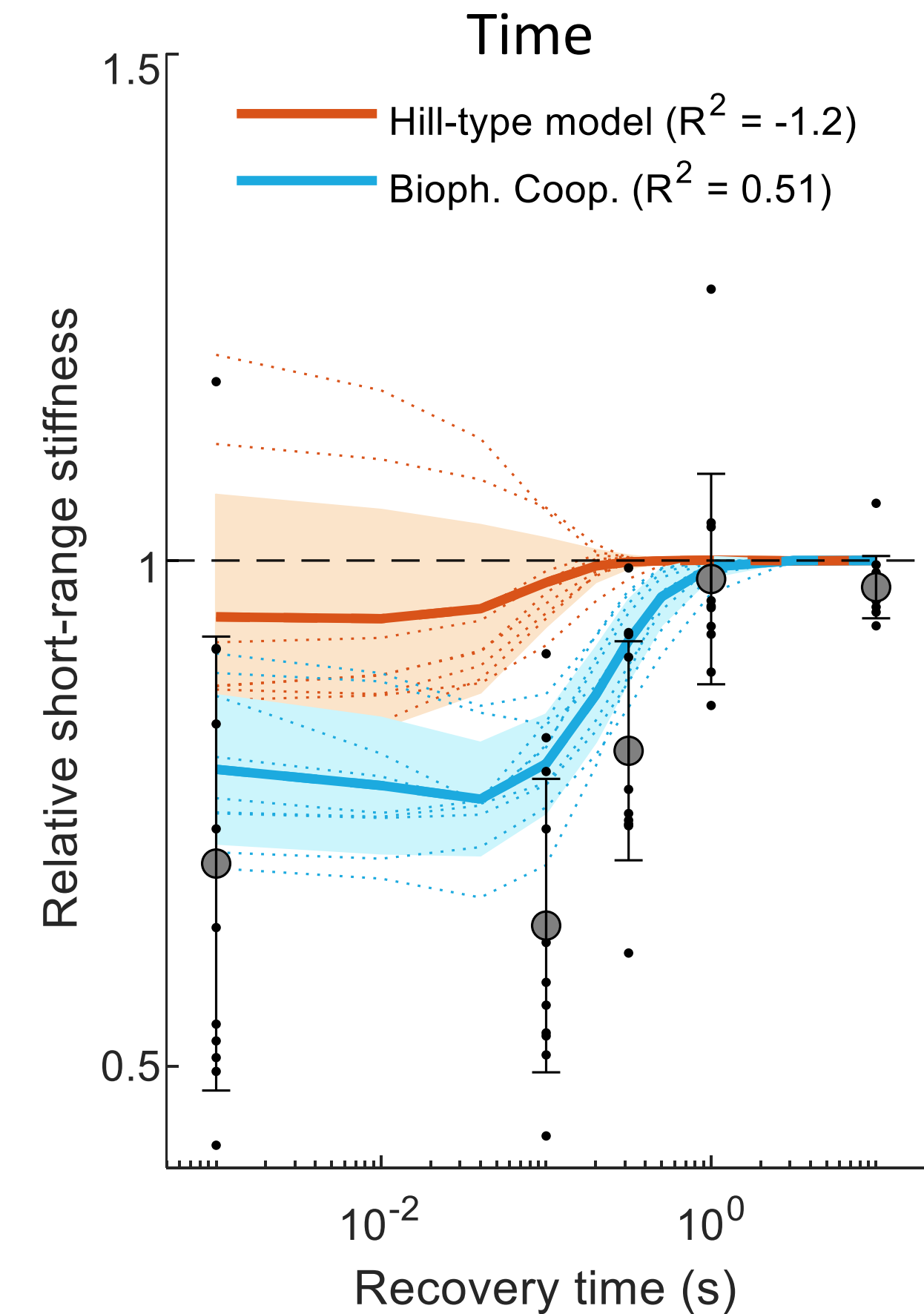
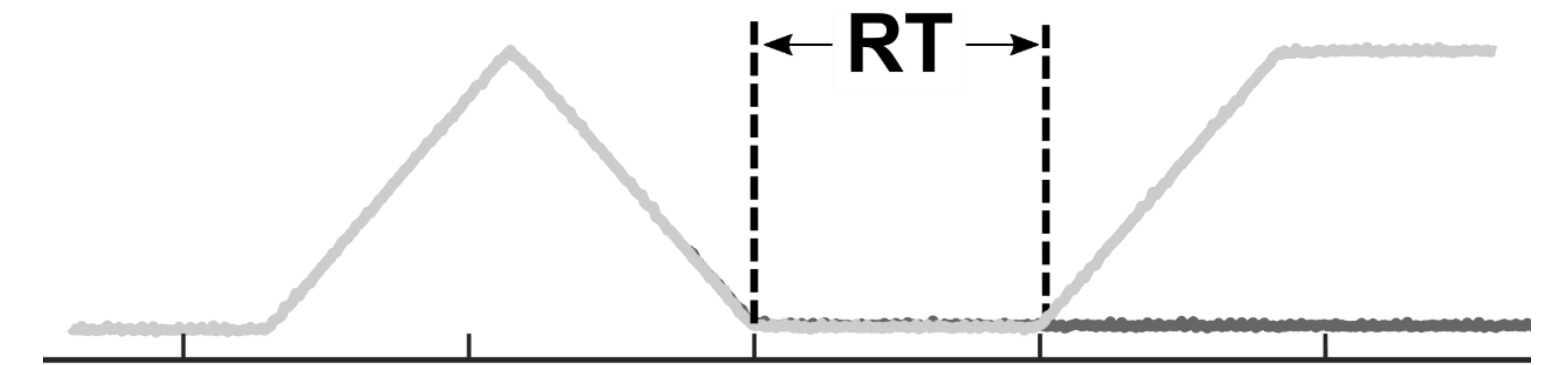


Willaert et al 2020, 2024; De Groote et al., *J Biomech*, 2018

# Four-state cross-bridge model – but not Hill model – captures movement history-dependent short-range stiffness



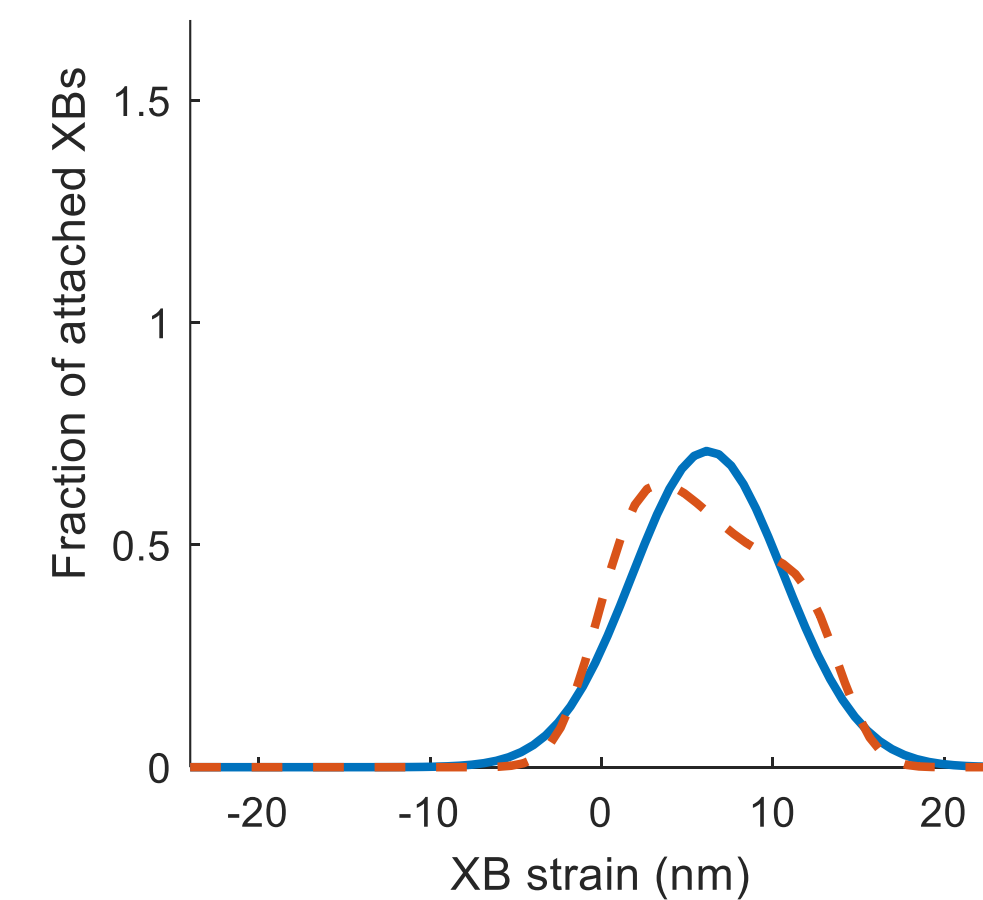
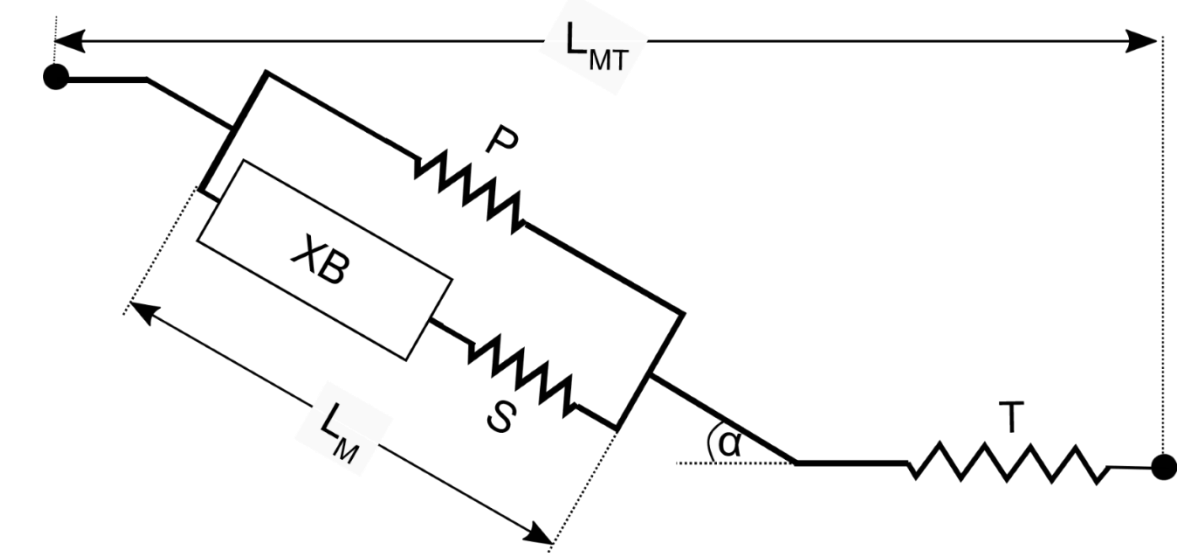
Constant  $Ca^{2+}$ , variable recovery time (RT)



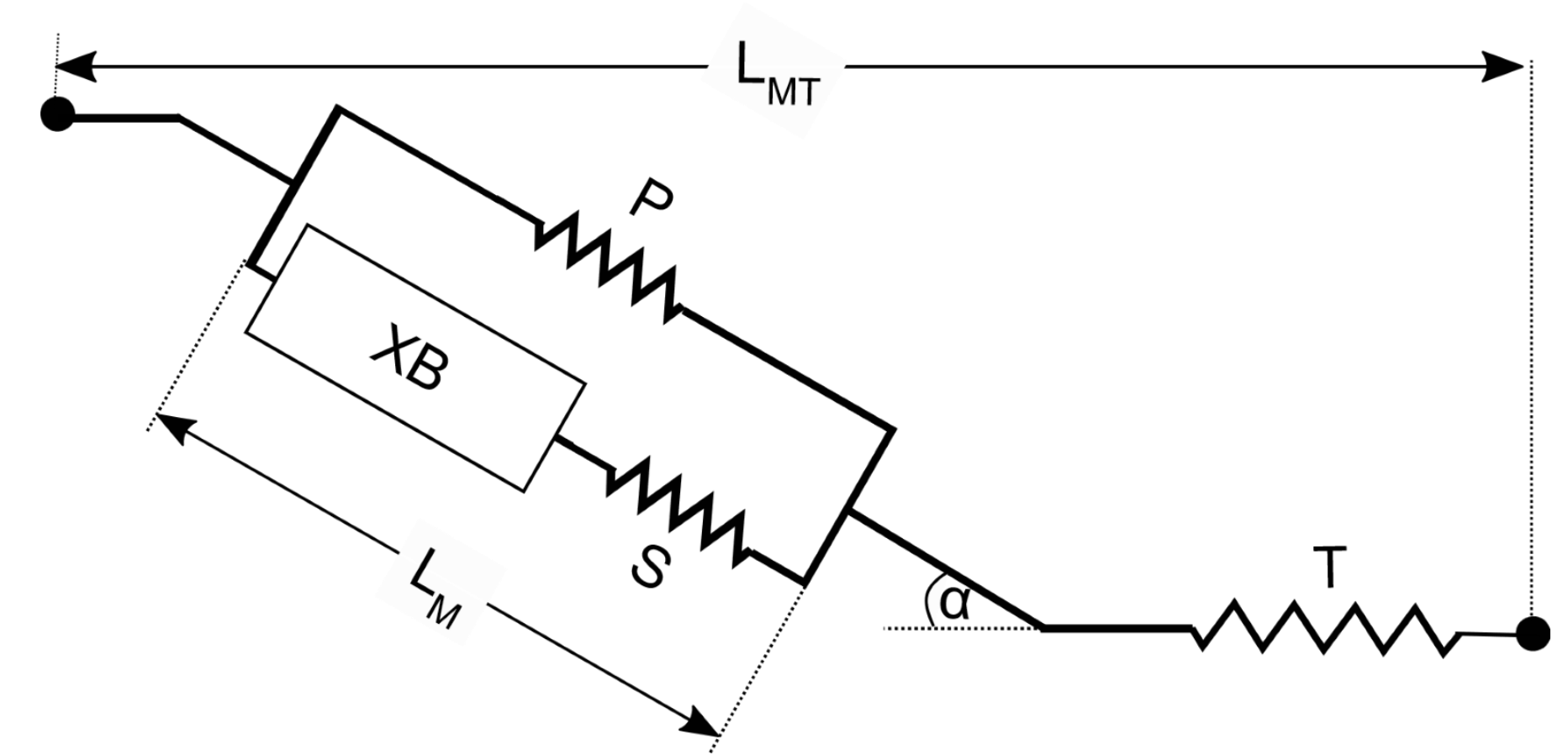


# Using the biophysical muscle model in musculoskeletal simulations

- **Scale half-sarcomere up to whole muscle**
- Distribution moment approximation to improve numerical efficiency



# Scaling up a half sarcomere to a muscle



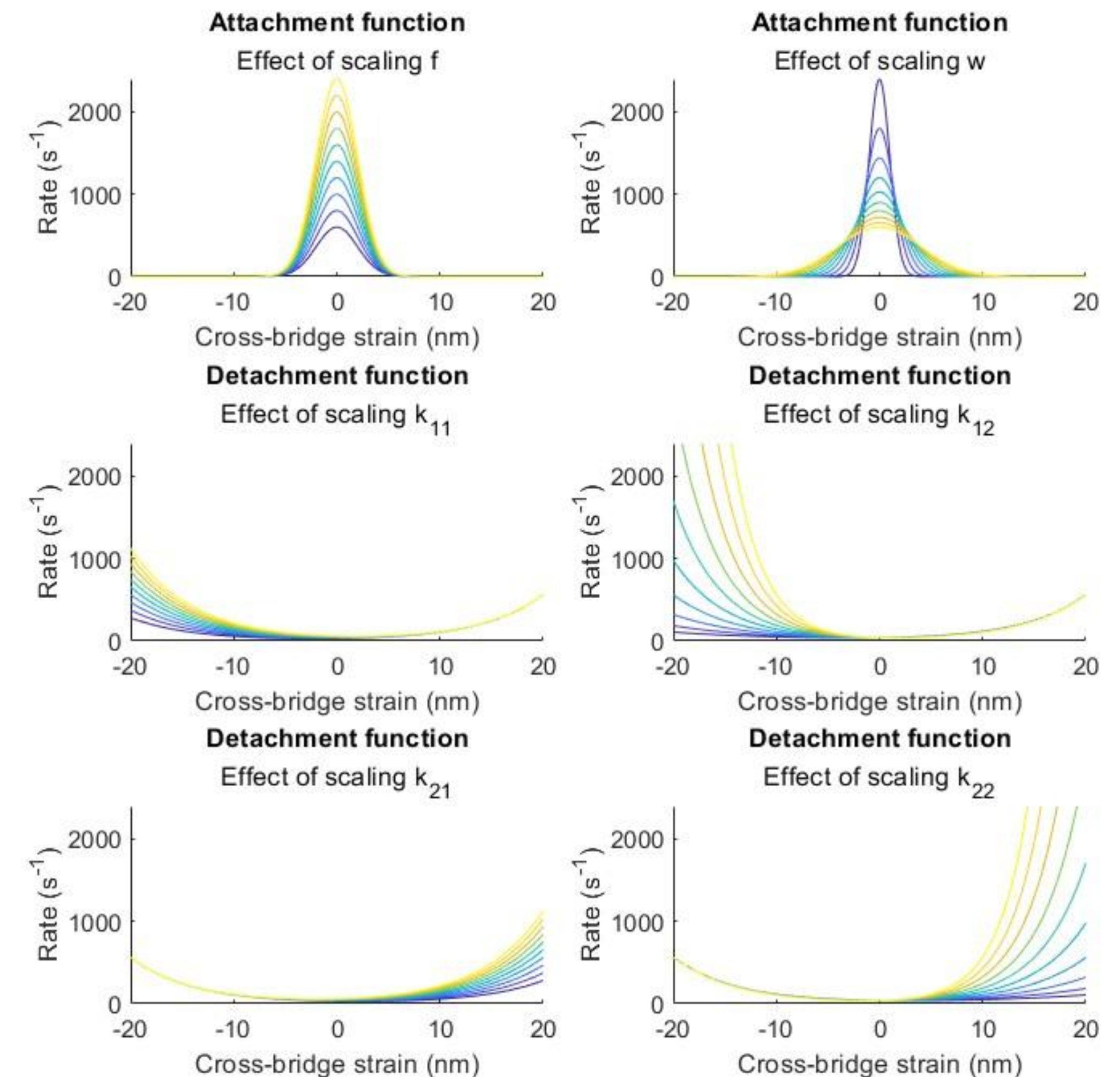
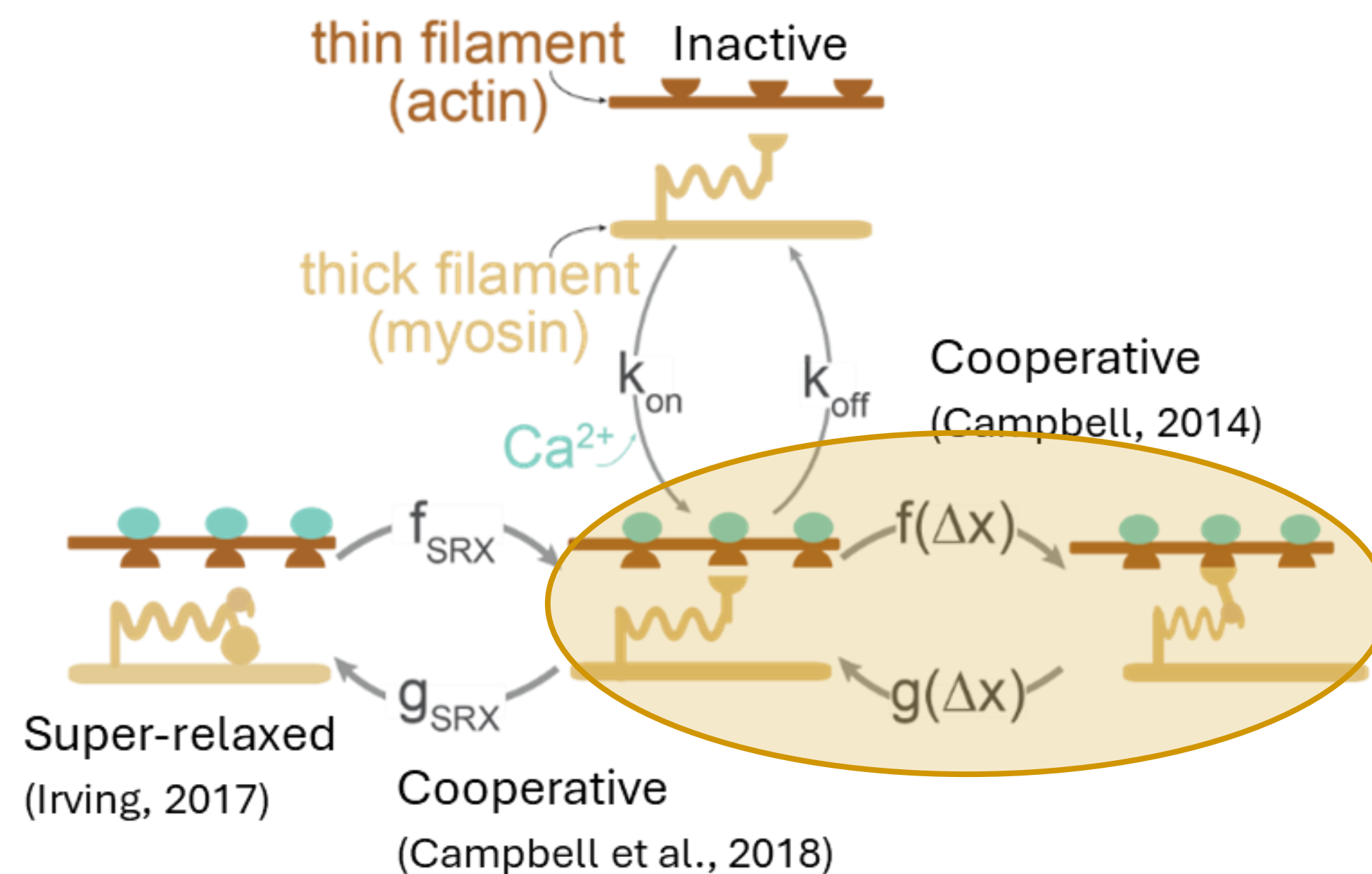
- Scale contractile force based on  $F_{max}$
- Scale resting length based on optimal fiber length from Hill-type muscle model
- Add tendon (T) with stiffness based on Hill model
- Passive stiffness (P) and pennation angle ( $\alpha$ ) based on Hill-model
- Rate constants estimated from experimental data collected in rat soleus muscle fibers at low temperature not representative for in vivo human muscle  
→ Estimate rate parameters

# Estimate rate constants

6 parameters to specify the attachment and detachment rates

$n(x)$  is distribution of attached XB

$$\frac{dn}{dt} - \frac{\partial x}{\partial t} \cdot \frac{\partial n}{\partial x} = f(x) \cdot DRX \cdot \underbrace{\left\{ N_{on} - \int n(x) dx \right\}}_{\text{open binding sites}} - g(x) \cdot n(x)$$



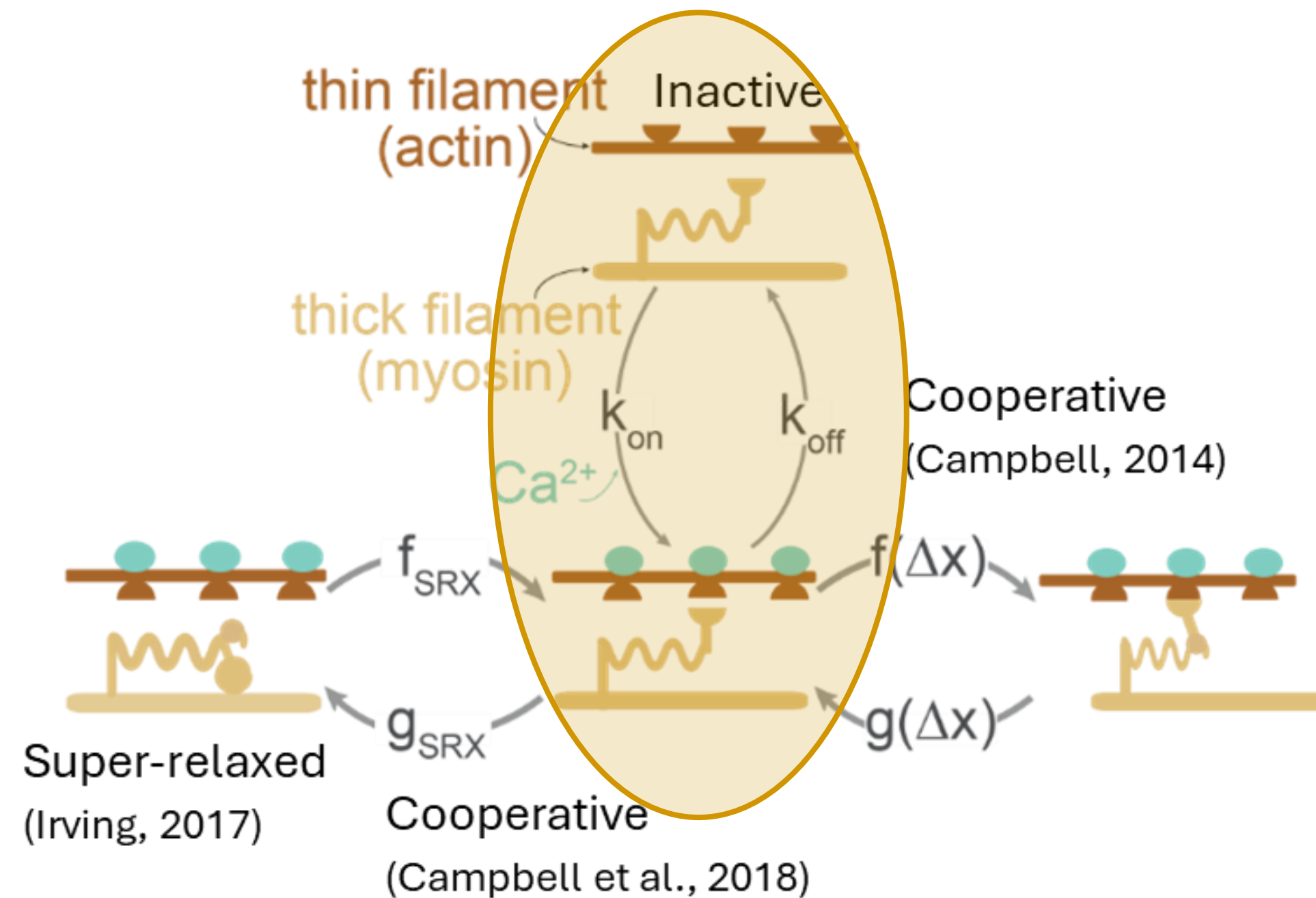


# Estimate rate constants

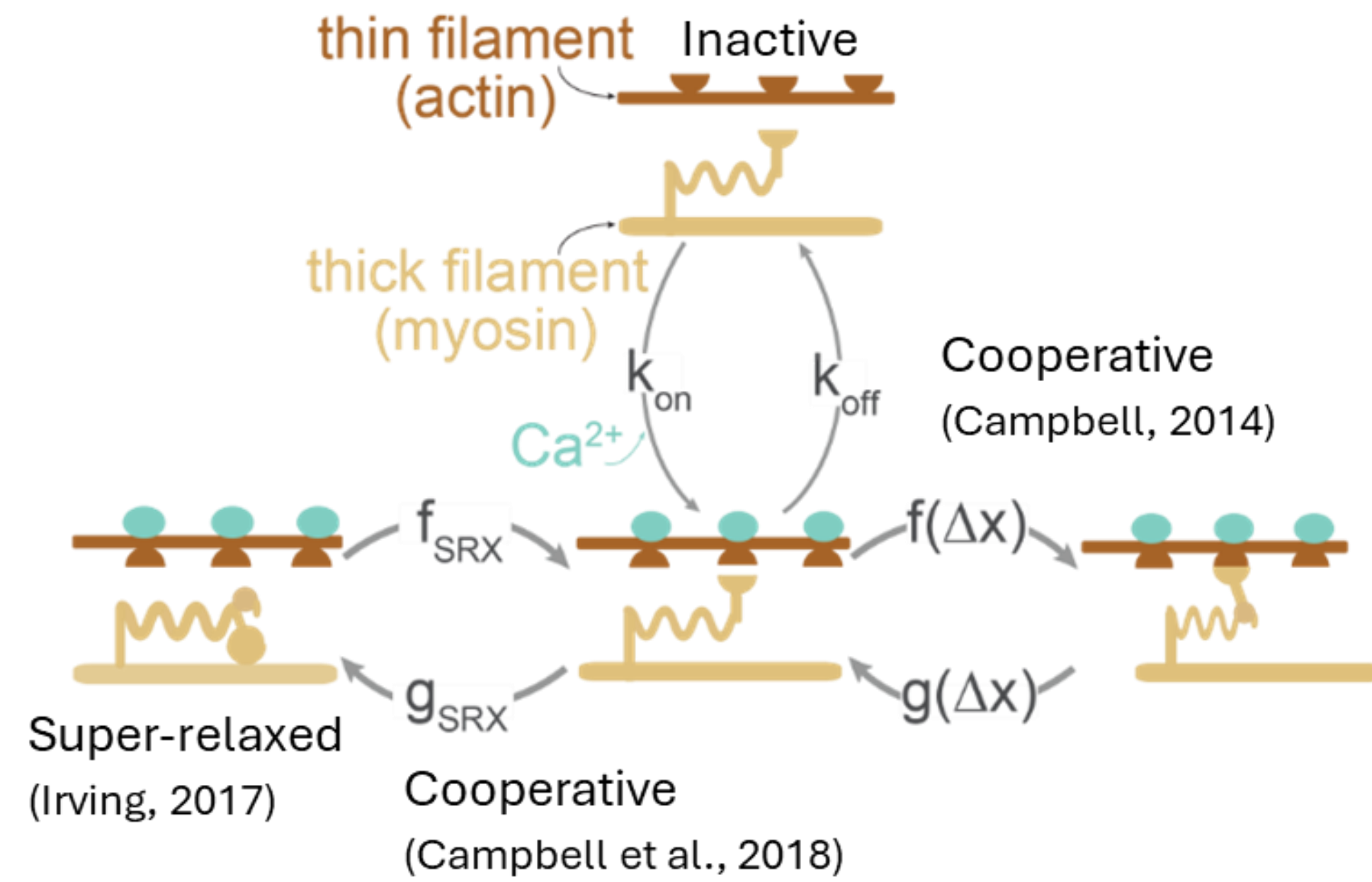
3 parameters to specify thin filament dynamics rates

$N_{on}$  is number of available binding sites on active

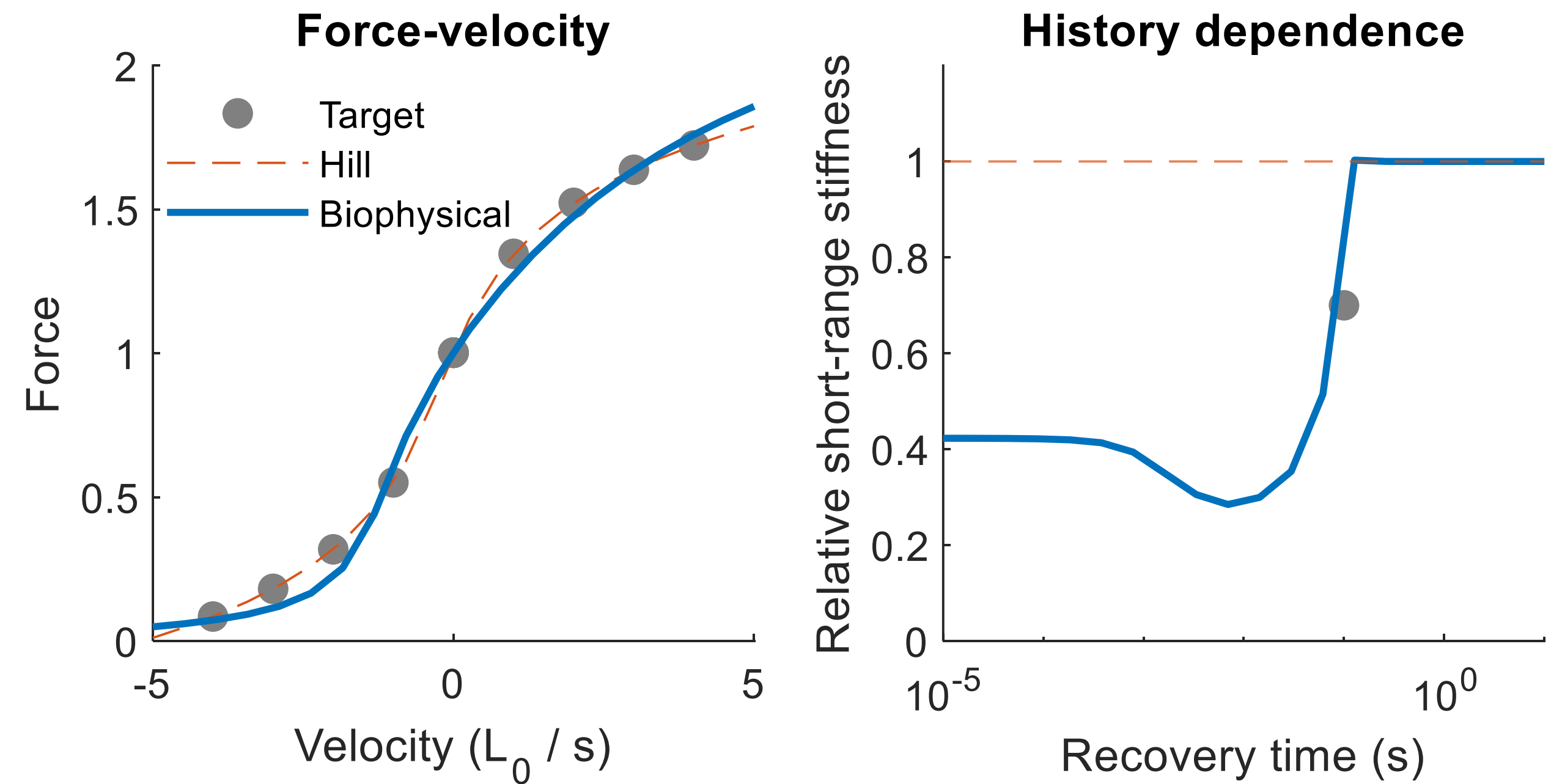
$$\frac{dN_{on}}{dt} = k_{on} \cdot Ca \cdot (F_{overlap} - N_{on}) \cdot \left(1 + k_c \cdot \frac{N_{on}}{F_{overlap}}\right) - k_{off} \cdot \left(N_{on} - \int n(x) dx\right) \cdot \left(1 + k_{oop} \cdot \frac{f_L - N_{on}}{f_L}\right)$$



# Estimate rate constants

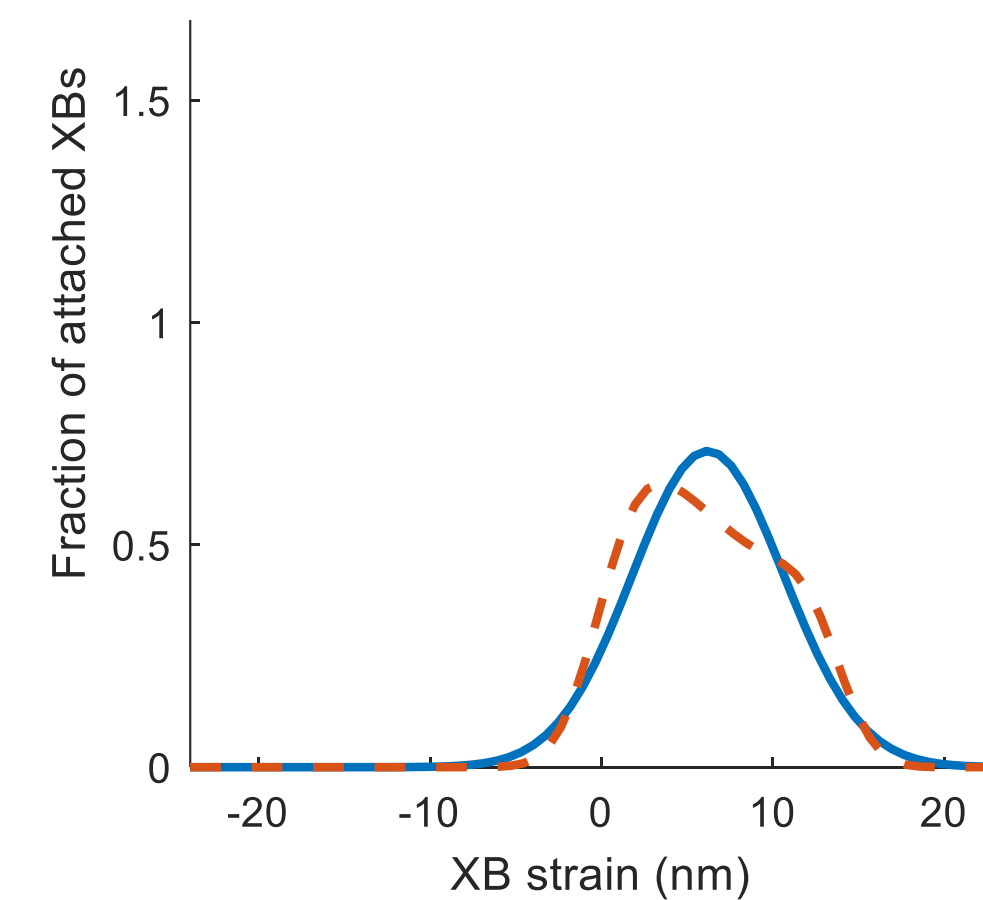
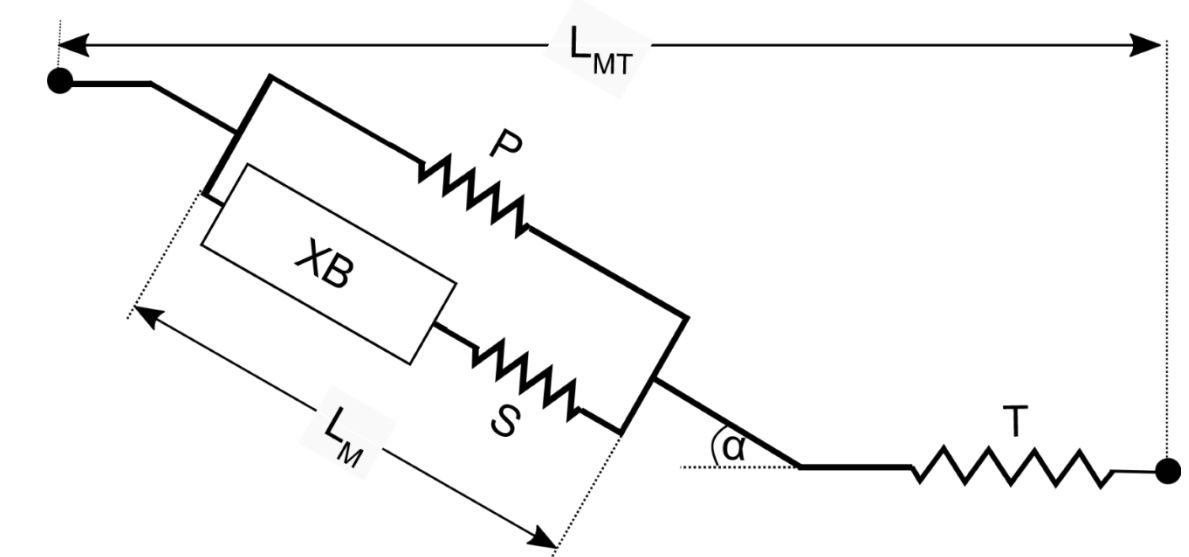


Find rate functions by maximizing the fit between target and modelled force-velocity and history dependence



# Using the biophysical muscle model in musculoskeletal simulations

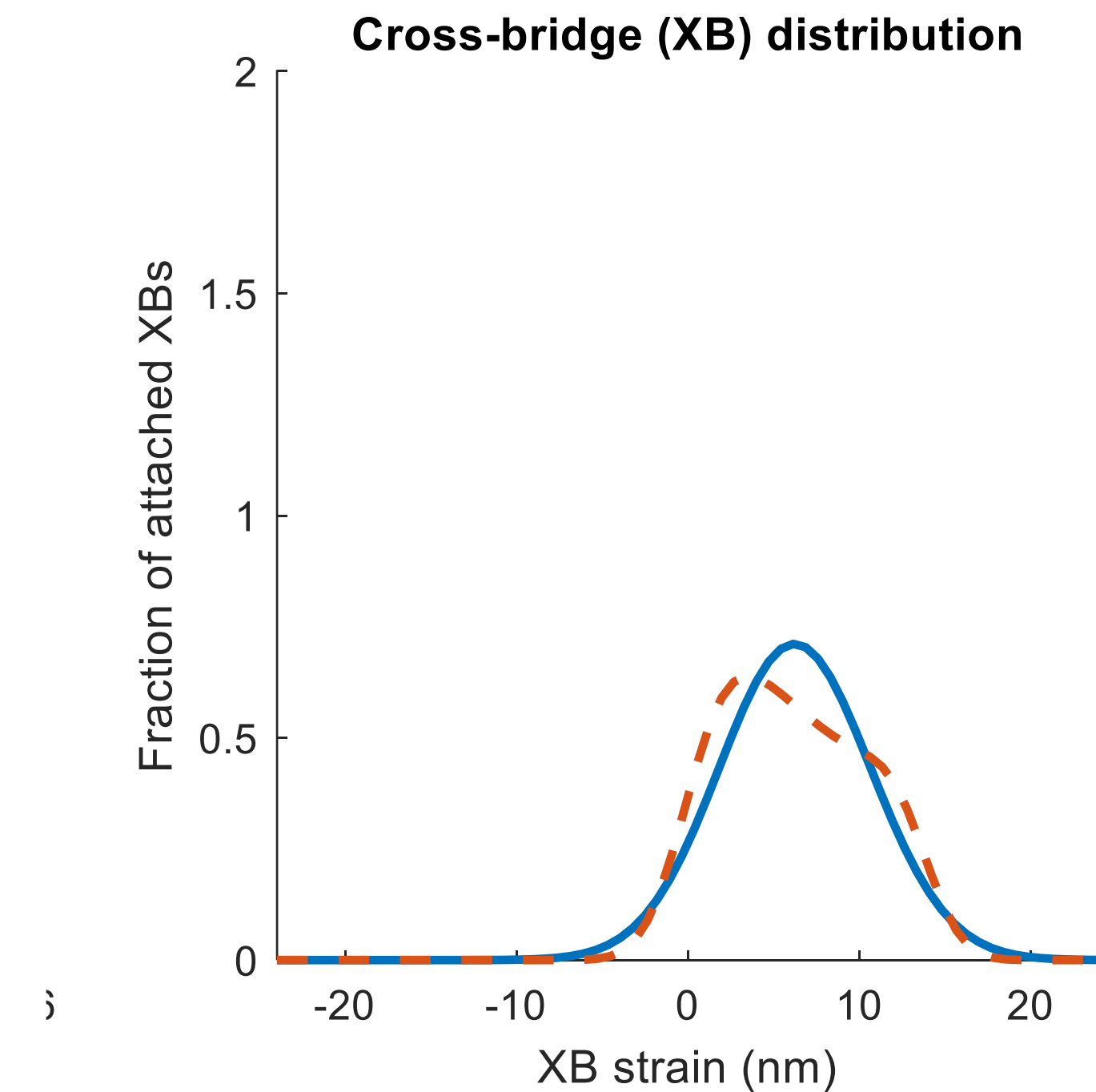
- Scale half-sarcomere up to whole muscle
- **Distribution moment approximation  
to improve numerical efficiency**





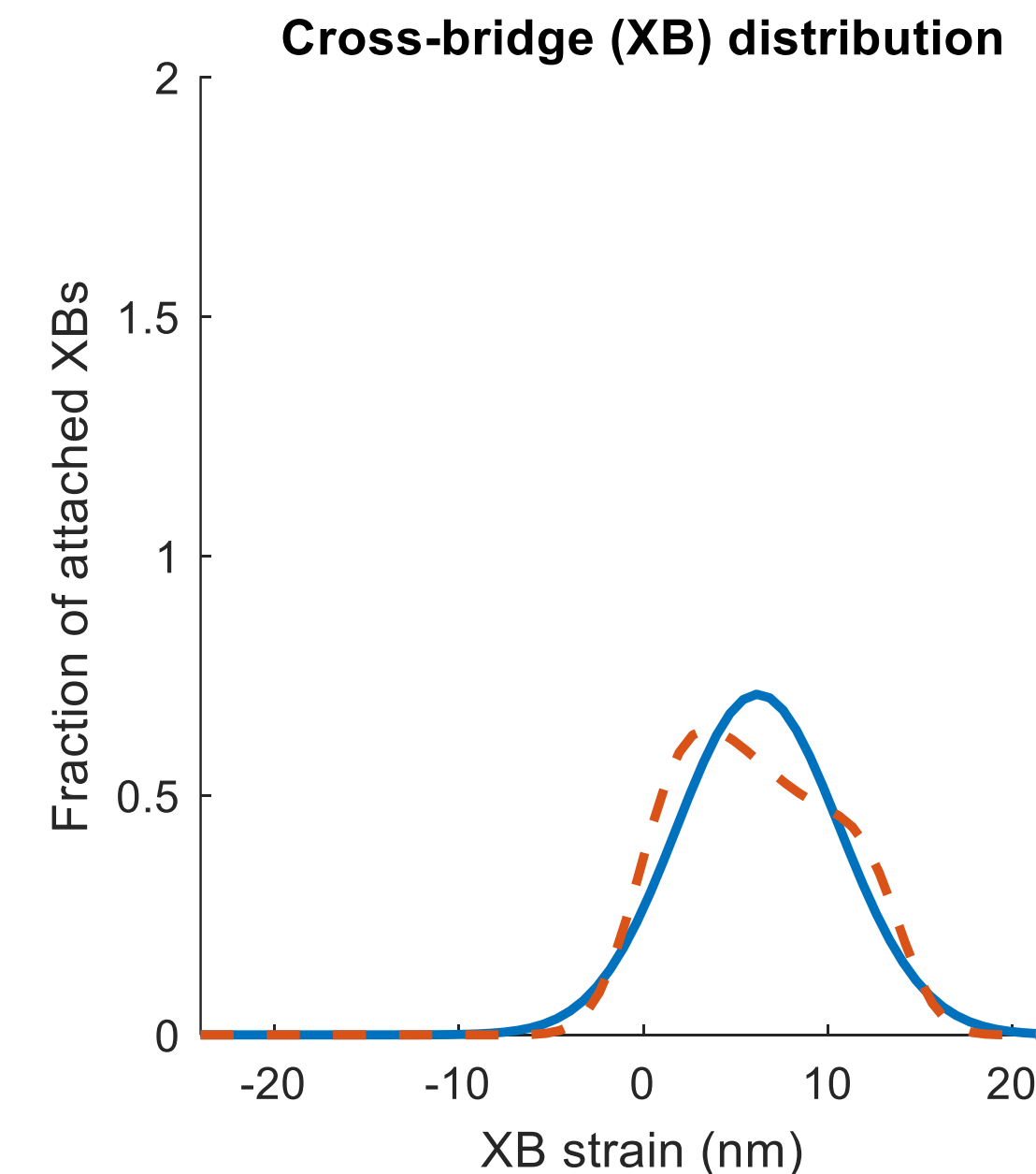
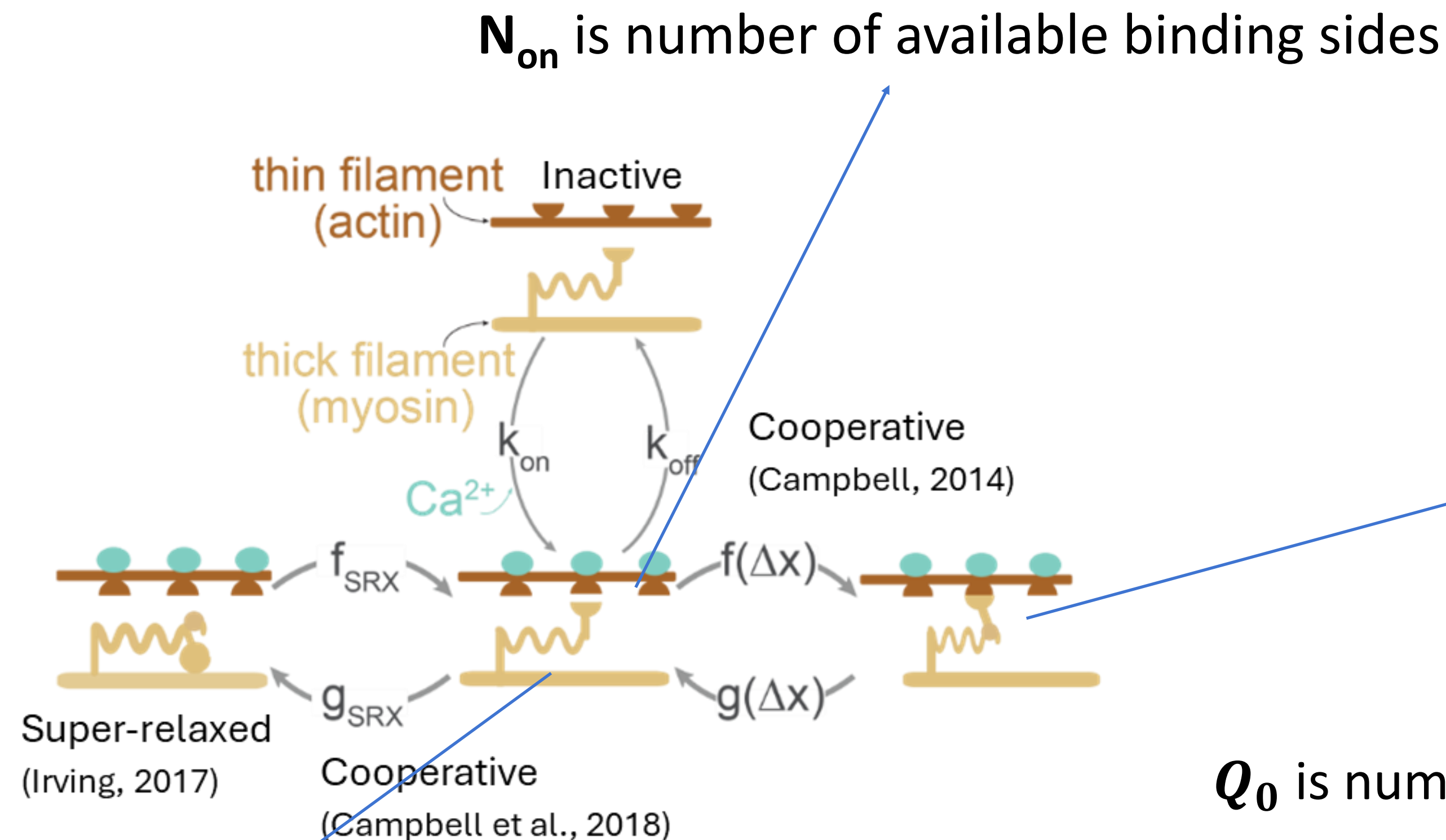
# Distribution moment approximation to improve computational efficiency

- Need to discretize cross-bridge distribution to perform forward simulations  
→ many states → long computational times
- Only lower-order moments of distribution needed to describe macroscopic muscle behavior.
- Approximate distribution by a Gaussian (Zahalak, 1981)  
Moments of Gaussian distribution have physical meaning:
  - $Q_0$  is number of attached XB/muscle stiffness
  - $Q_1$  is proportional to force given constant XB stiffness
  - $Q_2$  is proportional to elastic energy stored in XB



# Distribution moment approximation to improve computational efficiency

## 5 states



**DRX** is number of active myosin heads

$Q_0$  is number of attached XB/muscle stiffness

$Q_1$  is proportional to force given constant XB stiffness

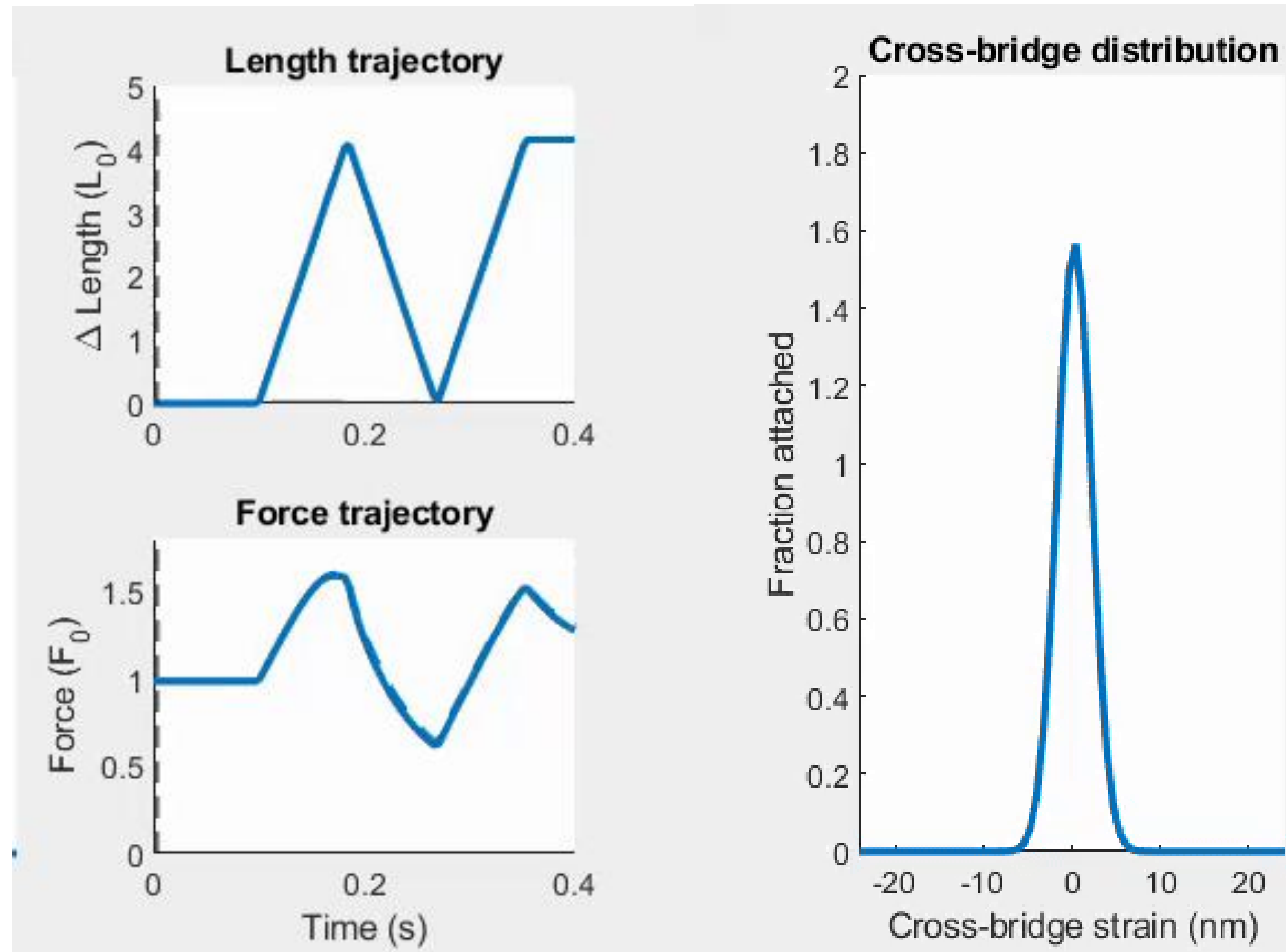
→ normalized tendon force **fse**

$Q_2$  is proportional to elastic energy stored in XB

# The equations



# The DM approximation accurately captures fiber force in response to stretch



$$F \propto \int n(x) \cdot x \, dx$$

Force                      Distribution                      Strain

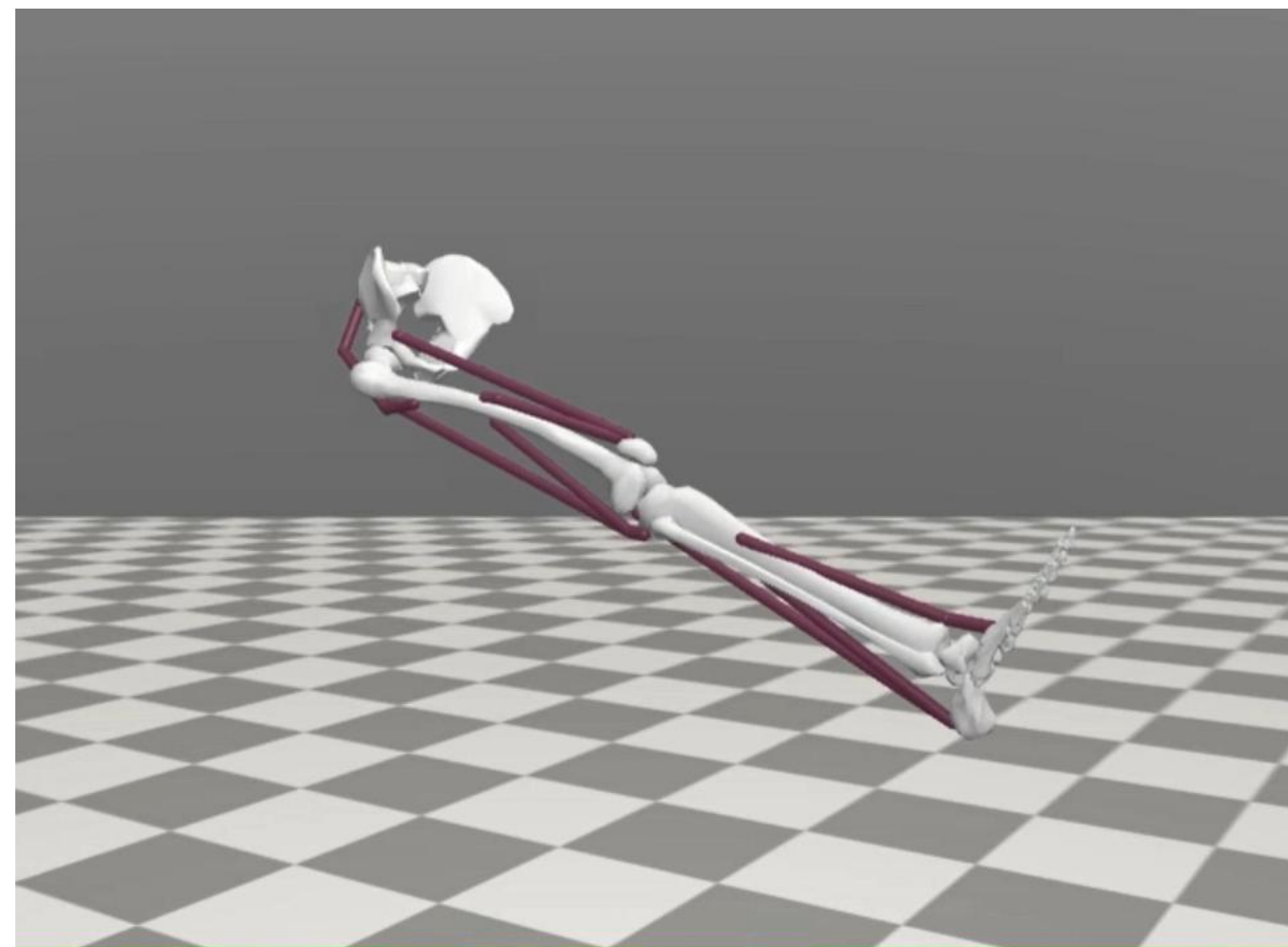
Extra: (refer to comparison of both as extra for tutorial)

# Tutorial - option 1

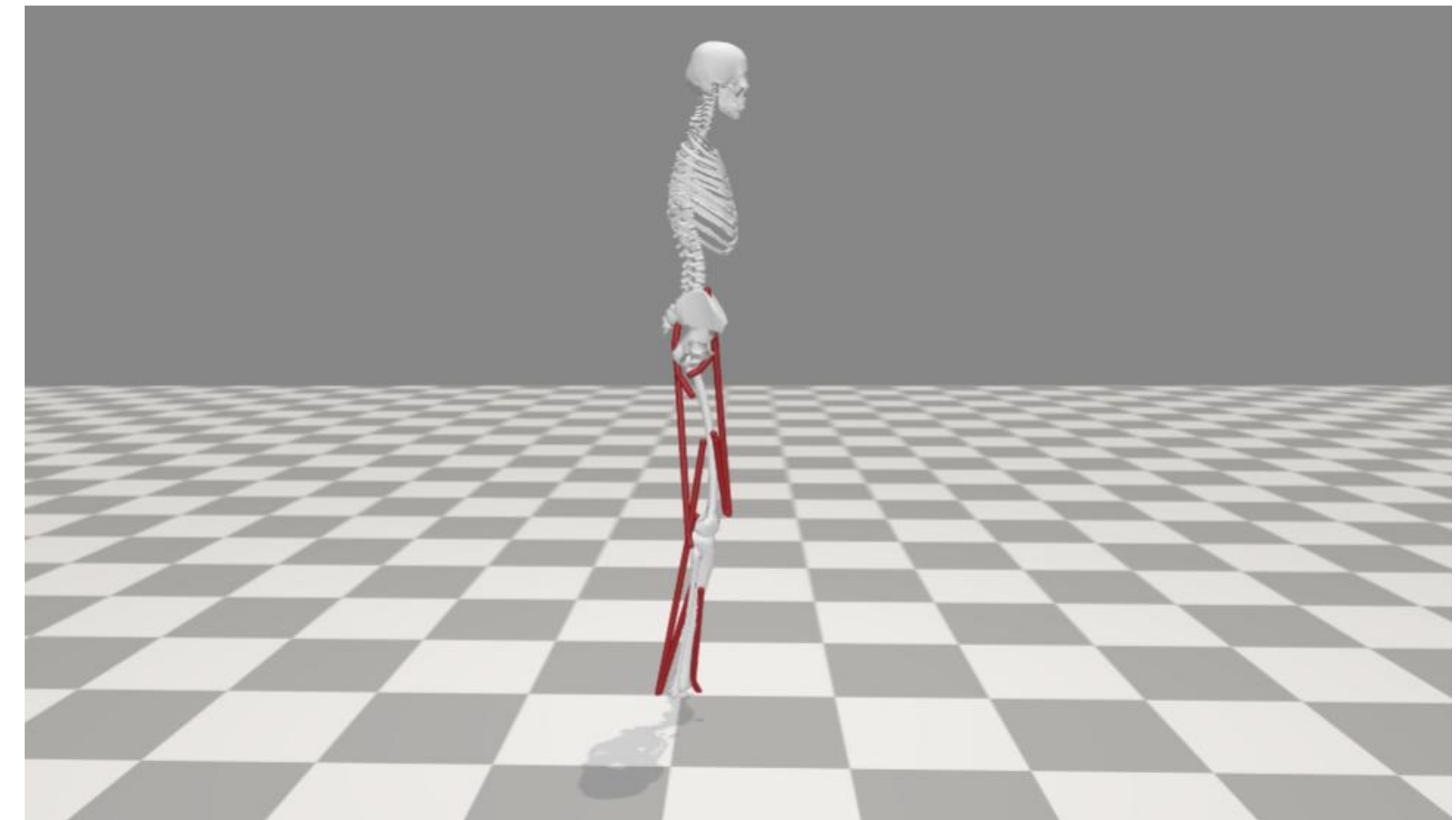
## Musculoskeletal simulations through matlab-OpenSim interface

<https://github.com/timvanderzee/ISB2025> Part 2 - OpenSim

Example 1: “pendulum test” leg swing



Example 2: perturbed standing balance



# Tutorial - option 2

## Musculoskeletal simulations based on simple models in Matlab

<https://github.com/timvanderzee/ISB2025> Part 2 - Custom

